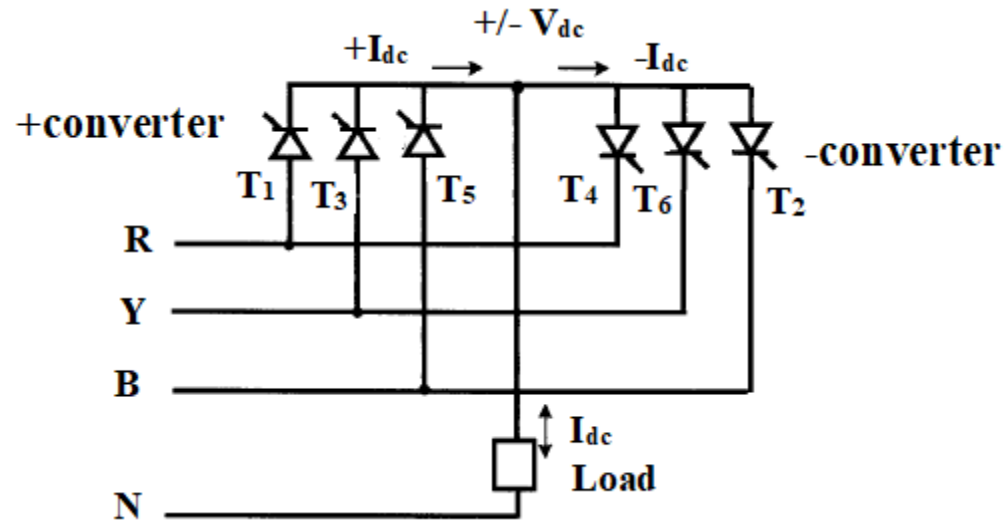


# 3 Pulse Dual Converter

- Circuit diagram
- Each device conducts for 120°
- Four quadrant operation
- DC O/P voltage

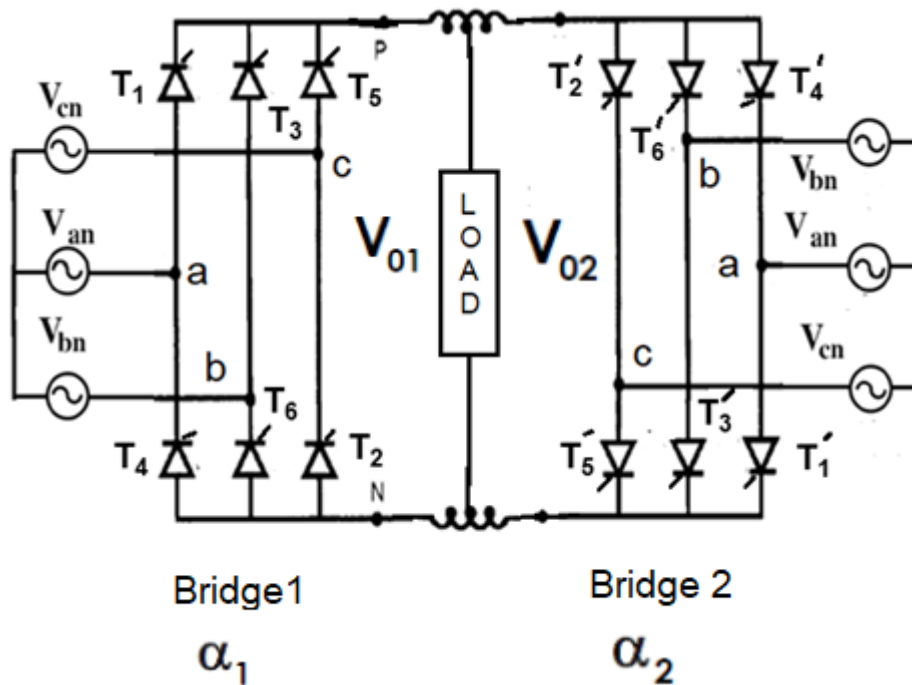
$$V_{dc} = (3 \sqrt{3} V_{mp} \cos \alpha) / 2\pi$$

where  $V_{mp}$  peak value of phase to neutral voltage



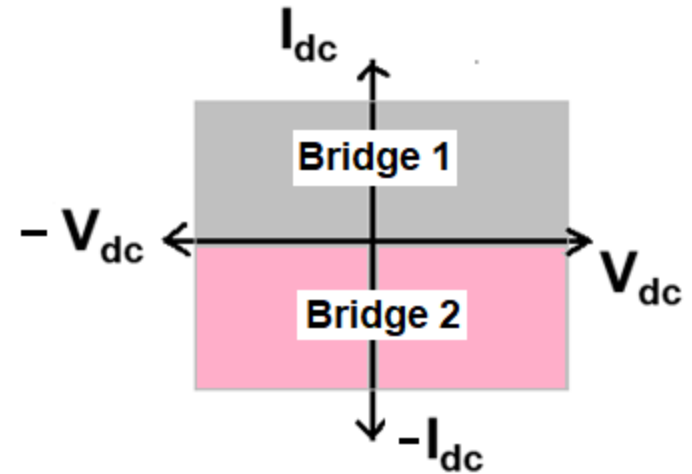
# 6 pulse dual converter

- 6 pulse dual converter => two six pulse converters connected in anti parallel



# 6 pulse Dual converter

- Quadrant operation
- Bridge 1 = I and II
- Bridge 2 = III and IV



- Bridge 1 provides +ve current to load and provides +ve and -ve voltage.

- Bridge 1  $\Rightarrow \alpha_1$

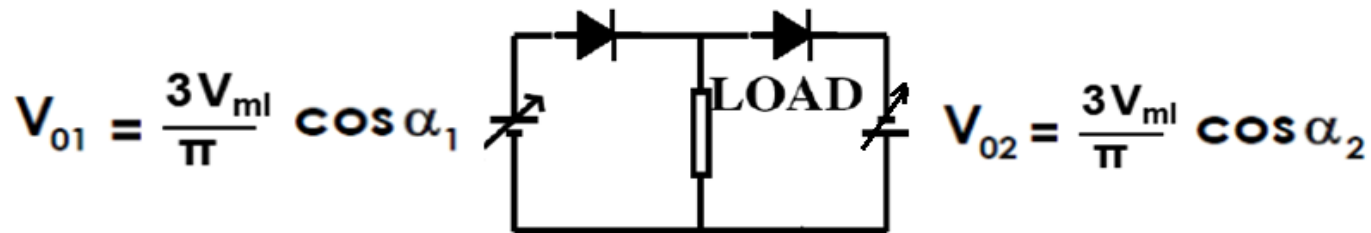
$$V_{o1} = \frac{3V_{m1}}{\pi} \cos \alpha_1$$

- Bridge 2  $\Rightarrow \alpha_2$

$$V_{o2} = \frac{3V_{m1}}{\pi} \cos \alpha_2$$

# 6 pulse Dual converter

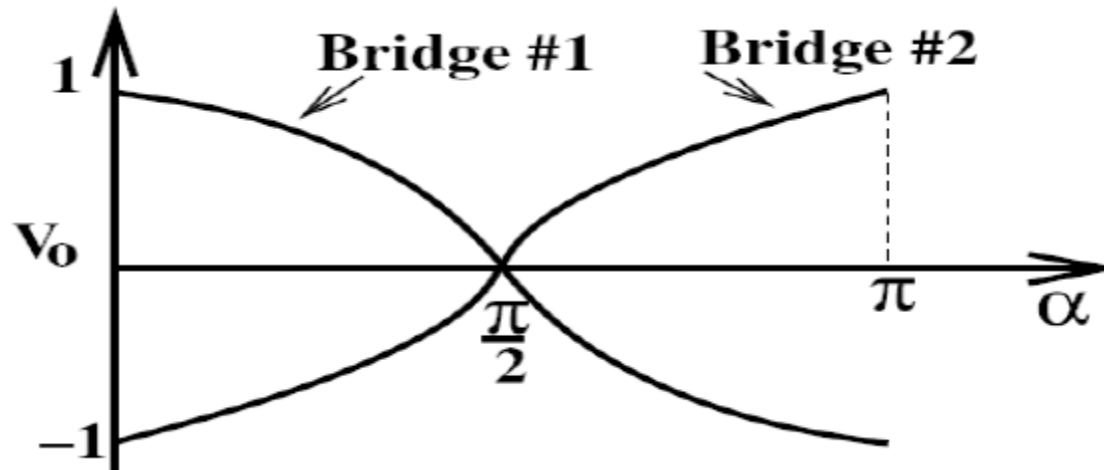
- Average voltage provided by both converters are same



- Applying KVL gives  $V_{O1} + V_{O2} = 0$
- $\cos \alpha_1 + \cos \alpha_2 = 0$
- $\cos \alpha_1 = -\cos \alpha_2 \Rightarrow \cos \alpha_1 = \cos(\pi - \alpha_2)$
- $\alpha_1 + \alpha_2 = \pi$

# 6 pulse Dual converter

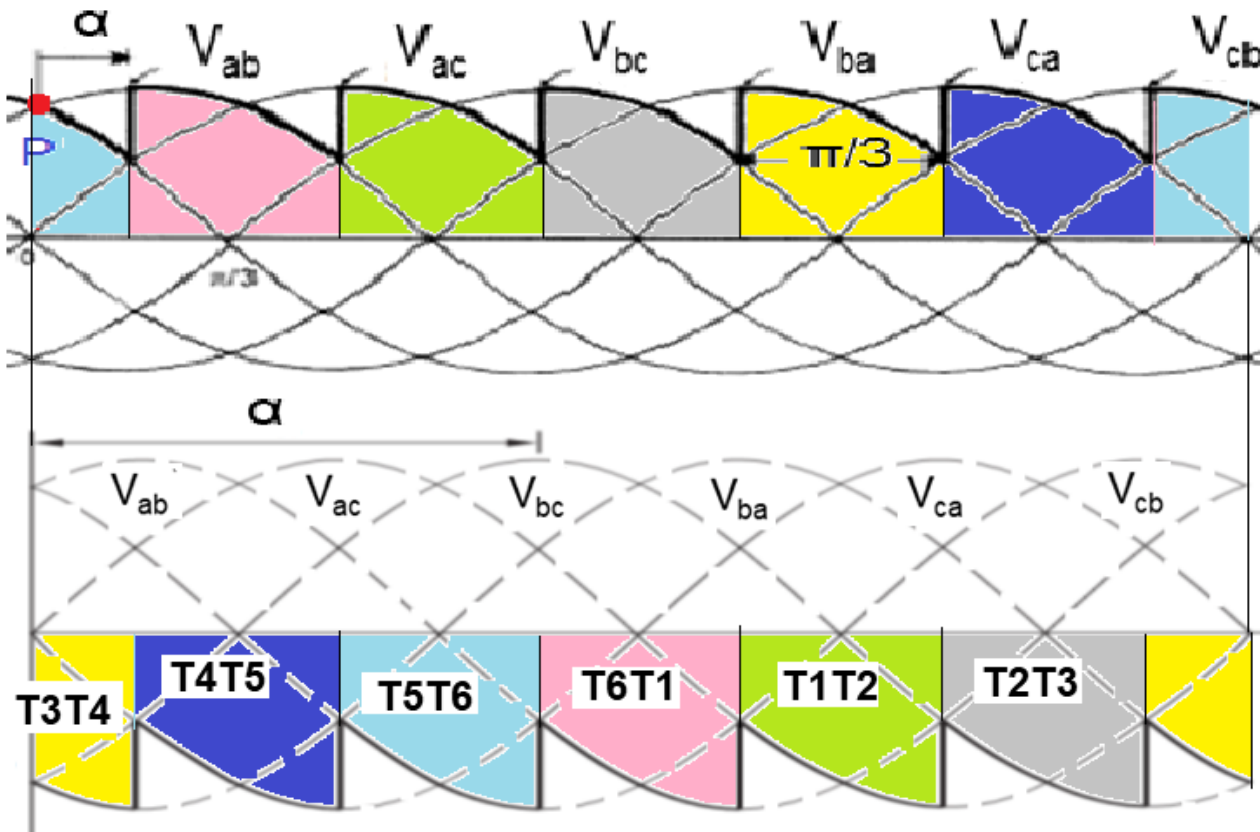
- Circulating mode and non circulating mode



