

Worst case of insertion sort for $n=8$. (descending order) Input: 87654321.

No. of processes to 8 in place = $1+1$

No. of processes to 7 in place = $2+2$

No. of processes to 6 in place = $3+3$

No. of processes to 5 in place = $4+4$

No. of processes to 4 in place = $5+5$

No. of processes to 3 in place = $6+6$

No. of processes to 2 in place = $7+7$

No. of processes to 1 in place = $8+8$

Total = $2*8+2*7+\dots+2*1$

$=2(1+2+3+\dots+8)$

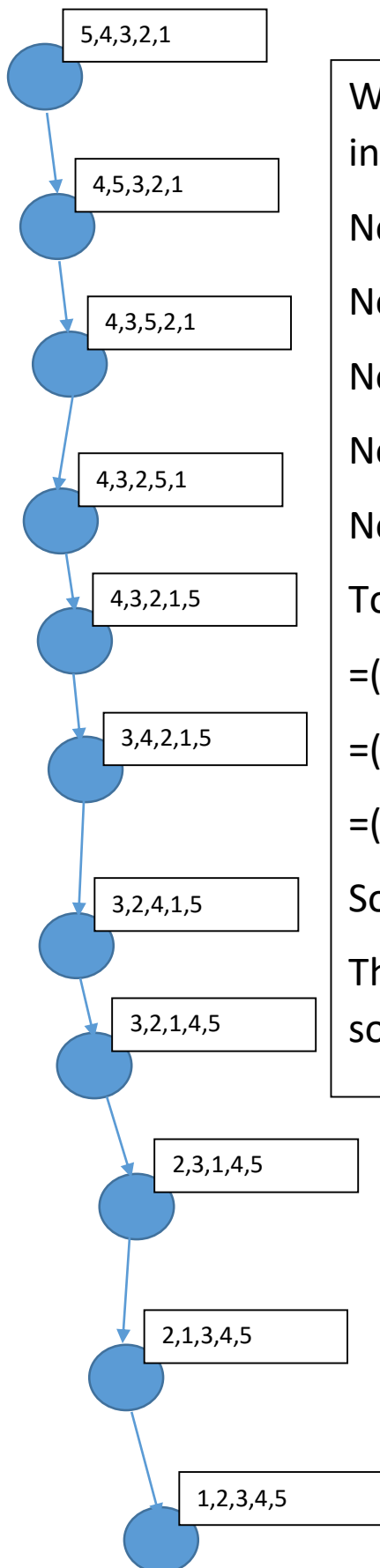
$=2(1+2+\dots+n)$

$=2n(n+1)/2$

$=n(n+1)$

Here, the highest order is n^2 .

Therefore, the complexity of the bubble sort for worst case is $O(n^2)$.



Worst Case scenario of bubble sort for input : 5,4,3,2,1. i.e.: $n=5$

No. of comparisons to put 5 in place:4

No. of comparisons to put 4 in place:3

No. of comparisons to put 3 in place:2

No. of comparisons to put 2 in place:1

No. of comparisons to put 1 in place:0

Total no. of comparisons= $4+3+2+1+0$

$=(n-1)+(n-2)+\dots+1$

$=((n-1)((n-1)-1))/2$

$=((n-1)(n-2))/2$

So the highest order is n^2 .

Therefore, the complexity of the bubble sort for worst case is $O(n^2)$.