

10.5.2.14

EE23BTECH11003 - pranav

Question: How many multiples of 4 lie between 10 and 250?

Solution:

| Variable | Description | Value |
|----------|---|----------|
| $x(0)$ | First term of the AP | 0 |
| d | Common difference of the AP | d |
| $x(n)$ | General term of the AP | $4nu(n)$ |
| n | no of multiples of 4 between 10 and 250 | ? |

TABLE 1: Variables Used

$$n = \frac{250 - 250 \bmod 2 - 10 - 10 \bmod 2}{4} + 1 \quad (1)$$

$$n = 60 \quad (2)$$

considering the series to start from $n = 0$ the general term

$$x(n) = [x(0) + nd]u(n) \quad (3)$$

$$x(n) = 4nu(n) \quad (4)$$

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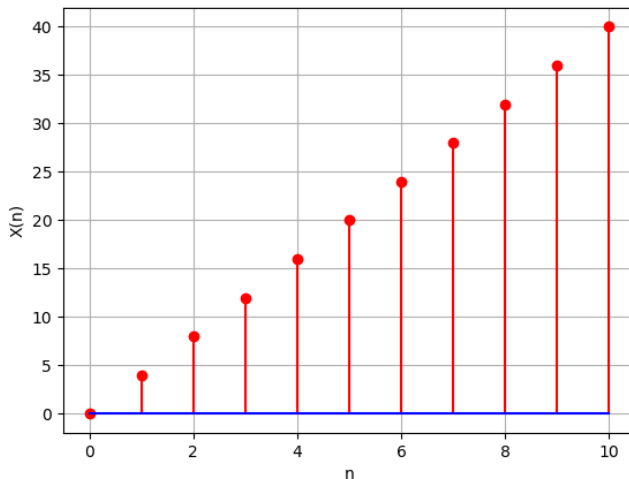


Fig. 1: stem plot of $X(n)$

applying Z transform

$$x(z) = \sum_{n=-\infty}^{\infty} x(n)z^{-n} \quad (5)$$

$$\Rightarrow x(z) = \sum_{n=-\infty}^{\infty} 4nu(n)z^{-n} \quad (6)$$

$$\Rightarrow x(z) = \sum_{n=0}^{\infty} 4nz^{-n} \quad (7)$$

$$(8)$$

from ??

$$\Rightarrow x(z) = \frac{4z^{-1}}{(1 - z^{-1})^2} \quad |z| > 1 \quad (9)$$