- Inductors  $L_1$  and  $L_2$  are required to limit the circulating current
- Dual converter for speed control of DC Motor

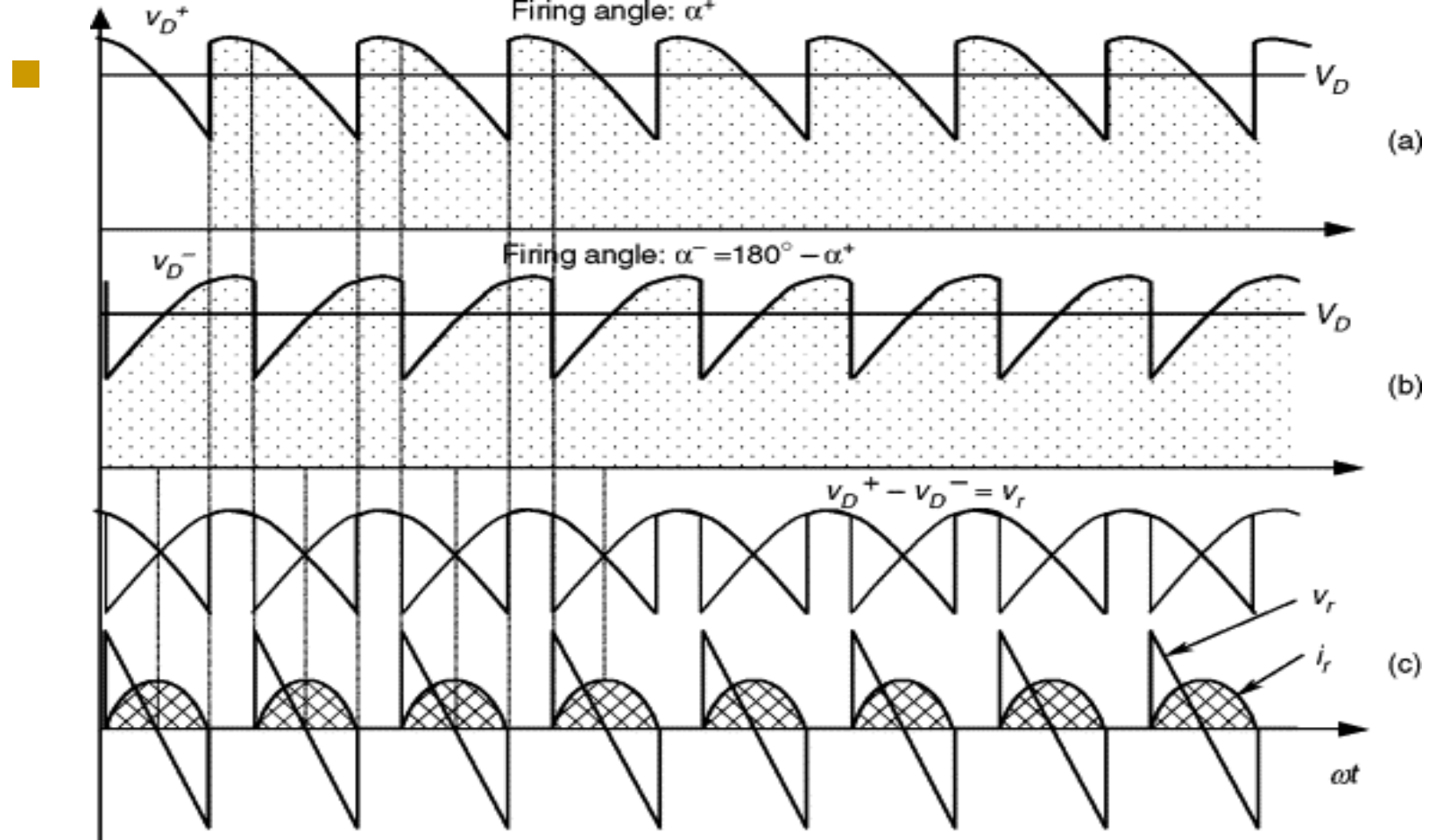
# 6 pulse dual converter

- $30^\circ$  and  $150^\circ$  waveforms



# 6 pulse dual converter

## ■ Circulating current

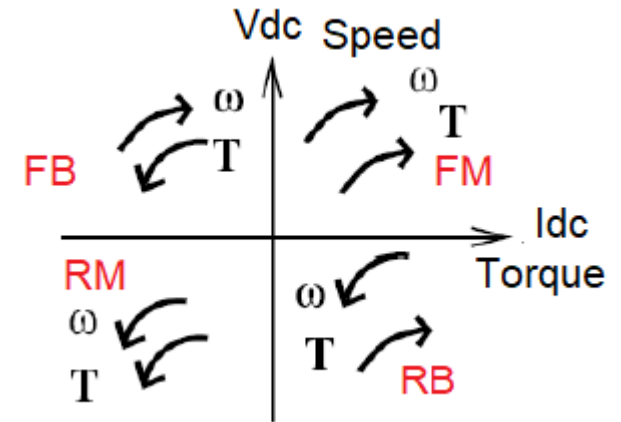


# Operating Modes

- Circulating and Non circulating current Mode
- Advantages and disadvantages of circulating current mode
- Simple control
- Fast change over
- higher device rating
- Cost of Inductors



- 4 quadrant DC Drive
- Armature voltage control

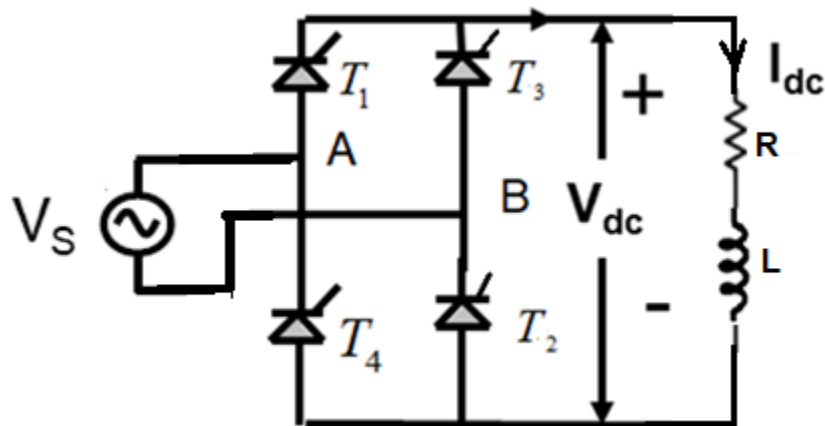


# 6 pulse dual converter : Application

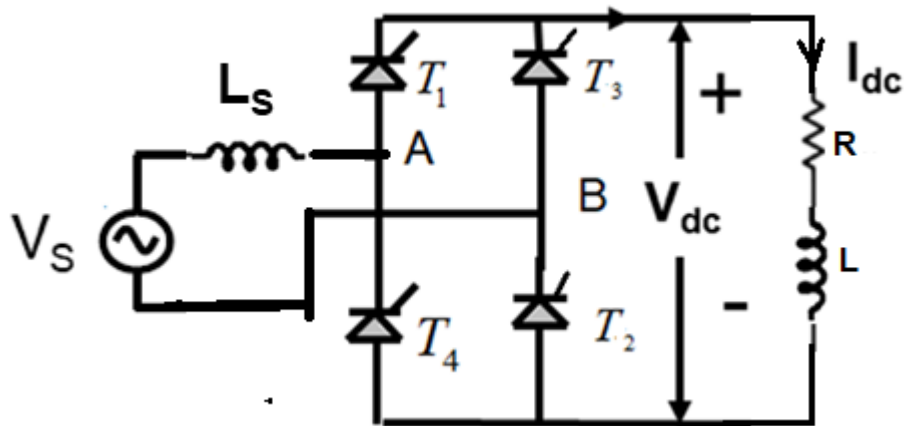
- 4 quadrant DC drive
- Speed control method = armature voltage control
- Regenerative braking
- Speed control range = min to rated speed
- Flux remains constant
- Torque is proportional to  $I_a$
- Applications: Electric traction, lift , cranes , hoists rolling mills

# 2 pulse Full controlled converter with source Inductance

- With and without source inductance



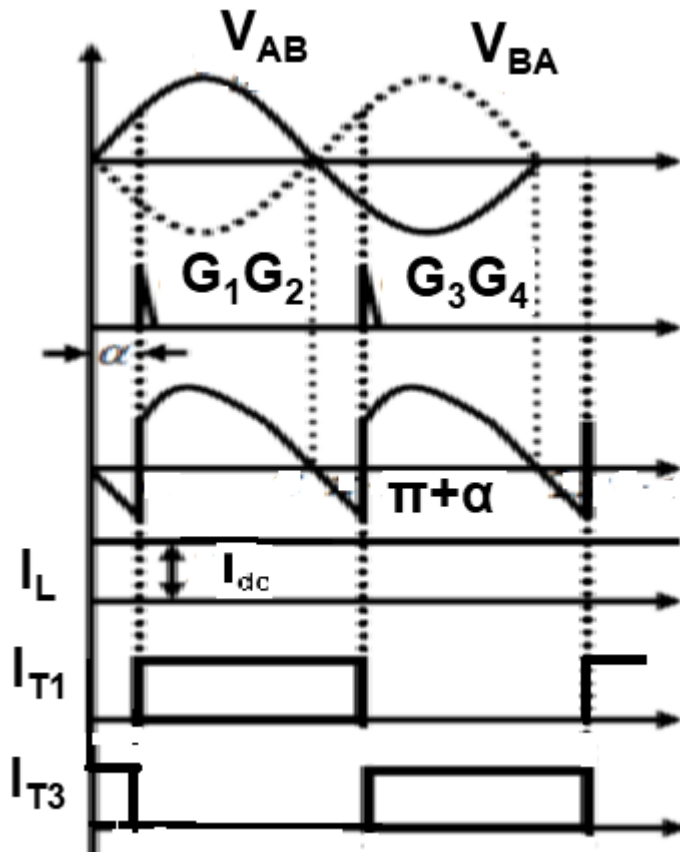
- Change of current from one
- Device to other is instantaneous



