

Assignment Week 9

Social Networks

1. Which of the following is true for $G(1000, 0.5)$ random network:
 - a. The density of the network will be 0.5
 - b. The clustering coefficient will be 0.5
 - c. Each node will be added with probability 0.5.
 - d. **Each edge will be placed with probability 0.5.**
2. Given set $E = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$, we pick a value a_1 uniformly at random from this set E . Next, we pick another value a_2 , again uniformly at random from this set E . Similarly we pick 8 more values, a_3, a_4, \dots, a_{10} . Look at the sum $S = a_1 + a_2 + \dots + a_{10}$. Let $p(i)$ be the probability that $S = i$, i.e., the probability that the sum of these randomly chosen 10 elements is i . We plot i on the X-axis and $p(i)$ on the Y axis. Choose the correct statement from the following:
 - a. The plot has very high values in the beginning but then drops.
 - b. The plot is a constant curve.
 - c. **The plot is a bell shaped curve.**
 - d. The plot is linear.

Explanation: The probability distribution of the sum of random variables depicts a bell shaped curve.

3. Power law degree distribution in real world networks generally follows the characteristic equation $y = 1/k^a$. What is the value of 'a' here?
 - a. $1 < a < 2$
 - b. **$2 < a < 3$**
 - c. $3 < a < 4$
 - d. None of the above

Explanation: In real world power law degree distributions, the value of 'a' has been observed to be between 2 and 3.

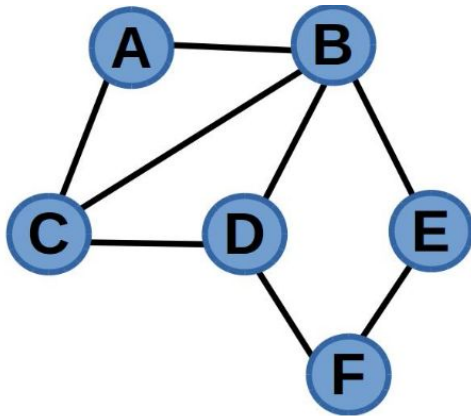
4. How does the power law degree distribution come by in real world networks?:
 - a. **By preferential attachment**
 - b. By random linking
 - c. By uniform edge connection
 - d. No hypothesis is found.

Explanation: Barabasi and Albert proposed a hypothesis that the real world networks are evolved using the preferential attachment and this gives birth to power law degree distribution.

5. In the preferential attachment, a new coming node will prefer to make the connection with the node having:
- Fewer friends
 - More friends**
 - Average number of friends
 - None of the above

Explanation: In the preferential attachment model, a new coming node prefers to make the connection with the node having the higher degree. So, this model gives birth to power law degree distribution.

6. Given a network being generated by 'rich get richer' phenomenon. The following Figure shows the snapshot of the network at time t . A new node 'u' enters the network at time $t+1$ and makes an edge with one of the existing nodes. The probability of 'u' making an edge with an existing node 'w' is defined as $p(w)$. Which of the following equations is correct?



- $p(A) < p(C) < p(B)$
- $p(E) < p(D) < p(B)$
- $p(F) < p(C) < p(B)$
- All of the above**

Explanation: $p(A) = 2/16$, $p(B) = 4/16$, $p(C) = 3/16$, $p(D) = 3/16$, $p(E) = 2/16$, $p(F) = 2/16$

7. Let G be a set of 5 graphs generated using Erdos-Renyi model with (n, p) parameters. Similarly, let H be a set of 5 graphs generated using Barabasi-Albert model with (n, m) parameters. Which of the following is true (Assume standard definitions for n , m and p):
- No. of edges in all the graphs in G is same, the no. of edges in all the graphs in H may vary.
 - No. of edges in all the graphs in H is same, the no. of edges in all the graphs in G may vary.**

- c. No. of edges in all the graphs in G is same, No. of edges in all the graphs in H is same
- d. No. of edges in all the graphs in both, G and H, varies in each iteration

Explanation: In (n, p) , p is the probability, while in (n, m) , m is the number of edges.

8. Given set $E = \{1, 2, 3, \dots, 19, 20\}$. We pick a value a_1 uniformly at random from this set E . Next, we pick another value a_2 , again uniformly at random from this set E . Similarly we pick 18 more values, a_3, a_4, \dots, a_{20} (a total of 20 numbers are picked). Look at the sum $S = a_1 + a_2 + \dots + a_{20}$. Which of the following sets define the range from which the sum S can have values from?
- a. $\{1, 2, \dots, 19, 20\}$
 - b. $\{20, 11, \dots, 19, 200\}$
 - c. $\{1, 2, \dots, 9, 400\}$
 - d. $\{20, 11, \dots, 399, 400\}$

Explanation: The minimum value of S will be 20 when all the selected elements a_1, a_2, \dots, a_{20} have a value 1 each. The maximum value of S will be 40000 when all the selected elements a_1, a_2, \dots, a_{20} have a value of 20 each. Hence the correct option is D.