

Data Mining and Data Warehousing

Chapter 2

Data warehousing

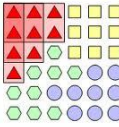
Instructor: Suresh Pokharel

ME in ICT (Asian Institute of Technology, Thailand)

BE in Computer (NCIT, Pokhara University)



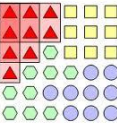
Data Mining Tasks



1. **Classification:** learning a function that maps an item into one of a set of predefined classes
2. **Regression:** learning a function that maps an item to a real value
3. **Clustering:** identify a set of groups of similar items
4. **Dependencies and associations:** identify significant dependencies between data attributes
5. **Summarization:** find a compact description of the dataset or a subset of the dataset



Data Mining Methods



1. Decision Tree Classifiers:

Used for modeling, classification

2. Association Rules:

Used to find associations between sets of attributes

3. Sequential patterns:

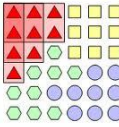
Used to find temporal associations in time series

4. Hierarchical clustering:

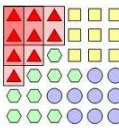
Used to group customers, web users, etc



What Is Frequent Pattern Analysis?



- **Frequent pattern**: a pattern (a set of items, subsequences, substructures, etc.) that occurs frequently in a data set
- First proposed by Agrawal, Imielinski, and Swami [AIS93] in the context of **frequent itemsets** and **association rule mining**
- Motivation: Finding inherent regularities in data
 - What products were often purchased together?— Beer and diapers?!
 - What are the subsequent purchases after buying a PC?
 - What kinds of DNA are sensitive to this new drug?
 - Can we automatically classify web documents?
- Applications
 - Basket data analysis, cross-marketing, Web log (click stream) analysis, and DNA sequence analysis.



Association Rule Mining

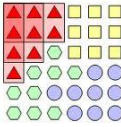
- Given a set of transactions, find rules that will predict the occurrence of an item based on the occurrences of other items in the transaction.

Market-Basket transactions

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

Example of Association Rules

$\{\text{Diaper}\} \rightarrow \{\text{Beer}\},$
 $\{\text{Milk, Bread}\} \rightarrow \{\text{Eggs, Coke}\},$
 $\{\text{Beer, Bread}\} \rightarrow \{\text{Milk}\},$



Definition: Frequent Itemset

■ Itemset

- A collection of one or more items
 - Example: {Milk, Bread, Diaper}
- k-itemset
 - An itemset that contains k items

■ Support count (σ)

- Frequency of occurrence of an itemset
- E.g. $\sigma(\{\text{Milk, Bread, Diaper}\}) = 2$

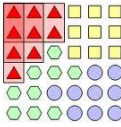
■ Support

- Fraction of transactions that contain an itemset
- E.g. $s(\{\text{Milk, Bread, Diaper}\}) = 2/5$

■ Frequent Itemset

- An itemset whose support is greater than or equal to a *minsup* threshold

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke



Definition: Association Rule

- Association Rule

- An implication expression of the form $X \rightarrow Y$, where X and Y are itemsets
- Example:
 $\{\text{Milk, Diaper}\} \rightarrow \{\text{Beer}\}$

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

- Rule Evaluation Metrics

- **Support (s)**

- ◆ Fraction of transactions that contain both X and Y

- **Confidence (c)**

- ◆ Measures how often items in Y appear in transactions that contain X

Example:

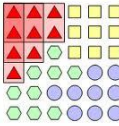
$\{\text{Milk, Diaper}\} \Rightarrow \text{Beer}$

$$s = \frac{\sigma(\text{Milk, Diaper, Beer})}{|T|} = \frac{2}{5} = 0.4$$

$$c = \frac{\sigma(\text{Milk, Diaper, Beer})}{\sigma(\text{Milk, Diaper})} = \frac{2}{3} = 0.67$$



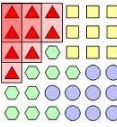
Association Rule Mining Task



- Given a set of transactions T , the goal of association rule mining is to find all rules having
 - support $\geq \textit{minsup}$ threshold
 - confidence $\geq \textit{minconf}$ threshold
 - Brute-force approach:
 - List all possible association rules
 - Compute the support and confidence for each rule
 - Prune rules that fail the *minsup* and *minconf* thresholds
- ⇒ **Computationally prohibitive!**



Mining Association Rules



Example of Rules:

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

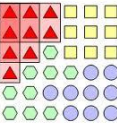
$\{\text{Milk, Diaper}\} \rightarrow \{\text{Beer}\} (s=0.4, c=0.67)$
 $\{\text{Milk, Beer}\} \rightarrow \{\text{Diaper}\} (s=0.4, c=1.0)$
 $\{\text{Diaper, Beer}\} \rightarrow \{\text{Milk}\} (s=0.4, c=0.67)$
 $\{\text{Beer}\} \rightarrow \{\text{Milk, Diaper}\} (s=0.4, c=0.67)$
 $\{\text{Diaper}\} \rightarrow \{\text{Milk, Beer}\} (s=0.4, c=0.5)$
 $\{\text{Milk}\} \rightarrow \{\text{Diaper, Beer}\} (s=0.4, c=0.5)$

Observations:

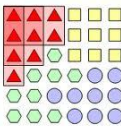
- All the above rules are binary partitions of the same itemset:
 $\{\text{Milk, Diaper, Beer}\}$
- Rules originating from the same itemset have identical support but can have different confidence
- Thus, we may decouple the support and confidence requirements



