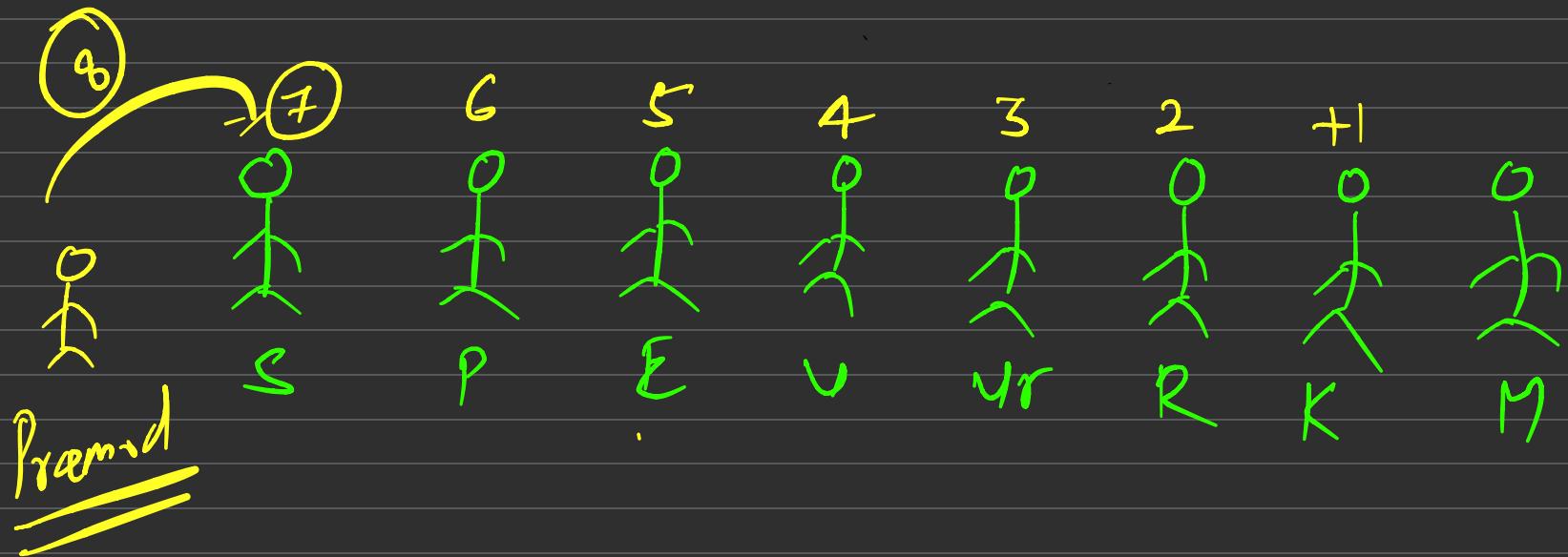


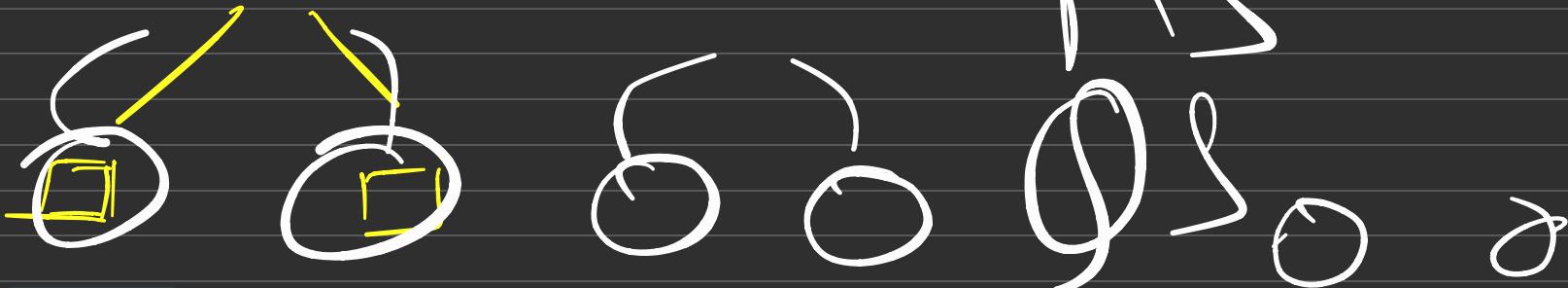
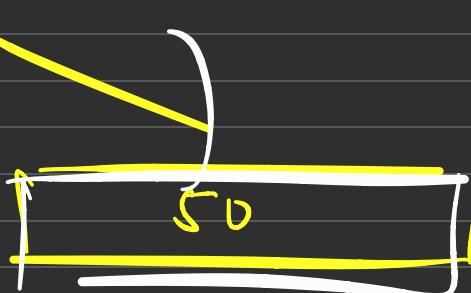
*Learning is a lifelong process of keeping your mind open to new ideas and experiences.*

