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Nama: Prames Ray Loptan
NPM: 140810210059 - A

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$$\begin{aligned} 1. \quad 2y dx - x dy &= 0 & y &= vx \\ 2y dx &= x dy & y' &= xv' + v \\ 2y/x &= dy/dx \end{aligned}$$

$$\begin{aligned} xv' + v &= 2v & \Rightarrow x dv + v dx &= 2v dx \\ x dv &= v dx \end{aligned}$$

$$\frac{dv}{v} = \frac{dx}{x}$$

$$\int \frac{dv}{v} = \int \frac{dx}{x}$$

$$\ln|v| = \ln|x| + \ln c$$

$$\ln|y| - \ln|x| = \ln|x| + \ln c$$

$$\ln|y| = \ln|x^2| + \ln c$$

$$\ln|y| = \ln|cx^2|$$

$$y = cx^2$$

$$2. \quad \frac{dy}{dx} = \frac{x^2 + 3y^2}{2xy}$$

$$y = vx =$$

$$y' = xv' + v$$

$$xv' + v = \frac{x^2}{2xy} + \frac{3y^2}{2xy} = \frac{x}{2y} + \frac{3y}{2x}$$

$$2(xv' + v) = \frac{x}{y} + \frac{3y}{x}$$

$$= \frac{1}{v} + 3v$$

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$$2xu' + 2u = \frac{1+3v^2}{v}$$

$$2xu' = \frac{1+v^2}{v}$$

$$2x \frac{dv}{dx} = \frac{1+v^2}{v}$$

$$\frac{v}{1+v^2} dv = \frac{dx}{2x}$$

$$\int \frac{v}{1+v^2} dv = \int \frac{dx}{2x}$$

$$\frac{1}{2} \ln |1+v^2| = \frac{1}{2} \ln |x| + \ln C$$

$$\ln |1+y^2/x^2| = \ln |x|$$

$$y^2/x^2 = xC - 1$$

$$y^2 = (xC - 1)(x^2)$$

$$y = \pm (x^3 C - x^2)^{1/2}$$

$$3. \quad \frac{dy}{dx} = \frac{y^2 + 2xy}{x^2}$$

$$y = vx$$

$$y' = xv' + v$$

$$xv' + v = \frac{y^2}{x^2} + \frac{2xy}{x^2} \Rightarrow xv' + v = v^2 + 2v$$

$$xv' = v^2 + v$$

$$4. \quad \frac{dy}{dx} = \frac{x+3}{x-y}$$

$$y = vx$$

$$y' = xv' + v$$

$$xv' + v = \frac{x+3vx}{x-vx}$$

$$xv' = \frac{x+3vx - vx + v^2x}{x-vx}$$

$$= \frac{x+2vx + v^2x}{x-vx}$$

$$= \frac{x(1+2v+v^2)}{x(1-v)}$$

$$\frac{dv}{dx} x = \frac{(1+2v+v^2)}{(1-v)}$$

$$\int \frac{(1-v)}{1+2v+v^2} dv = \int \frac{1}{x} dx$$

$$-\frac{2}{v+1} - \ln |v+1| = \ln |x| + \ln |C|$$

$$-\frac{2}{v+1} = \ln |xC \left(\frac{y}{x} + 1 \right)|$$

$$-\frac{2}{\frac{y+x}{x}} = \ln |Cy + Cx|$$

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$$-2 \left(\frac{x}{y+x} \right) = \ln |cy + cx|$$

$$\frac{x}{y+x} = \ln |cy + cx|^{-1/2}$$

$$5. \quad \frac{dy}{dx} = \frac{x^2 + xy + y^2}{x^2}$$

$$y = vx$$

$$y' = xv' + v$$

$$\frac{dy}{dx} = \frac{x^2}{x^2} + \frac{xy}{x^2} + \frac{y^2}{x^2}$$

$$xv' + v = 1 + v + v^2$$

$$xv' = 1 + v^2$$

$$x \frac{dv}{dx} = 1 + v^2$$

$$\int \frac{dv}{1+v^2} = \int \frac{dx}{x}$$

$$\arctan(v) = \ln|x| + c$$

$$\arctan\left(\frac{y}{x}\right) = \ln|x| + c$$

$$\frac{y}{x} = \tan(\ln|x| + c)$$

$$y = \tan(\ln|x| + c) x$$

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$$1. \quad y^2 + xy = e^{-x}$$