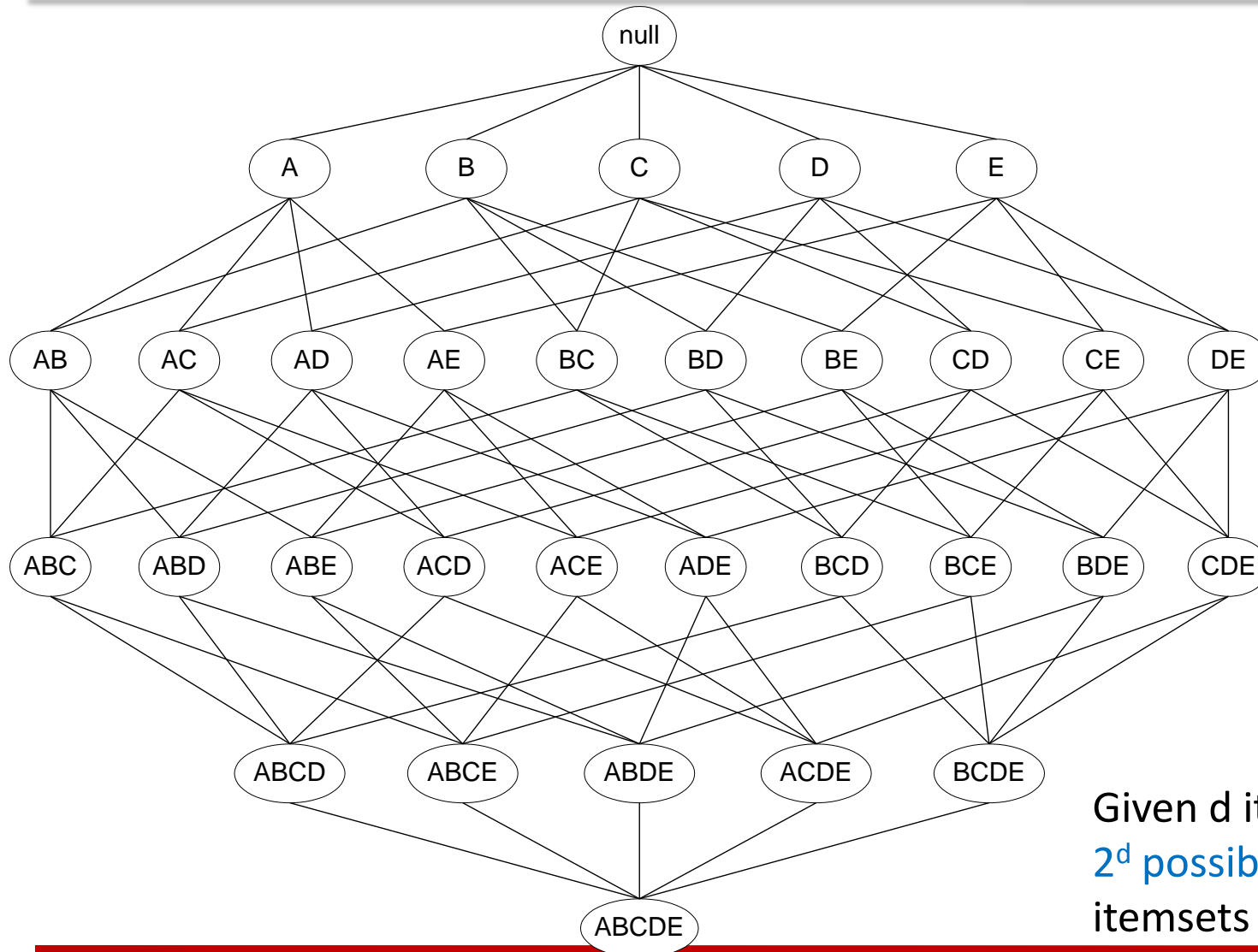
Mining Association Rules



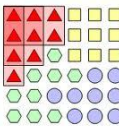
- Two-step approach:
 - Frequent Itemset Generation
 - Generate all itemsets whose support \geq minsup
 - Rule Generation
 - Generate high confidence rules from each frequent itemset, where each rule is a binary partitioning of a frequent itemset
- ❖ Frequent itemset generation is still computationally expensive



Frequent Itemset Generation



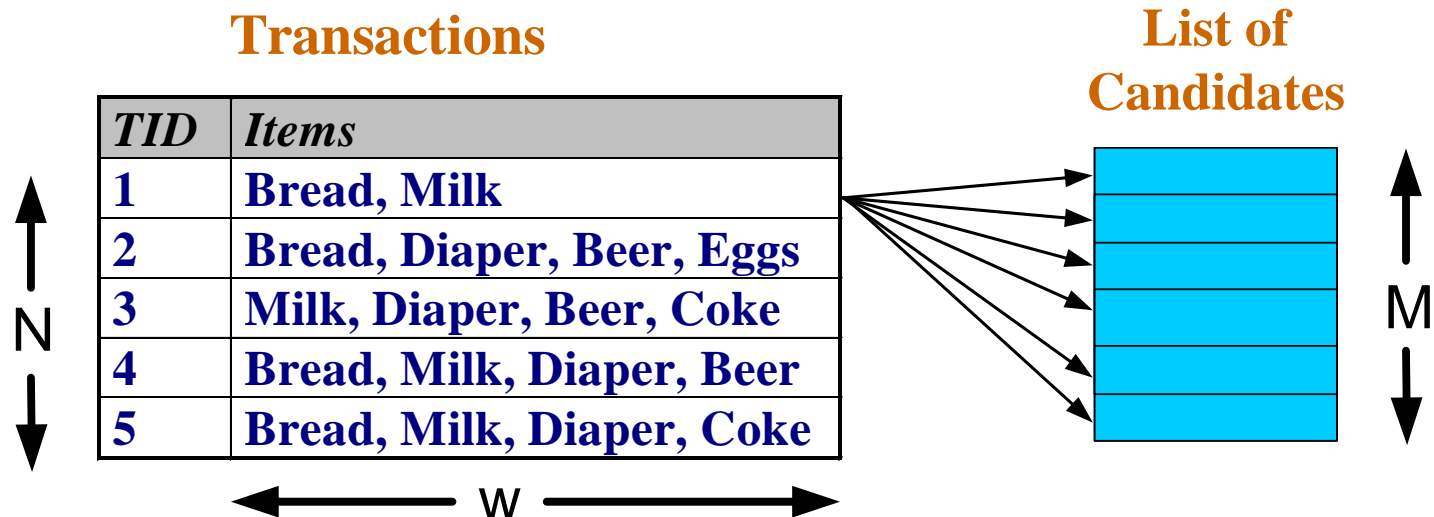
Given d items, there are 2^d possible candidate itemsets



