

Revision Notes: Find Two Unique Numbers Using XOR

Problem Statement:

Given an array where every number appears exactly twice except for two numbers that appear only once, find those two unique numbers using Bitwise XOR.

Key Properties of XOR:

- $a \wedge a = 0$ (same numbers cancel out)
- $a \wedge 0 = a$
- XOR is commutative and associative

Algorithm Steps:

- Step 1: XOR all elements of the array to get $res = unique1 \wedge unique2$.
- Step 2: Find the first set bit position k in res .
- Step 3: Divide the array elements based on the k -th bit.
- Step 4: XOR the selected group to get the first unique number.
- Step 5: XOR this value with res to get the second unique number.

Time & Space Complexity:

Time Complexity: $O(n)$

Space Complexity: $O(1)$

Important Interview Line:

First XOR all elements to cancel duplicates, then use the rightmost set bit to separate the two unique numbers.

Code with Clear Comments:

```
void findUniques(int *arr, int n)
{
    int res = 0;

    // Step 1: XOR all elements
    for(int i = 0; i < n; i++)
        res ^= arr[i];

    // Step 2: Find first set bit in res
    int temp = res, k = 0;
    while((temp & 1) == 0)
    {
        temp >>= 1;
        k++;
    }
```

```
}

// Step 3: XOR elements having k-th bit set
int firstUnique = 0;
for(int i = 0; i < n; i++)
if((arr[i] >> k) & 1)
firstUnique ^= arr[i];

// Step 4: Find second unique number
int secondUnique = firstUnique ^ res;

cout << firstUnique << " " << secondUnique;
}
```