

0/1 Knapsack Problem

Solved With

FIFO Branch and Bound

by
Dr.Jayashree Katti

Objective Function

Maximize profit..... $\sum p_i x_i$

Coverted to minimization problem

i.e $-\sum p_i x_i$

Bound Algorithm to calculate C

Algorithm Bound(cp ,cw, k)

//cp=current profit; cw=current weight;k=index of last removed item; m is knapsack size;//

{

 b=cp; c=cw;

 for i=k+1 to n do

 {

 c=c+w[i];

 if(c<m) then

 b=b+p[i];

 else

 return b+ (1- (c-m)/w[i]) *p[i]

 }

return b;

}

Ubound Algorithm to calculate u

Algorithm Uboud(cp ,cw, k ,m)

//cp=current profit; cw=current weight;k=index of last removed item; m is knapsack size;//

```
{
    b=cp; c=cw;
    for i=k+1 to n do
        {
            if(c+w[i]<=m) then
                {
                    c=c+w[i];b=b-p[i];
                }
            }
    return b;
}
```

Example

- $n=4$
- $P=[10,10,12,18]$
- $W=[2,4,6,9]$
- $m=15$

Upper=-32

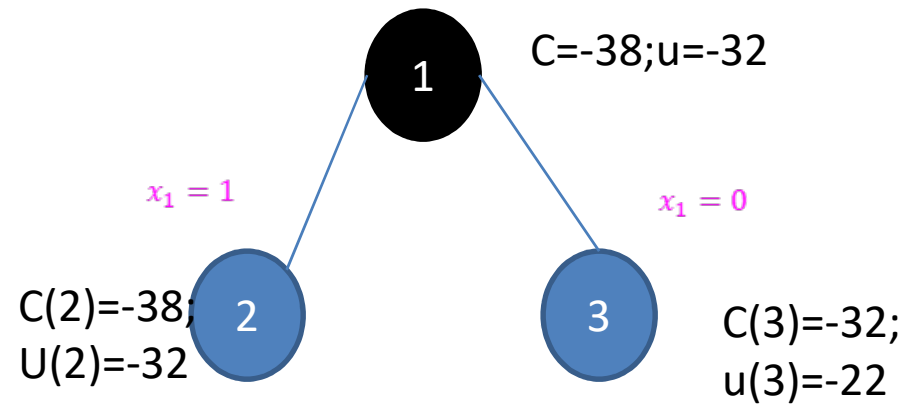


$C(1)=-38;$
 $u(1)=-32$

In FIFO search, first we will take E-node as a node 1.

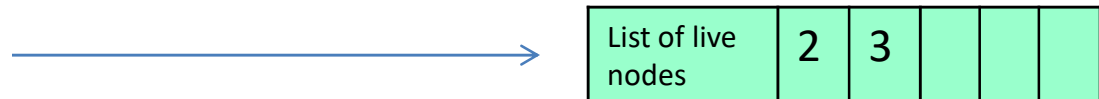
List of live nodes	1				
--------------------	---	--	--	--	--

