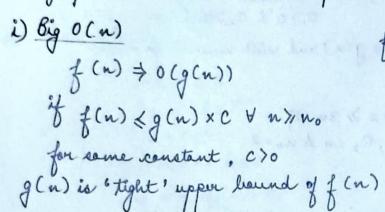
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Section - F

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91. What do you understand by Asymptotic notation, define different asymptotic rotation with example.



eg:- f(n) =) n2+n g(n) =) n3

n2+n < c \* n3  $n^2 + n = 0(n^3)$ 

ii) Big Omega ( 12)

When f(n) 2 52 (g(n))

neans g(n) is "tight" lawveleund of f(n) ie f(n) can go leey and g(n)

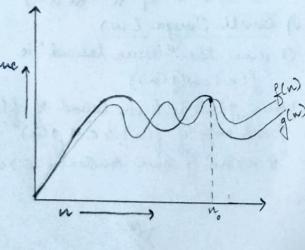
le f(x) = 52 g(n) if and only if

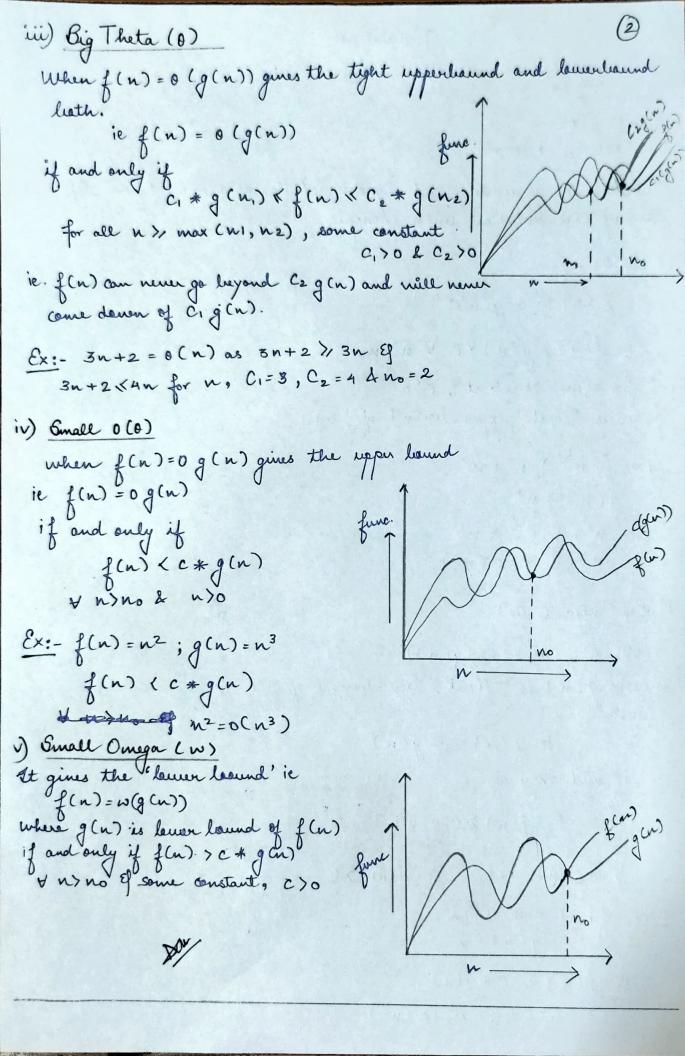
f(n) > c.g(n)

Y nz > no and C = constant > 0

 $\frac{\mathcal{E}_{X}}{f(n)} \Rightarrow n^{2} + 4n^{2}$   $g(n) \Rightarrow n^{2}$ 

le f(n) / c \* g(n) n3 + 4 n2 2 12 (n2)





```
92 What should be time complexity of:
         for (inti- 1 to u)
             i=i*2; \rightarrow o(1)
L) for i => 1, 2, 4, 6, 8 . . . . u times
   je Stries is a GP
So a=1, u=2/1
     Kth value of GIP:
             th = ank-1
            t_h = 1(2)^{k-1}
              2n=2k
           lag_2(2n) = k lag_2
            lag 2 + lag n = le
            leg 2 n+1 = le (Neglecting 61?)
  So, Time Complexity T(n) > 0 (lag, n) - Ans.
13. T(n) = [3T(n-1) if n>0
            otherwise 1
 4 ie T(n) = 3T(n-1) - (1)
    T(n)=)1
   put n => n-1 in (1)
   T(n-1) \Rightarrow 3T(n-2) - (2)
     put (2) in (1)
  T(n) = 3x 3T (n-2)
  T(n) \Rightarrow 9T(n-2) \rightarrow (3)
   put n => n - 2 in (1)
   T(n-2) = 3T (n-3)
        put in (3).
```

