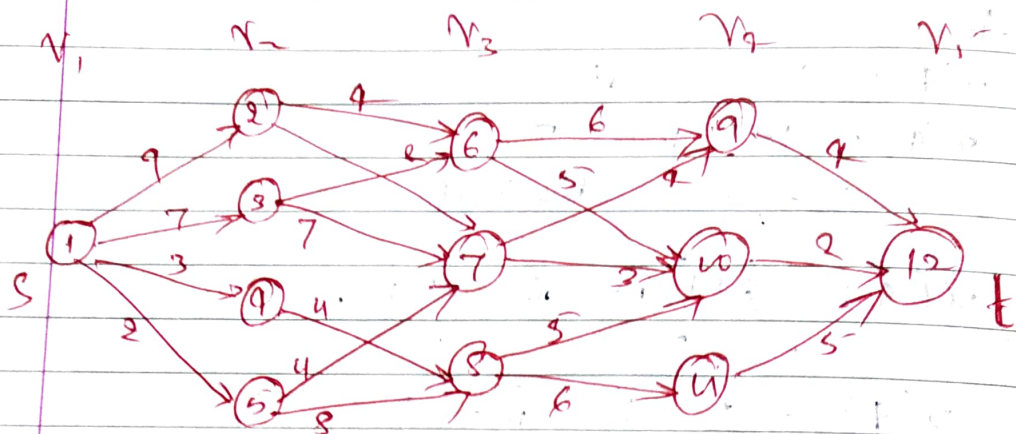


Multistage Graph.

DATE

PAGE



- Total $k-2$ decisions.
- s will be in first stage
- t will be in last stage

$\text{cost}(i, j)$ ^{minimum} represents distance from j^{th} node in i^{th} stage to " t ".

$$\text{cost}(i, j) = \min_{\substack{l \in V_{i+1} \\ (j, l) \in E}} \{ c(j, l) + \text{cost}(i+1, l) \}$$

i.e.

$\text{cost}(3, 6)$: find the minimum cost path from node 6 in stage 3 to destination node 12.

find the node having direct edge from 6. They are $(6, 9)$ and $(6, 10)$

Now find minimum cost path from 9 to 12 and minimum cost path from 10 to 12

and assign the minimum one to $\text{cost}(3,6)$.

$$\text{cost}(4,9) = 4 \quad \underline{\text{4th stage.}}$$

$$\text{cost}(\cancel{4}, 10) = 2$$

$$\text{cost}(4, 11) = 5$$

3rd stage.

$$\text{cost}(3,6) = \{c(6,9) + \text{cost}(4,9), c(6,10) + \text{cost}(4,10)\}$$

$$= \{6+4, 5+2\}$$

$$= \{10, 7\} = 7 //$$

$$\text{cost}(3,7) = \{c(7,9) + \text{cost}(4,9), c(7,10) + \text{cost}(4,10)\}$$

$$= \{5+4, 3+2\} = \{9, 5\} = 5 //$$

$$\text{cost}(3,8) = \{c(8,10) + \text{cost}(4,10), c(8,11) + \text{cost}(4,11)\}$$

$$= \{5+2, 6+5\} = \{7, 11\} = 7 //$$

2nd stage.

$$\text{cost}(2,2) = \{c(2,6) + \text{cost}(3,6), c(2,7) + \text{cost}(3,7), c(2,8) + \text{cost}(3,8)\}$$

$$= \{4+7, 2+5, 1+9\} = 7 //$$

DATE | | PAGE |

$$\text{cost}(2,3) = \min \{ c(3,6) + \text{cost}(3,6), c(3,7) + \text{cost}(3,7) \}$$

$$= \{ 2+7, 7+5 \} = 9 //$$

$$\text{cost}(2,4) = \min \{ c(4,8) + \text{cost}(3,8) \}$$

$$= \{ 11+7 \} = 18$$

$$\text{cost}(2,5) = \min \{ c(5,7) + \text{cost}(3,7), c(5,8) + \text{cost}(3,8) \}$$

$$= \{ 11+5, 8+7 \} = 15$$

$$\text{cost}(1,1) = \min \{ c(1,2) + \text{cost}(2,2), c(1,3) + \text{cost}(2,3), c(1,4) + \text{cost}(2,4), c(1,5) + \text{cost}(2,5) \}$$