Upper=-32

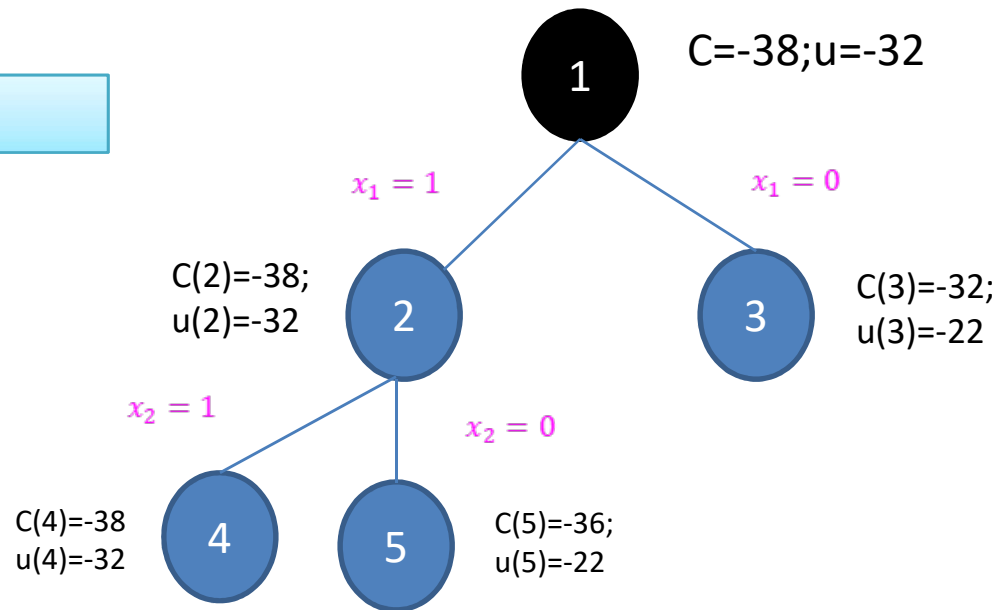


Next we generate the children of node 1.

They are placed in the queue.



Upper=-32

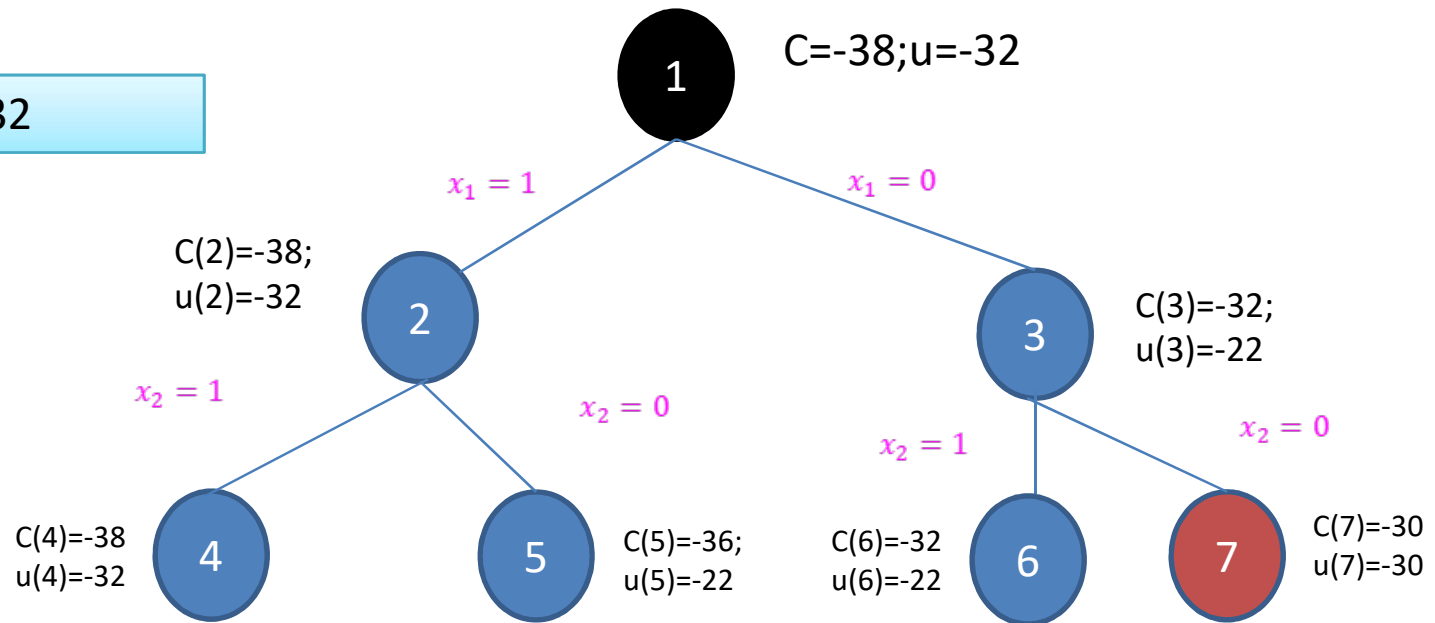


Upper bound doesn't
change and no node is
deleted.

