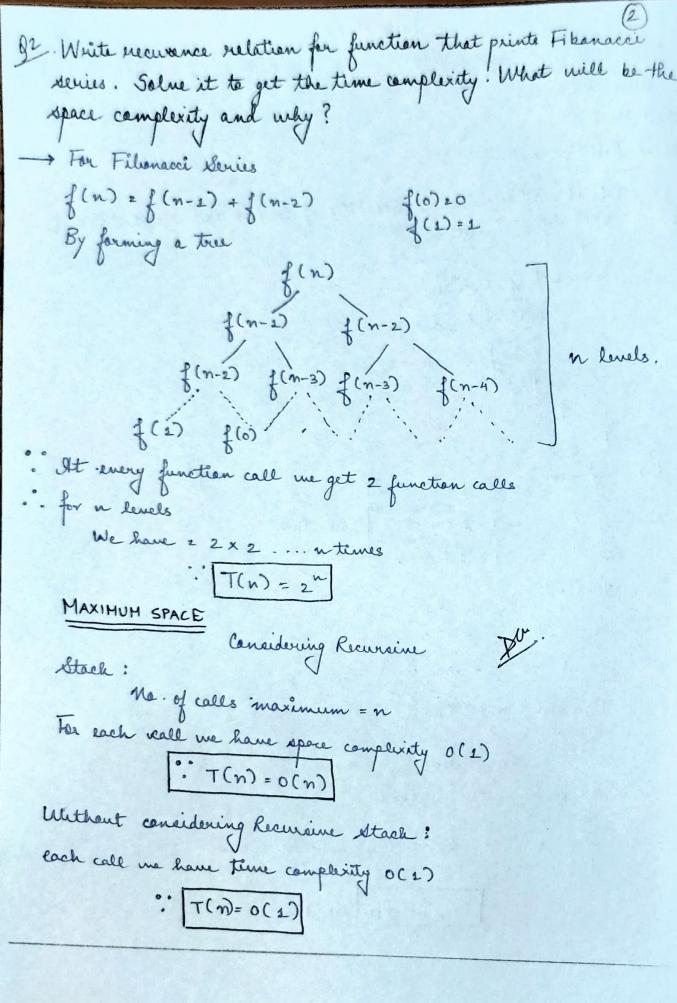
```
Tutarial -2
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Section - F
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    What is the time complexity of below cade and have?
         int j=1, i=0;
while (i(n) {
        i+=j;
j++,
     j=1
                              m-level
     J = 3
     for (i)
      , 1 + 2 + 3 + ... + < n
        1+2+3+m < n
      : m (m+1) (n
             m & Jn
      By summation method
              $ 1+1+ .... + In times
                 T(n) = In - Ans
```



```
Write pragrams which have complexity:
   n (lag n), n', lag (lag n)
1) n lagn - Juick sant
        Vaid quickent (int aur (), int lave, int high)
              if ( low < high)
               int pi = partition (aur, low, high);
quickent (arr, low, pi-1);
quickent (aur, pi+1, high);
    int partition (int arr [], int law, int high)
              int pivot = avolhigh];
int i = (low-1);
         for (int j = lane; j <= high -1; j ++)
                 if (arr(i) < pinet)
                     i++;
suap (darr[i], darr[j]);
            return (i+1); have [high]);
2) n3 -> Multiplication of 2 square matrix
        for (i=0; i < n1; i++) {
            for (j=0; j < c2; j++)
                   for (h=0; h< c1; h++)
                         Metillij + = a[i][h] * b[k][j];
```