Frequent Itemset Generation

Brute-force approach:

Each itemset in the lattice is a **candidate** frequent itemset
Count the support of each candidate by scanning the database

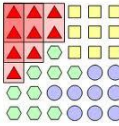


Match each transaction against every candidate

Complexity $\sim O(NMw) \Rightarrow$ **Expensive since $M = 2^d$!!!**



Reducing Number of Candidates



Apriori principle:

If an itemset is frequent, then all of its subsets must also be frequent

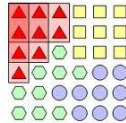
Apriori principle holds due to the following property of the support measure:

$$\forall X, Y : (X \subseteq Y) \Rightarrow s(X) \geq s(Y)$$

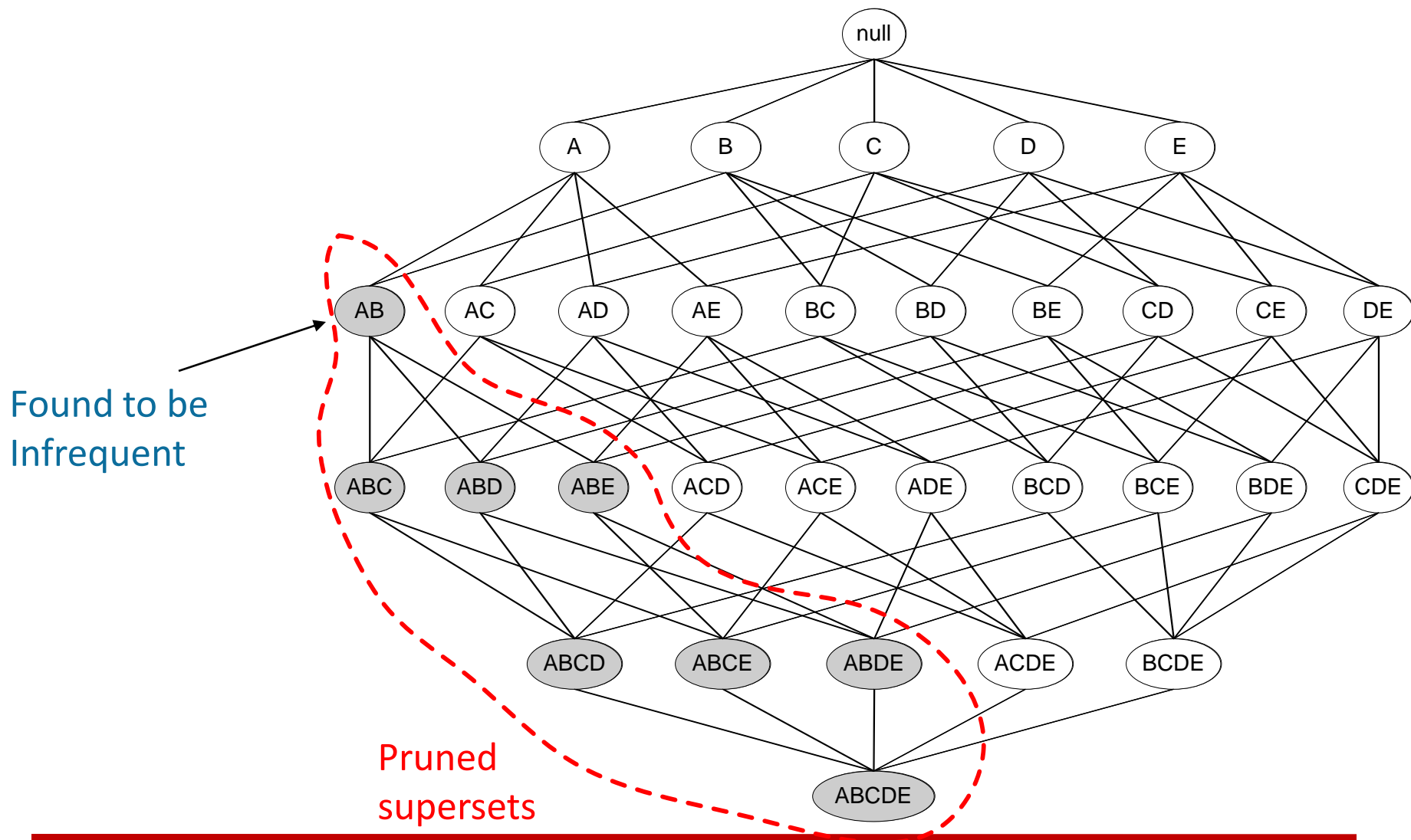
Support of an itemset never exceeds the support of its subsets

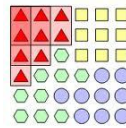
This is known as the **anti-monotone** property of support

Anti-monotone: if a set can't pass a test, all of its superset will fail the same test as well



Illustrating Apriori Principle





Item	Count
Bread	4
Coke	2
Milk	4
Beer	3
Diaper	4
Eggs	1

Items (1-itemsets)



Itemset	Count
{Bread,Milk}	3
{Bread,Beer}	2
{Bread,Diaper}	3
{Milk,Beer}	2
{Milk,Diaper}	3
{Beer,Diaper}	3

Pairs (2-itemsets)

(No need to generate candidates involving Coke or Eggs)

Minimum Support = 3

If every subset is considered,
 ${}^6C_1 + {}^6C_2 + {}^6C_3 = 41$
With support-based pruning,
 $6 + 6 + 1 = 13$



Triplets (3-itemsets)

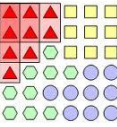
Itemset	Count
{Bread,Milk,Diaper}	3



Q: Total number of possible frequent itemsets ???