## RECURSION & BACKTRACKING

- RECURSIVE TREE
- DRY RUN
- FUNCTION CALL







$x = 1 \cancel{2} \cancel{3} \ 4 \ \cancel{+ 10}$



$1 + (2 \cancel{3} 4)$



$2 + (3 \cancel{4})$

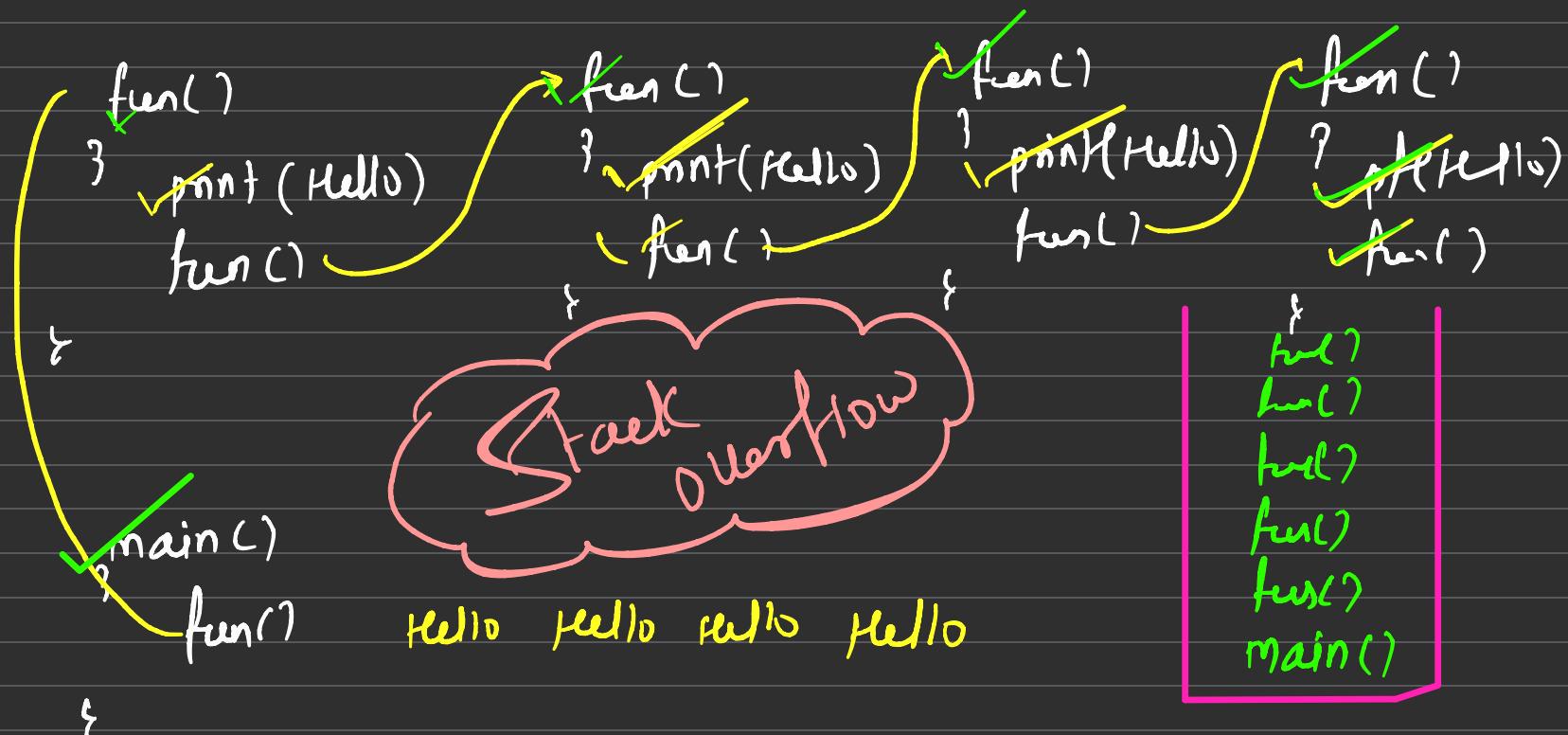


$\cancel{3} + (4)$

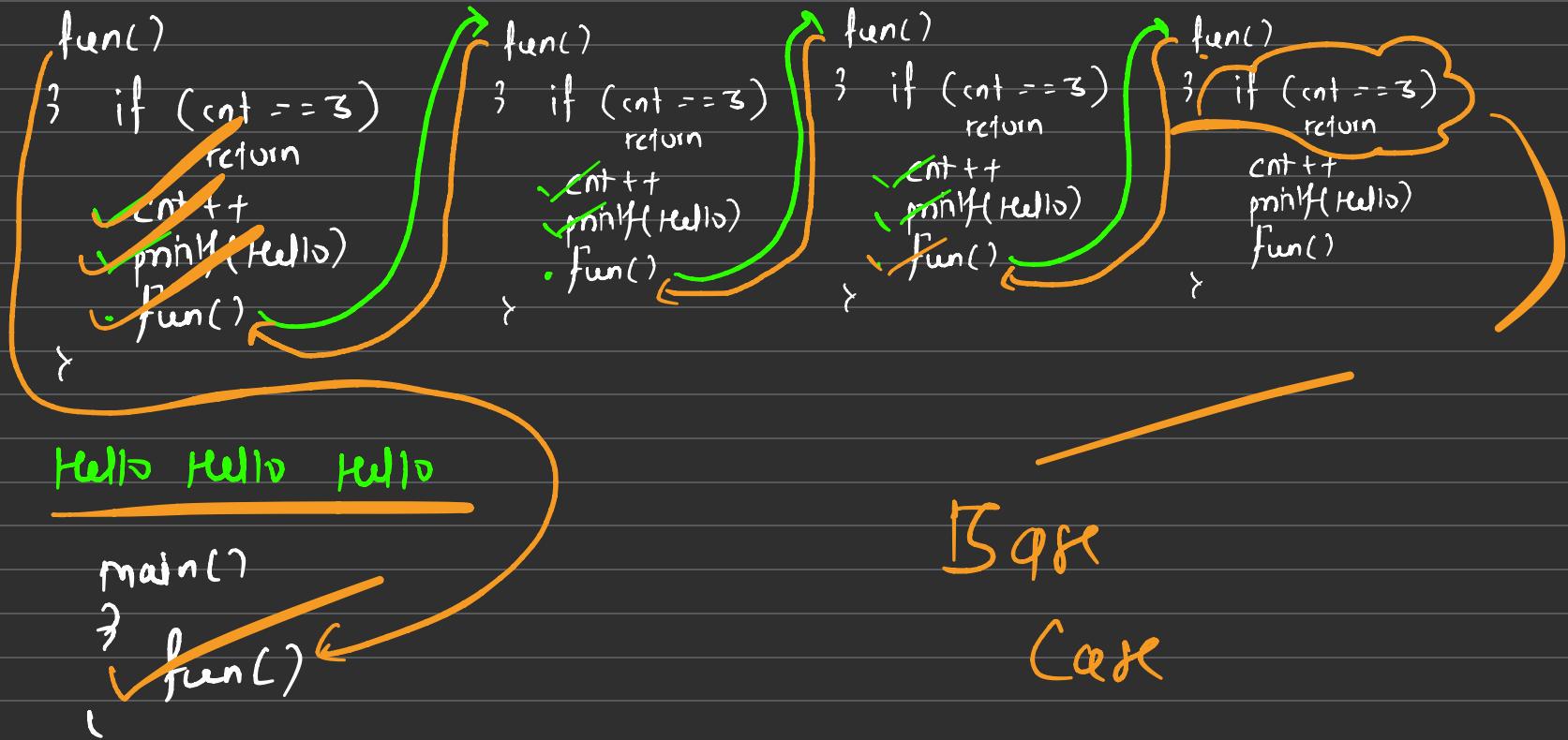