$$p(x) = 2 \quad r(x) = e^{-x}$$

$$2dx = 2x + e$$

$$y = e^{-2x} \left(\int e^{2x} e^{-x} dx + c \right)$$

$$= e^{-2x} \left(\int e^x dx + c \right)$$

$$= e^{-x} + c e^{-2x} \Rightarrow \text{S.V.}$$

$$2. \quad (x+1)y' + y = x^2 - 1$$

$$\frac{y' + y}{x+1} = \frac{x^2}{x+1} - \frac{1}{x+1}$$

$$p(x) = \frac{1}{x+1} \Rightarrow h(x) = \int \frac{1}{x+1} dx \Rightarrow \ln(x+1)$$

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$$y = e^{-\ln(x+1)} \left(\int \frac{(x+1) - \frac{x^2-1}{(x+1)} dx + c}{(x+1)} \right)$$

$$= \frac{1}{x+1} \left(\frac{x^3}{3} - x + c \right) \Rightarrow$$

$$= \frac{x^3}{3(x+1)} - \frac{x}{x+1} + \frac{c}{x+1} \Rightarrow \text{SU}$$

3. $y' + y \tan x = \sec x$

$$P(x) = \tan x \Rightarrow h(x) = \int \tan x dx = -\ln|\cos(x)|$$

$$y = e^{\ln|\cos(x)|} \left(\int e^{-\ln|\cos(x)|} \sec x dx + c \right)$$

$$= \cos(x) \left(\int \frac{\sec(x)}{\cos(x)} dx + c \right)$$

$$= \cos(x) \left(\int \frac{1}{\cos(x)} dx + c \right)$$

$$= \cos(x) \tan(x) + c \cos(x) \Rightarrow \text{SU}$$

4. $y' + \frac{2y}{x+1} = (x+1)^2$

$$P(x) = \frac{2}{x+1} \Rightarrow h(x) = 2 \int \frac{1}{x+1} dx = 2 \ln|x+1| + c$$

$$y = e^{-\ln|x+1|^2} \left(\int e^{\ln|x+1|^2} (x+1)^2 dx + c \right)$$

$$= \frac{1}{(x+1)^2} \left(\int (x+1)^2 (x+1)^2 dx + c \right)$$

$$= \frac{1}{(x+1)^2} \left(\int u^4 du + c \right)$$

$$= \frac{1}{(x+1)^2} \left(\frac{u^5}{5} + c \right) \Rightarrow \frac{u^5}{5(x+1)^2} + \frac{c}{(x+1)^2}$$

$$= \frac{(x+1)^5}{5(x+1)^2} + \frac{c}{(x+1)^2} \Rightarrow \text{SU}$$

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$$g. \quad y' = e^{2x} - 3y$$

$$y(0) = 1$$

$$P(x) = 3 \Rightarrow h(x) = \int 3 dx = 3x + C$$

$$y = e^{-3x} \left(\int e^{3x} e^{2x} dx + C \right)$$

$$= e^{-3x} \left(\int e^{5x} dx + C \right)$$

$$= e^{-3x} \left(\frac{1}{5} e^{5x} + C \right)$$

$$= \frac{e^{2x}}{5} + e^{-3x} \cdot C \Rightarrow \text{SU}$$

$$1 = \frac{e^2}{5} + \frac{C}{e^3}$$

$$5e^3 = e^5 + 5C$$

$$5e^3 - e^5 = 5C$$

$$y = \frac{e^{2x}}{5} + \frac{5e^3 - e^5}{5e^3} \Rightarrow \text{SU}$$

$$1 = \frac{e^5 + 5C}{5e^3}$$

$$C = \frac{5e^3 - e^5}{5}$$