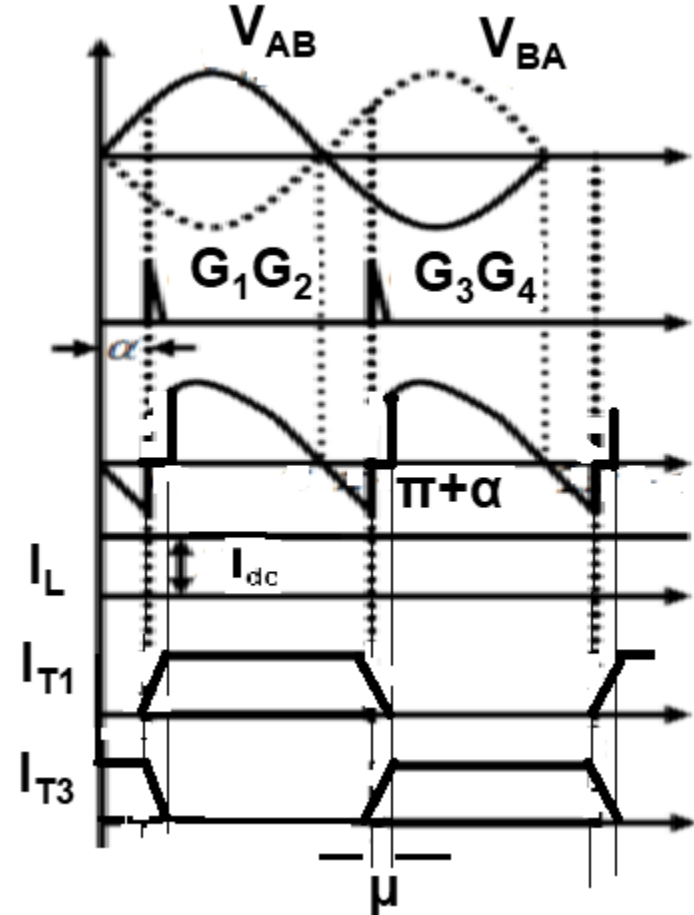
- simultaneously incoming and outgoing devices are conducting

# Effect of source Inductance -2 pulse converter

## ■ Without $L_s$



## With $L_s$



# Effect of source Inductance

## ■ O/P voltage without source inductance

$$V_{dc(av)} = \frac{2}{2\pi} \int_{\alpha}^{\pi+\alpha} V_m \sin \omega \cdot d\omega$$

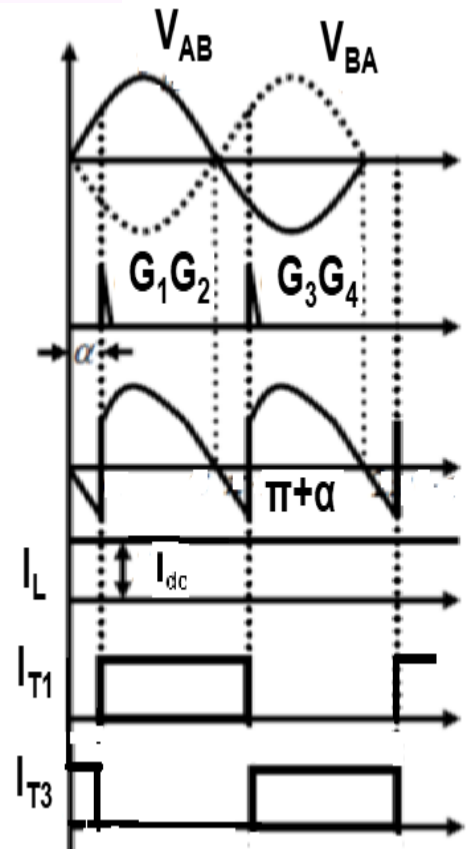
$$V_{dc(av)} = \frac{2V_m}{2\pi} \left[ -\cos \omega \right]_{\alpha}^{\pi+\alpha}$$

$$V_{dc(av)} = \frac{V_m}{\pi} \left[ -\cos(\pi+\alpha) + \cos \alpha \right]$$

$$V_{dc(av)} = \frac{V_m}{\pi} \left[ -\cos \pi \cos \alpha + \sin \pi \sin \alpha + \cos \alpha \right]$$

$$V_{dc(av)} = \frac{V_m}{\pi} \left[ \cos \alpha + \cos \alpha \right]$$

$$V_{dc(av)} = \frac{2V_m}{\pi} \cos \alpha$$



# Effect of source Inductance

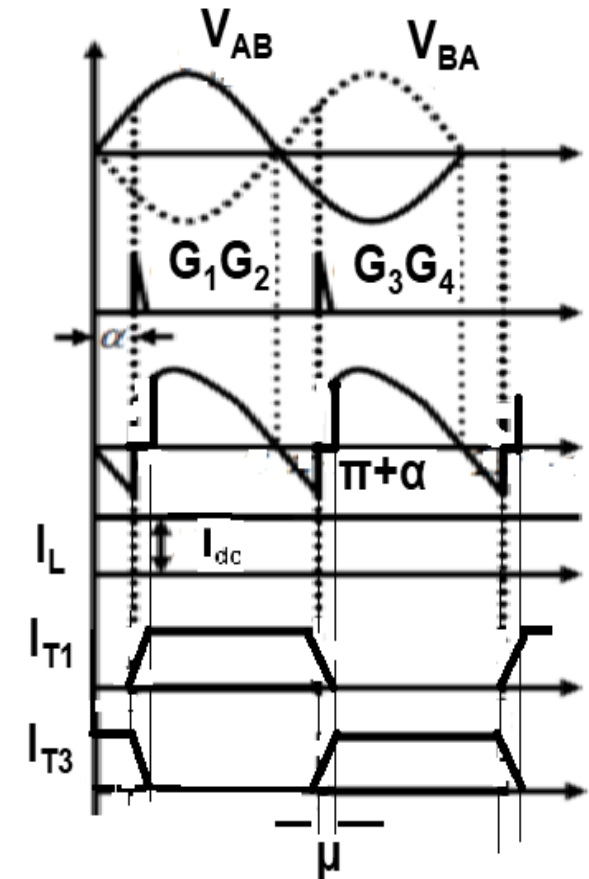
- O/P voltage with source inductance

$$V_{dc(av)} = \frac{2}{2\pi} \int_{\alpha+\mu}^{\pi+\mu} V_m \sin \omega \cdot d\omega$$

$$V_{dc(av)} = \frac{2V_m}{2\pi} \left[ -\cos \omega \right]_{\alpha+\mu}^{\pi+\mu}$$

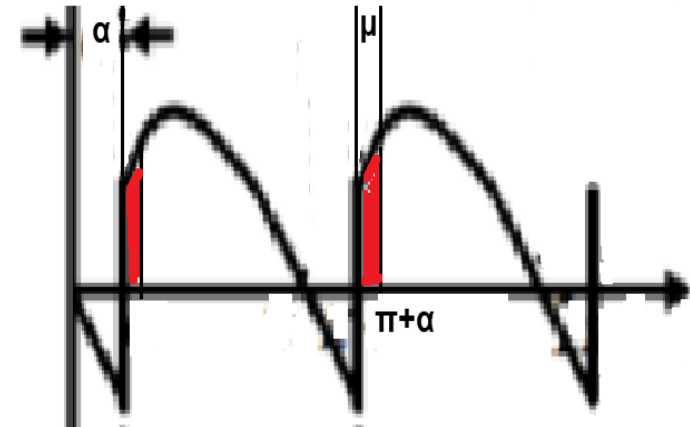
$$V_{dc(av)} = \frac{V_m}{\pi} \left[ -\cos(\pi+\mu) + \cos(\alpha+\mu) \right]$$

$$V_{dc(av)} = \frac{V_m}{\pi} \left[ \cos \mu + \cos(\alpha+\mu) \right]$$



# Effect of source Inductance

## ■ Reduction in O/P voltage



Drop in voltage due to overlap

=  $V_{dc(av)}$  without overlap -  $V_{dc(av)}$  with overlap

$$\Delta V = \frac{2V_m}{\pi} \cos \alpha - \frac{V_m}{\pi} [\cos \alpha + \cos(\alpha + \mu)]$$

$$\Delta V = \frac{V_m}{\pi} [\cos \alpha - \cos(\alpha + \mu)]$$

# Effect of source Inductance

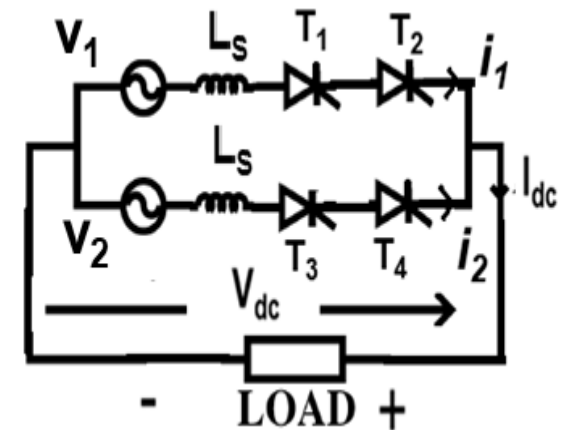
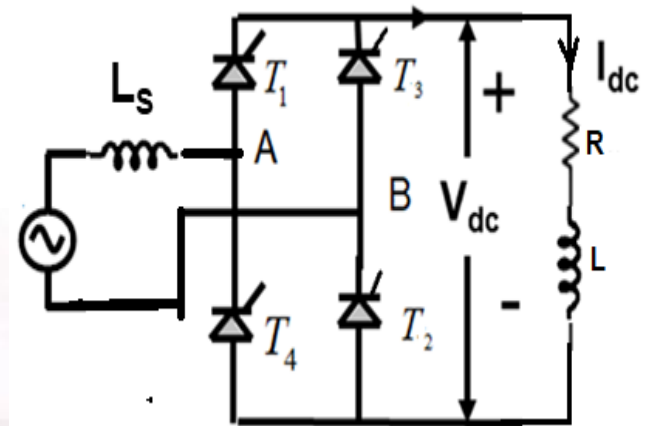
## ■ Vdc

$$v_1 - L_s \frac{di_1}{dt} = v_2 - L_s \frac{di_2}{dt}$$

$$v_1 - v_2 = L_s \left( \frac{di_1}{dt} - \frac{di_2}{dt} \right)$$

$$v_1 = V_m \sin \omega t, \quad v_2 = -V_m \sin \omega t$$

$$L_s \left( \frac{di_1}{dt} - \frac{di_2}{dt} \right) = 2 V_m \sin \omega t$$





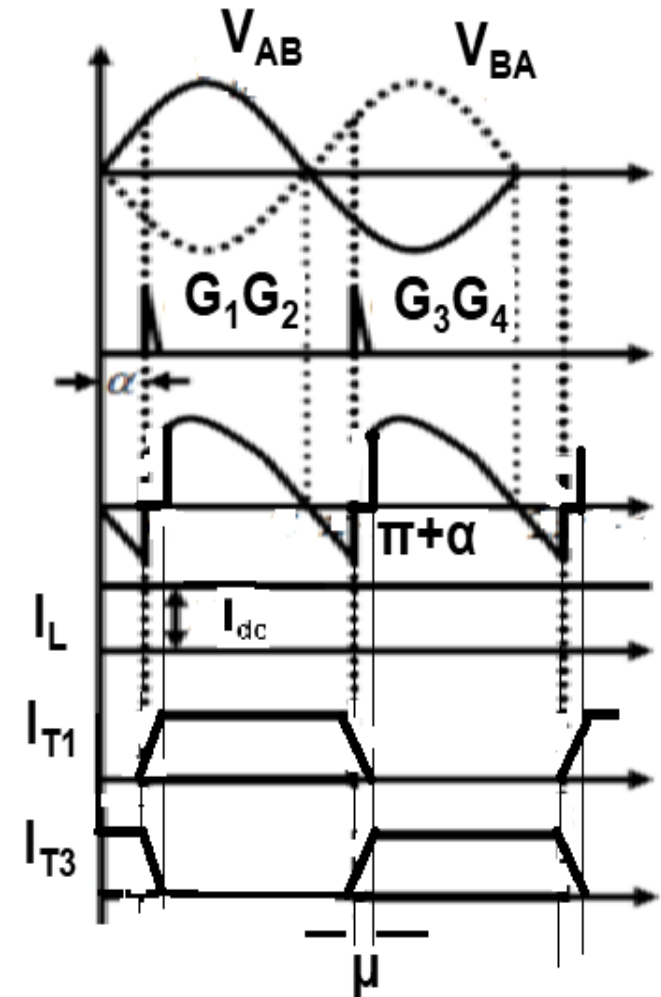
# Effect of source Inductance

## ■ Drop in voltage

$$i_1 + i_2 = I_{dc} = \text{constant}$$
$$\therefore \frac{di_1}{dt} + \frac{di_2}{dt} = 0 \quad \dots \text{I}$$
$$L_s \left( \frac{di_1}{dt} - \frac{di_2}{dt} \right) = 2 V_m \sin \omega t \quad \dots \text{II}$$

