

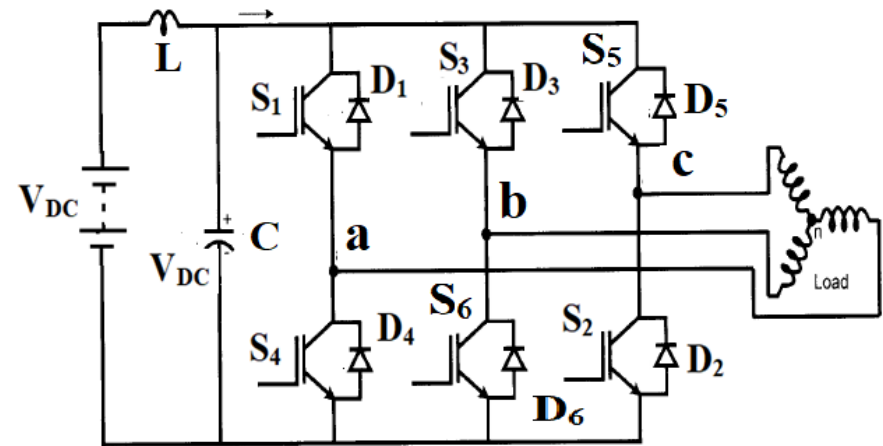
# DC to AC Converter: Inverter



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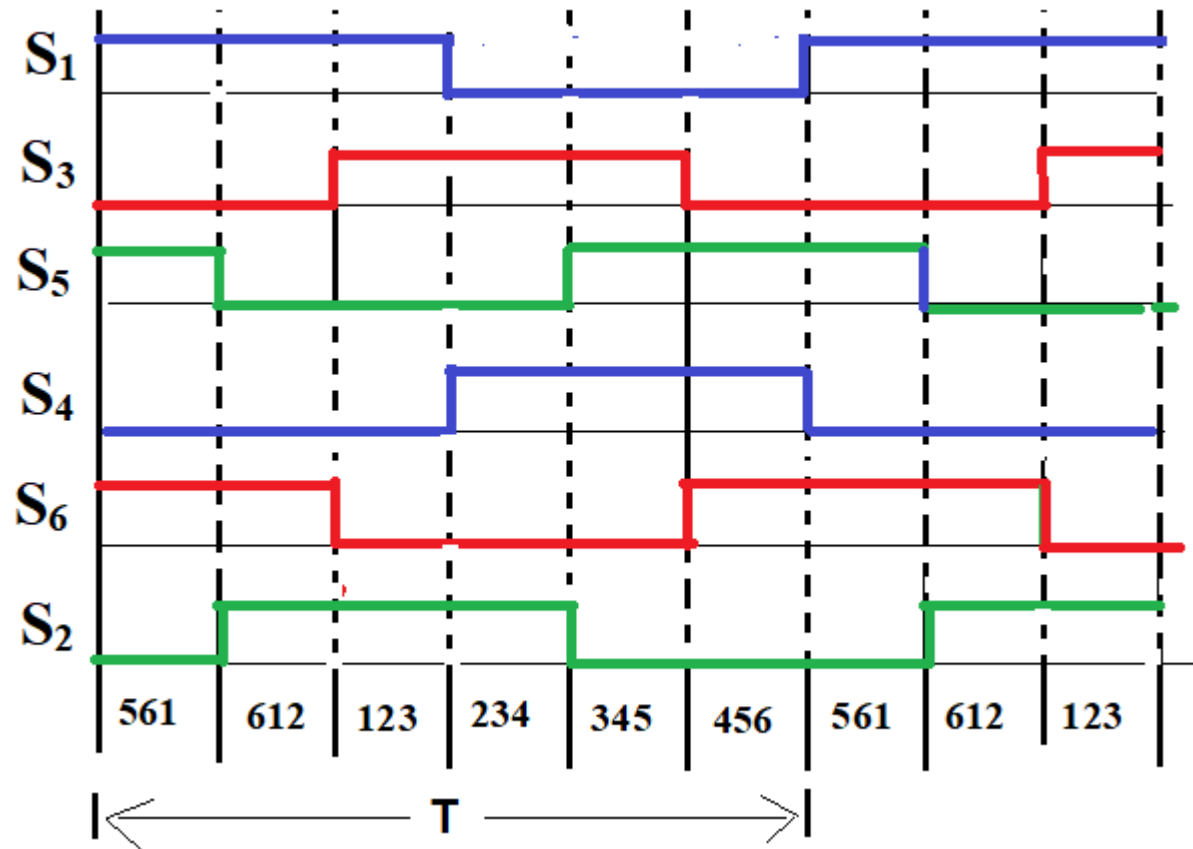
# Three Phase VSI Bridge Inverter

- It consists of 3 legs
- Devices are named as per conducting sequence
- Controlled quantities  
Voltage, frequency  
and phase sequence
- Operating modes  
 $180^\circ$ ,  $120^\circ$  and PWM



# 180° mode of conduction

## ■ Switching signal



# 180° mode of conduction

- Each device conducts for 180°
- One device from each leg is ON
- Three devices are on simultaneously
- Devices are named as per conducting sequence
- Dead time is required to avoid the short circuit of DC link
- Phase shift between the legs is 120°.

# 180° mode of conduction

■  $V_{ab}$

Switch ON	O/P Voltage
$S_1 S_6$	$+V_{DC}$
$S_3, S_4$	$-V_{DC}$
$S_1 S_3$ OR $S_4 S_6$	O

■  $V_{bc}$

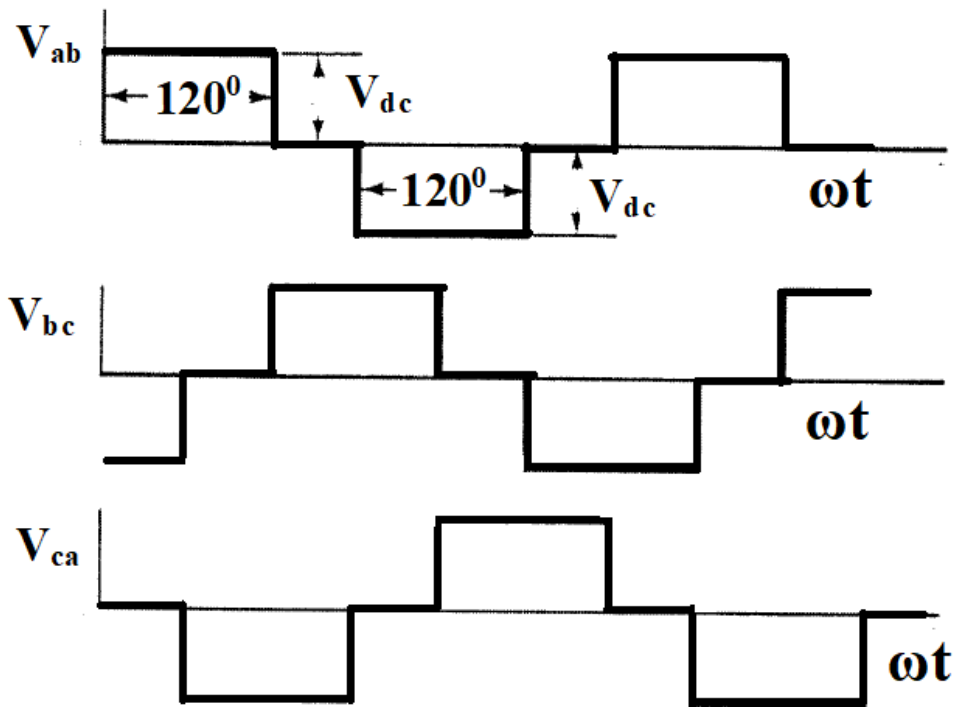
Switch ON	O/P Voltage
$S_2 S_3$	$+V_{DC}$
$S_5 S_6$	$-V_{DC}$
$S_3 S_5$ OR $S_2 S_6$	O

