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1.

$$\sum_{n=1}^{\infty} \frac{n^2}{n^5 + 5}$$

$$a_n = \frac{n^2}{n^5 + 5}, \quad b_n = \frac{n^2}{n^5}$$

$$a_n = \frac{n^2}{n^5 + 5}, \quad b_n = \frac{1}{n^3} \rightarrow \sum_{n=1}^{\infty} \frac{1}{n^3} \rightarrow \text{uji banding } p(p=3), p > 1, \text{ maka konvergen}$$

$$\text{Karena } \frac{n^2}{n^5 + 5} < \frac{1}{n^3}, \text{ dan } \sum_{n=1}^{\infty} \frac{1}{n^3} \text{ konvergen, maka } \sum_{n=1}^{\infty} \frac{n^2}{n^5 + 5} \text{ konvergen}$$

2.

$$\sum_{n=6}^{\infty} \frac{1}{n-5}$$

$$a_n = \frac{1}{n-5} > b_n = \frac{1}{n} \rightarrow \sum_{n=6}^{\infty} \frac{1}{n} \rightarrow \text{uji banding } p(p=1), p \leq 1, \text{ maka divergen}$$

$$\text{Karena } \frac{1}{n-5} > \frac{1}{n} \text{ dan } \sum_{n=1}^{\infty} \frac{1}{n} \text{ divergen, maka } \sum_{n=6}^{\infty} \frac{1}{n-5} \text{ divergen}$$

3.

$$\sum_{n=1}^{\infty} \frac{1}{2^n + 1}$$

$$a_n = \frac{1}{2^n + 1} < b_n = \frac{1}{2^n}$$

uji b_n

$$\begin{aligned} \sum_{n=1}^{\infty} \frac{1}{2^n} &= \lim_{b \rightarrow \infty} \int_1^b \frac{1}{2^{bx}} dx = \left[-\frac{1}{\ln(2) \cdot 2^x} + C \right]_1^b \\ &= \lim_{b \rightarrow \infty} \left[-\frac{1}{\ln(2) \cdot 2^b} + \frac{1}{\ln(2) \cdot 2^1} \right] = \left[-\frac{1}{\infty} + \frac{1}{(0,6)2} \right] \\ &= 0 + \frac{1}{(0,6)(2)} = \frac{1}{(0,6)(2)} \end{aligned}$$

$$\text{Karena } a_n = \frac{1}{2^n + 1} < b_n = \frac{1}{2^n} \text{ dan } \sum_{n=1}^{\infty} \frac{1}{2^n} \text{ konvergen, maka}$$

$$\sum_{n=1}^{\infty} \frac{1}{2^n + 1} \text{ konvergen}$$

4. $\sum_{n=1}^{\infty} \frac{6 + \cos n}{n^2}$

$a_n = \frac{6 + \cos n}{n^2} < b_n = \frac{8}{n^2} \approx 0 \rightarrow 8 \sum_{n=1}^{\infty} \frac{1}{n^2} \rightarrow$ uji banding $P(P > 1)$, maka b_n konvergen

karena $a_n = \frac{6 + \cos n}{n^2} < b_n = \frac{8}{n^2}$ dan $\sum_{n=1}^{\infty} \frac{8}{n^2}$ konvergen, maka

$\sum_{n=1}^{\infty} \frac{6 + \cos n}{n^2}$ konvergen

5. $\sum_{n=1}^{\infty} \frac{1}{\sqrt{2n-1}}$

$a_n = \frac{1}{\sqrt{2n-1}} > b_n = \frac{1}{\sqrt{2n}} \rightarrow \frac{1}{\sqrt{2}\sqrt{n}} \rightarrow \frac{1}{\sqrt{2}} \sum_{n=1}^{\infty} \frac{1}{\sqrt{n}} \rightarrow$ uji banding $P(P \leq 1)$, maka

karena $a_n = \frac{1}{\sqrt{2n-1}} > b_n = \frac{1}{\sqrt{2n}}$ dan $\sum_{n=1}^{\infty} \frac{1}{\sqrt{2n}}$ divergen, maka b_n divergen

$\sum_{n=1}^{\infty} \frac{1}{\sqrt{2n-1}}$ adalah divergen

6. $\sum_{n=1}^{\infty} \frac{\sqrt{n}}{n-1}$

$a_n = \frac{\sqrt{n}}{n-1} > \frac{\sqrt{n}}{n} \rightarrow \sum_{n=1}^{\infty} \frac{1}{\sqrt{n}} \rightarrow$ uji banding $P(P \leq 1)$, maka b_n divergen.