She salue the following recommer relation
$$T(n) = T(n/4) + T(n/2) + Cn^2$$

$$T(n/4) \qquad T(n/2) \rightarrow 1$$

$$T(n/6) \qquad T(n/6) \qquad T(n/4) \qquad T(n/6) \rightarrow 2$$
At level

$$1 \to \frac{n^{2}}{4^{2}} + \frac{n^{2}}{2^{2}} = \frac{C5n^{2}}{16}$$

$$2 \to \frac{n^{2}}{8^{2}} + \frac{n^{2}}{16^{2}} + \frac{n^{2}}{4^{2}} + \frac{n^{2}}{8^{2}} = \left(\frac{5}{16}\right)^{2} n^{2} c$$

$$\vdots$$

$$\max \text{ level} = \frac{n}{2^{k}} = 1$$

O -> Cn2

$$T(n) = C(n^{2} + (5/16)n^{2} + (5/16)^{2}n^{2} + ... + (5/16)^{2}n^{n} + ... + (5/16)^{2}n^{2} + ... + (5/16)^{2}n^{n} + ... + (5/16)^{2}n^{n}$$

$$T(n) = Cn^{2} \left[1 + \left(\frac{5}{16}\right) + \left(\frac{5}{16}\right)^{2} + ... + \left(\frac{5}{16}\right)^{2}n^{n}\right]$$

 $T(n) = Cn^2 \times 1 \times \left( \frac{1 - (5/16)^{\log n}}{1 - (5/16)} \right)$ 

$$T(n) z C n^2 \times \frac{11}{5} \times \left(1 - \left(\frac{5}{16}\right)^{\log n}\right)$$

$$T(n) = o(n^2c)$$

$$o(cn^2)$$

$$qus.$$

gs. What is the time complexity of following funt?? int fun (int n) {
 for (int k=2; i <= n; k++) { for ( int j = 1; jen ; 1 + = 1) { 11 Some O(x) task j=(n-1)/i-times 1+5+9 ¿ (n-1) :  $T(n) = (\frac{n-1}{1}) + (\frac{n-1}{2}) + (\frac{n-1}{3}) + \cdots + (\frac{n-1}{n})$ T(n) = n[1+1/2+1/3+...+1/n]-1x[1+1/2+1/3+..+/n] z nlogn-lagn T(n)=O(nlegn) -> Ans go What should be time camplexity of for ( int i=2, i <= n; i = pow(i, k)) 11 Some 0(1) where he is a constant 2 km <= n km z lagzn m= lagh lagzn · · £ 1 1+1+1. ... in times T(n) = O (lag klagn) -Ans.

It Write a recurrence relation when quick nort repeatedly divides array into 2 parts of 99% and 1%. During time complexity in this case. Show the recurrence true while devining time complexity Ef find difference in heights of both extreme parts. What do you understand by this analysis? Given algorithm divides away in 99%, and 1%, part •  $T(n) = \{T(n-1) + O(1)\}$  $\begin{array}{c|c}
n-1 & 1 \\
1 & 3 \\
\end{array}$   $\begin{array}{c|c}
n^{2} & \\
\end{array}$ "n" work is done at each level T(n) = (T(n-1)+T(n-2)+. ... + T(1) + O(1) xn = nxn  $T(n) = O(n^2)$ hewest height = 2 highest height = n · · différence = n-2 n)1 The given algorithm produces linear result

Annange fallacuing in since asing order of nate of grawth:

a) n, n!, lagn, laglagn, neat (n), lag(n!), n lagn, lag2(n), 2, 2, 4, n, 100

look laglagn < lagn < (lagn)<sup>2</sup> < Tn < n < n lagn < lag (n!) < n<sup>2</sup> <

2 (2<sup>n</sup>), 4n, 2n, 1, lag (n), lag (lag(n)), Tlag (n), lag2n, 2 lag (n), n,

lag (n!), n!, n2, n lag (n)

< lag lagn < Jlagn < lagn < lag 2n < 2 lagn < n < n lagn

< 2n < 4n < lag(n!) < n<sup>2</sup> < n! < 2<sup>n</sup>

7 n3,5n

96 < lag n < lag 2n < 5n < n lag (n) < n lag (n!) < n lag (n!), n!, neg (n!) < n lag (n!), n!, lags(n), 96, 8n2,

7 n3 < n! < 8<sup>2</sup>

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