$V_{ca}$

Switch ON	O/P Voltage
$S_4 S_5$	$+V_{DC}$
$S_1 S_2$	$-V_{DC}$
$S_1 S_5$ OR $S_2 S_4$	O

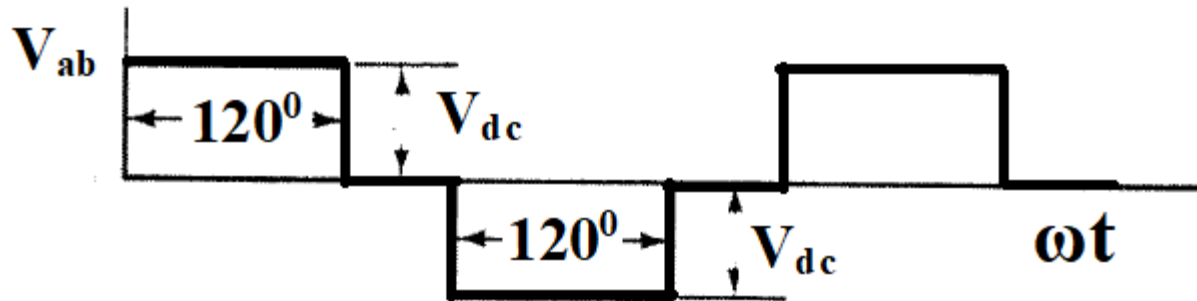
# 180° mode of conduction

- line voltages

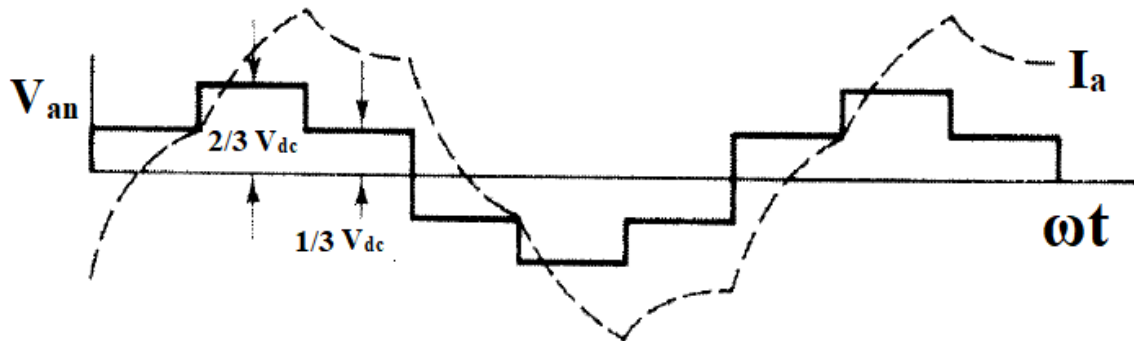


# 180° mode of conduction

## ■ Line voltage

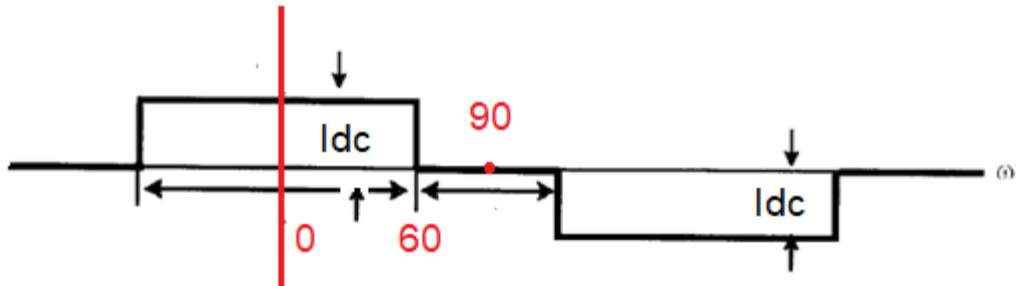


## ■ Phase voltage



# Harmonic spectrum of a waveform

- $A_n = \frac{8}{2\pi} \int_0^{\pi/2} F(\theta) \cos(n\theta) d\theta$



- $A_n = \frac{8}{2\pi} \int_0^{\pi/3} Idc \cos(n\theta) d\theta$

- $A_n = (4/n\pi) I_{dc} \sin(n\pi/3)$

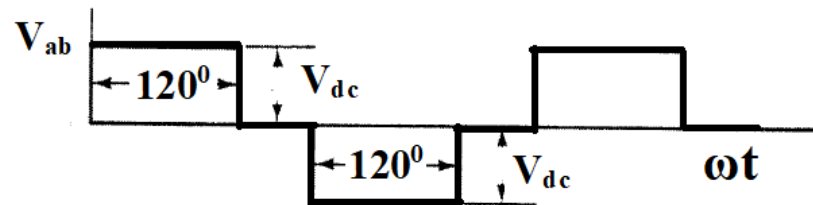
- $I^2 = I_1^2 + I_h^2$

- $A_1 = \frac{2\sqrt{3}}{\pi} I_{dc} \quad I_1 = \frac{\sqrt{6}}{\pi} I_{dc}$



# 180° mode of conduction

- Harmonic analysis
- It is also called as square wave inverter



- Harmonic spectrum is given by

$$V_{ab} = \frac{2\sqrt{3}}{\pi} V_{dc} \left\{ \sin \omega t - \frac{1}{5} \sin 5\omega t - \frac{1}{7} \sin 7\omega t - \dots \right\}$$

- It contains  $6m+1$  and  $6m-1$  harmonics
- THD = 30.4%

# 180° mode of conduction

- o/p voltage

$$\text{R.M.S of L-L is } \sqrt{\frac{2}{3}} V_{dc} = 0.816 V_{dc}$$

- Fundamental component of line voltage

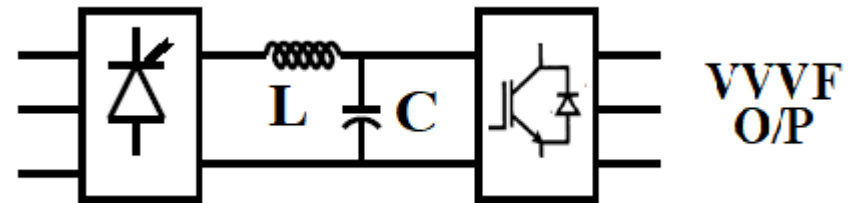
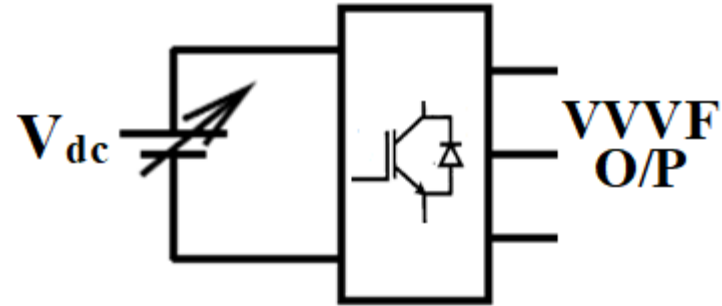
$$\text{Fundamental} = \frac{\sqrt{6}}{\pi} V_{dc} = 0.78 V_{dc}$$

