

Brian Kernighan's Algorithm — Interview & Coding Notes (C++)

What it does:

Counts the number of set bits (1s) in an integer faster than checking every bit.

Core Trick:

$n = n \& (n - 1)$

This removes the rightmost set bit from n.

Why it works:

Subtracting 1 from a number flips all bits after the last set bit. AND operation with the original number removes that last 1 bit.

C++ Implementation:

```
int countSetBits(int n) {
    int cnt = 0;
    while (n > 0) {
        n = n & (n - 1);
        cnt++;
    }
    return cnt;
}
```

Time Complexity:

Let k be the number of set bits.

Time = $O(k)$

Worst Case = $O(\log n)$

Space = $O(1)$

Example:

$n = 12$ (1100)

$12 \rightarrow 8 \rightarrow 0$

Set Bits = 2

Power of 2 Check:

```
bool isPowerOfTwo(int n) {
    return n > 0 && (n & (n - 1)) == 0;
}
```

Interview Summary:

Brian Kernighan's algorithm efficiently counts set bits by removing the lowest set bit in each iteration with $O(k)$ time and $O(1)$ space.