We will place the generated children of E-node(Node 2)
in the Queue i.e Node 4 and 5

List of live nodes	3	4	5		
-----------------------	---	---	---	--	--

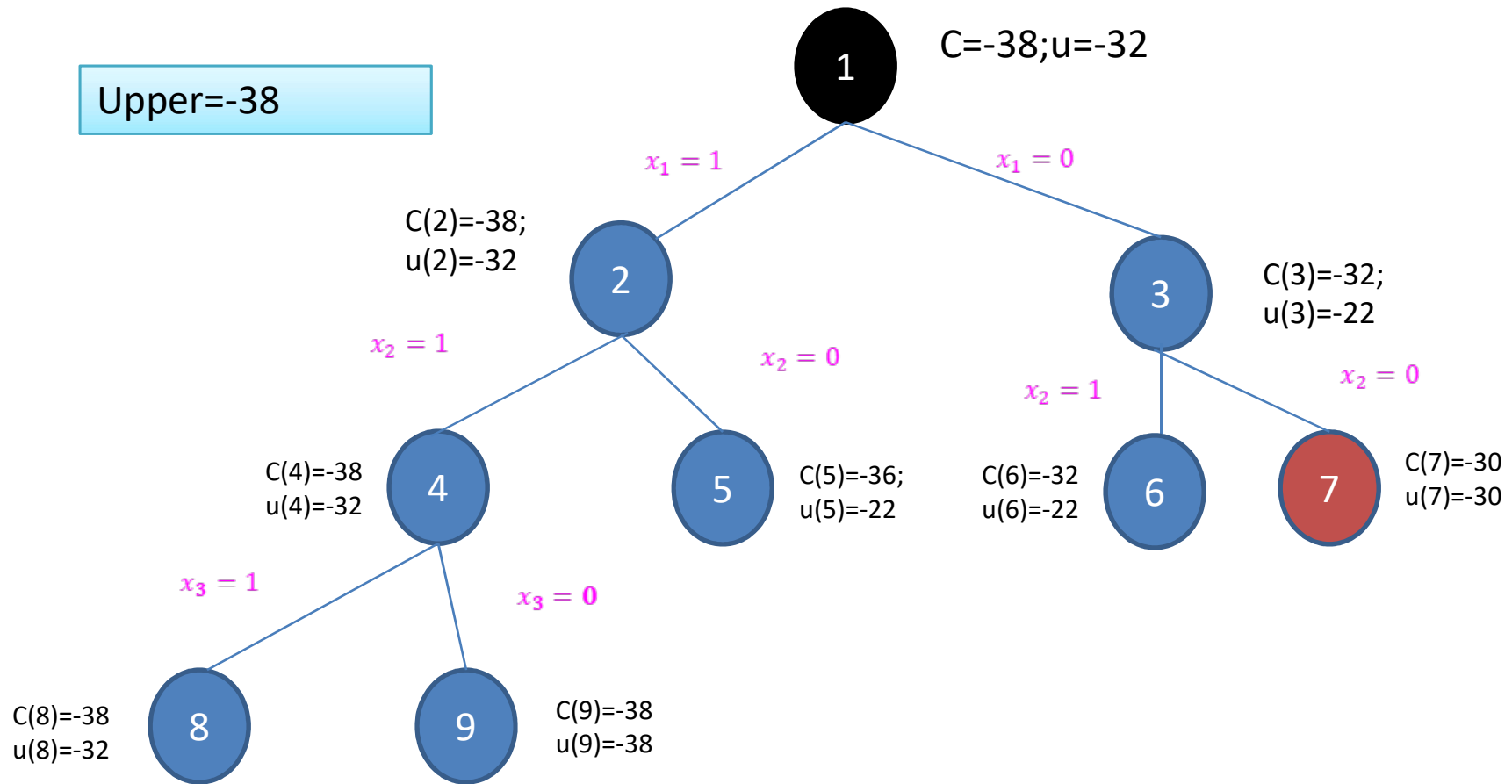
Upper=-32



We will place the generated children of E-node(Node 3) in the Queue i.e Node 6 and 7.

Since $c(7) > \text{global upper bound}$ it is killed.