# 180° mode of conduction

- O/P voltage control by controlling the input dc voltage applied to the inverter.
- Switching signal will not control the output voltage
- Switching signal will control the o/p frequency
- It is controlled by controlling T period of the switching signal

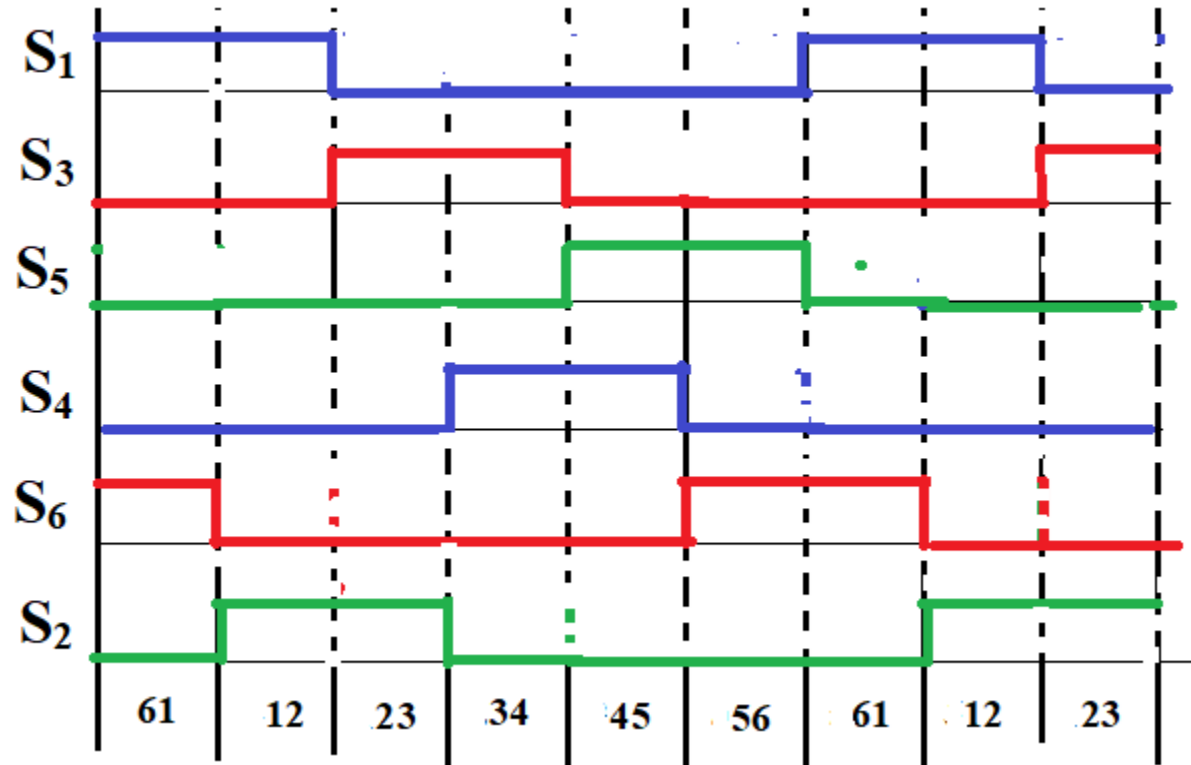
# 180° mode of conduction

- Variable voltage can be obtained from converter
- As  $V_{dc}$  decreases  $\alpha$  increase and PF decreases



# 120° mode of conduction

## ■ Switching signal

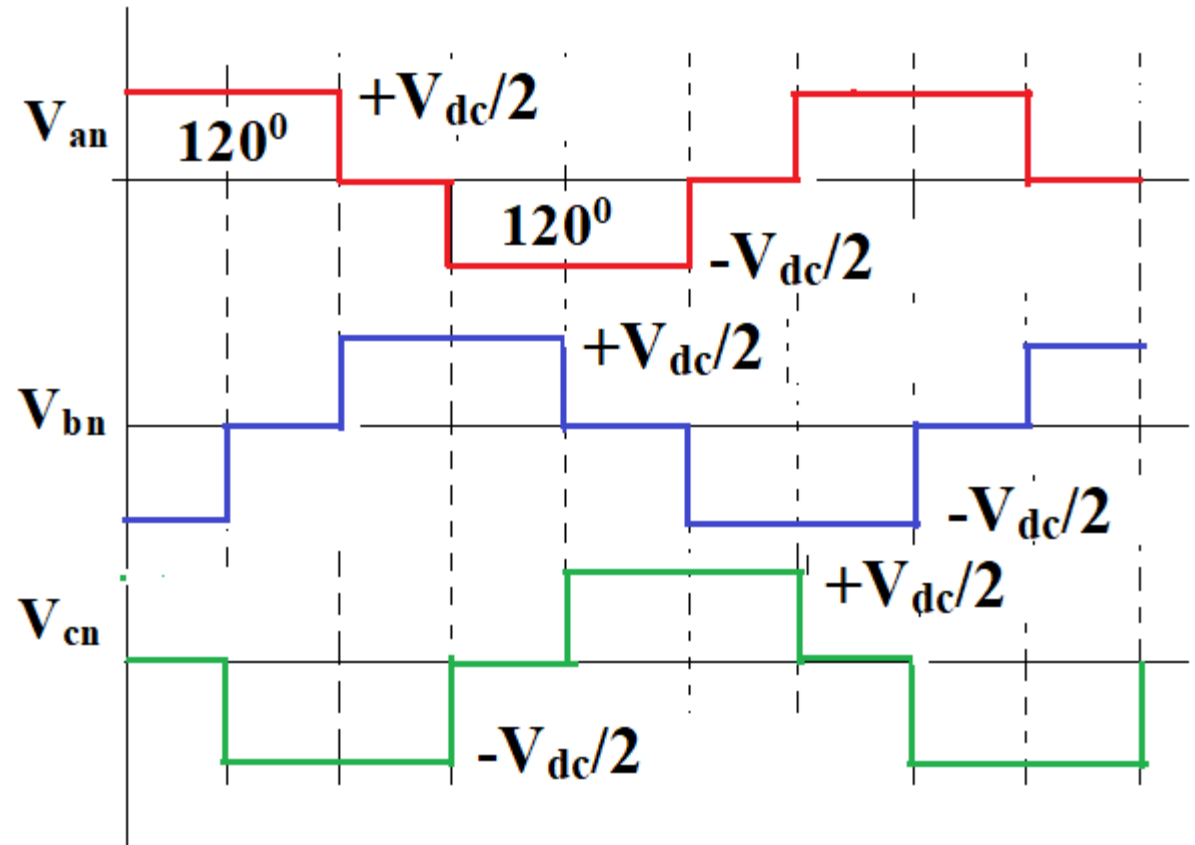
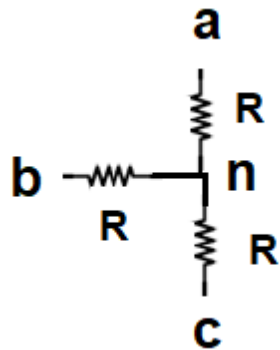


# 120° mode of conduction

- Each device conducts for 120°
- Two devices are on simultaneously
- Devices are named as per conducting sequence
- Dead time is not required
- Phase shift between the legs is 120°.