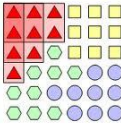


Apriori Algorithm



Method:

- Let $k=1$
- Generate frequent itemsets of length 1
- Repeat until no new frequent itemsets are identified
 - Generate length $(k+1)$ candidate itemsets from length k frequent itemsets
 - Prune candidate itemsets containing subsets of length k that are infrequent
 - Count the support of each candidate by scanning the DB
 - Eliminate(**prune**) candidates that are infrequent, leaving only those that are frequent



Database D

TID	Items
100	1 3 4
200	2 3 5
300	1 2 3 5
400	2 5

Scan D

C_1

itemset	sup.
{1}	2
{2}	3
{3}	3
{4}	1
{5}	3

L_1

itemset	sup.
{1}	2
{2}	3
{3}	3
{5}	3

C_2

itemset	sup
{1 2}	1
{1 3}	2
{1 5}	1
{2 3}	2
{2 5}	3
{3 5}	2

Scan D

C_2

itemset
{1 2}
{1 3}
{1 5}
{2 3}
{2 5}
{3 5}

L_2

itemset	sup
{1 3}	2
{2 3}	2
{2 5}	3
{3 5}	2

C_3

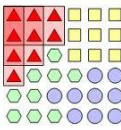
itemset
{2 3 5}

Scan D

L_3

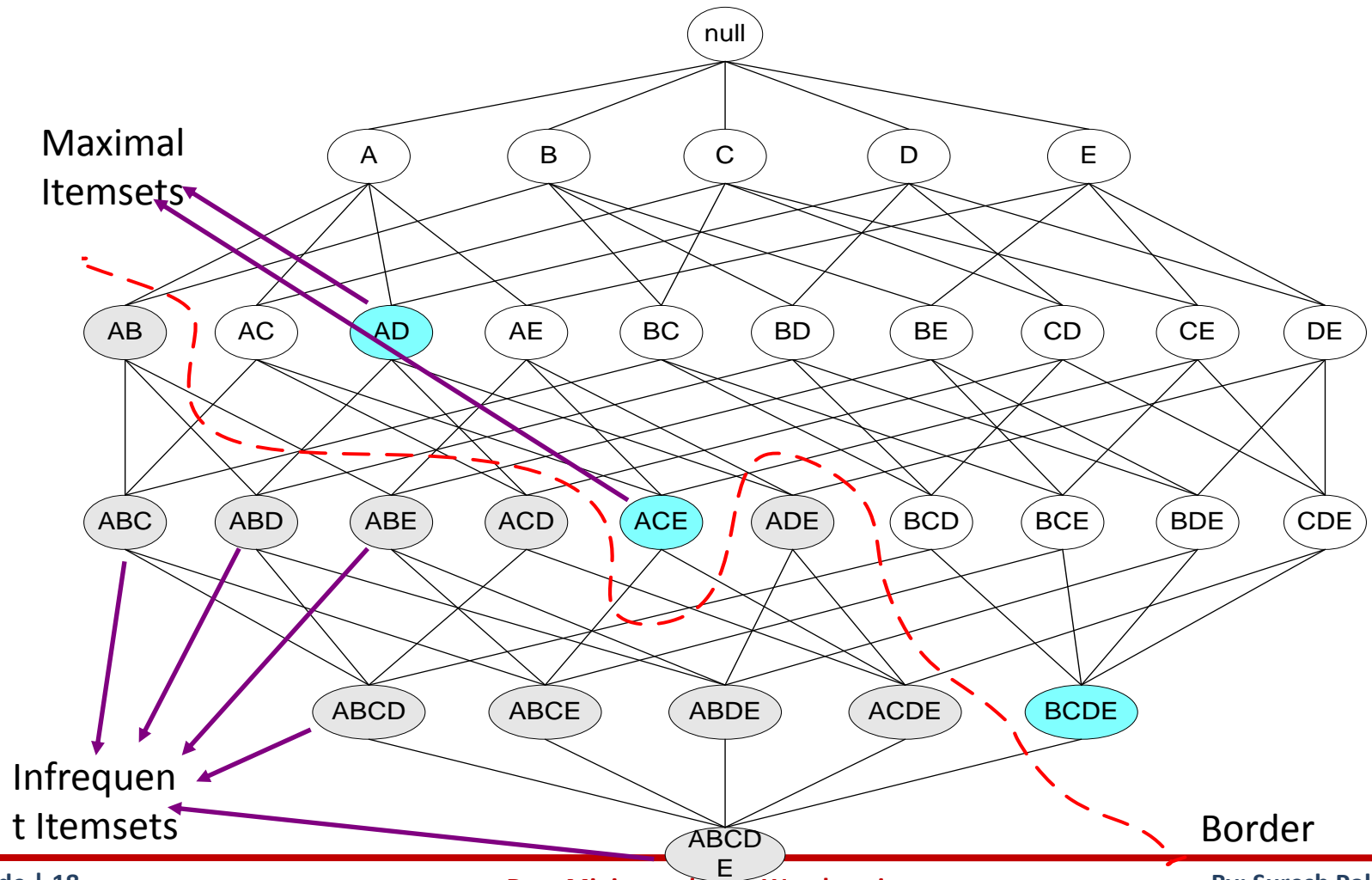
itemset	sup
{2 3 5}	2

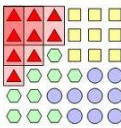
Why {1 2 3}, {1 2 5}, {1 3 5} are not listed in C3???