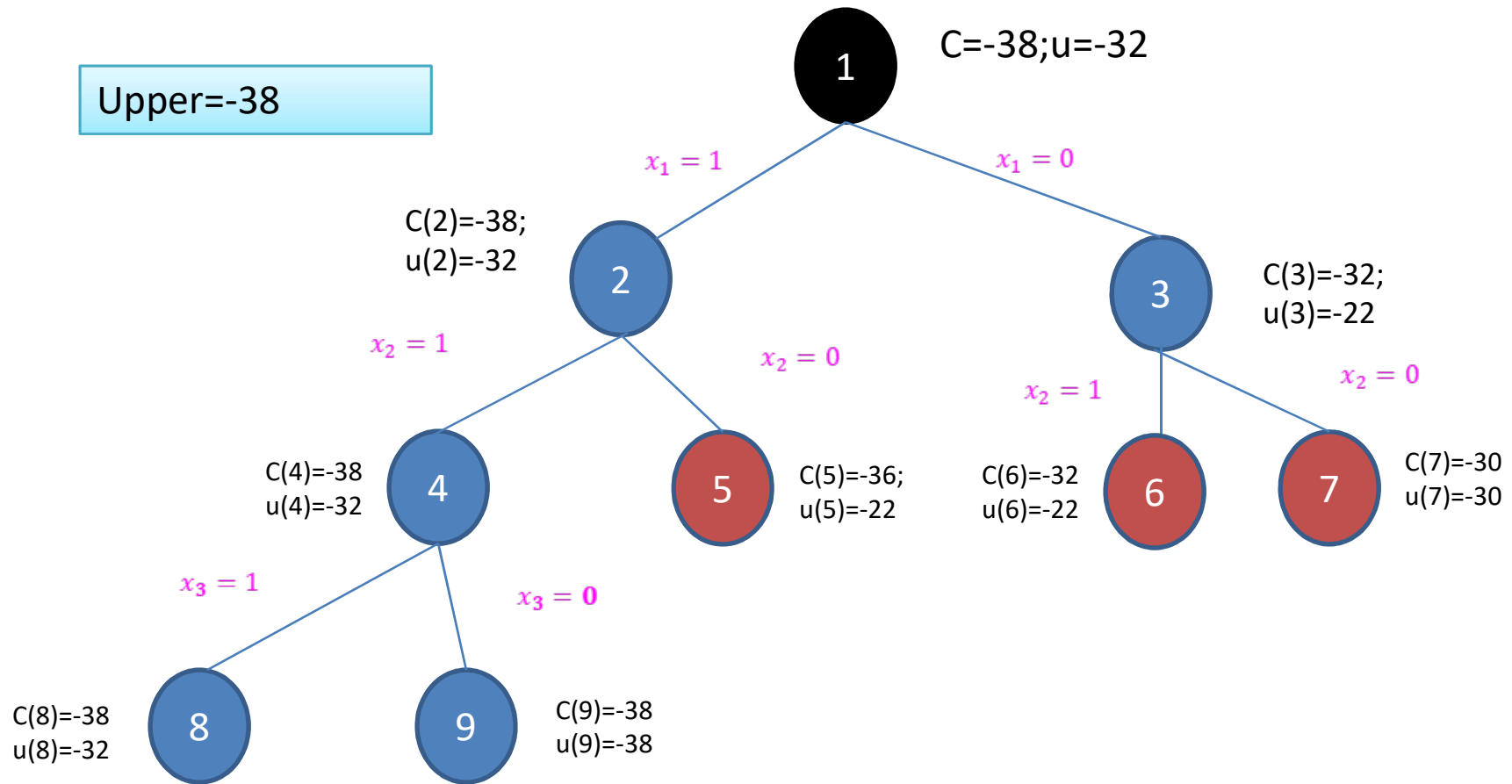
List of live nodes	4	5	6		
--------------------	---	---	---	--	--



We will place the generated children of E-node(Node 4) in the Queue i.e Node 8 and 9.

