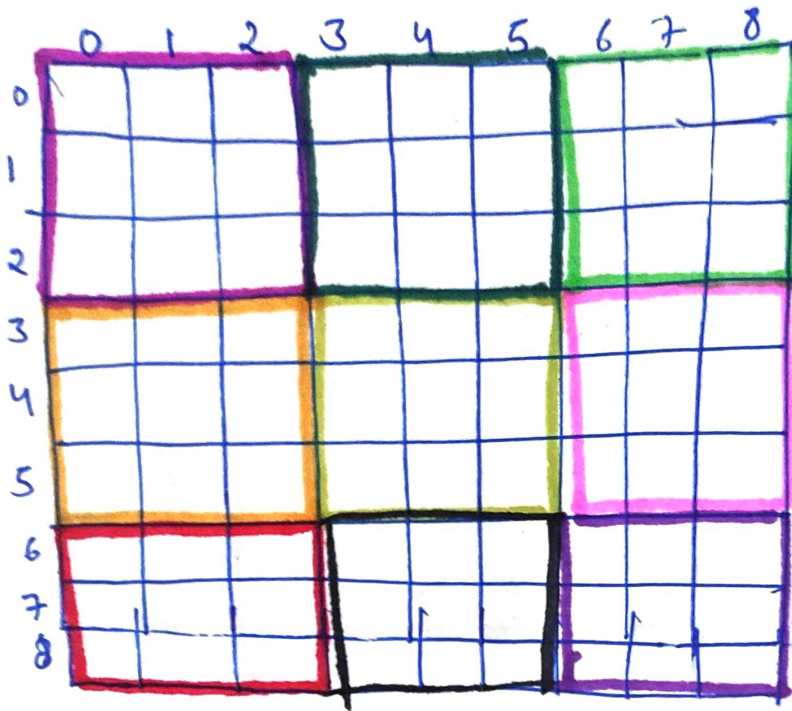


Valid Sudoku



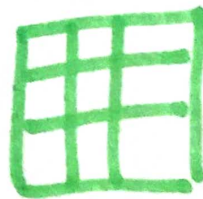
Question Type : Matrix

Data structures : Hashmap, HashSet.

Conditions for validity of Sudoku.

- Each row can contain 1-9 without repetition
- Each col can contain 1-9 without repetition

- Each grid box (3x3)



← This guy also can contain 1-9 without repetition.

- Partially filled is valid too.
(even iff unsolvable).

- Only filled cells needs to be checked.

(Corner case)

if (current == '.') \Rightarrow skip.

Bautifore.

→ For storing and calculating count, there are '2' approaches

- 1.) Use loops and determine the counts of ~~any~~ ^{all} elements ~~is duplicate~~ and then store it somewhere.
- 2.) Use hashmap or hashset for efficient find
Hashset would be better here but we would explore ^{how} the hashmap route for just checking ~~if~~ ^{if} that works.
- 3.) For calculating count we have 9 rows, 9 cols, 9 gridboxes
so for each of them we need to mark counts and check for validity at end.

- For rows and cols, its pretty straightforward
- For grid boxes its a bit hard.

Each grid has to be identified in some way so that elements are identified in particular of which grid they are.



	0	1	2	3	4	5	6	7	8
0	1	2	3	4	5	6	7	8	
1	4	5	6	7	8	9	0	1	
2	7	8	9	0	1	2	3	4	

	0	1	2	3	4	5	6	7	8
0	0	1	2	3	4	5	6	7	8
1	3	4	5	6	7	8	9	0	1
2	6	7	8	9	0	1	2	3	4

If we remove the smaller boxes and consider each grid box as its own; we can assign indexes to the grids in this way.

For rows : 0, 1, 2

For cols : 0, 1, 2.

So if any element has index $(4, 5)$

what would be its index in terms of grid box.

As we have identified that each gridbox is made of 3×3 matrix; there are '3' rows and '3' cols. in each box

\therefore If we divide the index by 3 we would get position in terms of whole box.

But why we are doing all these things

because if we know elements index in terms of grid box it will be easier to store count of each box.

The issue is the column number uniquely identifies the grid but the row number still won't give you the grid. **What do you mean??**

^{You will say} Each index is already getting identified according to grid index but the original indexes of each

grid box should be $(0, 1, 2, 3, 4, 5, 6, 7, 8, 9)$
~~for not~~ $(0, 1, 2)$ ^{not} $(0, 1, 2)$
_{for cols} _{for rows}

~~Why~~ We need to scale that number to form the grid index accurately for rows.

i.e. new gridRow index = $\left(\frac{i}{3}\right) * \text{scaling factor}$

$$(i') = \left(\frac{i}{3}\right) * 3$$

because each grid is 3×3 and if its resetting to $(0, 1, 2)$ we need to use 3 to ~~bring~~ upscale it.