Maximal Frequent Itemset

An itemset is maximal frequent if none of its immediate supersets is frequent





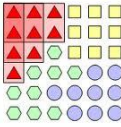
Closed Itemset

An itemset is closed if none of its immediate supersets has the same support as the itemset

TID	Items
1	{A,B}
2	{B,C,D}
3	{A,B,C,D}
4	{A,B,D}
5	{A,B,C,D}

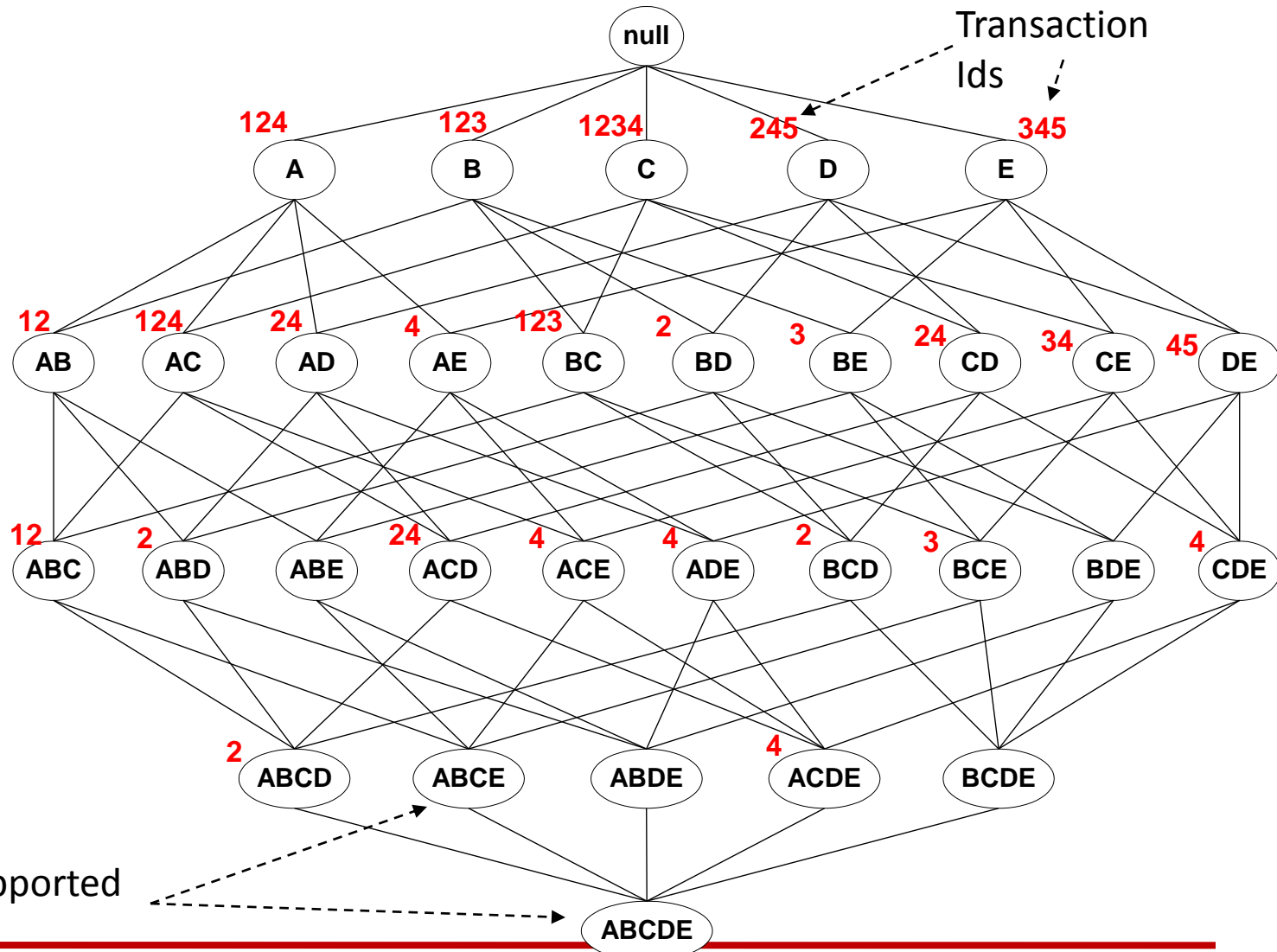
Itemset	Support
{A}	4
{B}	5
{C}	3
{D}	4
{A,B}	4
{A,C}	2
{A,D}	3
{B,C}	3
{B,D}	4
{C,D}	3

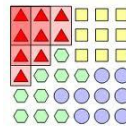
Itemset	Support
{A,B,C}	2
{A,B,D}	3
{A,C,D}	2
{B,C,D}	3
{A,B,C,D}	2



