

Product except self.

nums	1	2	3	4	5
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ans	120	60	40	30	24
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Understanding the problem.

Conditions given in the question.

1.) $a * b = c$

where a, b are numbers from `nums` array

c : 32 bit int even after multiplying 2 32 bit ints.

2.) No division algo to be used.

Although its suggested, division algo is not to be used but let's explore it once to know what it is.

nums	1	2	3	4	5
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product = $1 * 2 * 3 * 4 * 5 = 120$

ans	$120/1$	$120/2$	$120/3$	$120/4$	$120/5$
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↓

ans	120	60	40	30	24
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But why we divided ??

Because we want to remove that element from product.

Why this is not suitable method?

- Division by zero is possible
- large values may cause underflow or overflow.



numo	1	2	3	4	5
	0	1	2	3	4

1

0
1
2
3
4

j

0	1	X	0	1	0	1	0	1	0	1
1	2		1	X	1	2	1	2	1	2
2	6		2	3	2	X	2	6	2	6
3	24		3	12	3	8	3	X	3	24
4	120		4	60	4	40	4	30	4	X
res	120		60		40		30		24	

Brute force.

~~100%~~ product = 1;

```
for i to n
    product = 1;
    for j to n
```

if $i == j$

~~Continue~~; continue;

else

```
product *= arr[j];
```

```
res[i] = product;
```

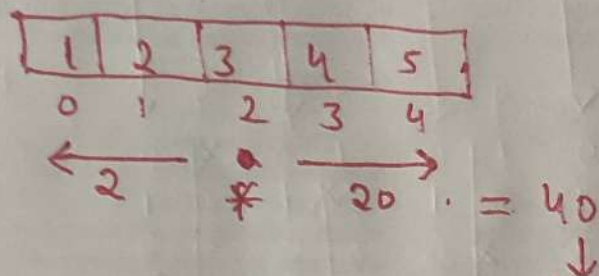
Time: $O(n^2)$

$$S: O(1)$$

Repetitive operations observed.

⇒ we are calculating the product repeatedly for each element from front and behind

For example



So if we calculate previous and next for each element we can find product except self for all.

nums

1	2	3	4	5
---	---	---	---	---

'prevProd' iterations must start from left as the first element would have no prev product and can be set to '1'

Similarly 'nextProd' must start from right as the last element would n't have any right product and can be set to '1'

Thus formulae for prevProd and nextProd are

$$\text{prevProd}[i] = \text{prevProd}[i-1] * \text{nums}[i-1]$$

$$\text{nextProd}[i] = \text{nextProd}[i+1] * \text{nums}[i+1]$$

⊗ Semi optimised code

nums

1	2	3	4	5
---	---	---	---	---

prevProd[0] = 1, nextProd[n-1] = 1

nums

1	2	3	4	5
---	---	---	---	---

prevProd

1	1	2	6	24
---	---	---	---	----

→ move right

nums

1	2	3	4	5
---	---	---	---	---

nextProd

120	60	20	5	1
-----	----	----	---	---

← move left

prevProd

1	1	2	6	24
---	---	---	---	----

*

nextProd

120	60	20	5	1
-----	----	----	---	---

Total Prod

120	60	40	30	24
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Pseudo code
n = nums.size();

res[n]

prevProd[n, 1]

nextProd[n, 1]

prevProd[0] = 1, nextProd[n-1];

for i to n (i++)

prevProd[i] = prevProd[i-1] * nums[i-1];

for i = n-2 to i >= 0 (i--)

~~next[i]~~

nextProd[i] = nextProd[i+1] * nums[i+1];

for i to n

res[i] = $\frac{\text{prev}[i]}{\text{prod}} * \text{nextProd}[i];$

return res;