Time & Space Complexity

Time Complexity can be explained as a relation between input size and time taken by p computer to execute it.

- *Amout of Space or Time taken up by an algorithm look as function of input size is called complexity.
- * Relationship blun space & input size: Space Complexity
 Relationship blun time 4 input size: Time complexity
 it isn't about actual execution time.

How to derive Time Complexity:

1- Experimental Analysis:

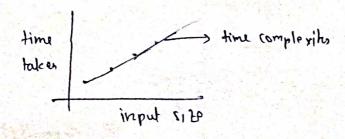
for the code that we have written, we use inbuilt classes to find the execution time.

Then we experiment with input size to find different execution times.

We plot all the values and find a function as time Complexity

There we actually run code multiple times

2. Theretical Analysis



Y = ax+b
ignore constants
L = ax+b
L = O(n)

T(= O(n) for linear

* Always analyse for the worst case.

Big O Notation

Big O notation denotes the upper bound on the upper limit of the time complexity function

It means , the programme won't exerced time representation in any case.

NOTE: - We always try to find worst case complexity

How to write

a Function of n.

F(n) = an2 +bn+c

Dtepl: Ignore all constants

= h2 +n +1

Dtep 2: largest term

$$= n^2$$

$$\left(\overline{1} (= 0 (n^2)) \right)$$

There are 5-6 Common patterns in TC for which we derive theoreticals

END
$$E(n) = an^3 + b \log n + c$$

$$n^3 + \log n + 1$$

$$n^3 \cdot argest$$

$$50 / O(n^3) - 7c$$

Mathametically

$$f(n) = O(g(n))$$

$$\frac{|f(n)|}{|f(n)|} < \infty$$

$$\lim_{n \to \infty} g(n)$$

$$= \lim_{n\to\infty} 1 + \frac{2}{n} + \frac{2}{n^2}$$

$$= 1+0+0$$

$$= 1$$

120

Big Omega Notation

Represents lower bound or the best case of time complexity function.

This means code out run in the time less than specified in the omega notation

____UB O(n)
_____LB sz(n)

Big Theta (0) Notation

Average bound
In cases where LB=WB, we say it is Average
Bound
Ex SZ(n2) & O(n2) we represent it as O(n2)

THE REPORT OF A STATE OF THE PARTY OF THE PA

Complexities

Or (logh)

Or (logh)

Or Dotasize

note:

exponential time complexity is good only for very small inputs.

It is the worst time complexity & is not advised to using use then interviews or coding Contests

Most of the recursion are in exponential time

Space Complexity

memory/space is of two types.

- 1. heap has objects
- 2. Stack -> has Function calls

The relationship between input size and amount of space taken to store it is called space complexity

A programme has two types of space

- 1. Input spore :- Space occupied by permenand wriable
- 2. Auxilorg spore :- Spore occupied by temporary variable (we optimise this one)

Provide of Completion

Some common Care

1 - Loops

K instructions are executed in times in a for lost so it will be 0 (n+12)

On k is a constant, it is ignered

· O(n)

- Linear time - space relation

2. Nested loops

Cork 1 1=0 to n; j=0 to n

Time Complexity = outer loop x somer top

(worst 70) (worst 70)

Wested by TC = O(n2)

Case 2 outer loop iso to n

Inner loop j=0 to i

= 0 (n2) only

Case 3: Find time Complexity for given code

11 some KZn

Tumping for loop

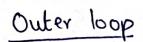
for (int i= 0; 1< n; &i=i+k) {

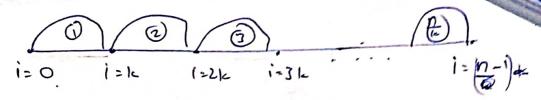
For (int j=j+1; j <=k;j++) (

11 some constant work is done in

3

}





* no of jumps or iterations done by outer bop is n

Inner loop!

If we consider for the a single order loop iteration the inner loop runs le times at maximum

$$: \qquad \left(\frac{\gamma_1}{k}\right) \not \propto k$$