

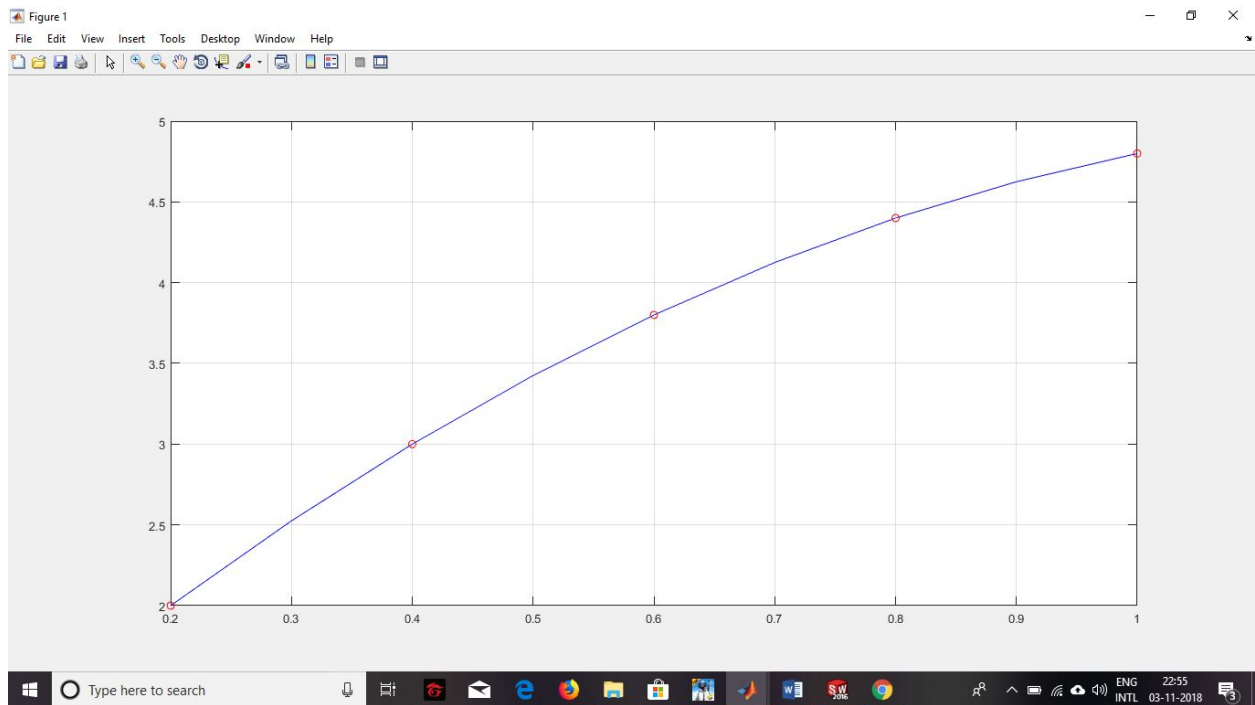
PA-3

a) Polynomial least square:-

5

0.2 0.4 0.6 0.8 1

2 3 3.8 4.4 4.8



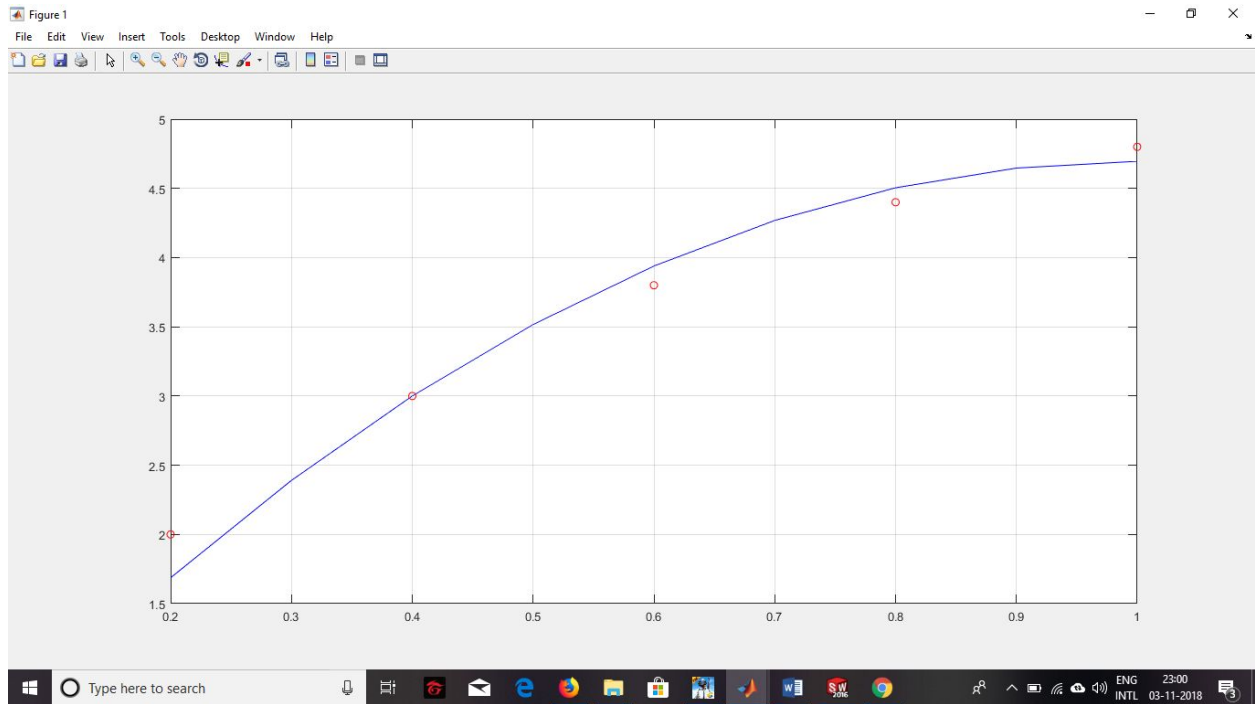
Coeff:-

$a=0.8000000000000014$

$b=6.4999999999999941$

$c=-2.4999999999999953$

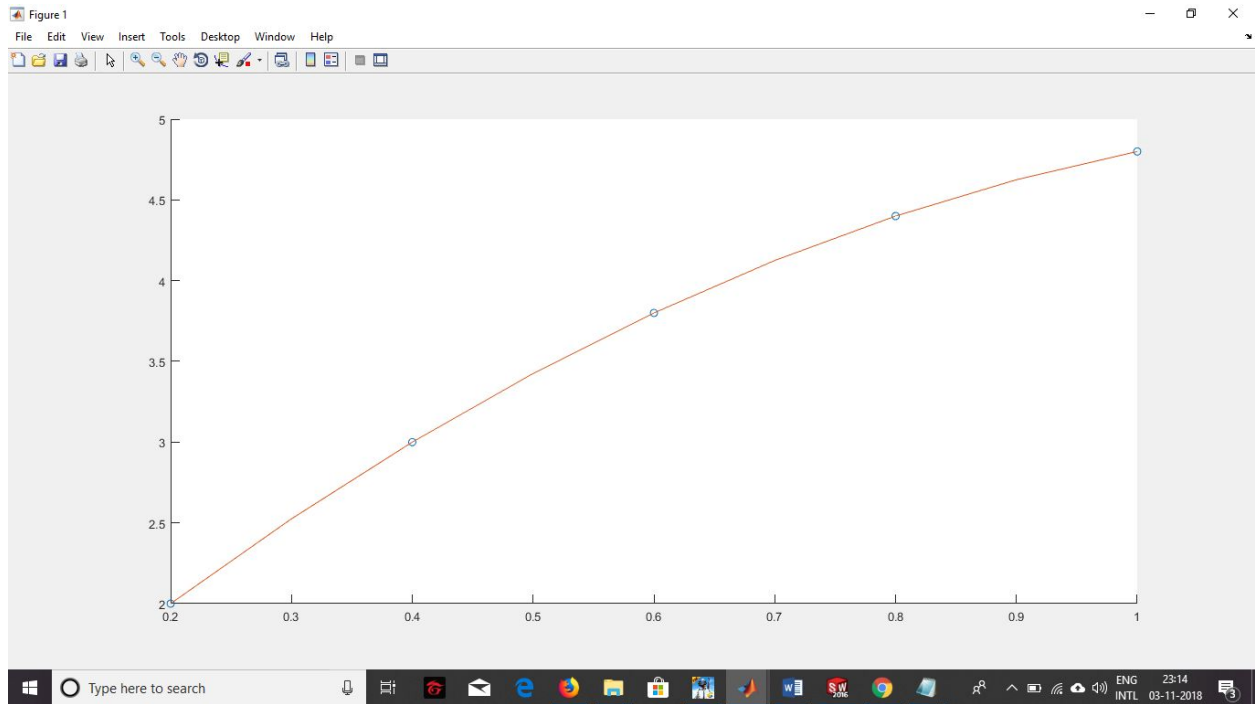
When intercept is zero:-