\therefore Whole box index will be calculated in similar way as we calculate index of element in normal matrix

$$= (i + j) = (i' + j') * 2$$
$$= \left(\frac{i}{3}\right) * 3 + \left(\frac{j}{3}\right)$$

$$\therefore \text{grid } x = \frac{i}{3}, \text{ grid } y = \frac{j}{3}.$$

$$\mathbb{B}(4,5) \equiv \left(\frac{5}{3}, \frac{4}{3}\right) \equiv (1,1).$$

But this has an issue this will correctly locate the element in the grid if we expand the element calculated grid indexes of whole 9×9 grid.

1 $(i/3, j/3)$ of table 2

	0	1	2	3	4	5	6	7	8
0	(0,0)	(0,0)	(0,0)	(0,1)	(0,1)	(0,1)	(0,2)	(0,2)	(0,2)
1	(0,0)	(0,0)	(0,0)	(0,1)	(0,1)	(0,1)	(0,2)	(0,2)	(0,2)
2	(0,0)	(0,0)	(0,0)	(0,1)	(0,1)	(0,1)	(0,2)	(0,2)	(0,2)
3	(1,0)	(1,0)	(1,0)	(1,1)	(1,1)	(1,1)	(1,2)	(1,2)	(1,2)
4	(1,0)	(1,0)	(1,0)	(1,1)	(1,1)	(1,1)	(1,2)	(1,2)	(1,2)
5	(1,0)	(1,0)	(1,0)	(1,1)	(1,1)	(1,1)	(1,2)	(1,2)	(1,2)
6	(2,0)	(2,0)	(2,0)	(2,1)	(2,1)	(2,1)	(2,2)	(2,2)	(2,2)
7	(2,0)	(2,0)	(2,0)	(2,1)	(2,1)	(2,1)	(2,2)	(2,2)	(2,2)
8	(2,0)	(2,0)	(2,0)	(2,1)	(2,1)	(2,1)	(2,2)	(2,2)	(2,2)

Note:

We didn't multiply cols with scaling factor because cols were correct.

For example if we add $(1, 2)$ it would not point to right grid box index

$\downarrow \quad \downarrow$
row col

$$= 1 + 2 = 3 \neq 5$$

$\downarrow \text{row} \quad \downarrow \text{scaling factor}$

But if we add $(1 * 3 + 2)$

\uparrow
col

$$= 5 (\checkmark)$$

Also if we did the reverse

	0	1	2
0	0	1	2
3	3	4	5
6	6	7	8

$$(1 * 1 + 2 * 3)$$
$$= 1 + 6 = 7 (\times)$$

← imagine as it as this for ease.

Code

```
vector<unordered_map<int, int>> rows (9);  
vector<unordered_map<int, int>> cols (9);  
vector<unordered_map<int, int>> bones(9);  
board m[ ][ ] (matrix) // matrix.
```

// For rows validation

```
for i to 9  
    for j to 9  
        cur = board [i][j]  
        if cur == '.'  
            continue;  
        rows [i] [cur] ++;
```

// For cols validation .

```
for i to 9  
    for j to 9  
        cur = board [j] [i]  
        if if cur == '.'  
            continue;  
        cols [i] [cur] ++;
```

// For checking grid bones

boxIndex = (i/3)*3 + j/3

curr = board[~~box~~i][j];

if curr == '.'

continue;

bones[boxIndex][curr]++;

$T(n) = O(n^2)$

$S(n) = O(18n)$

// End check for the count.

for i do a

for ~~it~~ it : rows[i]

if it.second > 1
return false

for it : cols[i]

if it.second > 1
return false

for it : bones[i]

if it.second > 1
return false

return true;

Optimised .

1-) In Brute force we saw there were many repetitions done .

Taking '3' vectors of a hashmaps each which is a lot of memory

Now we would try to reduce that by using temp unordered sets for each ~~row~~ rows and cols and vector of unordered sets for bones .

(because ^{all} bones need to be checked ~~all~~ and there is no indexing for which is the current bone).

// For rows

for i to 9

unordered-set ^{char .} ~~set~~ rows

for j to 9

~~char~~ curr = board[i][j];

if curr == '.'

continue;

if row.count(curr)

return false;

row.insert(curr)

← return true;

// For cols.

for i to 9

~~for~~ unordered-set <char> col.

for j to 9.

curr = board[j][i]

if curr == '.'

continue;

if col.count(curr)

return false;

col.insert(curr;

// For rows.

vector < unordered-set <char> > rows(9);

for i to 9

for j to 9.

curr = board[i][j];

rowIndex = (i/3) * 3 + j/3

if curr == '.'

~~return~~ continue;

if rows[rowIndex].count(curr)

return false.

rows[rowIndex].insert(curr);

← return true;