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1. $\sum_{n=1}^{\infty} \frac{n}{n^2+2n+3} \quad B_n = \frac{n}{n^2}$

$$\lim_{n \rightarrow \infty} \frac{\frac{n}{n^2+2n+3}}{\frac{1}{n}} = \lim_{n \rightarrow \infty} \frac{n^2}{n^2+2n+3} = \lim_{n \rightarrow \infty} \frac{n^2}{n^2(1 + \frac{2}{n} + \frac{3}{n^2})}$$

$$\frac{1}{(1 + \frac{2}{\infty} + \frac{3}{\infty})} = \frac{1}{(1+0+0)} = 1$$

karena $\sum_{n=1}^{\infty} \frac{1}{n}$ adalah divergen, maka $\sum_{n=1}^{\infty} \frac{n}{n^2+2n+3}$ divergen

2. $\sum_{n=1}^{\infty} \frac{1}{n\sqrt{n+1}} = \sum_{n=1}^{\infty} \frac{1}{\sqrt{n^3+n^2}} \quad B_n = \frac{1}{\sqrt{n^3}}$

$$\lim_{n \rightarrow \infty} \frac{\frac{1}{n\sqrt{n+1}}}{\frac{1}{\sqrt{n^3}}} = \lim_{n \rightarrow \infty} \frac{\sqrt{n}}{\sqrt{n+1}} = \lim_{n \rightarrow \infty} \sqrt{\frac{n}{n(1+\frac{1}{n})}} = \sqrt{\frac{1}{1+0}} = 1$$

karena $\sum_{n=1}^{\infty} \frac{1}{\sqrt{n^3}}$ adalah konvergen, maka $\sum_{n=1}^{\infty} \frac{1}{n\sqrt{n+1}}$ konvergen

3. $\sum_{n=1}^{\infty} \frac{\sqrt{2n+3}}{n^2} \quad b_n = \frac{\sqrt{2n}}{n^2}$

$$\lim_{n \rightarrow \infty} \frac{\frac{\sqrt{2n+3}}{n^2}}{\frac{\sqrt{2n}}{n^2}} = \lim_{n \rightarrow \infty} \frac{\sqrt{2n+3}}{\sqrt{2n}} = \lim_{n \rightarrow \infty} \sqrt{\frac{2n(1+\frac{3}{2n})}{2n}} = \sqrt{\frac{1+\frac{3}{\infty}}{1}} = 1$$

karena $\sum_{n=1}^{\infty} \frac{\sqrt{2n}}{n^2}$ konvergen, maka $\sum_{n=1}^{\infty} \frac{\sqrt{2n+3}}{n^2}$ konvergen

4. $\sum_{n=1}^{\infty} \frac{3n+1}{n^3-4} \quad B_n = \frac{3n}{n^3} = \frac{3}{n^2}$

$$\lim_{n \rightarrow \infty} \frac{\frac{3n+1}{n^3-4}}{\frac{3}{n^2}} = \lim_{n \rightarrow \infty} \frac{3n+1}{n^3-4} \cdot \frac{n^2}{3} = \frac{3n^3+n^2-4n^2}{3n^3-12} = \frac{3n^3(1+\frac{n^2}{3n^3})}{3n^3(1-\frac{4}{n^3})}$$

$$= \frac{(1+\frac{1}{3n})}{(1-\frac{4}{n^3})} = \frac{(1+0)}{(1-0)} = 1$$

karena $\sum_{n=1}^{\infty} \frac{3}{n^2}$ konvergen, maka $\sum_{n=1}^{\infty} \frac{3n+1}{n^3-4}$ konvergen

$$5. \sum_{n=1}^{\infty} \frac{\ln n}{n^2} \quad b_n = \frac{1}{n^{3/2}}$$

$$\lim_{n \rightarrow \infty} \frac{\frac{\ln n}{n^2}}{\frac{1}{n^{3/2}}} = \frac{\ln n}{\sqrt{n}} = 0$$

karena $\sum_{n=1}^{\infty} \frac{\ln n}{(n)^{3/2}}$ konvergen, maka $\sum_{n=1}^{\infty} \frac{\ln n}{n^2}$ konvergen

$$6. \sum_{n=1}^{\infty} \frac{1}{2^n - 1} \quad b_n = \frac{1}{2^n}$$

$$\lim_{n \rightarrow \infty} \frac{\frac{1}{2^n - 1}}{\frac{1}{2^n}} = \lim_{n \rightarrow \infty} \frac{2^n}{2^n - 1} = \frac{2^n}{2^n(1 - \frac{1}{2^n})} = \frac{1}{1 - 0} = 1$$

karena $\sum_{n=1}^{\infty} \frac{1}{2^n}$ konvergen, maka $\sum_{n=1}^{\infty} \frac{1}{2^n - 1}$ konvergen

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1.