## What is Recursion

Function calling itself until a specific condition is called as Recursion.



$\text{cnt} = 0 \times 2^3$



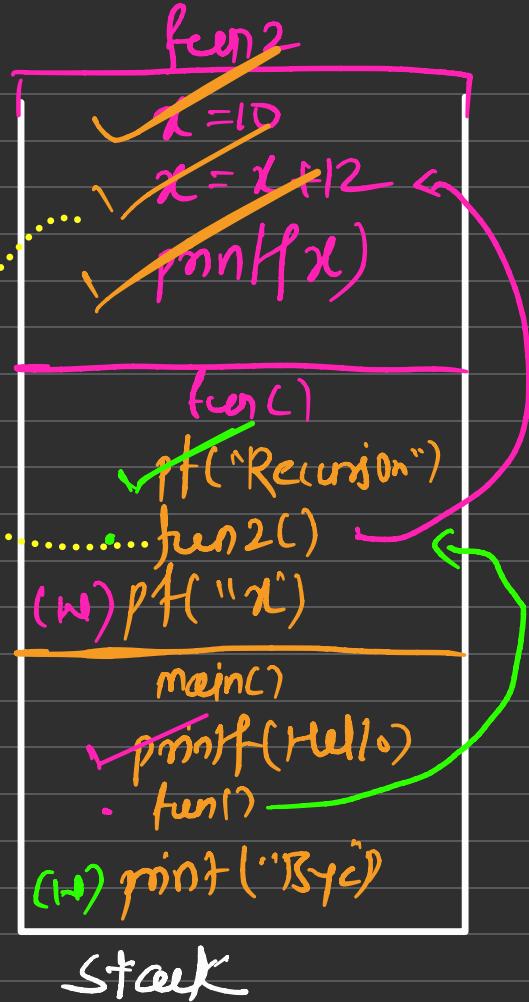
## Activation Stack Record

✓ main()  
} print("Hello")  
fun()  
print("Bye")

