

PRANAV TAGADEESH IBM18CS071 5B

① →

Step 1: Eliminate

Given: $\forall x [\exists z \text{ Animal}(z) \Rightarrow \text{Kills}(x, z)] \Rightarrow [\forall y \neg \text{Loves}(y, x)]$
 $\Rightarrow \forall x [\neg \exists z \neg \text{Animal}(z) \vee \text{Kills}(x, z)] \vee [\forall y \neg \text{Loves}(y, x)]$

Step 2: \neg inward
$$\forall x [\forall z \text{ Animal}(z) \wedge \neg \text{Kills}(x, z)] \vee [\forall y \neg \text{Loves}(y, x)]$$

Step 3: Change quantifier

$$\forall x [\forall z \text{ Animal}(z) \wedge \neg \text{Kills}(x, z)] \vee [\forall y \neg \text{Loves}(y, x)]$$

Step 4: Skolemize

$$\forall x [\text{Animal}(F(x)) \wedge \neg \text{Kills}(x, F(x))] \vee \neg \text{Loves}(G(x), x)$$

Step 5: Drop universal quantifier

$$[\text{Animal}(F(x)) \wedge \neg \text{Kills}(x, F(x))] \vee \neg \text{Loves}(G(x), x)$$

Step 6: Distribute

$$[\text{Animal}(F(x)) \vee \neg \text{Loves}(G(x), x)] \wedge$$

$$[\text{Animal}(F(x)) \vee \neg \text{Loves}(G(x), x)]$$

②

RULES

- Cold and precipitation \rightarrow Snow $\neg \text{Cold} \vee \neg \text{precipitation} \vee \text{Snow}$ - January \rightarrow cold $\neg \text{January} \vee \text{cold}$ - Clouds \rightarrow precipitation $\neg \text{clouds} \vee \text{precipitation}$

Facts - January, clouds

Prove - Snow

$$\neg \text{Snow} \rightarrow \neg \text{cold} \vee \neg \text{precipitation} \vee \text{Snow}$$

$$\neg \text{cold} \vee \neg \text{precipitation} \rightarrow \neg \text{January} \vee \text{cold}$$

$$\neg \text{January} \vee \neg \text{precipitation} \rightarrow \neg \text{clouds} \vee \text{precipitation}$$

$$\text{January} \rightarrow \neg \text{January} \vee \neg \text{clouds}$$

$$\neg \text{clouds} \rightarrow \text{clouds}$$