Addition of I + II equation

$$2 \frac{di_1}{dt} = \frac{2 V_m \sin \omega t}{L_s}$$
$$\frac{di_1}{dt} = \frac{V_m \sin \omega t}{L_s}$$



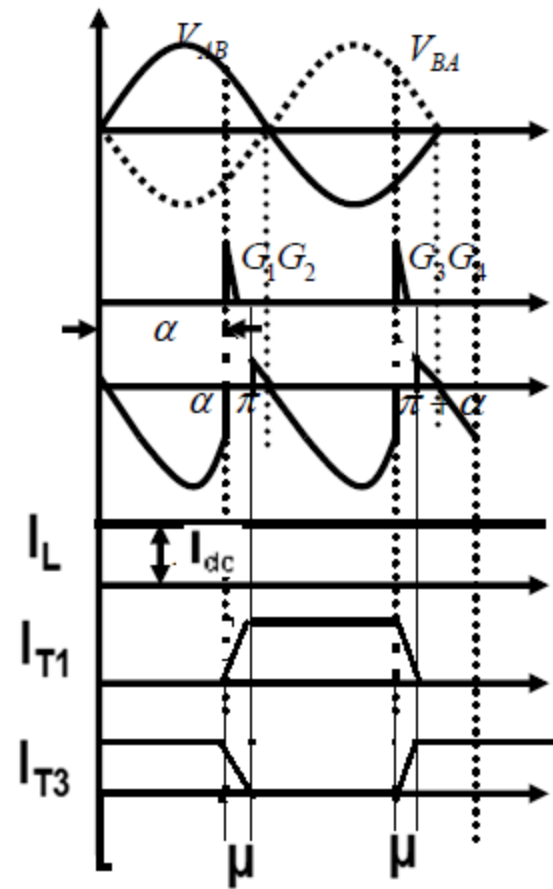
# Effect of source Inductance

$$\begin{aligned} i_1 &= 0 \quad \text{at} \quad \omega t = \alpha \\ i_1 &= I_{dc} \quad \text{at} \quad \omega t = \alpha + \pi \\ \int_0^{I_{dc}} di_1 &= \frac{V_m}{L_s} \int_{\alpha/\omega}^{\alpha+\pi/\omega} \sin \omega t \cdot dt \end{aligned}$$

$$I_{dc} = \frac{V_m}{L_s} \left[ -\frac{\cos \omega t}{\omega} \right] \bigg|_{\alpha/\omega}^{(\alpha+\pi)/\omega}$$

$$I_{dc} = \frac{V_m}{\omega L_s} (\cos \alpha - \cos(\alpha + \pi))$$

$$I_{dc} \cdot \omega L_s = V_m (\cos \alpha - \cos(\alpha + \pi)) \quad \dots \textcircled{III}$$



# Effect of source Inductance

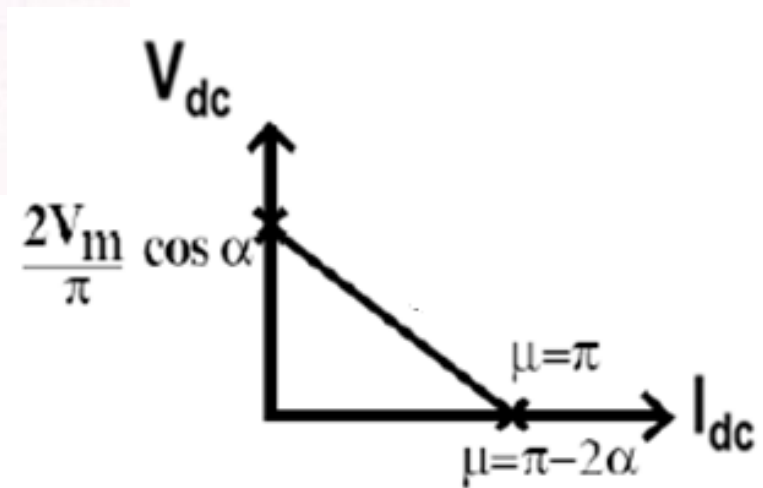
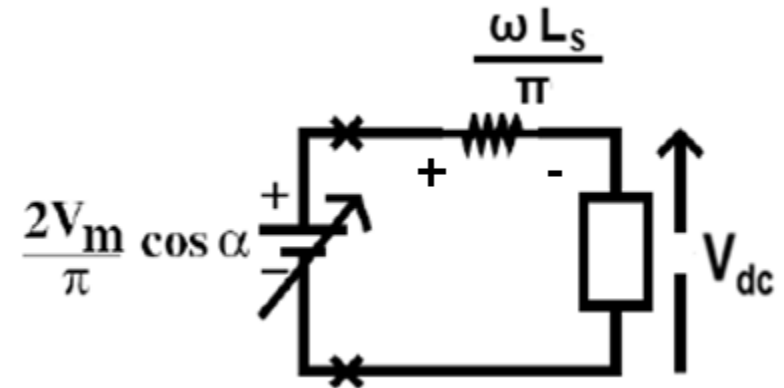
## ■ Equivalent circuit

divide equation III by  $\pi$

$$\frac{I_{dc} \cdot \omega L_s}{\pi} = \frac{V_m}{\pi} [\cos \alpha - \cos(\alpha + \mu)]$$

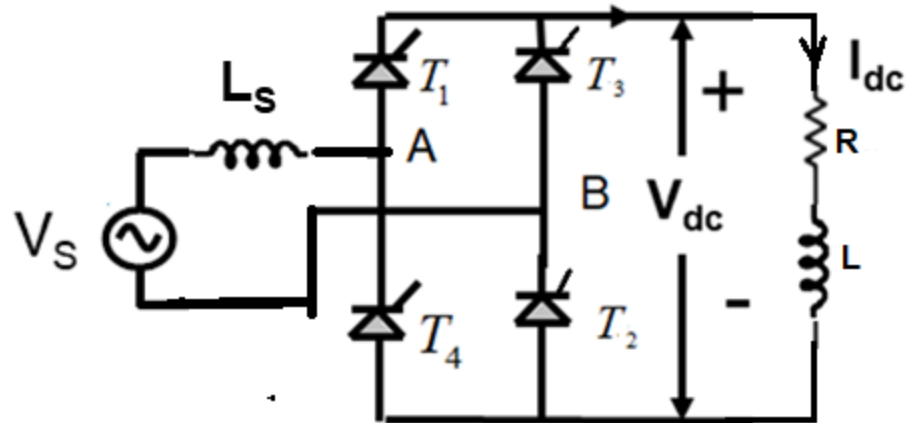
Drop in voltage =  $\frac{I_{dc} \cdot \omega L_s}{\pi}$

Drop in Voltage =  $\frac{\omega L_s}{\pi} \cdot I_{dc}$



# Source inductance Numerical Problem

- $V_{ph} \text{ (rms)} = 230 \text{ V}$
- $\alpha = 45^\circ$ ,  $I_{dc} = 5 \text{ A}$
- $V_{dc} = 135 \text{ V}$
- Determine  $L_s$ , angle  $\mu$ ,
- And load resistance



o/p voltage without overlap for  $\alpha = 45^\circ$

$$V_{dc(av)} = \frac{2V_{ml}}{\pi} \cos \alpha = \frac{2 \times \sqrt{2} \times 230}{\pi} \cos 45^\circ$$

$$\therefore V_{dc(av)} = 146.42$$

# Source inductance Numerical Problem

$$\text{Voltage with overlap} = 135 \text{ V}$$

$$\begin{aligned}\text{Drop in voltage due to overlap} &= 146.42 - 135 \\ &= 11.42 \text{ V}\end{aligned}$$

$$\text{Drop in voltage} = \frac{\omega L_s}{\pi} \cdot I_{dc}$$

$$11.42 = \frac{2\pi f \times L_s}{\pi} \times 5 \text{ A}$$

$$L_s = \frac{11.42}{2 \times 50 \times 5} = 22.84 \text{ mH}$$

$$\text{Drop in voltage} = \frac{V_m}{\pi} (\cos \alpha + \cos(\alpha + \mu))$$

# Source inductance Numerical Problem

Putting the values

$$11.42 = \frac{\sqrt{2} \times 230}{\pi} (\cos 45^\circ - \cos(\alpha + \mu))$$

$$\cos 45^\circ - \cos(\alpha + \mu) = \frac{11.42 \times \pi}{\sqrt{2} \times 230} = 0.1102$$

$$0.1102 = \cos 45^\circ - \cos(\alpha + \mu)$$

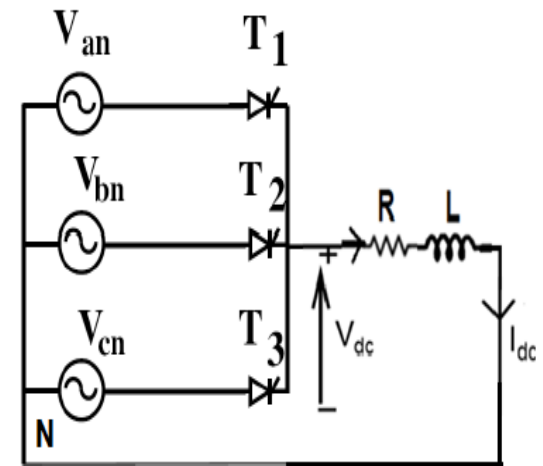
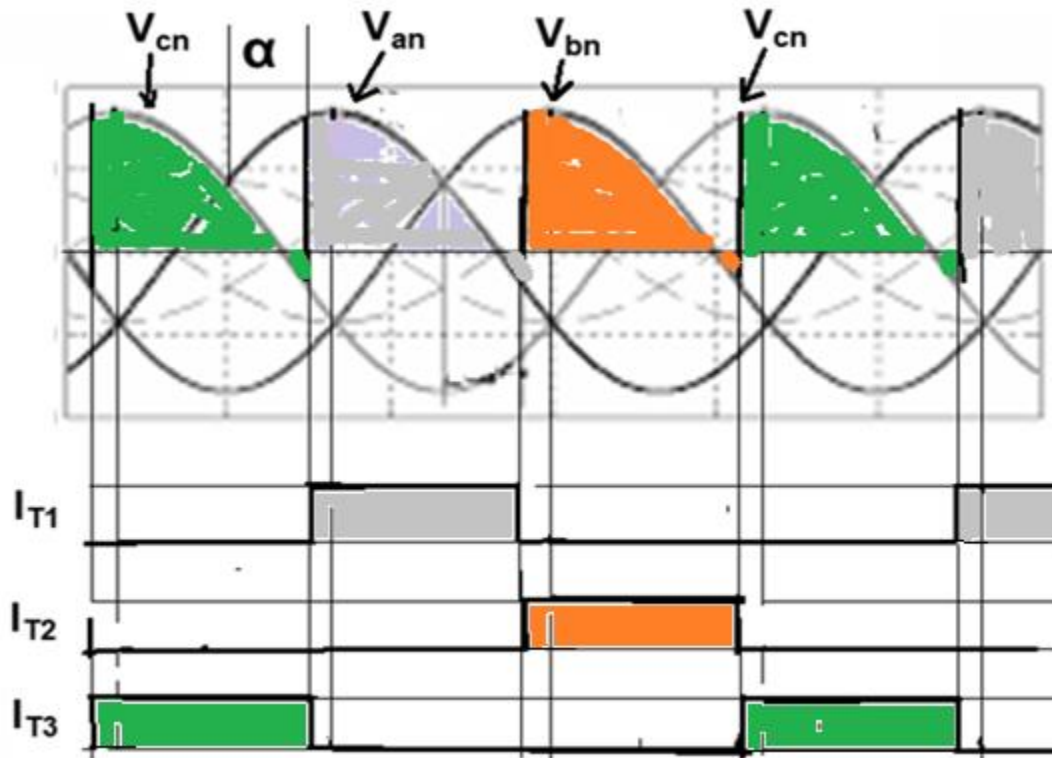
$$\begin{aligned} \therefore \cos(\alpha + \mu) &= \cos 45^\circ - 0.1102 \\ &= 0.566906 \end{aligned}$$