Maximal vs Closed Itemsets

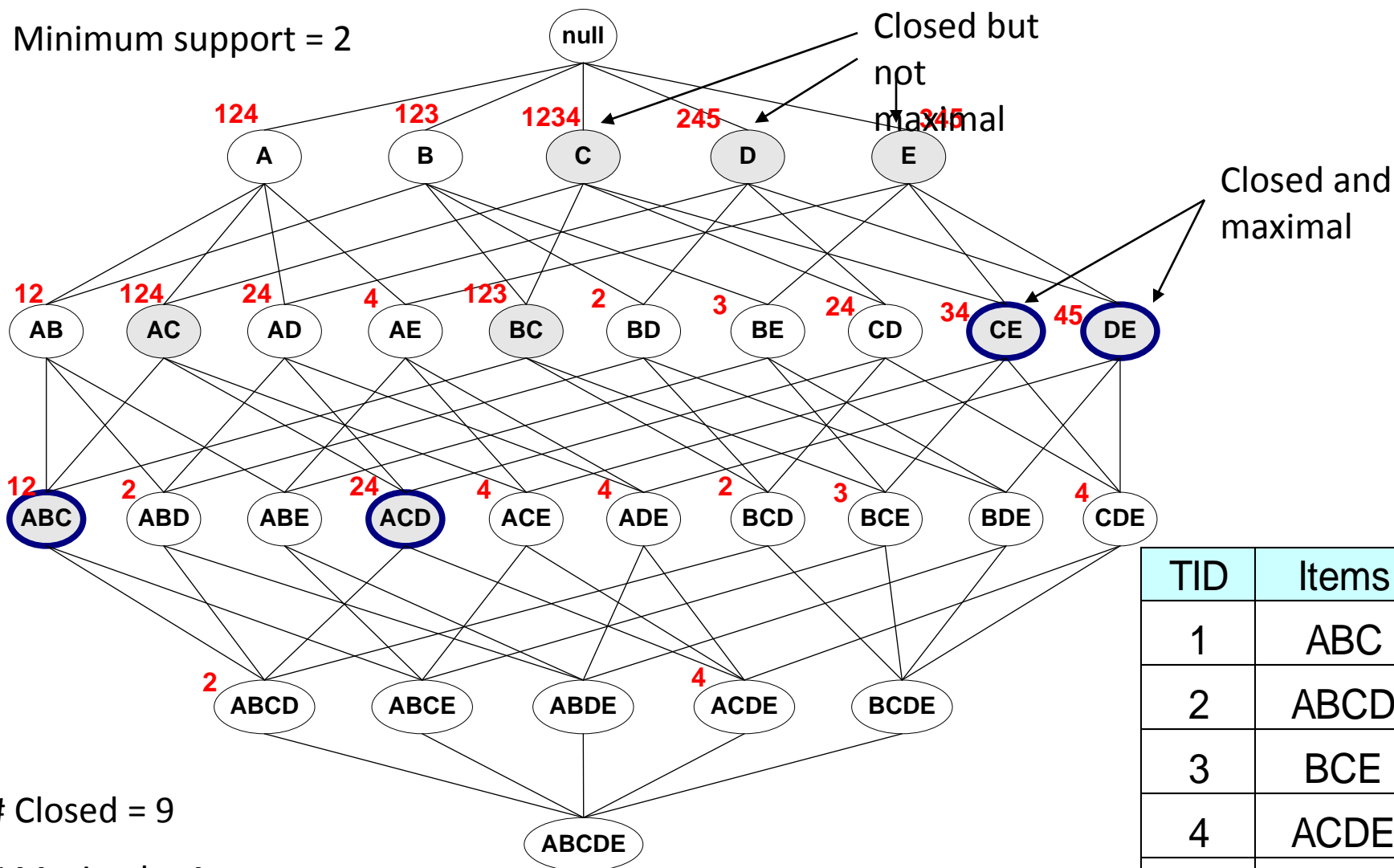
TID	Items
1	ABC
2	ABCD
3	BCE
4	ACDE
5	DE