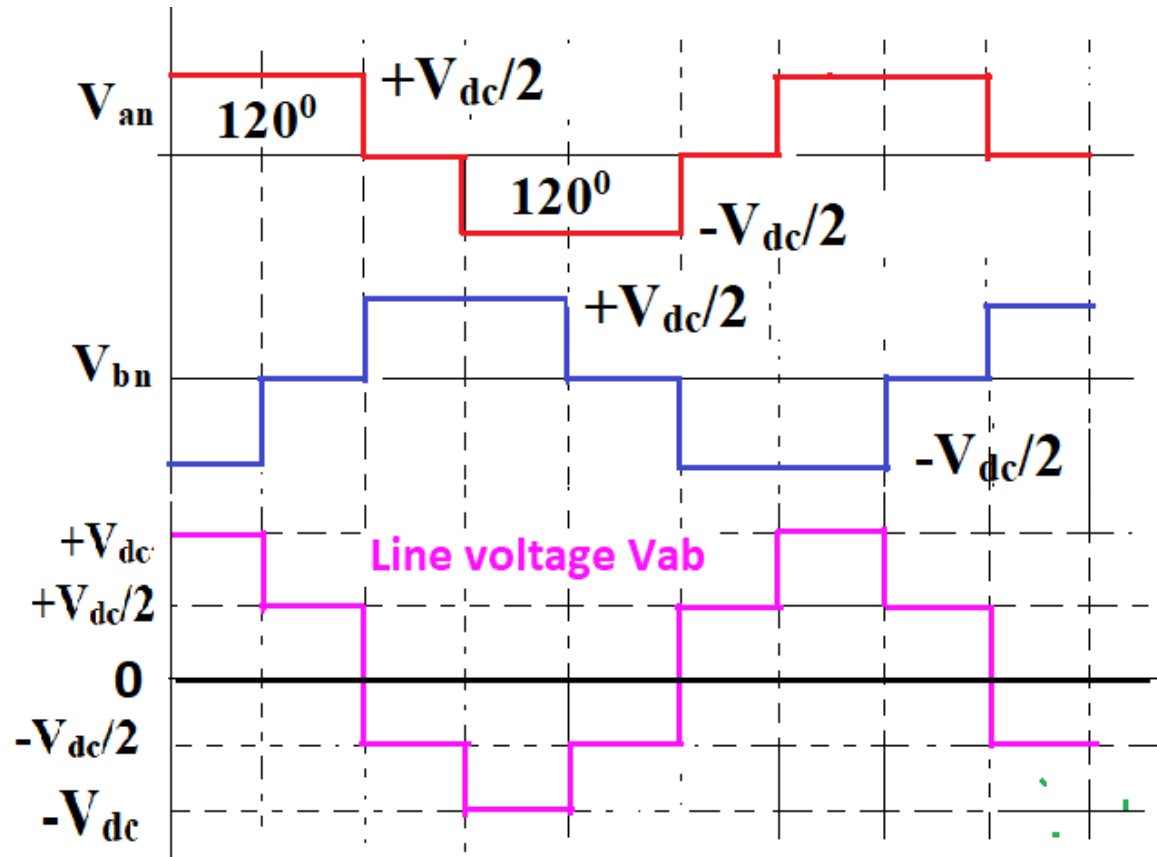
# 120° mode of conduction

## ■ Phase voltages



# 120° mode of conduction

## ■ Line voltages



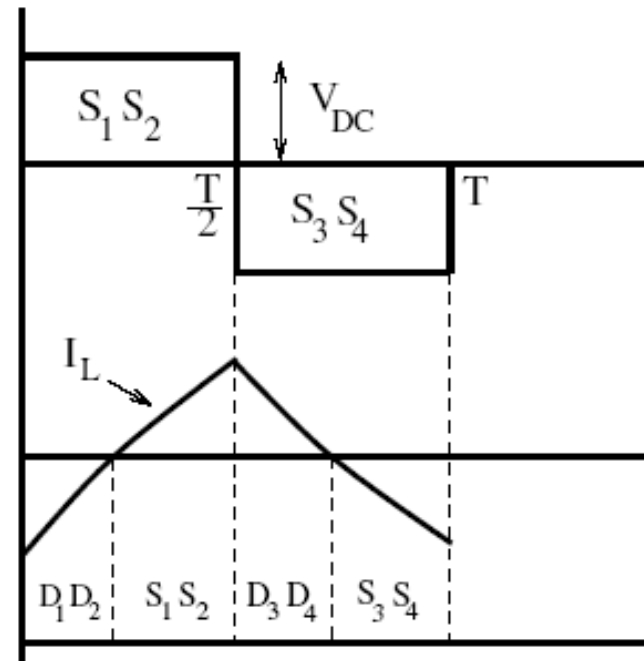
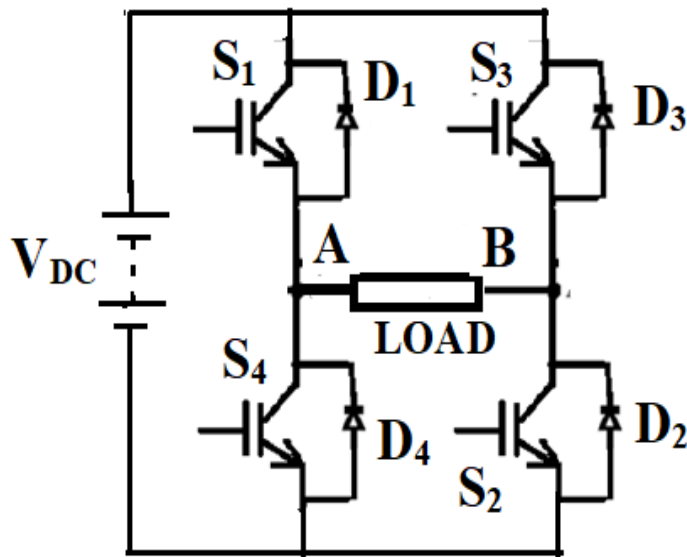


# 120° mode of conduction

- Disadvantages
- Output voltage is less as compared to square wave inverter.

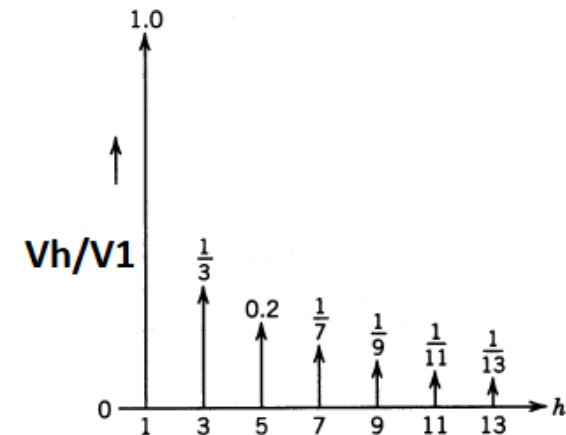
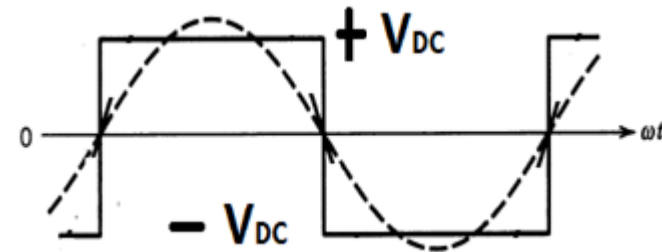
# 1 $\phi$ full bridge Inverter

- Square wave Mode
- Two devices are conducting simultaneously
- Center point of DC link is not required