$$\therefore \cos(\alpha + \mu) = 55.46^\circ \quad \therefore \mu = 10.46^\circ$$

$$\text{Load } R = \frac{V_{dc}}{I_{dc}} = \frac{135}{5} = 27 \Omega$$

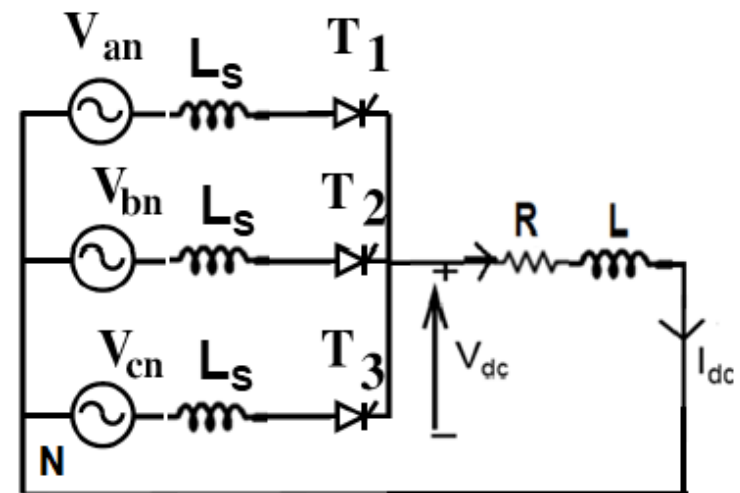
# Source Inductance- 3 pulse converter

- o/p voltage without source inductance  $\alpha = 45^\circ$



# Source Inductance- 3 pulse converter

- Commutation from T3 to T1
- Transfer of current is gradual from T3 to T1
- Line to line voltage is shorted
- Voltage is absorbed across source inductance



- O/P voltage during commutation is the average of outgoing and incoming voltages



# Source Inductance- 3 pulse converter

Considering commutation from  $T_3$  to  $T_1$

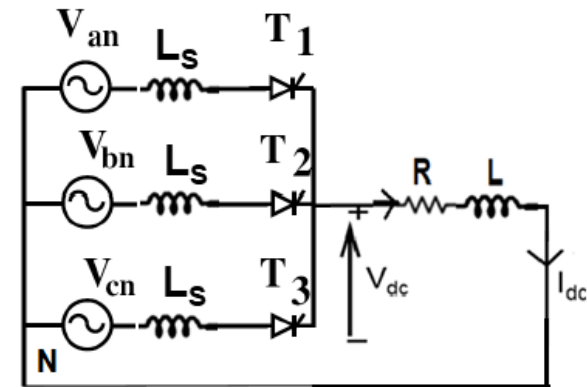
$$V_{an} = L_s \frac{di_{T_1}}{dt} + V_d' \quad \text{..... (I)}$$

$$V_{cn} = L_s \frac{di_{T_3}}{dt} + V_d' \quad \text{..... (II)}$$

During commutation  $I_{dc} = \text{constant}$

$$i_{T_1} + i_{T_3} = I_{dc} \quad \text{..... (III)}$$

$$\frac{di_{T_1}}{dt} + \frac{di_{T_3}}{dt} = 0 \quad \text{..... (IV)}$$



# Source Inductance- 3 pulse converter

Adding equations I and II

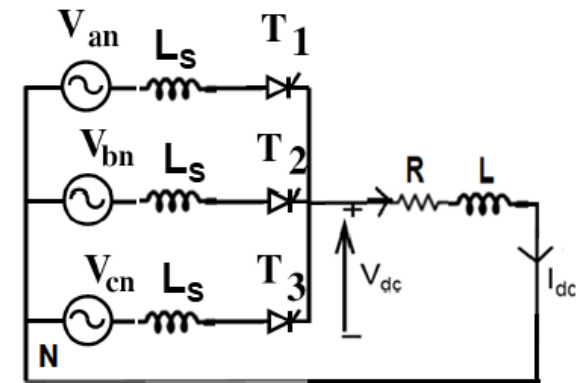
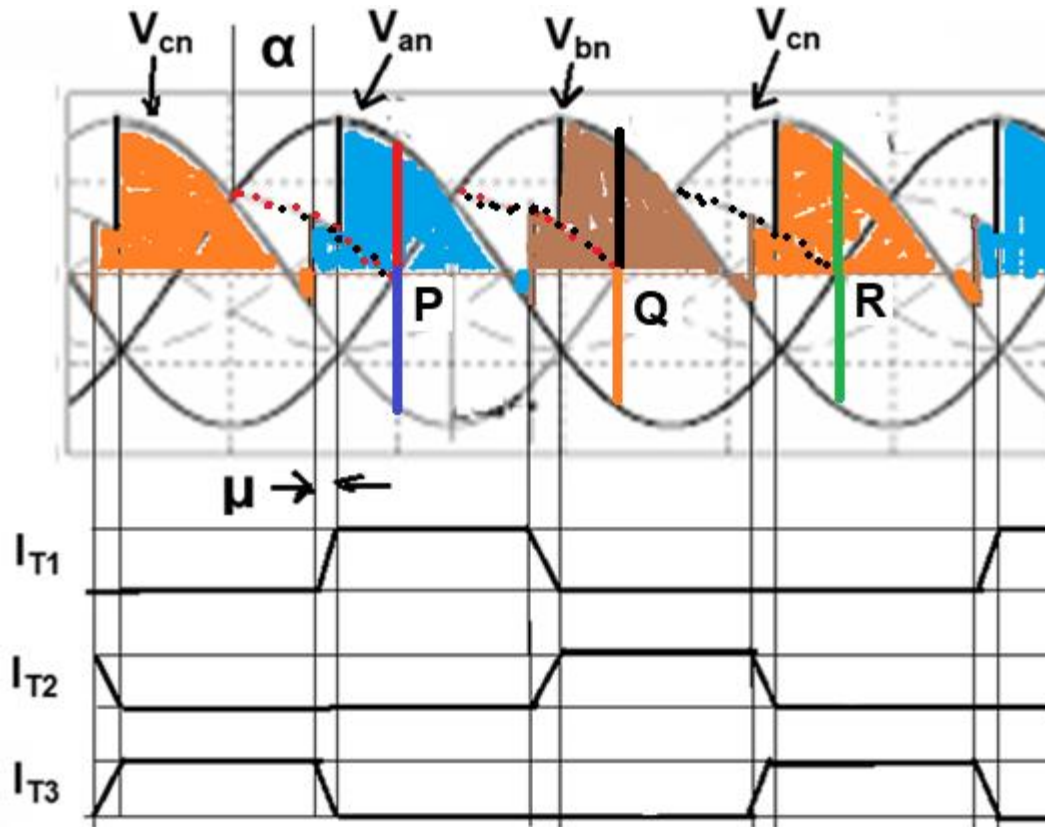
$$V_{an} + V_{cn} = L_s \left( \frac{di_{T1}}{dt} + \frac{di_{T3}}{dt} \right) + 2V_d'$$

$$\therefore V_d' = \frac{1}{2} (V_{an} + V_{cn})$$

- During commutation period ( overlap period) output voltage is average of incoming and outgoing voltages

