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$$1. \quad f(x) = \frac{1}{1+x} = \frac{1}{1-(-x)} = \sum_{n=0}^{\infty} (-x)^n = \sum_{n=0}^{\infty} (-1)^n x^n$$

$$2. \quad f(x) = \frac{1}{(1+x)^2} = D_x \left(\frac{1}{1-(-x)} \right) = \sum_{n=0}^{\infty} n (-x)^{n-1}$$

$$3. \quad f(x) = \frac{x^2}{1+x} = x^2 \frac{1}{1-(-x)} = x^2 \sum_{n=0}^{\infty} (-x)^n x^2 = \sum_{n=0}^{\infty} (-1)^n x^{n+2}$$

$$4. \quad f(x) = \frac{1}{1-(-x^2)} = \sum_{n=0}^{\infty} (-1)^n x^{2n}$$

$$5. \quad f(x) = \tan^{-1}(x) = \sum_{n=0}^{\infty} \frac{x^{2n+1}}{2n+1} = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots$$

$$\begin{aligned} 6. \quad f(x) &= \ln \left(\frac{1-x}{1+x} \right) = \ln(1-x) - \ln(1+x) \\ &= \left(\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} (-x)^n \right) - \left(\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} x^n \right) \\ &= \left(\sum_{n=1}^{\infty} \frac{(x)^n}{n} \right) - \left(\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} x^n \right) \\ &= \sum_{n=1}^{\infty} \left(\frac{(x)^n}{n} - \frac{(-1)^{n+1}}{n} x^n \right) \\ &= \sum_{n=1}^{\infty} \left(\frac{x^n}{n} (1 - (-1)^{n+1}) \right) \end{aligned}$$

$$7. \quad f(x) = \frac{1}{(2+\sqrt{x})} = \frac{\sqrt{x}}{1+\sqrt{x}} = \frac{1}{2} \cdot \frac{1}{1-(-\frac{1}{2}\sqrt{x})} = \frac{1}{2} \sum_{n=0}^{\infty} (-1)^n \left(\frac{\sqrt{x}}{2} \right)^n$$

$$8. \quad f(x) = e^x + e^{-x} = \sum_{n=0}^{\infty} \frac{x^n}{n!} + \sum_{n=0}^{\infty} \frac{(-1)^n x^n}{n!} = \sum_{n=0}^{\infty} \frac{x^n}{n!} (1 + (-1)^n)$$

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$$F(x) = e^{3x} = \sum_{n=0}^{\infty} \frac{(3x)^n}{n!}$$