t  
fun()  
} print("Recursion")  
fun2()  
print("x")

fun2()  
}  $x = 10$   
 $x = x + 12$   
printf(x)

Hello  
Recursion  
12  
x  
Bye



## Print Numbers from 1 to N

```
void fun (int n)
{
    if(n > 4) return
    printf(n)
    fun(n+1)
```

```
void fun (int n)
{
    if(n > 4) return
    printf(n)
    fun(n+1)
```

```
void fun (int n)
{
    if(n > 4) return
    printf(n)
    fun(n+1)
```

```
void fun (int n)
{
    if(n > 4) return
```

```
printf(n)
```

```
fun(n+1)
```

5

```
void fun (int n)
{
    if(n > 4) return
```

```
printf(n)
fun(n+1)
```

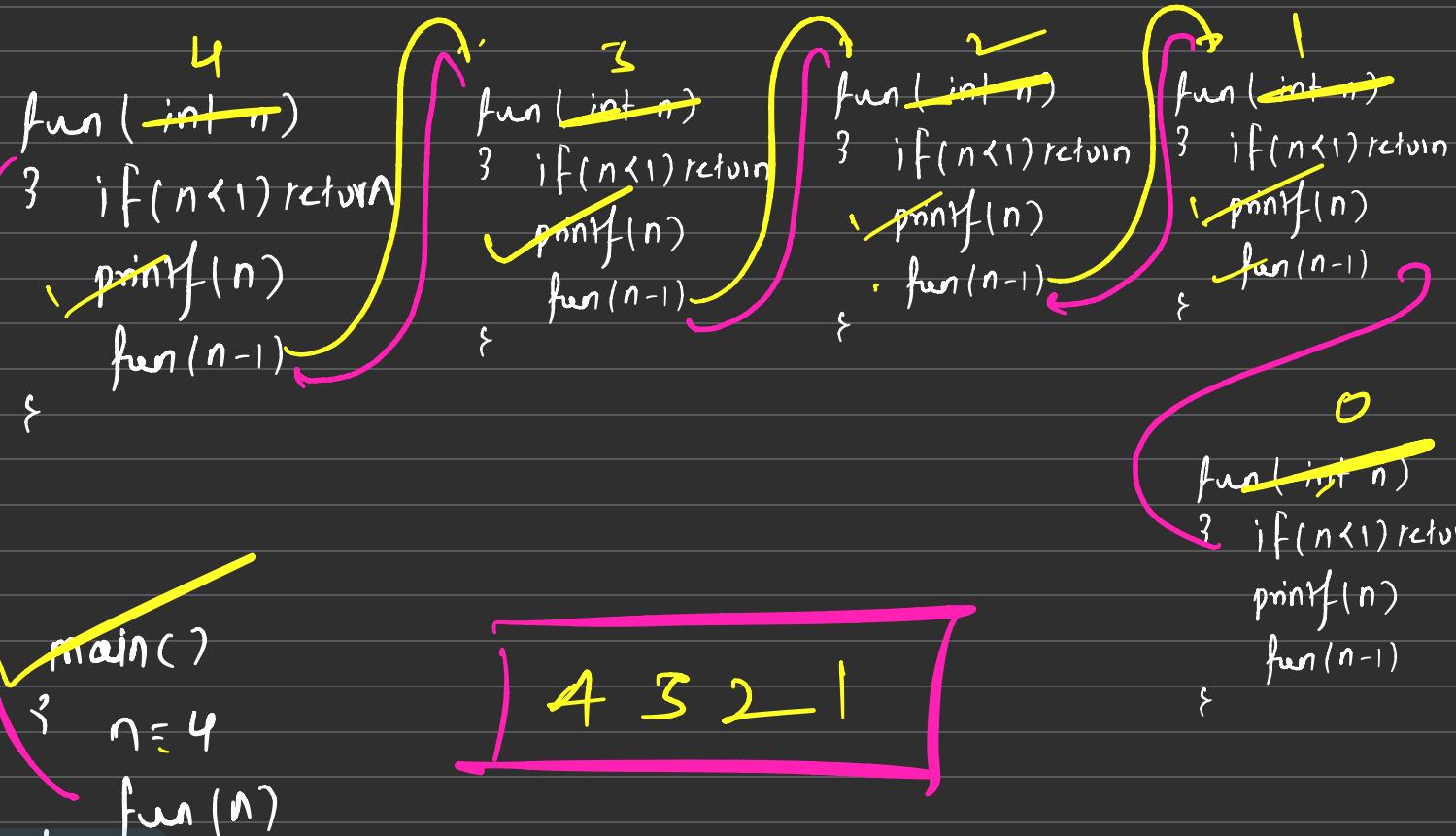
4

1 2 3 4

main()
{ }

fun(1)