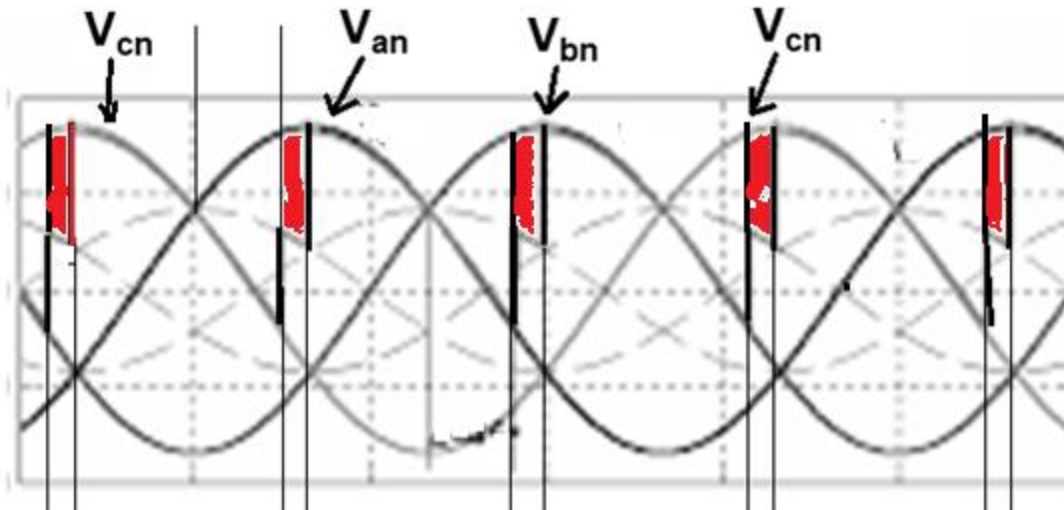
# Source Inductance- 3 pulse converter

- Output voltage with source inductance  $\alpha = 45^\circ$



# Source Inductance- 3 pulse converter

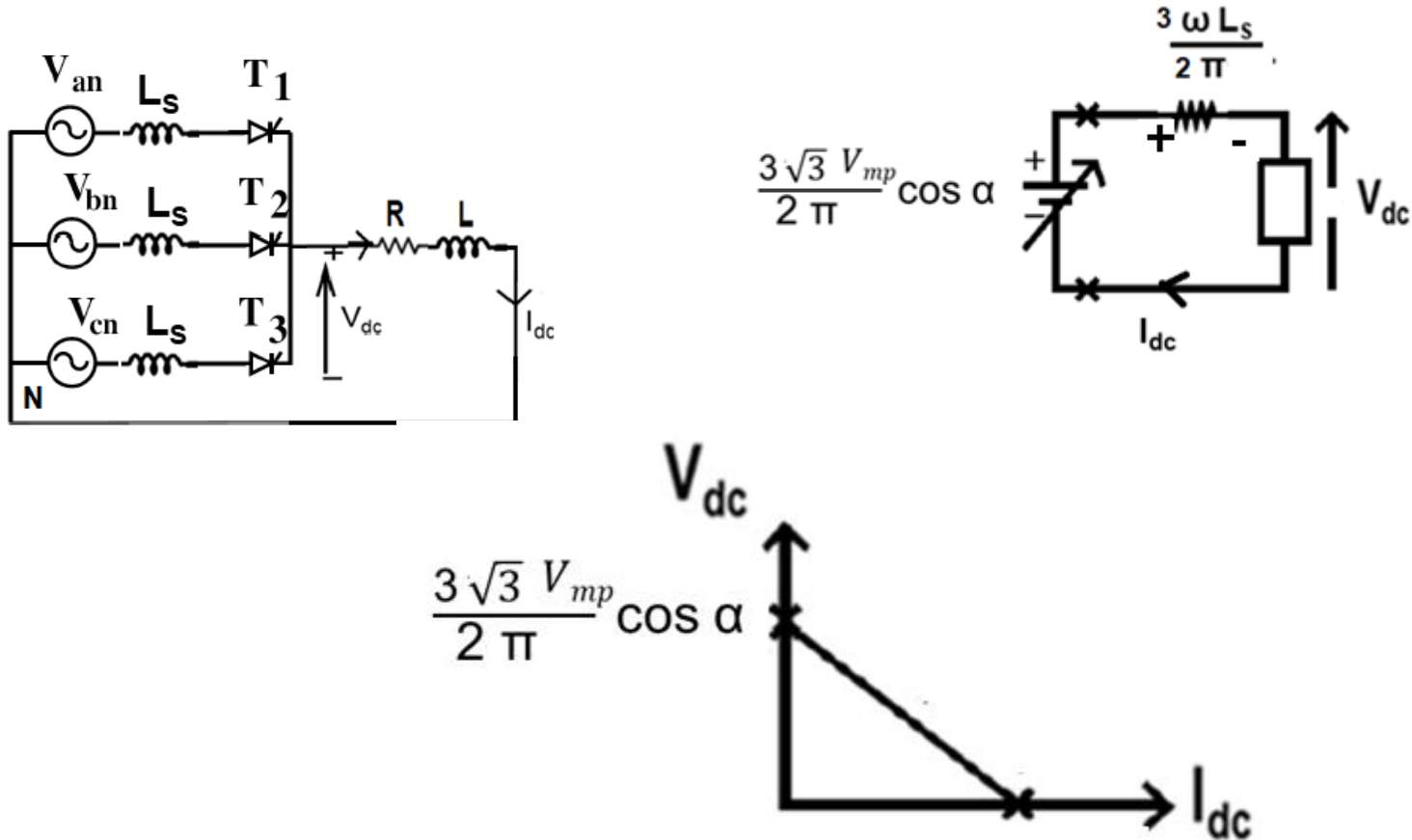
- Loss of voltage due to overlap



- Hatched area will represent reduction in O/P voltage
- Reduction of o/p voltage =  $(3\omega L_s I_{dc}) / 2\pi$

# Source Inductance- 3 pulse converter

## ■ Equivalent circuit



# Converter with source induction

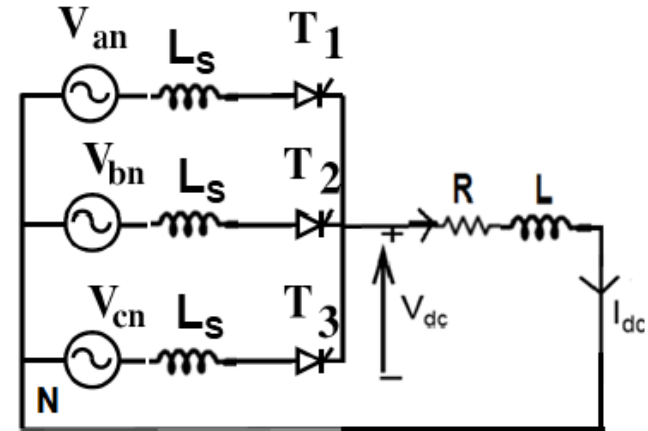
- 2 pulse  $\Rightarrow$  Drop in voltage =  $\frac{\omega L_s I_{dc}}{\pi}$
- 3 pulse  $\Rightarrow$  Drop in voltage =  $\frac{3 \omega L_s I_{dc}}{2 \pi}$
- 6 pulse  $\Rightarrow$  Drop in voltage =  $\frac{3 \omega L_s I_{dc}}{\pi}$

# Converter with source inductance

- O/P voltage without source inductance
- $V_{dc(av)} = V_{dc(max)} \cos\alpha$
- O/P voltage with overlap
- $V_0 = (V_{dc(max)}/2)(\cos\alpha + \cos(\alpha+\mu))$
- Drop in voltage =  $(V_{dc(max)}/2)(\cos\alpha - \cos(\alpha+\mu))$
  
- $V_{dc(max)} = \frac{2V_m}{\pi} \Rightarrow$  For 2 pulse converter
- $V_{dc(max)} = \frac{3\sqrt{3} V_{mp}}{2\pi} \Rightarrow$  For 3 pulse converter
- $V_{dc(max)} = \frac{3V_{ml}}{\pi} \Rightarrow$  For 6 pulse converter

# Source Inductance- 3 pulse converter

- Numerical problem
- $V_{ph} \text{ (rms)} = 230 \text{ V}$
- $\alpha = 30^\circ$ ,  $I_{dc} = 15 \text{ A}$
- $V_{dc} = 220 \text{ V}$
- Determine  $L_s$ , angle  $\mu$ , and load resistance





# Source Inductance- 3 pulse converter

$$V_{dc(av)} = \frac{3\sqrt{3} V_{mp}}{2\pi} \cos \alpha = \frac{3\sqrt{3} \times \sqrt{2} \times 230}{2\pi} \cos 30^\circ$$

$$V_{dc(av)} = 232.9568 \text{ V}$$

$$\text{Voltage without overlap} = 232.9568 \text{ V}$$

$$\text{Voltage with overlap} = 220 \text{ V}$$

$$\begin{aligned} \text{Drop in voltage due to overlap} &= 232.95 - 220 \\ &= 12.9568 \text{ V} \end{aligned}$$

$$\text{Drop in voltage} = \frac{3 \omega L_s}{2\pi} \cdot I_{dc}$$

Putting values

$$12.9568 = \frac{3 \times 2\pi \times 50 \times L_s \times 15}{2\pi}$$

$$\therefore L_s = 5.758 \text{ mH}$$

# Source Inductance- 3 pulse converter

$$\text{Drop in voltage} = \frac{3\sqrt{3} V_{mp}}{2\pi} \times \left( \frac{\cos \alpha - \cos(\alpha + \mu)}{2} \right)$$

Putting values,

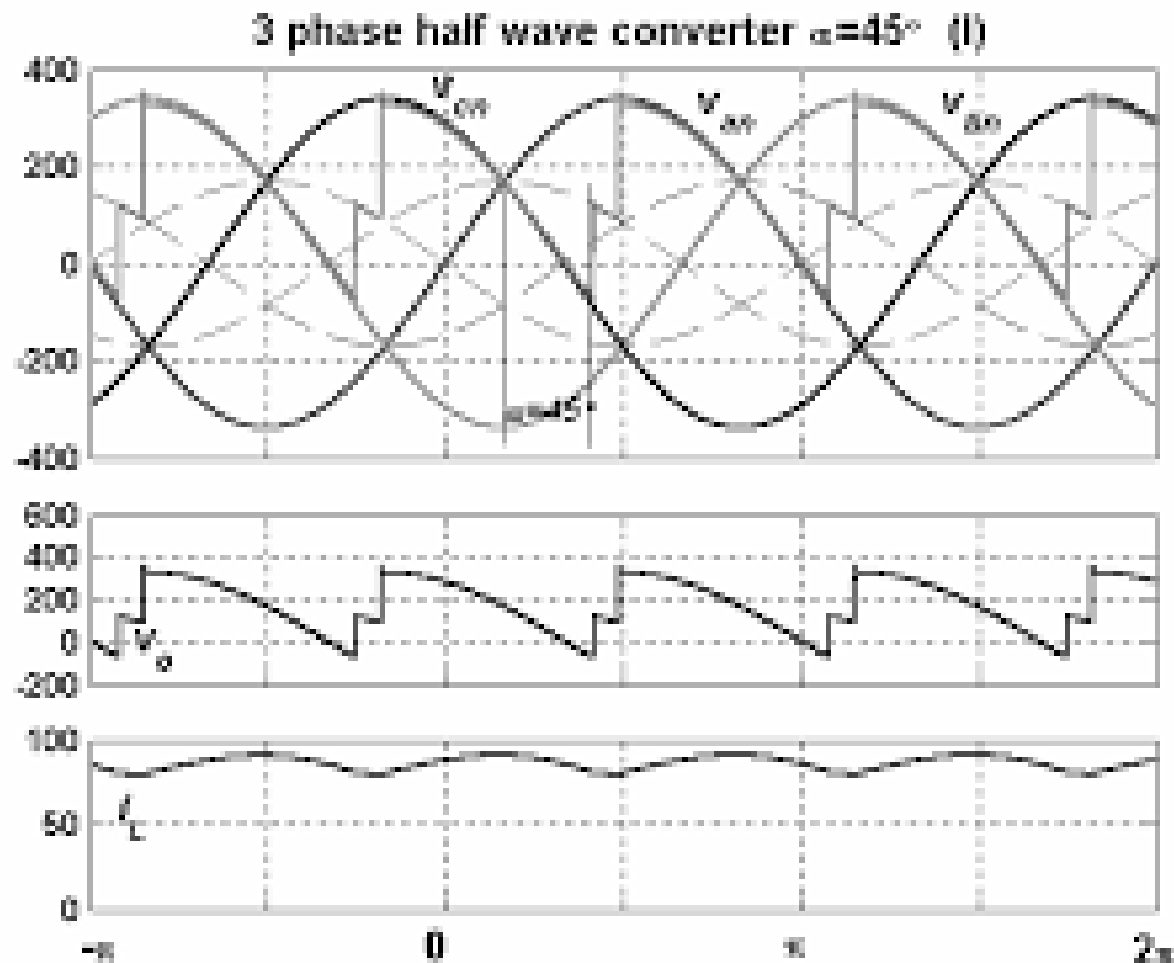
$$12.9568 = \frac{3\sqrt{3} \times \sqrt{2} \times 230}{4\pi} (\cos \alpha - \cos(\alpha + \mu))$$

$$\begin{aligned} \cos(\alpha) - \cos(\alpha + \mu) &= \frac{12.9568 \times 4\pi}{3\sqrt{3} \times \sqrt{2} \times 230} \\ &= 0.09633 \end{aligned}$$

$$\begin{aligned} \cos(\alpha + \mu) &= \cos 30 - 0.09633 \\ &= 0.7696 \end{aligned}$$