# 1 $\phi$ full bridge Inverter

- Output voltage and harmonic spectrum
- Output voltage is square wave ( $V_{DC}$  Amplitude)
- It contains all
- odd harmonics
- $V_1$  peak =  $4V_{dc}/\pi$
- THD is 48 %
- AC o/p voltage(rms) =  $V_{DC}$

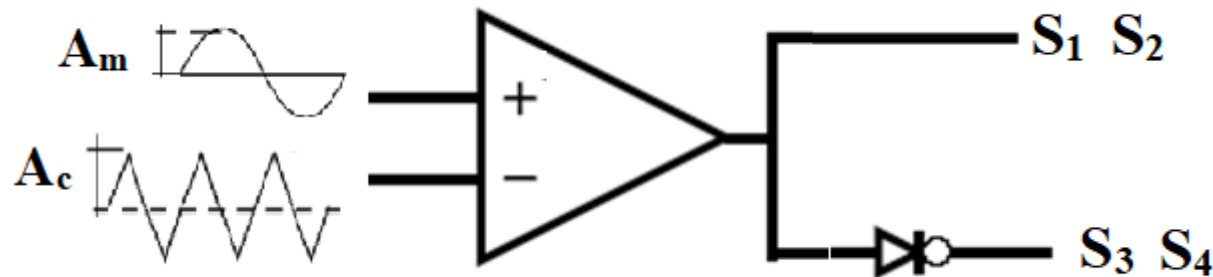


# 1 $\phi$ full bridge Inverter

- Square wave mode
- Output is square wave and contains harmonics, THD = 48%
- Output voltage control within inverter is not possible.

# PWM Switching

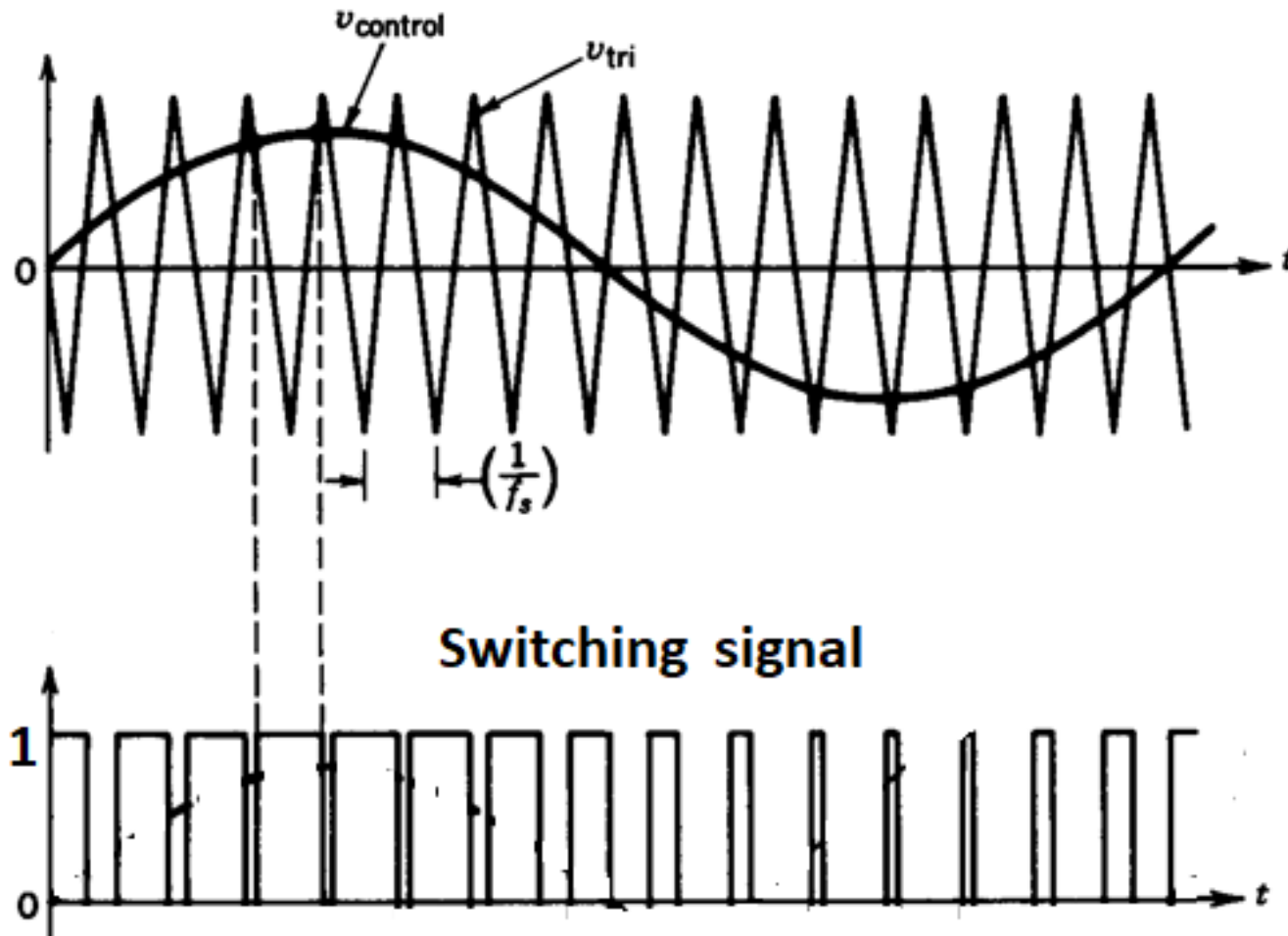
- 1 $\phi$  Bridge Inverter – bipolar switching



- Switching signals are obtained by comparison of modulating ( sine ) wave with carrier (triangular) wave.

# PWM Switching – Bipolar switching

- Switching signal for S1 and S2

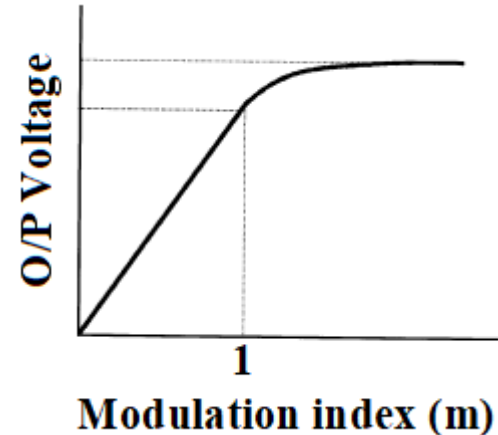


# PWM Switching – Bipolar switching

- Modulating (sine) wave: Its frequency and amplitude can be changed
- Carrier (triangular) wave : Its frequency and amplitude is fixed.
- Modulation index  $m = A_m / A_c$
- Output frequency is same as modulating wave frequency.
- Switching frequency of inverter depends upon carrier wave frequency