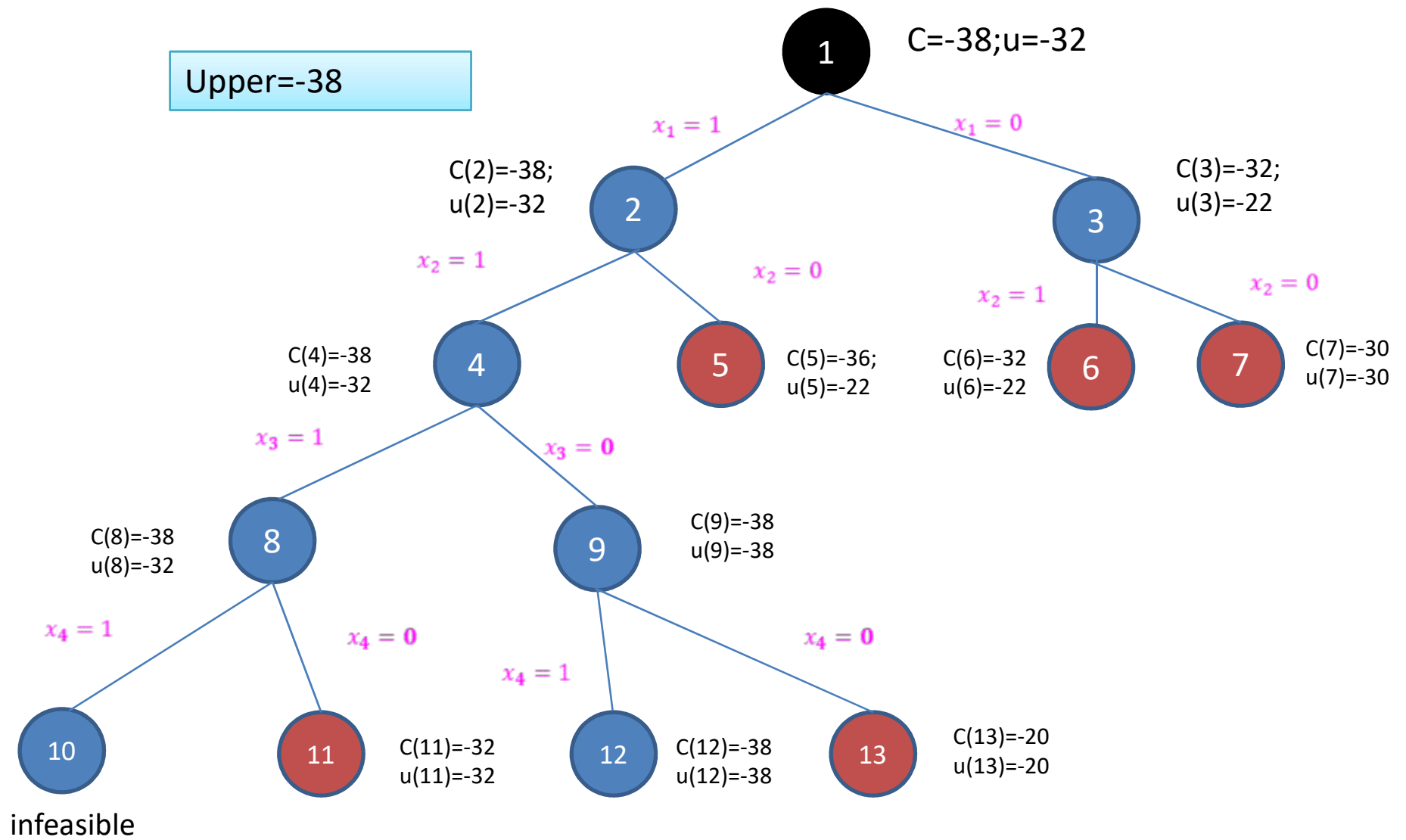
List of live nodes	5	6	8	9	
--------------------	---	---	---	---	--

Global upper bound will be changed to -38.



The nodes 5 and 6 will be killed as $c(5), c(6) > \text{upper bound}$.