Maximal vs Closed Frequent Itemsets

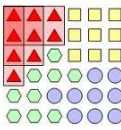
Minimum support = 2



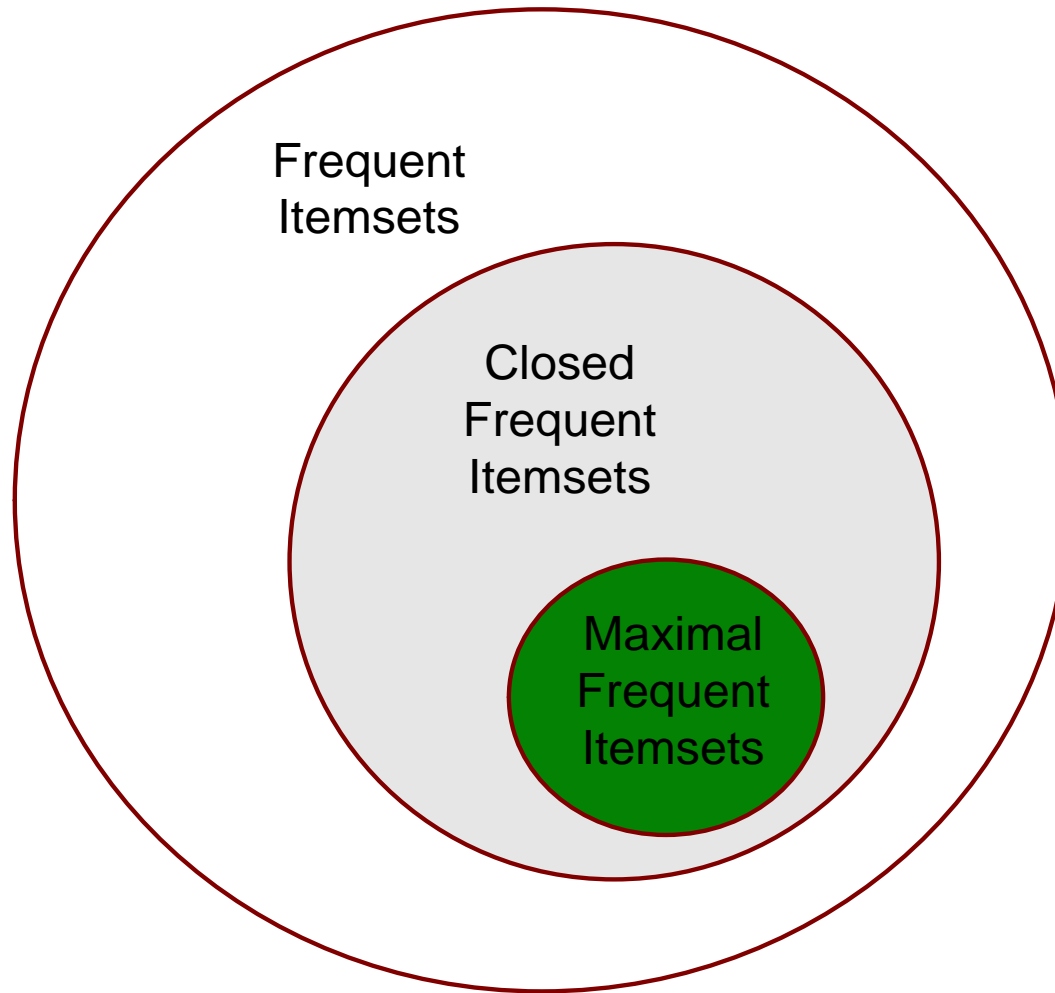
Closed = 9

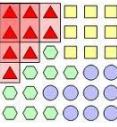
Maximal = 4

TID	Items
1	ABC
2	ABCD
3	BCE
4	ACDE
5	DE



Maximal vs Closed Itemsets

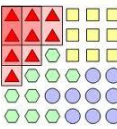




Frequent Pattern Tree

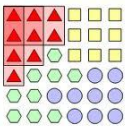


Generating Association Rule (Example)



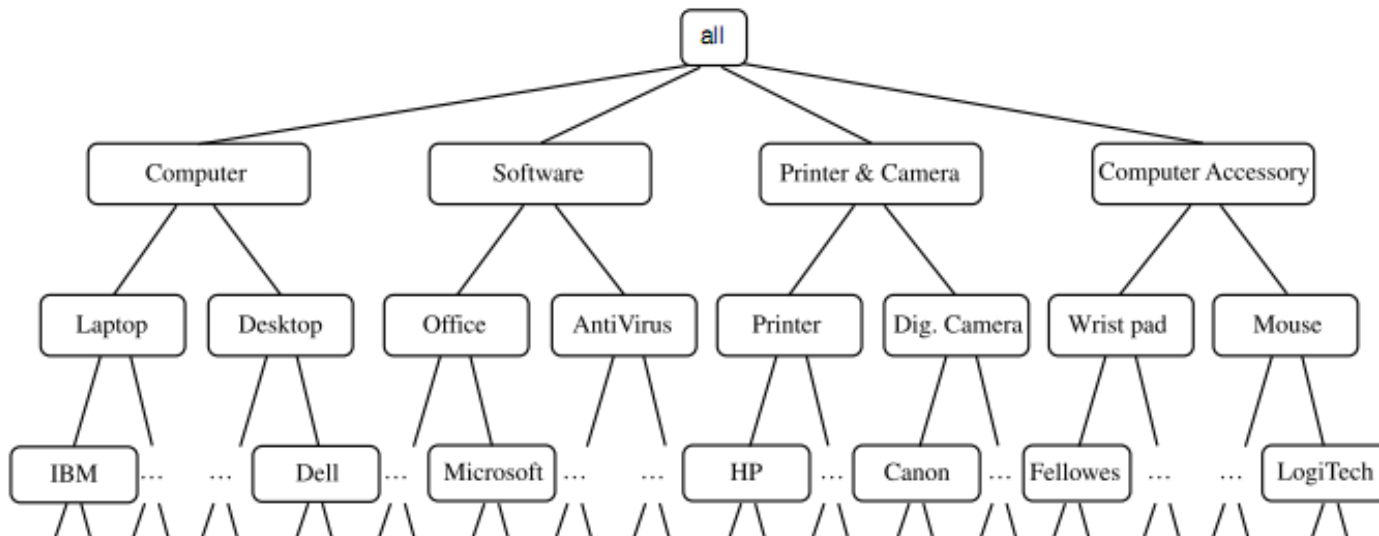
- **Given a frequent itemset L**
 - Find all non-empty subsets F in L, such that the association rule $F \Rightarrow \{L-F\}$ satisfies the minimum confidence
 - Create the rule $F \Rightarrow \{L-F\}$

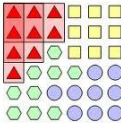
- **If $L=\{A,B,C\}$**
 - The candidate itemsets are: $AB \Rightarrow C$, $AC \Rightarrow B$, $BC \Rightarrow A$, $A \Rightarrow BC$, $B \Rightarrow AC$, $C \Rightarrow AB$
 - In general, there are $2^k - 2$ candidate solutions, where k is the length of the itemset L



Recap : A Concept Hierarchy

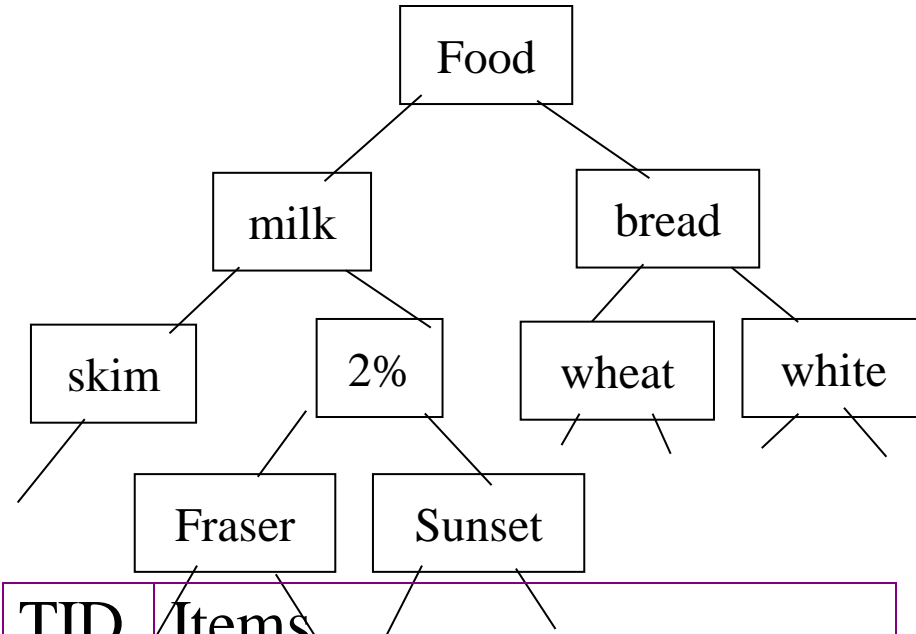
TID	Items Purchased
T100	IBM-ThinkPad-T40/2373, HP-Photosmart-7660
T200	Microsoft-Office-Professional-2003, Microsoft-Plus!-Digital-Media
T300	Logitech-MX700-Cordless-Mouse, Fellowes-Wrist-Rest
T400	Dell-Dimension-XPS, Canon-PowerShot-S400
T500	IBM-ThinkPad-R40/P4M, Symantec-Norton-Antivirus-2003
...	...