# PWM Switching – Bipolar switching

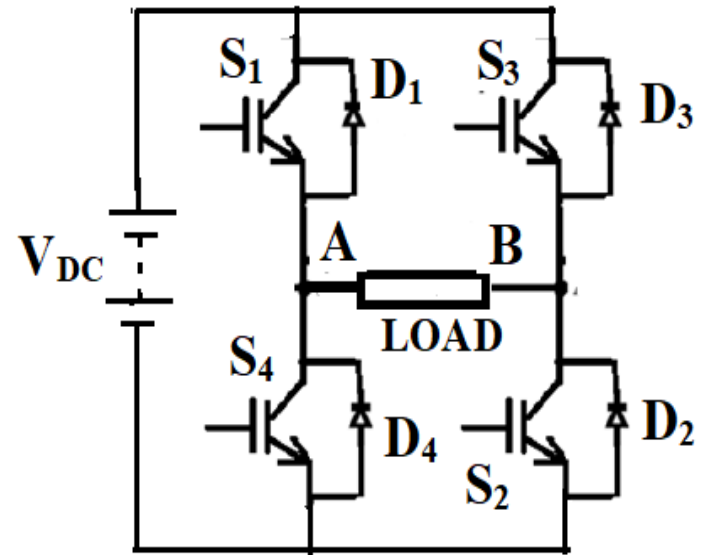
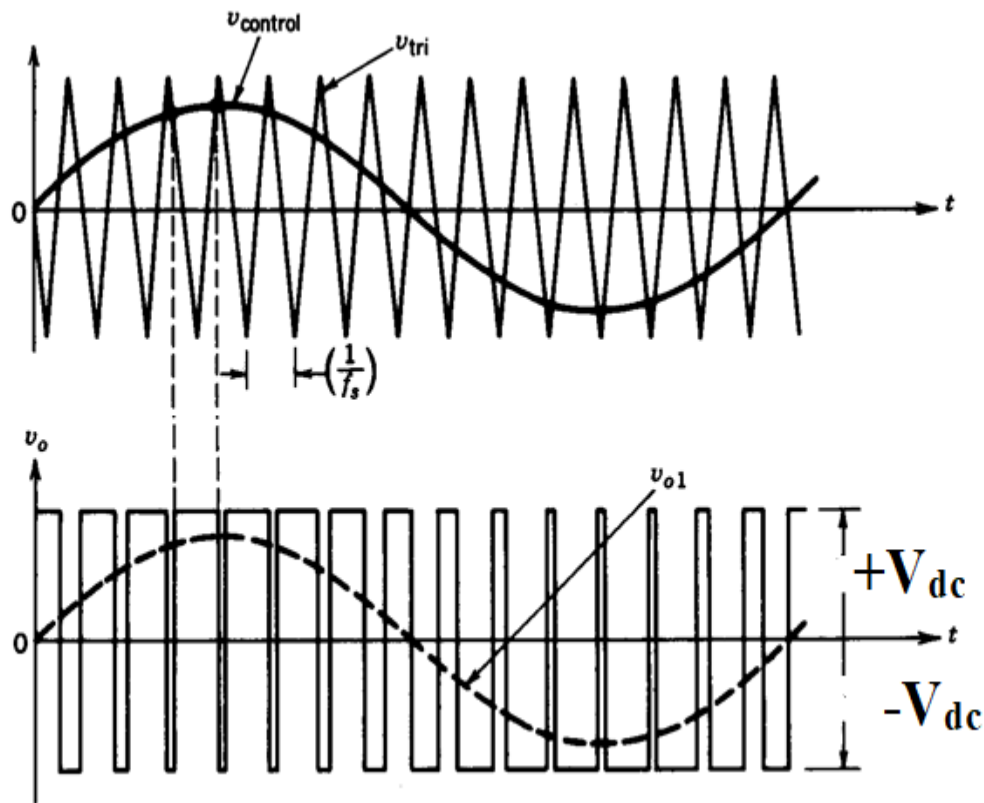
- Output voltage is proportional to  $m$
- $M$  is controlled by
- Controlling amplitude of
- Modulating wave





# PWM Switching – Bipolar switching

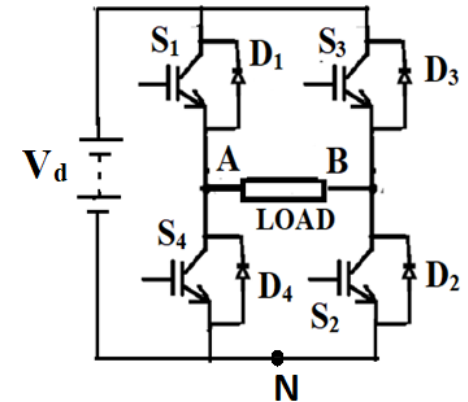
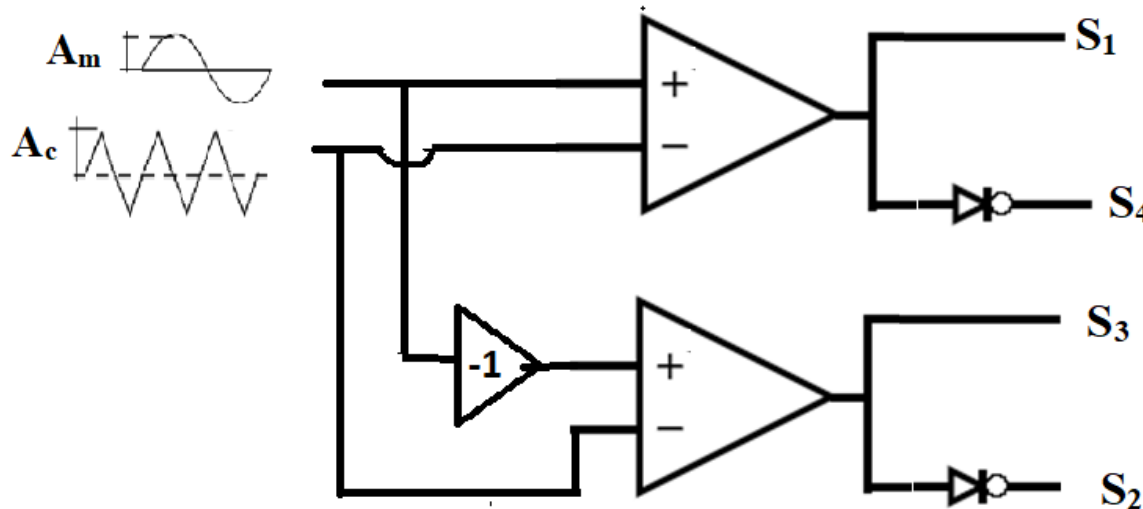
## ■ Bipolar switching



On switches	O/P Voltage
S1 and S2	$+V_{\text{DC}}$
S3 and S4	$-V_{\text{DC}}$

# Unipolar PWM Switching

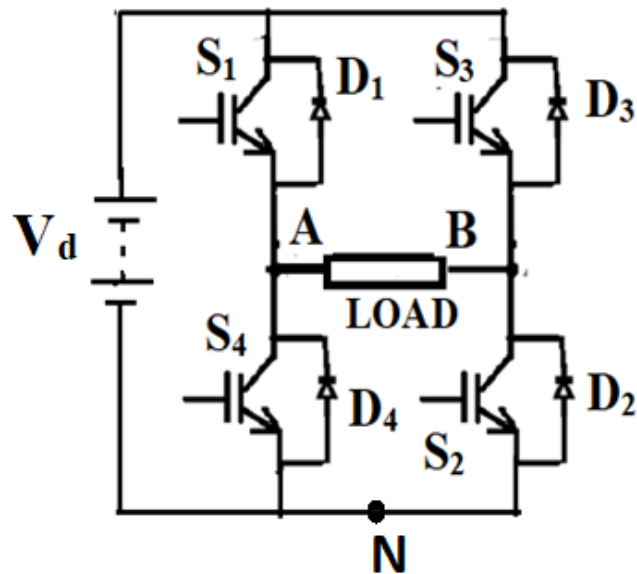
- switching signal generation



- It requires two modulating waves which are out of phase
- One leg is controlled by one modulating wave

