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Kelas: A

TUGAS 10 (INTEGRAL)

Carilah anti turunan $f(x) + C$

1. $f(x) = 3x^2 + 10x + 5$

$$\begin{aligned}\int f(x) &= \int 3x^2 + 10x + 5 \\ &= \frac{3x^3}{3} + \frac{10x^2}{2} + \frac{5x^1}{1} + C \\ &= x^3 + 5x^2 + 5x + C\end{aligned}$$

2. $f(x) = x^2(20x^7 - 7x^5 + 6)$
 $= 20x^9 - 7x^7 + 6x^2$

$$\begin{aligned}\int f(x) &= \int 20x^9 - 7x^7 + 6x^2 \\ &= \frac{20x^{10}}{10} - \frac{7x^8}{8} + \frac{6x^3}{3} + C \\ &= 2x^{10} - \frac{7}{8}x^8 + 2x^3 + C\end{aligned}$$

3. $f(x) = x^{-3/4}$

$$\begin{aligned}\int f(x) &= \int x^{-3/4} \\ &= \frac{x^{-3/4+1}}{-3/4+1} + C \\ &= \frac{x^{1/4}}{1/4} + C\end{aligned}$$

$$\begin{aligned}&= \frac{4}{1} \cdot x^{1/4} + C \\ &= 4x^{1/4} + C \\ &= 4\sqrt[4]{x} + C\end{aligned}$$

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Selesaikan integral tak tentu berikut

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4.

$$\int (x^2 - 9)^3 \cdot 2x \, dx$$

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misal : $u = x^2 - 9$ $\left\{ \begin{array}{l} du = 2x \, dx \\ dx = \frac{du}{2x} \end{array} \right.$

$$\Rightarrow \int (u)^3 \cdot \cancel{2x} \cdot \frac{du}{\cancel{2x}}$$

$$= \int u^3 \cdot du$$

$$= \frac{1}{4} u^4 + C$$

$$= \frac{1}{4} (x^2 - 9)^4 + C //$$

5.

$$\int (x^2 - 3x + 2)^2 (2x - 3) \, dx$$

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misal : $u = x^2 - 3x + 2$ $\left\{ \begin{array}{l} du = 2x - 3 \, dx \\ dx = \frac{du}{2x - 3} \end{array} \right.$

$$\Rightarrow \int (u)^2 \cdot \cancel{2x - 3} \cdot \frac{du}{\cancel{2x - 3}}$$

$$= \frac{1}{3} u^3 + C$$

$$= \frac{1}{3} (x^2 - 3x + 2)^3 + C //$$

Hitung $\int_0^5 f(x) dx$

$$f(x) = \begin{cases} x+2, & 0 \leq x < 2 \\ 6-x, & 2 \leq x \leq 5 \end{cases}$$

$$\int_0^5 f(x) = \int_0^2 (x+2) dx + \int_2^5 (6-x) dx$$

$$= \left. \frac{1}{2}x^2 + 2x \right|_0^2 + \left. 6x - \frac{1}{2}x^2 \right|_2^5$$

$$= ((2+4) - (0)) + ((30 - \frac{25}{2}) - (12-2))$$

$$= 6 + \frac{15}{2}$$

$$= \frac{27}{2} // = 13 \frac{1}{2} //$$

$$f(x) = |x-1| = \begin{cases} x-1, & x \geq 1 \\ -(x-1), & x < 1 \end{cases}$$

$$\int_0^5 f(x) = \int_0^1 -(x-1) dx + \int_1^5 (x-1) dx$$

$$= \left. -\frac{1}{2}x^2 + x \right|_0^1 + \left. \frac{1}{2}x^2 - x \right|_1^5$$

$$= ((-\frac{1}{2} + 1) - (0)) + ((\frac{25}{2} - 5) - (\frac{1}{2} - 1))$$

$$= \frac{1}{2} + 8$$

$$= \frac{17}{2} //$$

$$= 8 \frac{1}{2} //$$