T(n)= 27T (n-3) -4)

```
4
```

```
Generalising series,
       T(h) = 3^k T(n-k) - (5)
   for be terms, Let n-k=1 (Base Case)
         k = n-1
         put in (5)
       T(n) = 3"-1 T(1)
                               ( neglecting 3')
       T(n) = 3^{n-1}
       T(n)=0(3")
84. T(n)= {2+(n-1)-1 of n>0,
                 otherwise 1
     T(n) = 2T(n-1)-1
                               -> (1)
        put n=n-1
     T(n-1) = 2T(n-2)-1
       put in (1)
     T(n) = 2x(2T(n-2)-1)-1
           =4T(n-2)-2-1-(3)
          put n=n-2 in (1)
   T(n-2) 2 2T (n-3)-1
        Put in (1)
        T(n)_2 8T(n-3)-4-2-1 - (4)
   Generalising series
         T(n) = 2^{k} T(n-k) - 2^{k-1} - 2^{k-2} \dots 2^{\circ}
 * k+h term Let n-k=1 &= n-1
    T(n) = 2^{k-1} T(1) - 2^{k} \left( \frac{1}{2} + \frac{1}{2^{2}} + \dots + \frac{1}{2^{k}} \right)
           2 21 - 2 - 1 ( + + + + ... 1 21/2-1 )
          ie Svivs in GP.
```

a=1/2, n=1/2.

$$T(n) = O(1) \text{ Ans}$$

If what should be time camplexity of int i=1, s=1; while  $C = x = n$ )

i i+1; s=s+i; print  $f("#");$ 

$$f("#");$$

$$f("""$$

T(n) = O(Jn) Que.

Ste Time Camplexity of

void f(int n)int i, count = 0;

far(i=61; i\*i(=n; ++i))

3

L. As  $i^2$  in  $i = \sqrt{n}$   $i = 4, 2, 3, 4, ... \sqrt{n}$   $= 4 + 2 + 3 + 4 + ... + \sqrt{n}$   $= 7(n) = \sqrt{n} + \sqrt{n}$   $= 7(n) = \sqrt{n} + \sqrt{n}$   $= 7(n) = 0(n) \rightarrow Ans$ 

07 Time Complexity of

void f (int n)

int i, j, h, count = 0;

for (int i = n/2; i (= n; ++i?)

for (j=1; j (= n; j=j\*2)

for (h=1; h (= n; h= h+2)

count ++;

blisse, for h=h²

k=1,2,4,8,... h

"Series is in GP

>10, a=1, n=2

 $\frac{A(n^{n}-1)}{n-1}$   $= \frac{1(2^{k}-1)}{1}$   $n = 2^{k}-1$   $n+1=2^{k}$   $\log_{2}(n) = k$ 

7 lag (n) \* lag(n) lag(n) lag (n) lag(n) \* lag(n) lag & n ? + lag (n) lag(n) T.C => O(n \* leg n \* leg n)  $\Rightarrow 0$  (n lag<sup>2</sup>(n))  $\rightarrow 9$ ths & Time Complexity of void function ( int n) if (n==1) return; for (i=1 to n) { for (j=1 to n) { printf (" \* "); function (n-3); 4 for (i= 1 to n) me get j=n times every turn  $i \cdot i * j = n^2$  $u^{x}$ , Now,  $T(n) = n^2 + T(n-3)$ ; T(n-3) = (n23)2 + T(n-6): T(n-6) = (n 6) 2 + T(n-9); and T(1)=1; Now, substitute each value in T(n)  $T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1$ Let 1 - 3h = 1 h = (n-1)/3 total tums = k+1  $T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1$ T(n) = ~ 4 n2 T(n)~(h-1)/3 # n2 50, T(n) 20(n3) → Ans

```
(8)
```

```
99. Time Camplexity of :-
      void function ( int n)
         for (inti= 1 to n) f
          for (intj=1; j <= n; j=j+i) [
             printf (" * "),
                  j=1+2+... (n),j+i)
      i = 1
4 for
                  j=1+3+5...(n),j+i)
       i = 2
                 1=1+4+7 ... (n >/ j+i)
      nthe term of AP is
          T(n)= a+d* m
          T(m) = 1 + d xm
          (n-1)/d=n
       for i=1
                  (n-1)/1 times
                (n-1)/2 times
   me get,
         T(n) 2 i 2 j 1 + i 2 j 2 + ... i n - 1 j n - 1
              2(n-1) + (n-2) + (n-3) + \cdots + (n-3) + \cdots
             2 n+n/2 + n/3 + .. n/n-1 - nx1
             2 n [1+1/2+1/3+ ·· 1/n-1] - N+1
             znxlagn-n+1
          Since 1 1/x = lag x
             T(n) = O(nlegn) + dus.
```

```
For the Function n' R & C<sup>n</sup>, what is the asymptotic Relationship b/or these functions?

Assume that h>=1 & C>1 are constants. Find out the value of C & no. of which relationship holds.

Is given nh and c<sup>n</sup>

Relationship b/w nh & c<sup>n</sup> is

nh = 0 (c<sup>n</sup>)

nh & a c c n)

V n > no h constant, a>0

for no=1; c=2

> 1k < a<sup>2</sup>

> no=1 & c=2 -> Ans
```