

## 5.1.1

### TFCS Assignment

(a)  $L = \{ 0^n 1^n \mid n \geq 1 \} \Rightarrow$  set of all strings of one or more zeroes followed by equal no of ones

CFG  $\Rightarrow M = \{ V, T, P, S \}$

$V = \{ S \} \rightarrow$  set of non terminal symbols

$T = \{ 0, 1 \} \rightarrow$  set of input symbols

$P =$  Production rule

$S \rightarrow 0S1$

$S \rightarrow 01$

Derivation of 0011

$S \xrightarrow{S \rightarrow 0S1} 0S1$

$\xrightarrow{S \rightarrow 01} 0S101$

$\xrightarrow{S \rightarrow 01} 0011$   $S \rightarrow$  start symbol

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$$b) L = \{ a^i b^j c^k, i, j, k \geq 0, (i \neq j)(j \neq k) \}$$

$$CFG \Rightarrow M = \{ V, T, P, S \}$$

$V = \{ S \}$  set of non terminal symbols

$T = \{ a, b, c \} \rightarrow$  set of input symbols

$P =$  Production rule

$$S \rightarrow Xc \quad [i \neq j]$$

$$S \rightarrow ay \quad [j \neq k]$$

$$X \rightarrow aXb$$

$$X \rightarrow a/b$$

$$Y \rightarrow bYc$$

$$Y \rightarrow b/c$$

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c)  $G = \{ \{S\}, \{a, b\}, P, S \}$

$$P \Rightarrow S \rightarrow asa$$

$$S \rightarrow bsb$$

$$S \rightarrow a$$

$$S \rightarrow b$$

$$S \rightarrow \epsilon$$

5.1.1

$$L = \{ 0^{2^n} \mid n \geq 0 \}$$

d)  $G = \{ \{S\}, \{0, 1\}, P, S \}$

$$P = \left\{ \begin{array}{l} S \rightarrow 00S1 \\ S \rightarrow 001 \\ S \rightarrow \epsilon \end{array} \right\}$$

5.1.2

$$S \rightarrow A1B \rightarrow (1)$$

$$0^*1(0+1)^*$$

$$A \rightarrow 0A / \epsilon \rightarrow (3)$$

$$B \rightarrow 0B / 1B / \epsilon \rightarrow (4, 5, 6)$$

a) 00101

Left Derivation

Right Derivation

Derivation

Rule

Derivation

Rule

S

$S \rightarrow A1B \rightarrow (1)$

S

$S \rightarrow A1B \rightarrow (1)$

A1B

$A \rightarrow 0A \rightarrow (2)$

A1B

$B \rightarrow 0B \rightarrow (4)$

0A1B

$A \rightarrow 0A \rightarrow (2)$

A10B

$B \rightarrow 1B \rightarrow (5)$

00A1B

$A \rightarrow \epsilon \rightarrow (3)$

A101B

$B \rightarrow \epsilon \rightarrow (6)$

001B

$B \rightarrow 0B \rightarrow (4)$

A101

$A \rightarrow 0A \rightarrow (2)$

0010B

$B \rightarrow 1B \rightarrow (5)$

0A101

$A \rightarrow 0A \rightarrow (2)$

00101B

$B \rightarrow \epsilon \rightarrow (6)$

00A101

$A \rightarrow \epsilon \rightarrow (3)$

00101

00101

5.1.2

(c) 00011  $S \rightarrow A1B \rightarrow \textcircled{1}$   
 $A \rightarrow 0A / \epsilon$   $0A \rightarrow \textcircled{2}$   $\epsilon \rightarrow \textcircled{3}$   
 $B \rightarrow 0B / 1B / \epsilon$   $0B \rightarrow \textcircled{4}$   $1B \rightarrow \textcircled{5}$   $\epsilon \rightarrow \textcircled{6}$

Left Derivation		Right Derivation	
Derivation	Rule	Derivation	Rule
S	$S \rightarrow A1B \rightarrow \textcircled{1}$	S	$S \rightarrow A1B \rightarrow \textcircled{1}$
A1B	$A \rightarrow 0A \rightarrow \textcircled{2}$	A1B	$B \rightarrow 1B \rightarrow \textcircled{5}$
0A1B	$A \rightarrow 0A \rightarrow \textcircled{2}$	A11B	$B \rightarrow \epsilon \rightarrow \textcircled{6}$
00A1B	$A \rightarrow 0A \rightarrow \textcircled{2}$	A11	$A \rightarrow 0A \rightarrow \textcircled{2}$
000A1B	$A \rightarrow \epsilon \rightarrow \textcircled{3}$	0A11	$A \rightarrow 0A \rightarrow \textcircled{2}$
0001B	$B \rightarrow 1B \rightarrow \textcircled{5}$	00A11	$A \rightarrow 0A \rightarrow \textcircled{2}$
00011B	$B \rightarrow \epsilon \rightarrow \textcircled{6}$	000A11	$A \rightarrow \epsilon \rightarrow \textcircled{3}$
00011		00011	