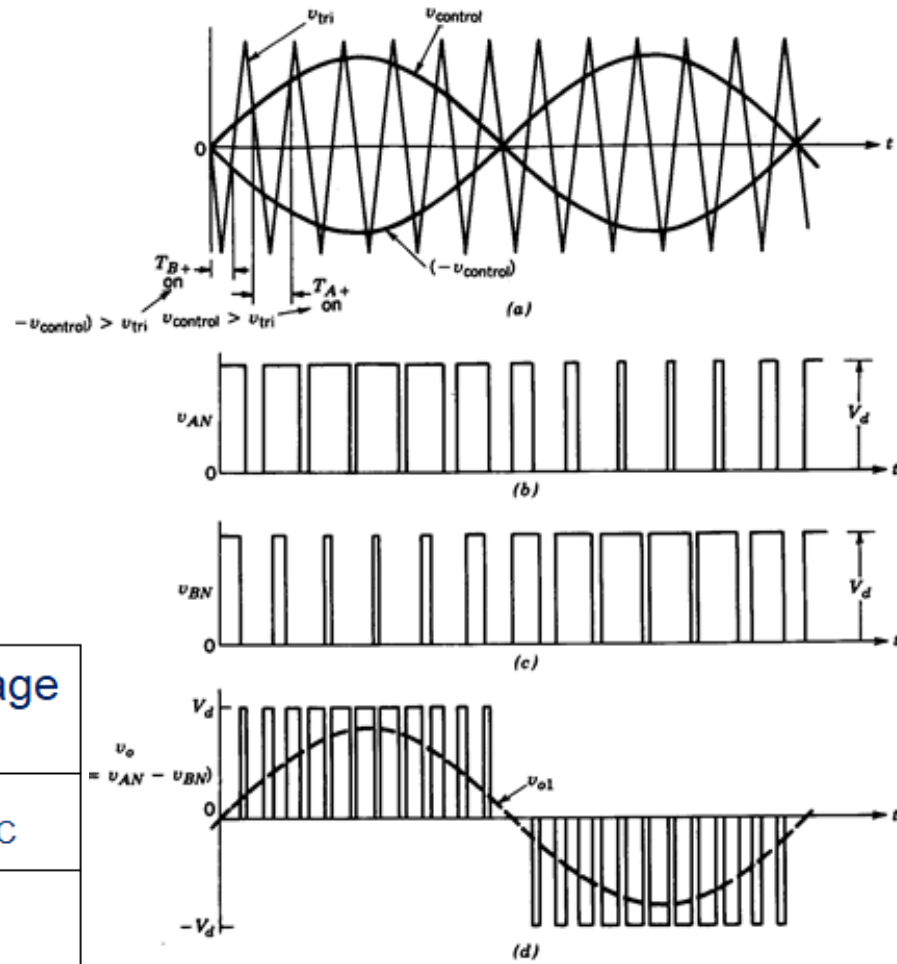
# Unipolar PWM Switching

## ■ Output voltage



On switch	Voltage $V_{an}$
S1	$+V_{DC}$
S4	0

On switch	Voltage $V_{bn}$
S3	$+V_{DC}$
S2	0

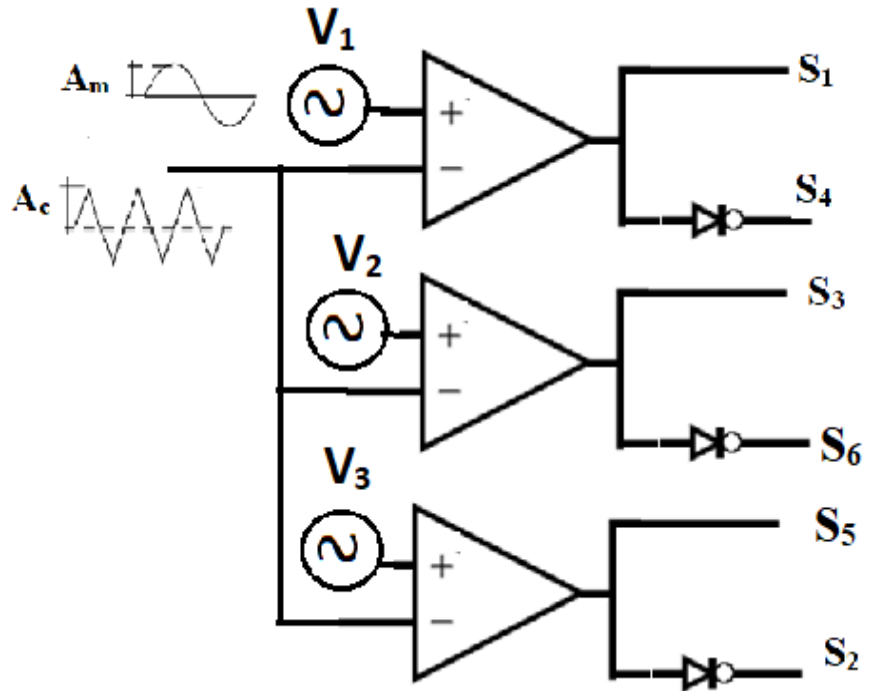


# PWM techniques for 3 $\phi$ Bridge inverter

- Various PWM techniques
- Sinusoidal PWM (SPWM)
- Selective harmonic elimination (SHE) PWM
- Space vector PWM (SVM )
- Hysteresis band current controlled PWM
- Sinusoidal PWM with instantaneous current control

