

Level: Bachelor Semester: Spring Year : 2018  
 Programme: BE Full Marks: 100  
 Course: Analysis and Design of Algorithm Pass Marks: 45  
 Time : 3hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

1. a) Explain the term Big-oh, Big-omega and Big-theta. Show that a function  $f=3n^2+4n+7$  is big theta of  $n^2$ . 8  
 b) In each of the following situations, indicate whether  $f = O(g)$ , or  $f = \Omega(g)$ , or both (in which case  $f = \Theta(g)$ ). 7

	$f(n)$	$g(n)$
(a)	$n - 100$	$n - 200$
(b)	$\frac{1}{n^2}$	$\frac{2}{n^3}$
(c)	$\log 2n$	$\log 3n$
(d)	$10 \log n$	$\log n^2$
(e)	$n!$	$2^n$

2. a) Briefly explain a circular queue. Write algorithm to add and remove an element from the circular queue and compute the complexity of your algorithm. 7  
 b) Briefly explain a link list data structure. Write algorithm to add and remove an element from the link list and compute the complexity of your algorithm. 8  
 3. a) Write an algorithm for bubble sort and trace out the algorithm for bubble sort with suitable example. 7  
 b) Discuss how Strassen's method can perform matrix multiplication of two  $n \times n$  matrix in  $O(n^{\log_2 7})$ . 8  
 4. a) Explain prim's algorithm for computing the MST of a given graph and analyze it. Also verify the correctness of this algorithm. 8  
 b) Briefly explain the dynamic programming method for problem solving. What is the basic difference between Dynamic programming 7

and Greedy method?

5. a) How can dynamic programming technique be applied to The Travelling salesman problem? 7  
 b) Explain Dijkstra's algorithm for computing the single source shortest path in a graph with suitable example. 8  
 6. a) Write an algorithm to determine biconnected components in a graph. 7  
 b) Let  $\omega = \{5, 7, 10, 12, 15, 18, 20\}$  and  $m = 35$ . Use Backtracking algorithm to systematically search the solution space to find few possible subsets of  $w$  that sum to  $m$ . Also, draw a portion of the tree diagram that shows the organization of state space. 8  
 7. Write short notes on: (Any two) 2×5  
 a) Binary Search Tree  
 b) Knapsack 0/1 problem  
 c) Graph Coloring Problem