

Assertion: For every vertex $v \in V$, the edge e of minimum weight that is incident to v is necessarily in any minimum spanning tree of G

The Assertion is true

Proof:

Assume that the Minimum Spanning Tree T for Graph G doesn't contain the minimum weight edge e incident on to v , for some $v \in V$, say $e = (v, u)$. Since T is a spanning tree, it contains a path P connecting u and v , which contains some edge $e' \neq e$ incident to v , say $e' = (v, w)$. By assumption the weight of e' is larger than that of e . It is very easy to see that $T' = (T \cup \{e'\}) \setminus \{e\}$ is also a spanning tree of G . Moreover the weight of T' is smaller than the weight T , which contradicts our assumption that T is a minimum spanning tree

Hence Proved.