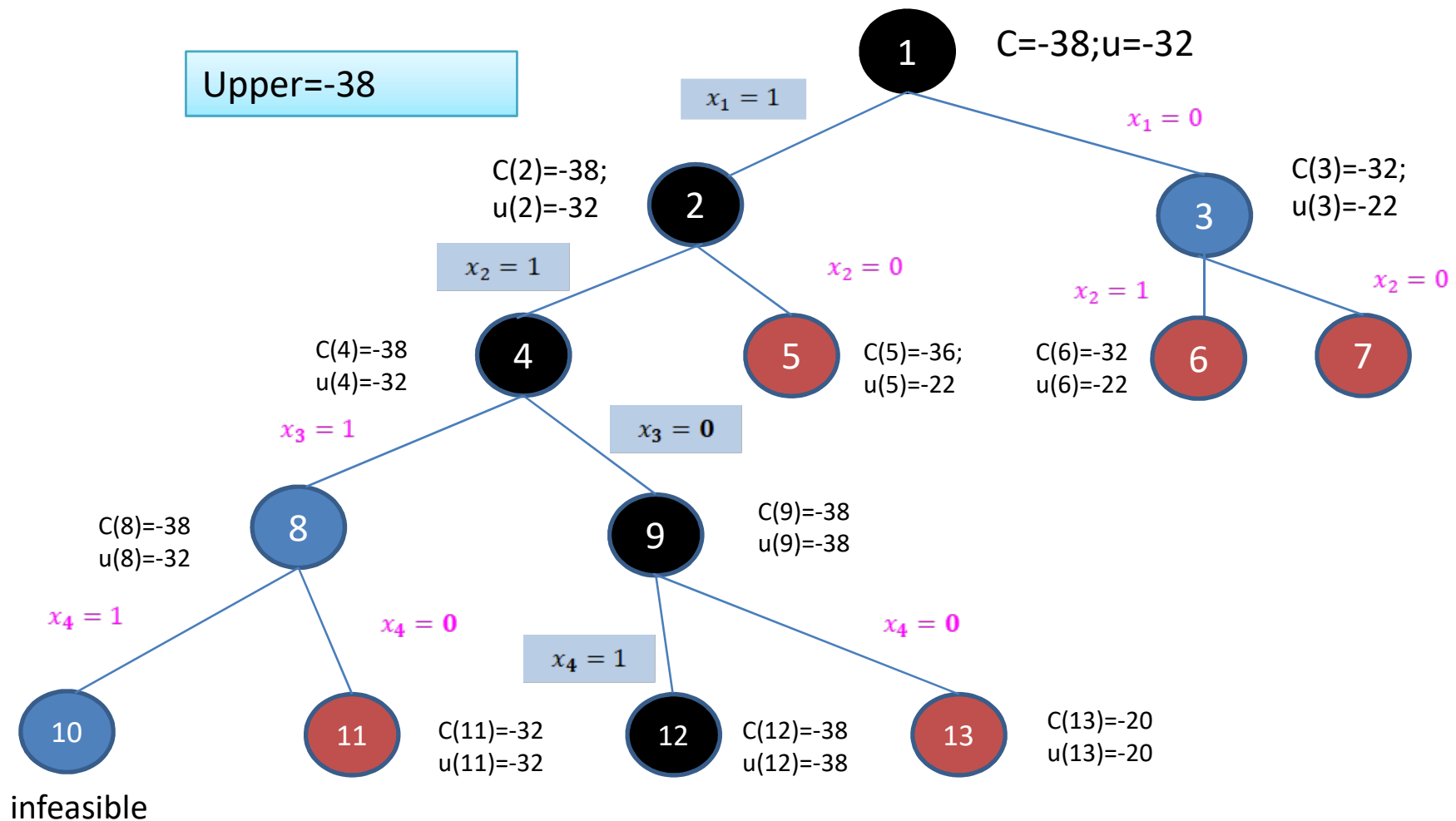
List of live nodes	8	9			
--------------------	---	---	--	--	--



We will now kill nodes 11 and 13.

The only feasible node is node 12.

List of live nodes	10	12			
--------------------	----	----	--	--	--



Since node 12 is the solution.

$$x_1 = 1 \quad x_2 = 1 \quad x_3 = 0 \quad x_4 = 1$$

Solution vector $X = [1, 1, 0, 1]$