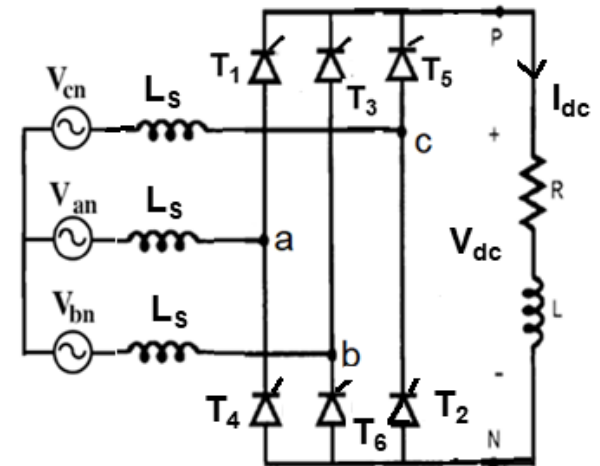
$$(\alpha + \mu) = 39.62^\circ \quad \therefore \mu = 9.62^\circ$$

# Source Inductance- 3 pulse converter



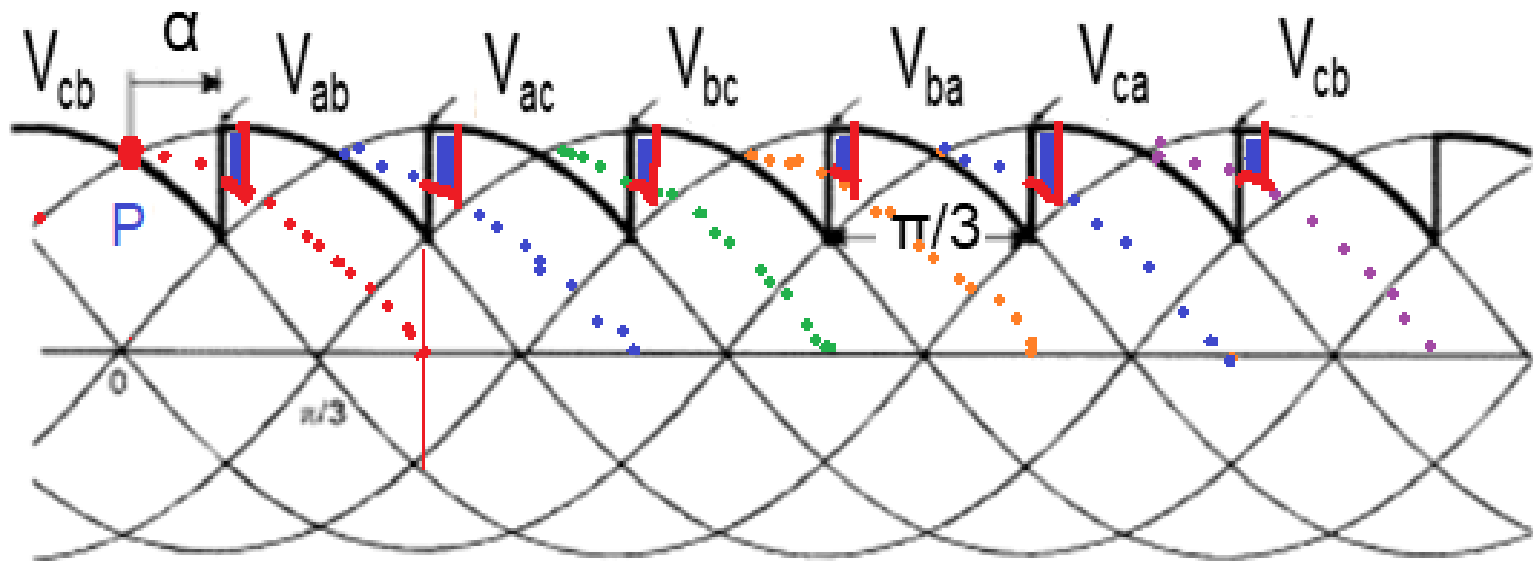
# Source inductance 6 pulse converter

- Commutation between  $T_1$ ,  $T_3$  and  $T_5$
- Commutation between  $T_2$ ,  $T_4$  and  $T_6$
- During commutation three deices are conducting
- a)  $T_1$   $T_2$   $T_3$  b)  $T_2$   $T_3$   $T_4$
- c)  $T_3$   $T_4$   $T_5$  d)  $T_4$   $T_5$   $T_6$
- e)  $T_5$   $T_6$   $T_1$  f)  $T_6$   $T_1$   $T_2$
- six commutations per cycle



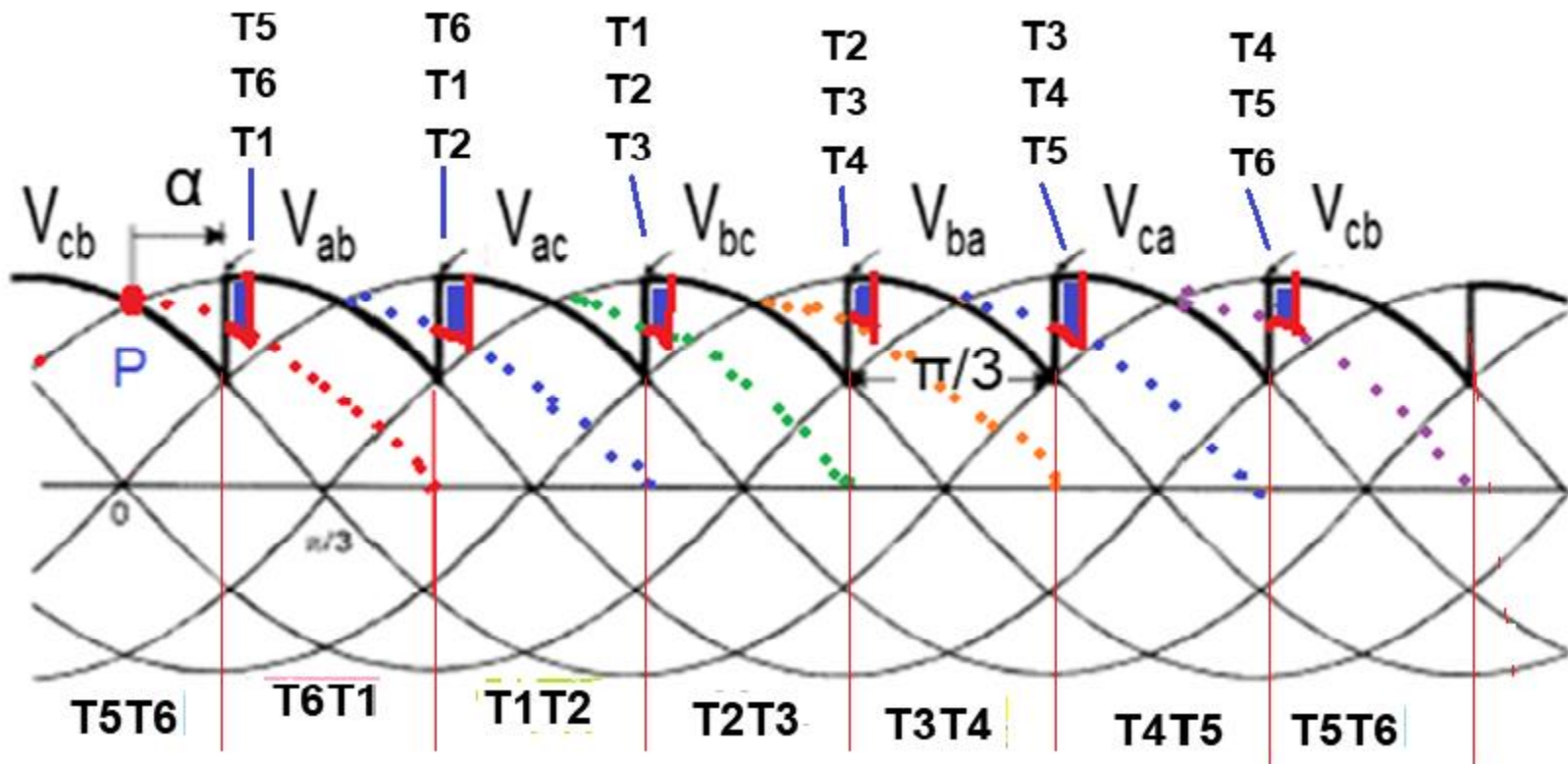
# Source inductance 6 pulse converter

- Waveform for  $\alpha = 30^\circ$
- Output voltage during commutation is average of incoming and outgoing voltages



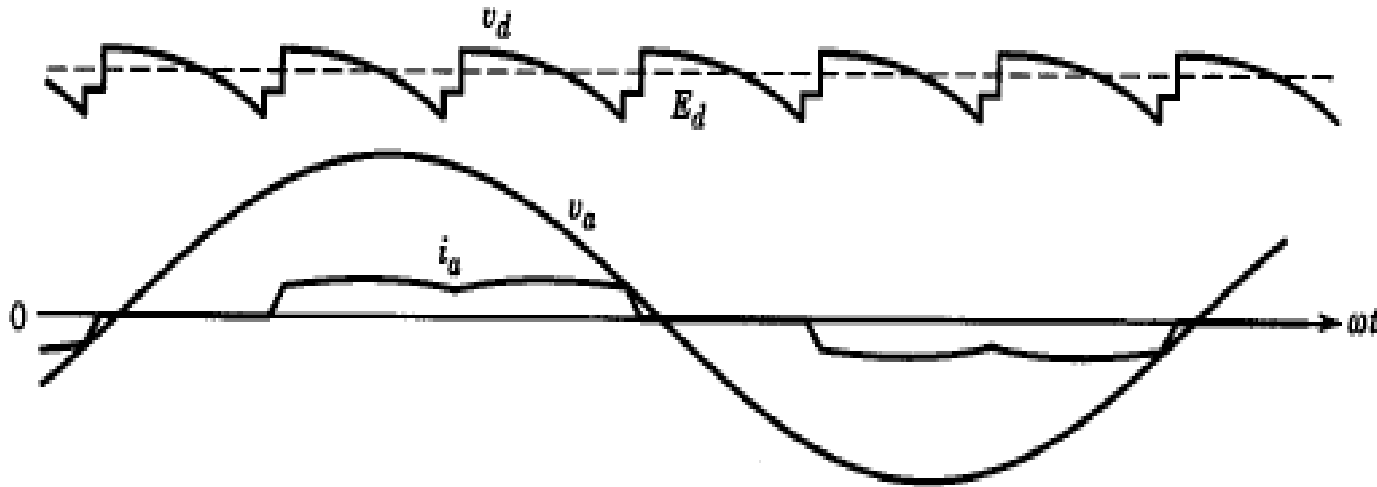
# 6 pulse converter : source inductance

## ■ Commutation process



# Source inductance 6 pulse converter

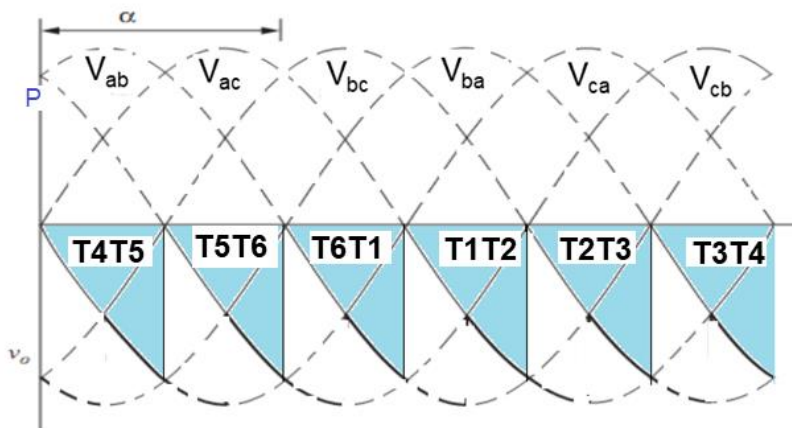
- Output voltage and source current
- Firing angle  $\alpha = 30^\circ$