## Print Numbers from N to 1

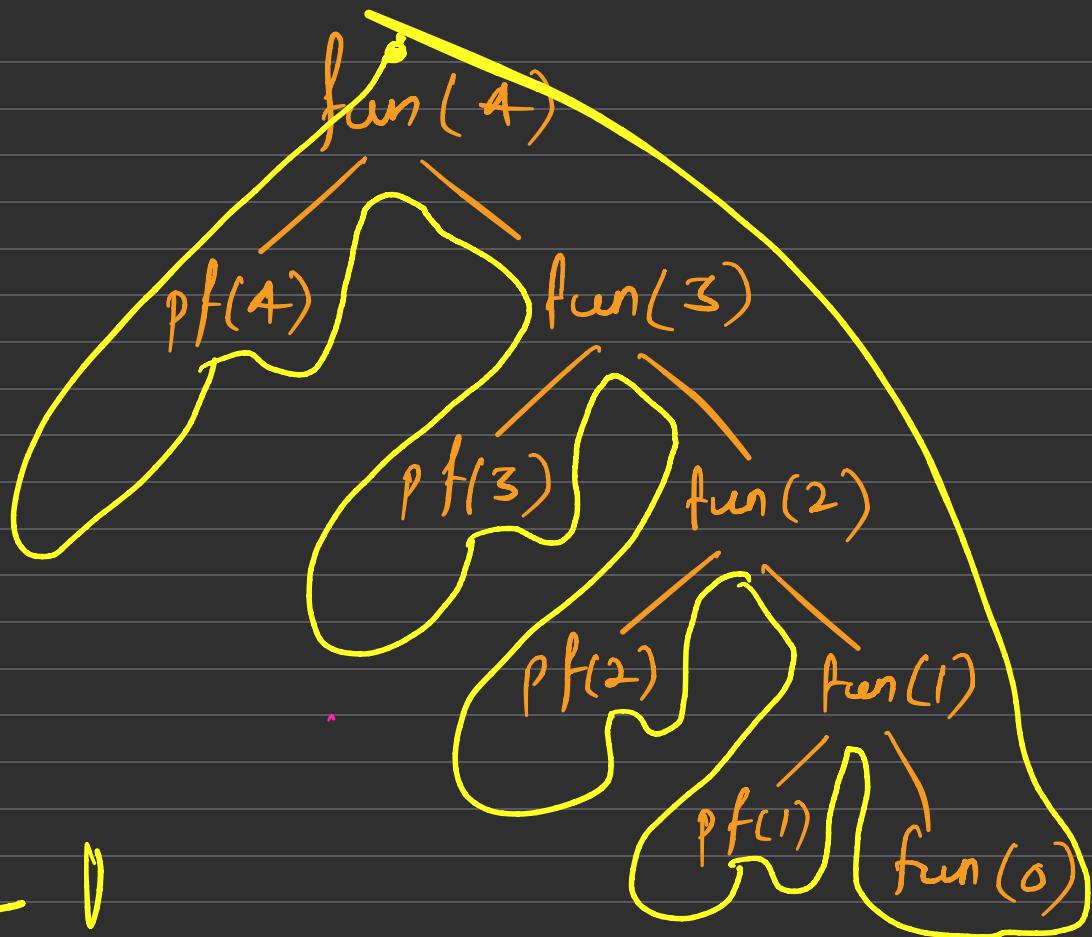


## Recursive Tree

```
fun( int n )
{ if(n<1) return
  printf(n)
  fun(n-1)
}
```

$N=4$

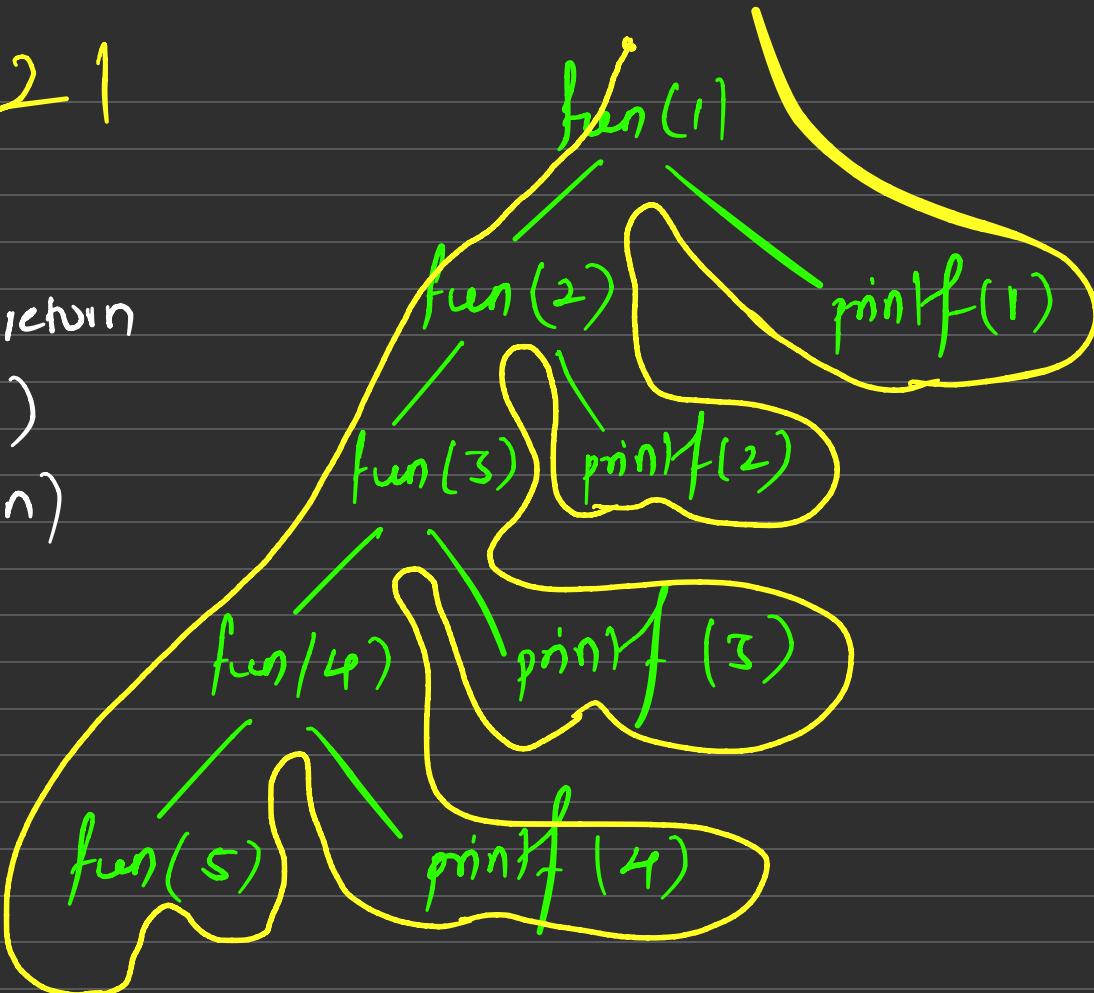
4 3 2 1



4 3 2 1

```
fun( int n )
3 if(n > 4) return
    fun(n+1)
}
{ printf(n)
```

fun(1)



print} in same order

print} (N)

fun (N+1)

fun (N+1)

print} (N)

print in Reverse Order

## Parameterised and Functional Recursion

### Parameterised Recursion

Find the Sum of all the numbers from 1 to N

```
main()
{
    N = 4
    sum = 0
    fun(1, N, sum)
}
```

```
void fun(i, N, sum)
{
    if (i > N)
        print(sum)
    return
    sum = sum + i
    fun(i+1, N, sum)
}
```

N=4

Sum = ~~0~~ ~~10~~ 10

1  
void fun(L, N, sum)  
{  
 if (i > N)  
 print(sum)  
 return  
 sum = sum + i  
 fun(i+1, N, sum)

2  
void fun(L, N, sum)  
{  
 if (i > N)  
 print(sum)  
 return  
 sum = sum + i  
 fun(i+1, N, sum)

3  
void fun(L, N, sum)  
{  
 if (i > N)  
 print(sum)  
 return  
 sum = sum + i  
 fun(i+1, N, sum)

4  
void fun(L, N, sum)  
{  
 if (i > N)  
 print(sum)  
 return  
 sum = sum + i  
 fun(i+1, N, sum)

5  
void fun(L, N, sum)  
{  
 if (i > N)  
 print(sum)  
 return  
 sum = sum + i  
 fun(i+1, N, sum)





## Functional Recursion

Find the Sum of all the numbers from 1 to N

main()