5.1.2

(b) 1001  $S \rightarrow A1B \rightarrow \textcircled{1}$   
 $A \rightarrow 0A / \epsilon$   $0A \rightarrow \textcircled{2}$   $\epsilon \rightarrow \textcircled{3}$   
 $B \rightarrow 0B / 1B / \epsilon$   $0B \rightarrow \textcircled{4}$   $1B \rightarrow \textcircled{5}$   $\epsilon \rightarrow \textcircled{6}$

Left Derivation		Right Derivation	
Derivation	Rule	Derivation	Rule
S	$S \rightarrow A1B \rightarrow \textcircled{1}$	S	$S \rightarrow A1B \rightarrow \textcircled{1}$
A1B	$A \rightarrow \epsilon \rightarrow \textcircled{3}$	A1B	$B \rightarrow 0B \rightarrow \textcircled{4}$
1B	$B \rightarrow 0B \rightarrow \textcircled{4}$	A10B	$B \rightarrow 0B \rightarrow \textcircled{4}$
10B	$B \rightarrow 0B \rightarrow \textcircled{4}$	A100B	$B \rightarrow 1B \rightarrow \textcircled{5}$
100B	$B \rightarrow 1B \rightarrow \textcircled{5}$	A1001B	$B \rightarrow \epsilon \rightarrow \textcircled{6}$
1001B	$B \rightarrow \epsilon \rightarrow \textcircled{6}$	A1001	$A \rightarrow \epsilon \rightarrow \textcircled{3}$
1001		1001	



5.4.7:

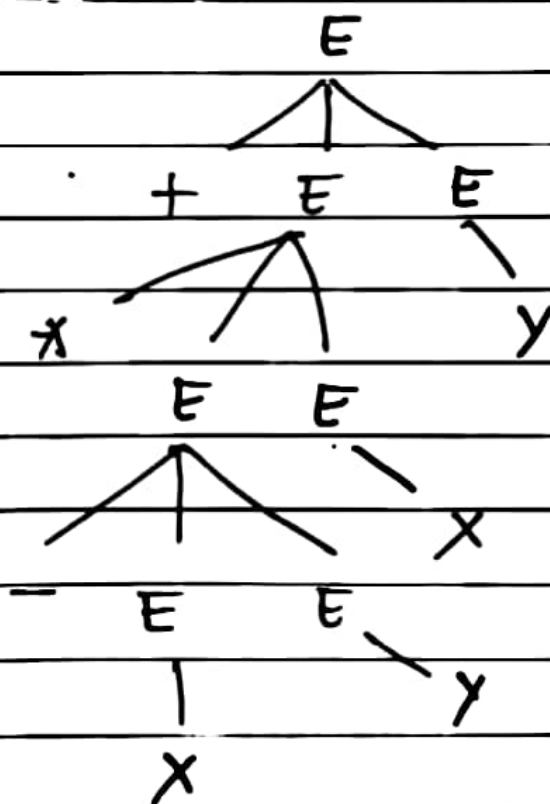
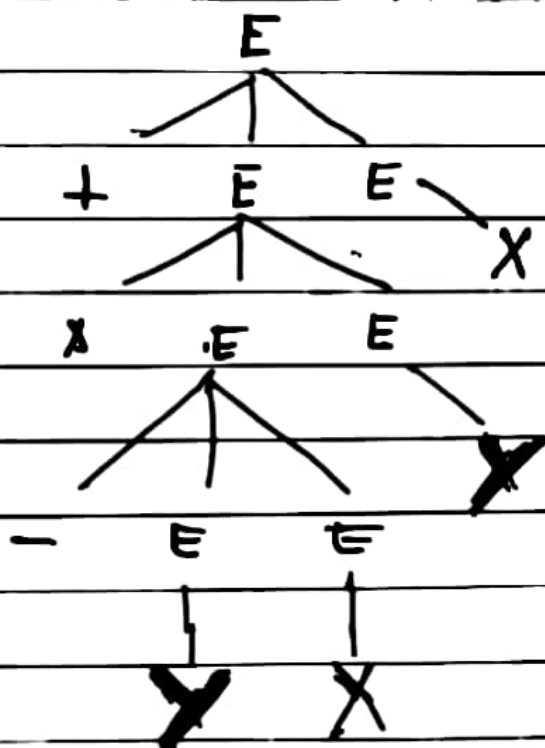
$E \rightarrow +EE$  ① |  $E \rightarrow *EE$  ② |  $E \rightarrow -EE$  ③ |  $E \rightarrow x$  ④ |  $E \rightarrow y$  ⑤