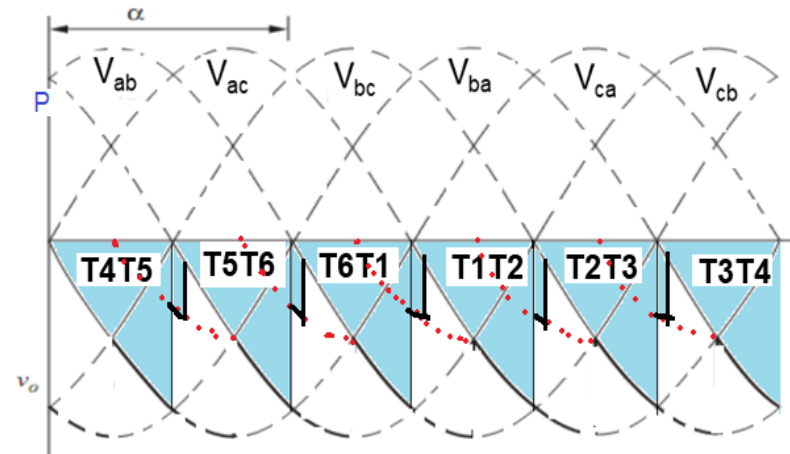
# Source inductance 6 pulse converter

- Firing angle  $\alpha = 120^\circ$

- Without overlap



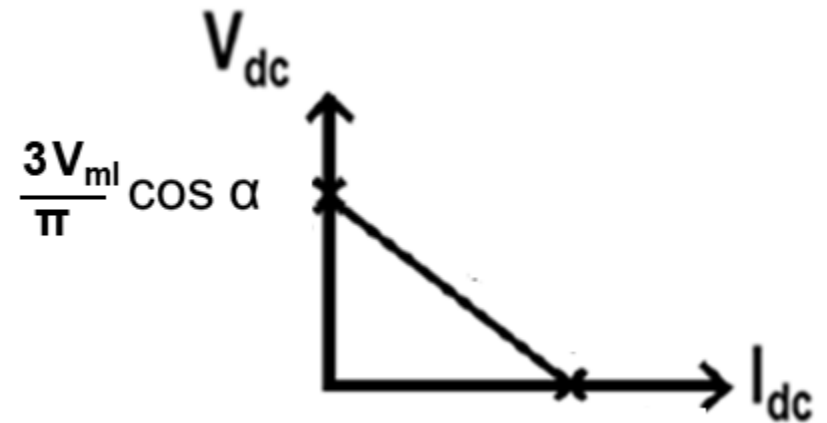
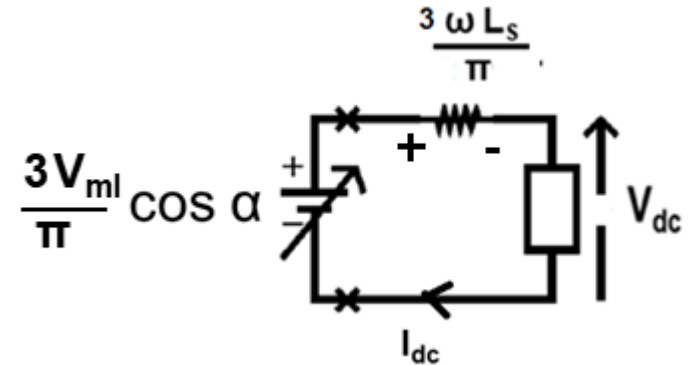
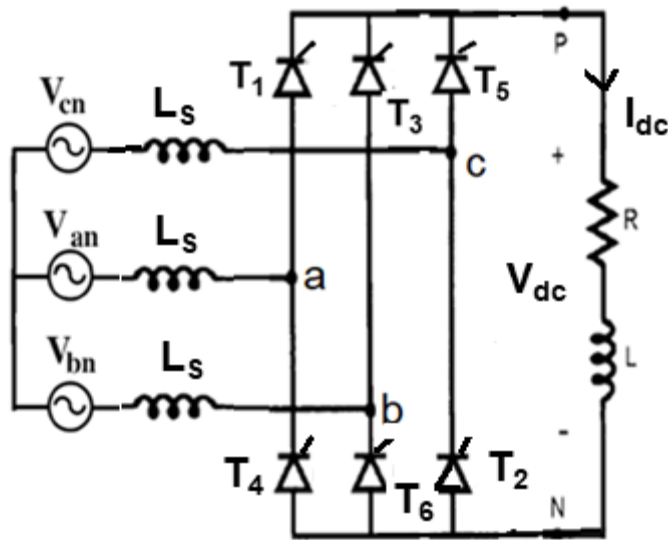
- With overlap





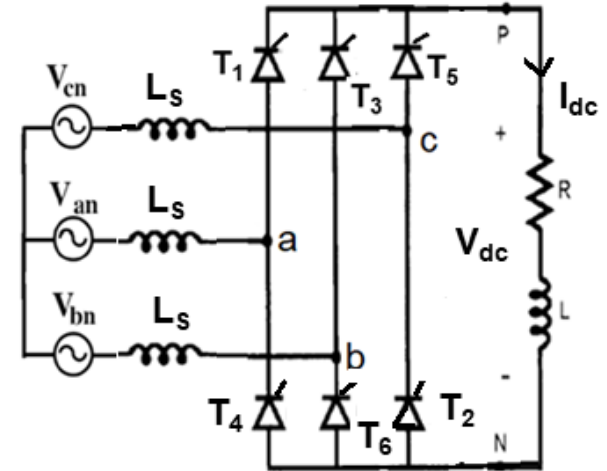
# Source inductance 6 pulse converter

## ■ Circuit diagram



# Source inductance 6 pulse converter

- Numerical problem
- $V_L(\text{rms}) = 400 \text{ V}$
- $\alpha = 60^\circ$ ,  $I_{dc} = 25 \text{ A}$
- $V_{dc} = 255 \text{ V}$
- Determine  $L_s$ , angle  $\mu$ , and load resistance



# Source inductance 6 pulse converter

$$\text{Voltage without overlap} = \frac{3 V_{ml}}{\pi} \cos \alpha$$

$$= \frac{3 \times \sqrt{2} \times 400}{\pi} \cos 60 = 270.09 \text{ V}$$

$$\text{Voltage with overlap} = 255 \text{ V}$$

$$\text{Drop due to overlap} = 270.09 - 255 = 15.09 \text{ V}$$

$$\text{Drop in voltage} = \frac{3 \omega \cdot L_s}{\pi} I_{dc}$$

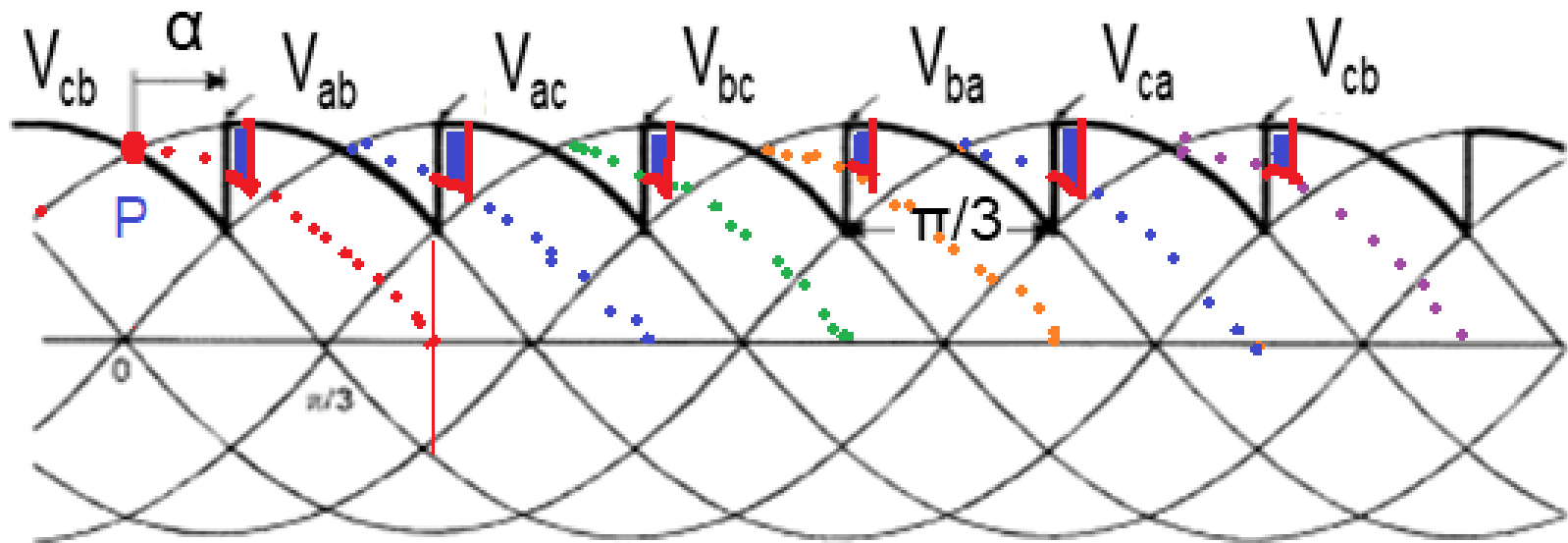
$$15.09 = \frac{3 \times 2\pi \times 50 L_s}{\pi} \times 25$$

$$\therefore L_s = \frac{15.09 \pi}{3 \times 2\pi \times 50 \times 25} = 2.01 \text{ mH}$$

# Source inductance 6 pulse converter

$$\begin{aligned}\text{Drop in voltage} &= \frac{3 V_{m\lambda}}{\pi} \left( \frac{\cos \alpha - \cos(\alpha + \mu)}{2} \right) \\ 15.09 &= \frac{3 \times \sqrt{2} \times 400}{2\pi} (\cos \alpha - \cos(\alpha + \mu)) \\ \cos \alpha - \cos(\alpha + \mu) &= \frac{15.09 \times 2\pi}{3 \times \sqrt{2} \times 400} = 0.05586 \\ \therefore \cos(\alpha + \mu) &= \cos 60 - 0.05586 \\ &= 0.4441 \\ \alpha + \mu &= 63.634^\circ \\ \mu &= 3.634^\circ\end{aligned}$$

# Source inductance 6 pulse converter



# Converter with source induction

- 2 pulse => Drop in voltage =  $\frac{\omega L_s I_{dc}}{\pi}$
- 3 pulse => Drop in voltage =  $\frac{3 \omega L_s I_{dc}}{2 \pi}$
- 6 pulse => Drop in voltage =  $\frac{3 \omega L_s I_{dc}}{\pi}$

# Converter with source inductance

- O/P voltage without source inductance
- $V_{dc(av)} = V_{dc(max)} \cos\alpha$
- O/P voltage with overlap
- $V_0 = (V_{dc(max)}/2)(\cos\alpha + \cos(\alpha+\mu))$
- Drop in voltage =  $(V_{dc(max)}/2)(\cos\alpha - \cos(\alpha+\mu))$
  
- $V_{dc(max)} = \frac{2V_m}{\pi} \Rightarrow$  For 2 pulse converter
- $V_{dc(max)} = \frac{3\sqrt{3} V_{mp}}{2\pi} \Rightarrow$  For 3 pulse converter
- $V_{dc(max)} = \frac{3V_{ml}}{\pi} \Rightarrow$  For 6 pulse converter

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THANKS !

Any Questions?