The Coefficients are a1 9.3696
The Coefficients are a2 -4.6739
The value or r_square is 0.972428

B)Lagrange Interpolation:-

5
0.2 0.4 0.6 0.8 1
2 3 3.8 4.4 4.8



C)Cubic Splines:-

4

0 2 4 8

1 0.7937 0.63 0.3968

1.Natural Spline

The Interval for Interpolation 0.000000 to 2.000000

The Coefficients are $a_3 = 0.0011$ $a_2 = 0.0000$ $a_1 = -0.1077$ $a_0 = 1.0000$

The Value of the first derivative at first node is -0.1077
and at second node is -0.0941

The Value of the second derivative at first node is 0.0000
and at second node is 0.0136

The Interval for Interpolation 2.000000 to 4.000000

The Coefficients are $a_3 = -0.0003$ $a_2 = -0.0088$ $a_1 = -0.1254$ $a_0 = 1.0118$

The Value of the first derivative at first node is -0.1648
and at second node is -0.2125

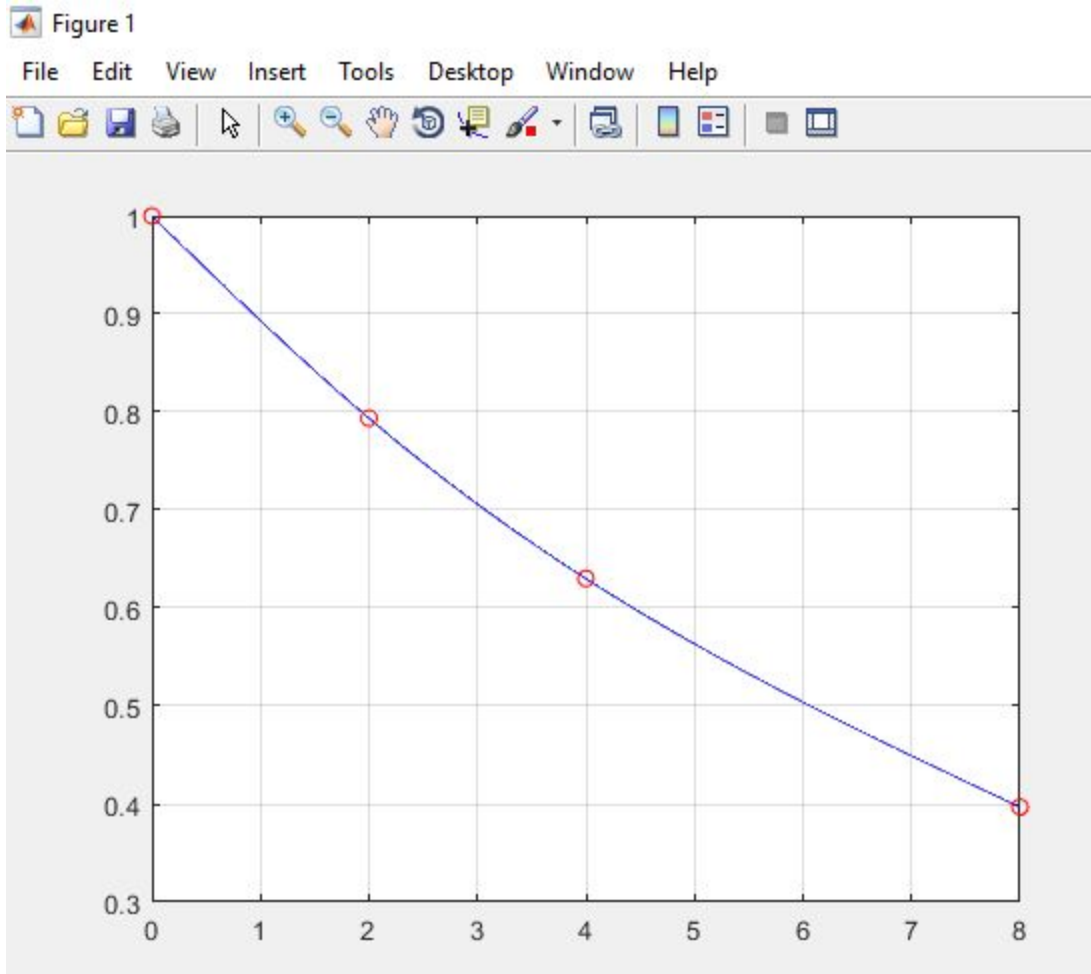
The Value of the second derivative at first node is 0.0136
and at second node is 0.0095