$$\sum_{n=1}^{\infty} \frac{n^2}{n!}$$

$$a_n = \frac{n^2}{n!} \quad a_{n+1} = \frac{(n+1)^2}{(n+1)!}$$

$$P = \lim_{n \rightarrow \infty} \frac{\frac{(n+1)^2}{(n+1)!}}{\frac{n^2}{n!}} = \lim_{n \rightarrow \infty} \frac{(n+1)^2}{(n+1)!} \cdot \frac{n!}{n^2} = \frac{(n+1)^2}{(n+1)(n!)} \cdot \frac{(n!)}{n^2} = \frac{(n+1)}{n^2} = \frac{n^2 \left(\frac{1}{n} + \frac{1}{n^2} \right)}{n^2} = 0$$

karena $P = 0$, $P < 1$, maka $\sum_{n=1}^{\infty} \frac{n^2}{n!}$ konvergen

2.

$$\sum_{n=1}^{\infty} \frac{n!}{4^n}$$

$$a_n = \frac{n!}{4^n} \quad a_{n+1} = \frac{(n+1)!}{4^{n+1}}$$

$$P = \lim_{n \rightarrow \infty} \frac{\frac{(n+1)!}{4^{n+1}}}{\frac{n!}{4^n}} = \frac{(n+1)(4^n)}{(4^{n+1})(1)} = \infty$$

karena $P = \infty$, $P > 1$, maka $\sum_{n=1}^{\infty} \frac{n!}{4^n}$ Divergen

3.

$$\sum_{n=1}^{\infty} \frac{n!}{n^n}$$

$$a_n = \frac{n!}{n^n} \quad a_{n+1} = \frac{(n+1)!}{(n+1)^{n+1}}$$

$$\lim_{n \rightarrow \infty} \frac{\frac{(n+1)!}{(n+1)^{n+1}}}{\frac{n!}{n^n}} = \frac{(n+1)(n^n)}{(n+1)(n+1)^n} = \left(\frac{n}{n+1} \right)^n = \frac{1}{\left(\frac{n+1}{n} \right)^n} = \frac{1}{\left(1 + \frac{1}{n} \right)^n} = \frac{1}{e} < 1$$

karena $P = \frac{1}{e}$, $P < 1$, maka $\sum_{n=1}^{\infty} \frac{n!}{n^n}$ konvergen

$$4. \sum_{n=1}^{\infty} \frac{4^n + n}{n!}$$

$$a_n = \frac{4^n + n}{n!} \quad a_{n+1} = \frac{4^{n+1} + (n+1)}{(n+1)!}$$

$$\lim_{n \rightarrow \infty} \frac{4^{n+1} + (n+1)}{(n+1)!} \cdot \frac{n!}{4^n + n} = \frac{(4^{n+1}) + (n+1)}{(n+1)(4^n + n)} = \frac{4^{n+1}}{(n+1)(4^n + n)} + \frac{n+1}{(n+1)(4^n + n)}$$

$$4 \lim_{n \rightarrow \infty} \frac{a_n}{4^n \left(\frac{4}{4^n} + \frac{1}{4^n} \right) \left(1 + \frac{n}{4^n} \right)} = 4(0+0) = 0$$

$$\sum_{n=1}^{\infty} \frac{4^n + n}{n!} \text{ konvergen, karena } p=0, p < 1$$

$$6. \sum_{n=1}^{\infty} \frac{n^3}{(2n)!}$$

$$a_n = \frac{n^3}{(2n)!} \quad a_{n+1} = \frac{(n+1)^3}{(2n+2)!}$$

$$\lim_{n \rightarrow \infty} \frac{(n+1)^3}{(2n+2)!} \cdot \frac{(2n)!}{n^3} = \frac{(n+1)^3}{(2n+2)(n^3)} = \frac{(n+1)(n+1)^2}{2(n+1)(n^3)}$$

$$\frac{1}{2} \lim_{n \rightarrow \infty} \frac{(n+1)^2}{n^3} = \frac{n^3 \left(\frac{1}{n^2} + \frac{2}{n^3} \right)}{n^3} = \left(\frac{1}{2} \right) (0+0) = 0$$

$$\sum_{n=1}^{\infty} \frac{n^3}{(2n)!} \text{ konvergen, karena } p=0, p < 1$$

$$5. \sum_{n=1}^{\infty} \frac{5+n}{n!}$$

$$a_n = \frac{5+n}{n!} \quad a_{n+1} = \frac{5+(n+1)}{(n+1)!}$$

$$\lim_{n \rightarrow \infty} \frac{5+(n+1)}{(n+1)!} \cdot \frac{n!}{5+n} = \frac{5+(n+1)}{(n+1)(5+n)} = \frac{5}{(n+1)} + \frac{(n+1)}{(n+1)} = \frac{0+1}{\infty} = 0$$

$$\sum_{n=1}^{\infty} \frac{5+n}{n!} \text{ konvergen, karena } p=0, p < 1$$