{  
    N = 4

    ans = fun(n)  
    print(ans)

~~}~~

10

int fun(int n)  
{  
    if (n == 0)  
        return 0

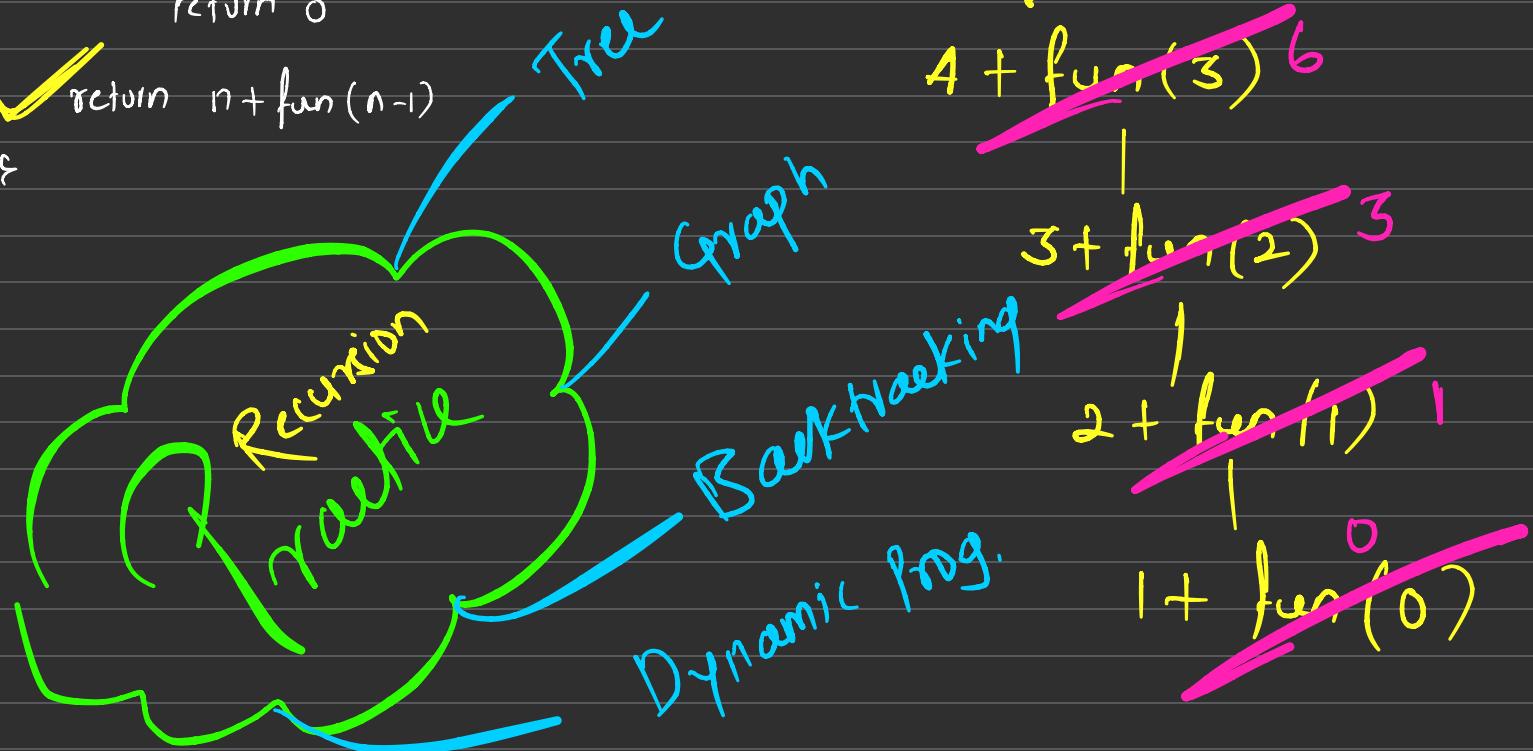
    return n + fun(n - 1)

8

```
int fun(int n)
{ if (n == 0)
    return 0
```

✓  $\text{return } n + \text{fun}(n-1)$

8



*Addition of digits in Number*

*Write a code to find the factorial of a number*

*Program to count digits in a number*

*Program to check if string is palindrome or not*

*Program to Reverse array Recursively*

int x=5, y=10, z=1

if (x>0 && y>z)

}

    minY("Pramod")

{  
else

}

    break

{

int i;

for (i=0 : i ≤ 5 : i++)

{ int a = 10

printf(a)

a=a+1

}

main()

}

int ans = fun(6)

printf(ans)