The Interval for Interpolation 4.000000 to 8.000000

The Coefficients are $a_3 = -0.0004$ $a_2 = -0.0095$ $a_1 = -0.1280$ $a_0 = 1.0153$

The Value of the first derivative at first node is -0.2231
and at second node is -0.3562

The Value of the second derivative at first node is 0.0095
and at second node is 0.0000



2)Not-a-Knot

The Interval for Interpolation 0.000000 to 2.000000

The Coefficients are $a_3 = -0.0004$ $a_2 = -0.0090$ $a_1 = -0.1197$ $a_0 = 1.0000$

The Value of the first derivative at first node is -0.1197
and at second node is -0.1601

The Value of the second derivative at first node is 0.0180
and at second node is 0.0137

The Interval for Interpolation 2.000000 to 4.000000

The Coefficients are $a_3 = -0.0004$ $a_2 = -0.0090$ $a_1 = -0.1257$ $a_0 = 1.0120$

The Value of the first derivative at first node is -0.1661
and at second node is -0.2151

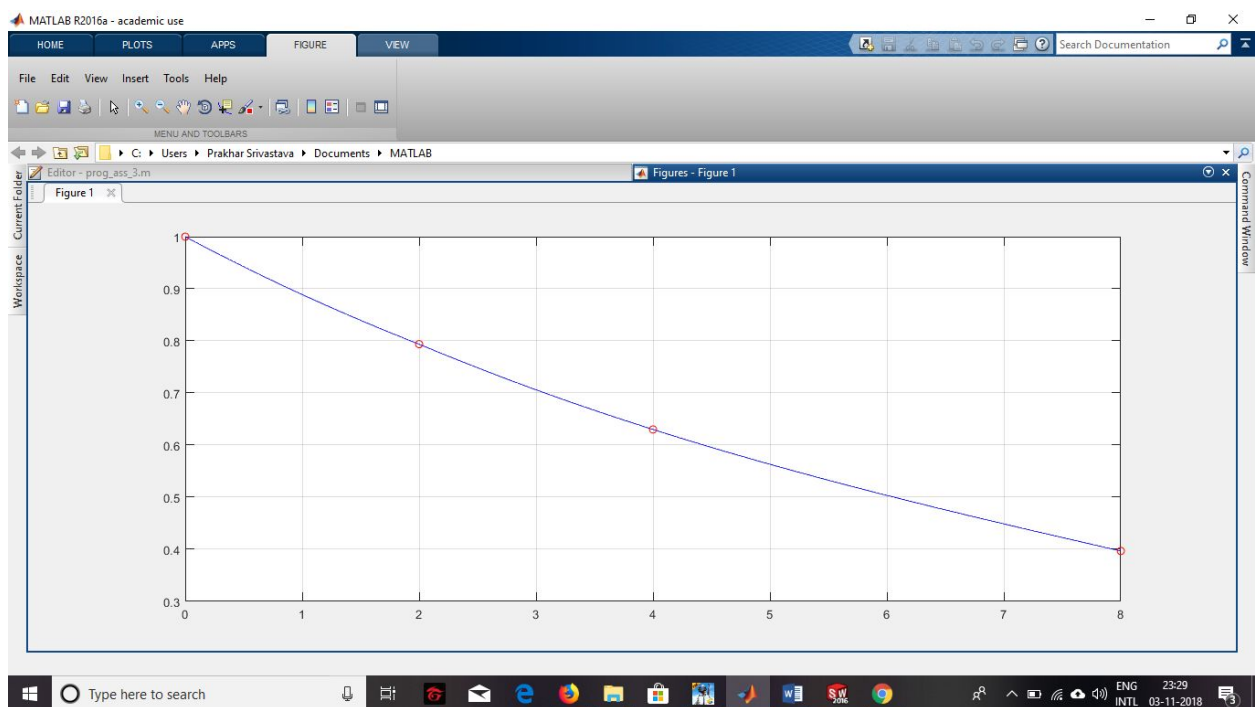
The Value of the second derivative at first node is 0.0137
and at second node is 0.0093

The Interval for Interpolation 4.000000 to 8.000000

The Coefficients are $a_3 = -0.0004$ $a_2 = -0.0090$ $a_1 = -0.1257$ $a_0 = 1.0120$

The Value of the first derivative at first node is -0.2151
and at second node is -0.3393

The Value of the second derivative at first node is 0.0093
and at second node is 0.0006



3)Periodic

The Interval for Interpolation 0.000000 to 2.000000

The Coefficients are $a_3 = 0.0007$ $a_2 = -0.0025$ $a_1 = -0.1110$ $a_0 = 1.0000$

The Value of the first derivative at first node is -0.1110
and at second node is -0.1127

The Value of the second derivative at first node is 0.0050
and at second node is 0.0135

The Interval for Interpolation 2.000000 to 4.000000

The Coefficients are $a_3 = -0.0007$ $a_2 = -0.0109$ $a_1 = -0.1278$ $a_0 = 1.0112$

The Value of the first derivative at first node is -0.1799
and at second node is -0.2488