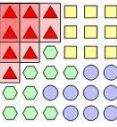


Multiple-Level Association Rules

- Items often form hierarchy.
- Items at the lower level are expected to have lower support.
- Rules regarding itemsets at appropriate levels could be quite useful.
- We can explore shared multi-level mining

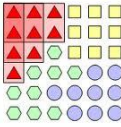


TID	Items
T1	{111, 121, 211, 221}
T2	{111, 211, 222, 323}
T3	{112, 122, 221, 411}
T4	{111, 121}
T5	{111, 122, 211, 221, 413}



Mining Multi-Level Associations

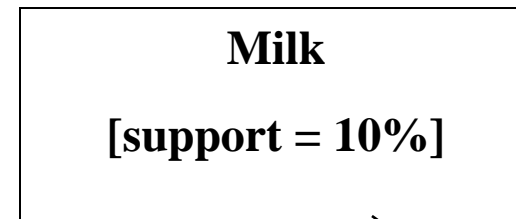
- A top_down, progressive deepening approach:
 - First find high-level strong rules:
milk \rightarrow bread [20%, 60%].
 - Then find their lower-level “weaker” rules:
2% milk \rightarrow wheat bread [6%, 50%].
- Variations at mining multiple-level association rules.
 - Association rules with multiple, alternative hierarchies:
2% milk \rightarrow *Wonder* bread



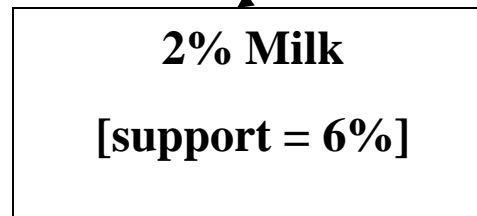
Uniform Support

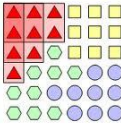
Multi-level mining with uniform support

Level 1
min_sup = 5%



Level 2
min_sup = 5%



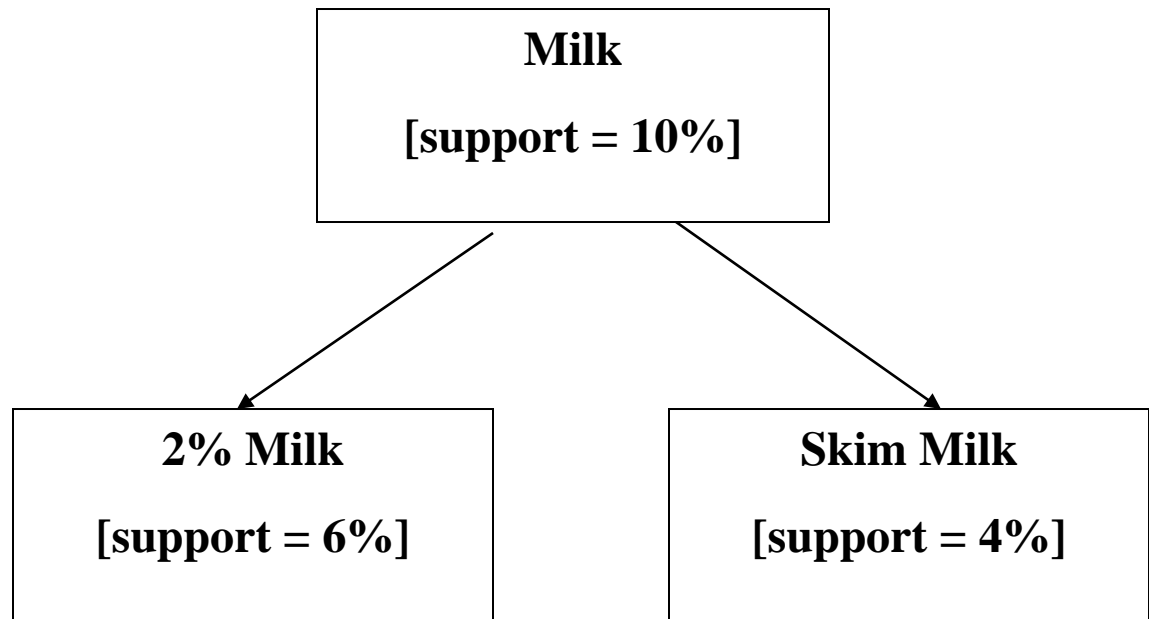


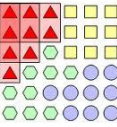
Reduced Support

Multi-level mining with reduced support

Level 1
min_sup = 5%

Level 2
min_sup = 3%





Interestingness Measurements

- Objective measures

Two popular measurements:

★ *support*; and

🕒 *confidence*

- Subjective measures

A rule (pattern) is interesting if

★ it is *unexpected* (surprising to the user); and/or

🕒 *actionable* (the user can do something with it)