{

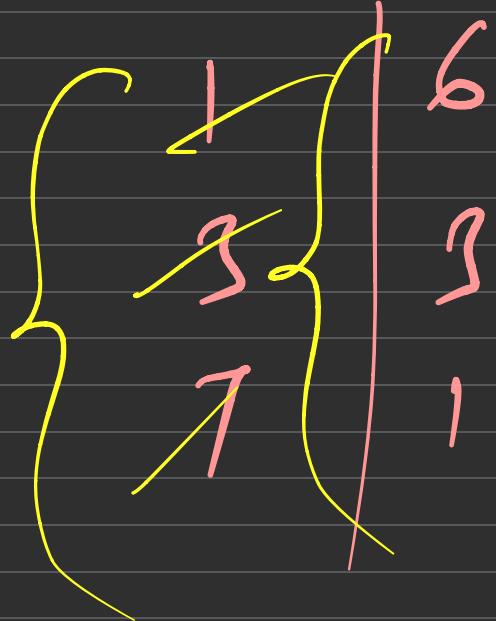
int fun( int n )

}

if ( n <= 1 ) return n

return 2 \* fun(n/2) + 1

}



6  
int fun( int n )  
{  
 if (n <= 1) return n  
 return 2 \* fun(n/2) + 1  
}

~~fun(6)~~ 7  
|  
~~2 \* fun(3) + 1~~  
↓ 1  
~~2 \* fun(1) + 1~~  
↓

main()

}

int ans = fun(12)

printf("%d")

(ans)

{

int fun(int n)

}

if ( $n \leq 1$ ) return n

return  $2 * \underline{\text{fun}(n/2)} + \underline{n/2}$

}

```
int fun( int n )  
{  
    if ( n <= 1 ) return n  
    return 2 * fun( n/2 ) + n/2
```

$$\begin{aligned} &\cancel{\text{fun}(12)} \quad 24 \\ &+ \cancel{9} \\ &2 \times \cancel{\text{fun}(6)} + 6 \\ &\downarrow \\ &\cancel{2 \times \text{fun}(5)} + 5 \\ &+ \cancel{1} \\ &2 \times \cancel{\text{fun}(1)} + 1 \\ &\downarrow \end{aligned}$$

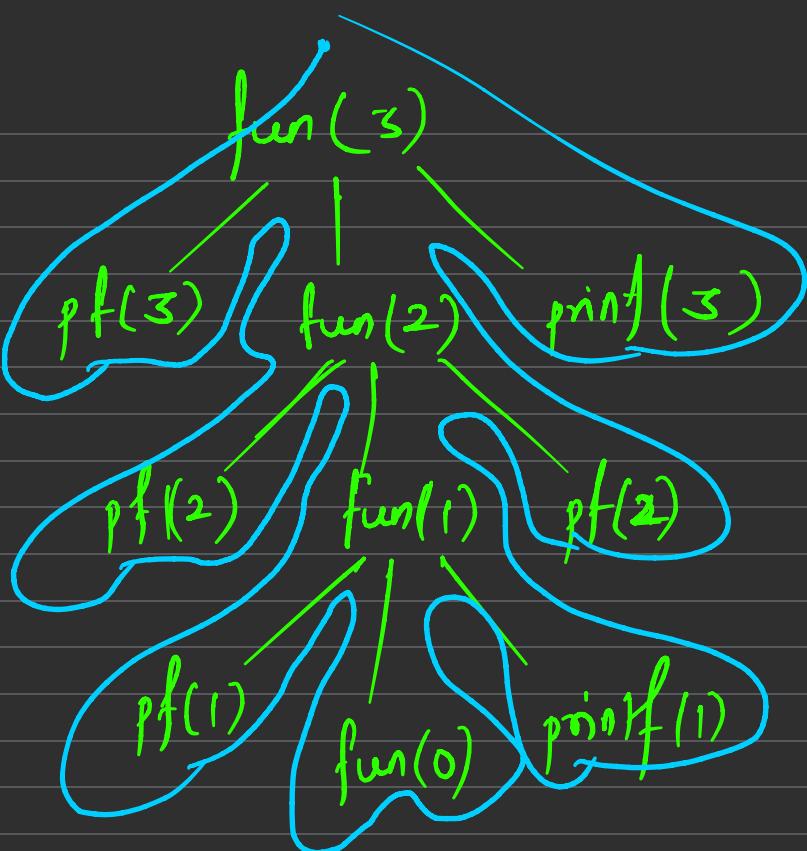
```
main()
{
    fun(3)
}

void fun(int n)
{
    if (n > 0)
    {
        printf("%d"
        fun(n-1)
        printf("%d")
    }
}
```

3 2 1

3 2 1 | 2 3

```
void fun(int n)
{
    if (n > 0)
        printf("%d"
    fun(n-1)
    printf("%d")
```



3 2 | | 2 3