$$= \{ 9+7, 7+9, 3+18, 2+15 \}$$

$$= \{ 16, 16, 21, 17 \}$$

$$= 16 //$$

Let $d(i,j)$ be the node number which minimized $\text{cost}(i,j)$

$$d(4,9) = 9$$

$$d(4,10) = 10$$

$$d(4,11) = 11$$

$$d(3,6) = 10$$

$$d(3,7) = 10$$

$$d(3,8) = 10$$

$$d(2,2) = 7$$

$$d(2,3) = 6$$

$$d(2,4) = 8$$

$$d(2,5) = 8$$

$$d(1,1) = 2$$

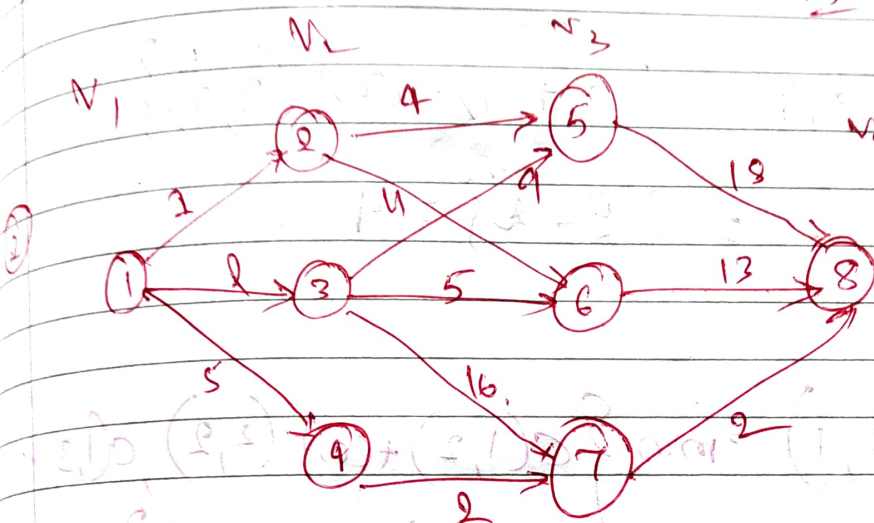
New path is $d(1, 1) = 2$. \therefore 2nd node is 2

$d(2, 2) = 7$ 3rd node in 3rd stage

$d(3,7) = 10$. 4th node in 4th str.

\therefore path is $1 - 2 - 7 - 10 - 12$
 $\quad \quad \quad 9 \quad \quad 2 \quad \quad 3 \quad \quad 2$

26



c Stage 3

$$\text{cost}(3, 5)$$
$$\text{cost}(3, 6) = 13$$
$$\text{cost}(3, 7) = 2.$$

Stage 2

$$\text{Cost}(2, 2) = \min \{ C(2, 5) + \text{Cost}(3, 5), C(2, 6) + \text{Cost}(3, 6) \}$$

$$= \{ 4 + 18, 11 + 13 \} = \{ 22, 24 \} = 22 //$$

$$\text{cost}(2,8) = \min \{ c(3,5) + \text{cost}(3,5), c(3,6) + \text{cost}(3,6), c(3,7) + \text{cost}(3,7) \}$$

$$= \min \{ 9+18, 5+13, 16+2 \}$$

$$= \min \{ 27, 18, 18 \} = 18.$$

$$\text{cost}(2,4) = \{ c(4,7) + \text{cost}(3,7) \}$$

$$= \{ 2+2 \} = 4.$$

$$\text{cost}(1,1) = \min \{ c(1,2) + \text{cost}(2,2), c(1,3) + \text{cost}(2,3), c(1,4) + \text{cost}(2,4) \}$$

$$= \{ 1+22, 2+18, 5+4 \}$$

$$= \{ 23, 20, 9 \} = 9 //$$

$$d(1,1) = 4.$$

$$d(2,4) = 7.$$

$$d(3,7) = 8 //$$

$$\therefore \text{path } 1-4-7-8 \text{ of cost } = 9.$$