a) Left Derivation

Derivation	Rule
E	
+EE	$E \rightarrow +EE \rightarrow$ ①
+*EEE	$E \rightarrow *EE \rightarrow$ ②
+*-EEE	$E \rightarrow -EE \rightarrow$ ③
+*-EEEE	$E \rightarrow x \rightarrow$ ④
+*-XEEE	$E \rightarrow y \rightarrow$ ⑤
+*-XYEE	$E \rightarrow x \rightarrow$ ④
+*-XYXE	$E \rightarrow y \rightarrow$ ⑤
+*-XYXY	

Right Derivation

Derivation	Rule
E	
+EE	$E \rightarrow +EE \rightarrow$ ①
+EY	$E \rightarrow y \rightarrow$ ⑤
+*EEY	$E \rightarrow *EE \rightarrow$ ②
+*EXY	$E \rightarrow x \rightarrow$ ④
+*-EXY	$E \rightarrow -EE \rightarrow$ ③
+*-EYXY	$E \rightarrow y \rightarrow$ ⑤
+*-EYXY	$E \rightarrow x \rightarrow$ ④
+*-XYXY	



b) Since Left Derivation and Right Derivation results in required strings, the grammar considered here is unambiguous.

5.4.5 a) Ambiguity  $\rightarrow$  For a given language CFG, if more than one parse trees exists  $\Rightarrow$  the CFG is ambiguous.  
 Generated sequences of left and right derivations are different  $\Rightarrow$  ambiguous.  
 Generated sequences of left and right derivations are same  $\Rightarrow$  unambiguous.

For the given language:  $S \Rightarrow A1B$ ,  $A \rightarrow OA|E$ ,  $B \rightarrow OB|1B|E$

is unambiguous because sequence 00101 can be produced by both left and right derivations as shown below

Left derivation		Right derivation	
Derivation	Rule	Derivation	Rule
S	$S \rightarrow A1B \rightarrow (1)$	S	$S \rightarrow A1B \rightarrow (1)$
A1B	$A \rightarrow OA \rightarrow (2)$	A1B	$B \rightarrow OB \rightarrow (4)$
OA1B	$A \rightarrow OA \rightarrow (2)$	A1OB	$B \rightarrow 1B \rightarrow (5)$
OOA1B	$A \rightarrow E \rightarrow (3)$	A1O1B	$B \rightarrow E \rightarrow (6)$
OO1B	$B \rightarrow OB \rightarrow (4)$	A1O1	$A \rightarrow OA \rightarrow (2)$
OO1OB	$B \rightarrow 1B \rightarrow (5)$	OA1O1	$A \rightarrow OA \rightarrow (2)$
OO1O1B	$B \rightarrow E \rightarrow (6)$	OOA1O1	$A \rightarrow E \rightarrow (3)$
OO1O1		OO1O1	

b) The grammar that is ambiguous for this language  
 Consider generating 00101 using grammar

$S \rightarrow A1B \rightarrow (1)$      $0A \rightarrow (2)$      $\epsilon \rightarrow (3)$

$A \rightarrow 0A / \epsilon \dots$

$B \rightarrow 1B / \epsilon$

$1B \rightarrow (4)$      $\epsilon \rightarrow (5)$

Left Derivation

Derivation	Rule
S	$S \rightarrow A1B \rightarrow (1)$
A1B	$A \rightarrow 0A \rightarrow (2)$
0A1B	$A \rightarrow 0A \rightarrow (2)$
00A1B	$A \rightarrow \epsilon \rightarrow (3)$
001B	$B \rightarrow 1B \rightarrow (4)$
0011B	$B \rightarrow \epsilon$
0011	

Right Derivation

Derivation	Rule
S	$S \rightarrow A1B \rightarrow (1)$
A1B	$B \rightarrow 1B \rightarrow (4)$
A11B	$B \rightarrow \epsilon \rightarrow (5)$
A11	$A \rightarrow 0A \rightarrow (2)$
0A11	$A \rightarrow 0A \rightarrow (2)$
00A11	$A \rightarrow \epsilon \rightarrow (3)$
0011	

Hence ambiguous, It is not possible to generate 00101.