Name - Delijit Chakraharty Section - F Roll No. - 52

91) $T(n) = 3T (n/2) + n^2$ $T(n) = aT(n/6) + f(n^2)$ a > 1, b > 1On compairing $a = 3, b = 2, f(n) = n^2$ Now, $C = log_a = log_3 = 1.584$ $n^2 = n^{1.584} \le n^2$ $f(n) > n^2$ $f(n) > n^2$ $f(n) > n^2$ $f(n) > n^2$

92) $T(n) = 4T(n/2) + n^2$ $\rightarrow a/1, b/1$ $a = 4, b = 2, f(n) = n^2$ $c = \log 4 = 2$ $n^2 = n^2 = f(n) = n^2$ $\therefore T(n) = 0 (n^2 \log_2 n)$

93) $T(n)_2 T(n/2) + 2^n$ A = 1 b = 2 $f(n)_2 2^n$ C = laga = lagc = 0 $h^c = h^o = 1$ $f(n) > h^c$ $T(n)_2 \theta(2^n)$

91) $T(n)_{2} 2^{n} T(n/2) + n^{n}$ $\rightarrow a = 2^{n}$ b = 2, $f(n) = n^{2}$ $c = \log_{2} a = \log_{2} 2^{n}$ $e = n^{2}$ $e = n^{2}$ $f(n) = n^{2}$ $f(n) = 0 (n^{2} \log_{2} n)$

95) T(n) = 16T(n/4) + n $\Rightarrow a = 16, b = 4$ f(n) = n $c = \log 16 = \log (4)^2 = 2\log 4$ $= 2^{16} = \log (4)^2 = 2\log 4$ $n^2 \Rightarrow n^2$ $f(n) < \beta n^2$ $f(n) < \beta n^2$ $f(n) < \beta n^2$

30) $T(n)=2T(n/2)+n \log n$ $\rightarrow a=2, b=2$ $f(n)=n \log n$ $c=\log 2=1$ $n^c=n^2=n$ $n \log n > n$ $f(n) > n^c$ $f(n) > n^c$

X

g7) T(n) = 2T(n/2) + n/lagn → a=2, b=2, f(n)= n/logn C= lag 2 = 1 nc=n1=n · n < n · . f(n) < nc · . T(n) = 0 (n) 98) T(n)=2T(n/4)+n0.51 -> a = 2, b = 4, f(n) = n0.51 $C = \log_{10} a = \log_{10} 2 = 0.5$ $n^{c} = n^{0.5}$ $n^{o} \le n^{o.5}$ \$(n)>nc .. T(n): 0 (nº.51) gg) T(n) 2 0.5 T(n/2) + 1/n \rightarrow a=0.5, b=2a 1/1 but here a is 0.5

so me cannet apply Master's Theorem.

910) T(n)= 16T(n/4)+n! -> a=16, b=4, f(n)=n! · · · C = lag a z lag 16 2 2 $n^{c} = n^{2}$ As n/ >n²

 $T(n) = \theta(n!)$

911) 4T(n/2) + lag n -, a=4, b=e, f(n)=lagn C = lega - leg 4 = 2 ne = n2 (n). legn : lagn < n2 4(n)(n° T(n): 0 (nc) = 0 (n2) Q12) T(n) = sqrt(n) T(n/2) + logn _, a= In, b=2 C= lego = legon = 1 legon · · · z leg n < leg (n) · + (n)>nc T(n) = 0 (f(n)) = 0 (leg (n)) (13) T(n)=3T(n/2)+n \rightarrow a=3; b=2; f(n)=nC = lag a = lag 3 = 1.5849 nc = n 1.5489 n < n1.5849 \Rightarrow $f(n) < n^c$ T(n)=0(n1.5849) Q14) T(n) = 3T(n/3) + sgrt (n) $\rightarrow a=3, b=3$ C = leg a = leg 3 = 1 $n^{c} = n^{1} = n$ As sgut (n) < n f(n)<nc T(n) 20(n)

$$g(5)$$
 $T(n) = 4T(n/2) + n$
 $\rightarrow 0 = 4, b = 2$
 $C = laga = lag_2 = 2$
 $h^c = n^2$
 $n < n^2$ (for any constant)
 $f(n) < n^c$
 $f(n) = 0$

$$g_{16}$$
) $T(n) = 3T(n/4) + n \log n$
 $\rightarrow a = 3, b = 4, f(n) = n \log n$
 $C = \log_{6} a = \log_{4} 3 = 0.792$
 $n^{c} = n^{0.792}$
 $n^{0.792} < n \log n$
 $T(n) = 0 (n \log n)$

$$g_{17}) T(n) = 3T(n/3) + n/2$$

$$\rightarrow a = 3; b = 3$$

$$c = \log_{3} a = \log_{3} 3 = 1$$

$$f(n) = n/2$$

$$\therefore n^{c} = n' = n$$

$$A = n/2 < n$$

$$f(n) < n^{c}$$

$$f(n) = O(n)$$

$$f(n) = GT(n/3) + n^{2} \log n$$

$$A = G; b = 3$$

$$C = \log_{b} a = \log_{3} G = 1.6309$$

$$n^{c} = n^{1.6309}$$

As $n^{1.6309} < n^{2} \log n$
 $\therefore T(n)_{20} (n^{2} \log n)$

$$g(9) T(n) = 4T(n/p) \frac{1}{n+1} + n/\log n$$

$$\Rightarrow a = 4, b = 2, f(n) = \frac{n}{\log n}$$

$$c = \log a = \log_2 4 = 2$$

$$e = n^2$$

$$e = n^2$$

$$\log n = n^2$$

$$\log n$$

$$T(n) = o(n^2)$$

 $\begin{array}{c}
g20) T(n) = 64T(n/8) - n^{2} \log n \\
\rightarrow \alpha = 64 \text{ b} = 8 \\
C = \log_{10} \alpha = \log_{10} 64 = \log_{10} (8)^{2} \\
C = 2 \\
N^{c} = n^{2} \\
\therefore n^{2} \log_{10} n > n^{2} \\
T(n) = O(n^{2} \log_{10})
\end{array}$

$$\begin{array}{c} g_{21}) \ T(n) = 7T \ (n/3) + n^{2} \\ \rightarrow a = 7; b = 3; f(n) = n^{2} \\ C = log_{b}a = log_{3}7 = 1.7712 \\ n^{c} = n^{1.7712} \\ n^{1.7712} < n^{2} \\ T(n) = 0 \ (n^{2}) \end{array}$$