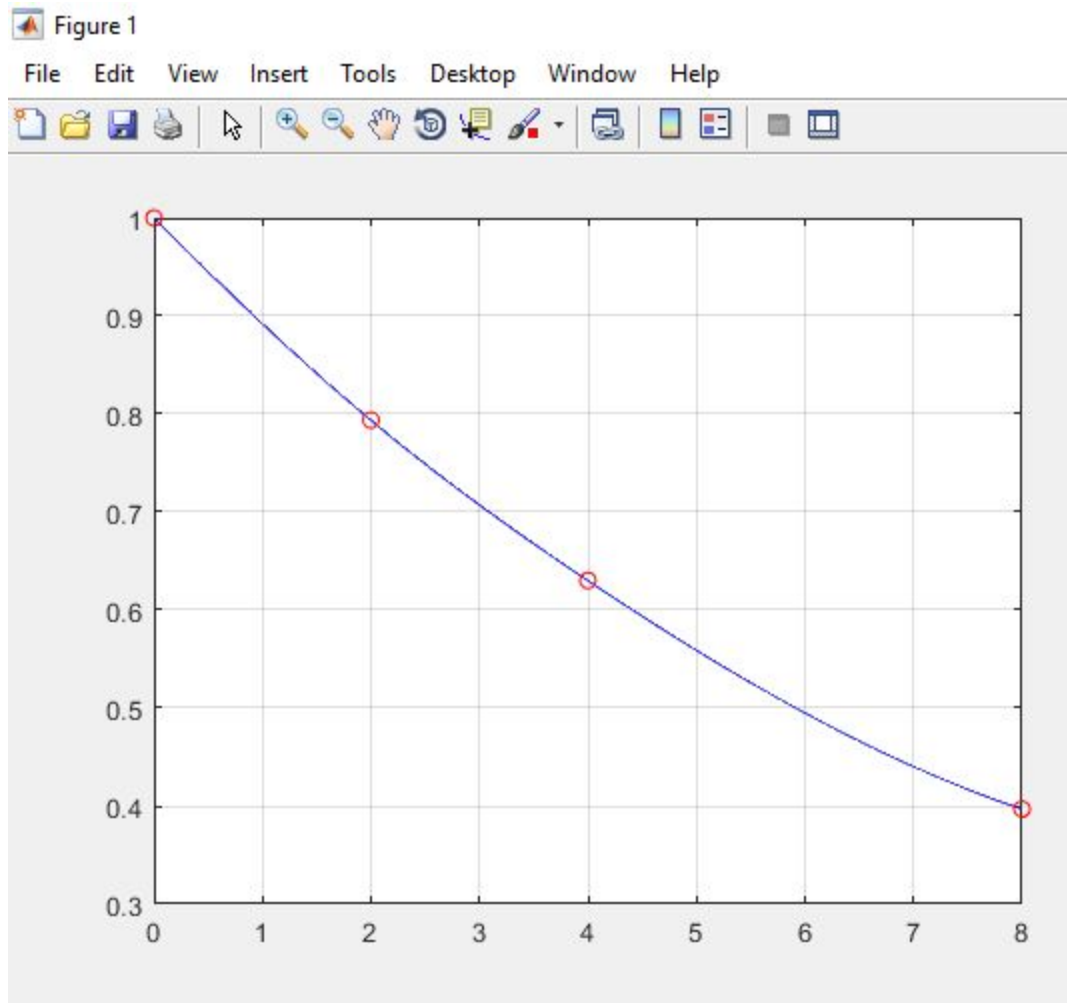
The Value of the second derivative at first node is 0.0135
and at second node is 0.0050

The Interval for Interpolation 4.000000 to 8.000000

The Coefficients are $a_3 = 0.0004$ $a_2 = 0.0017$ $a_1 = -0.0774$ $a_0 = 0.9440$

The Value of the first derivative at first node is -0.0472
and at second node is 0.0166

The Value of the second derivative at first node is 0.0050
and at second node is 0.0135



4)Clamped:-

Derivative at first node=4

Derivative at second node=6

The Interval for Interpolation 0.000000 to 2.000000

The Coefficients are $a_3 = 0.8168$ $a_2 = 3.6851$ $a_1 = 4.0000$ $a_0 = 1.0000$

The Value of the first derivative at first node is 4.0000
and at second node is 28.5414

The Value of the second derivative at first node is -7.3702
and at second node is 2.4309

The Interval for Interpolation 2.000000 to 4.000000

The Coefficients are $a_3 = -0.3934$ $a_2 = -3.5757$ $a_1 = -10.5215$ $a_0 = 10.6810$

The Value of the first derivative at first node is -29.5447
and at second node is -58.0087

The Value of the second derivative at first node is 2.4309
and at second node is -2.2895

The Interval for Interpolation 4.000000 to 8.000000

The Coefficients are $a_3 = 0.3324$ $a_2 = 5.1338$ $a_1 = 24.3163$ $a_0 = -35.7695$

The Value of the first derivative at first node is 81.3427
and at second node is 170.2812

The Value of the second derivative at first node is -2.2895
and at second node is 5.6885