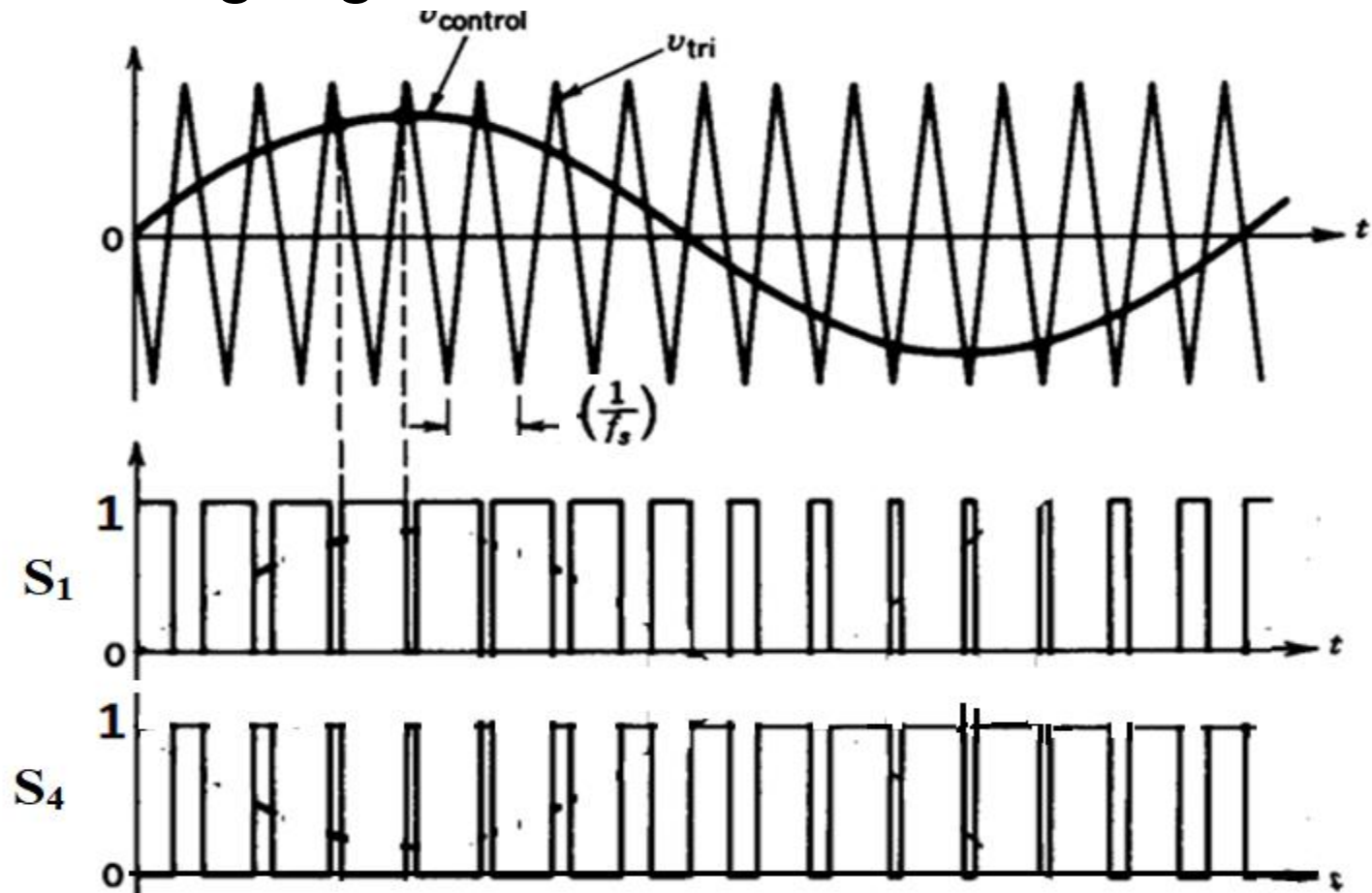
# Sinusoidal PWM

- Three sinusoidal modulating wave are given by
  - $V_1 = A_m \sin(\omega t)$
  - $V_2 = A_m \sin(\omega t - 120^\circ)$
  - $V_3 = A_m \sin(\omega t + 120^\circ)$
- Carrier wave is triangular wave with const. amplitude & F



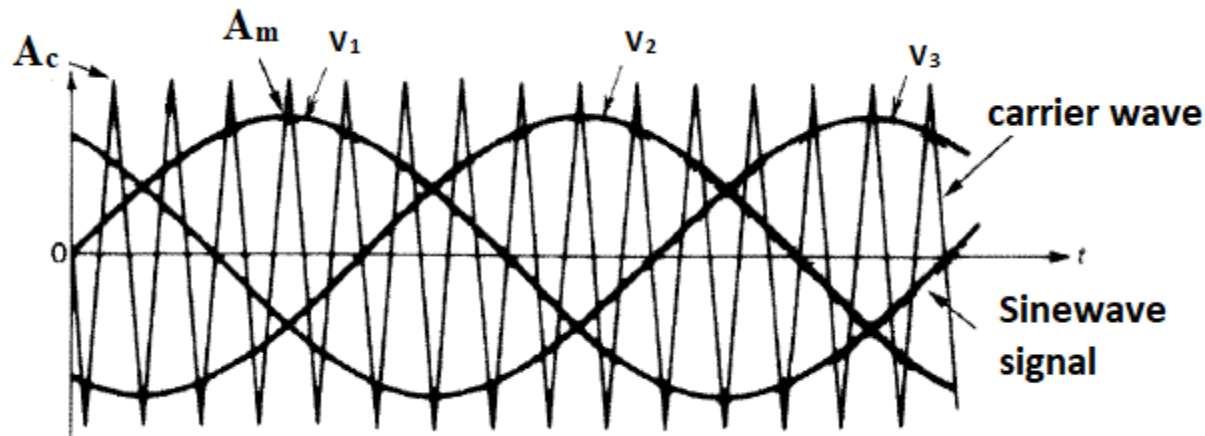
# Sinusoidal PWM

## ■ Switching signal



# Sinusoidal PWM

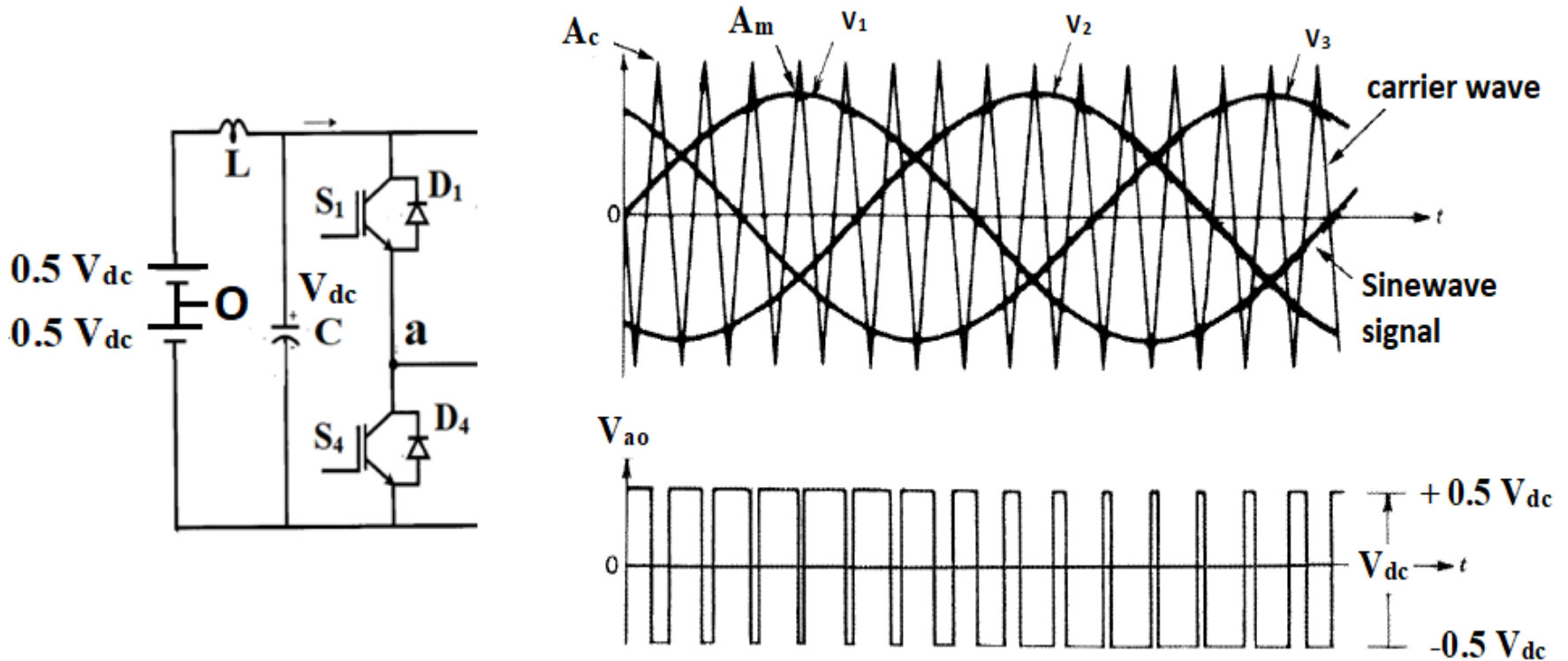
- Switching signal generation



- Six switching signals are generated.

# Sinusoidal PWM

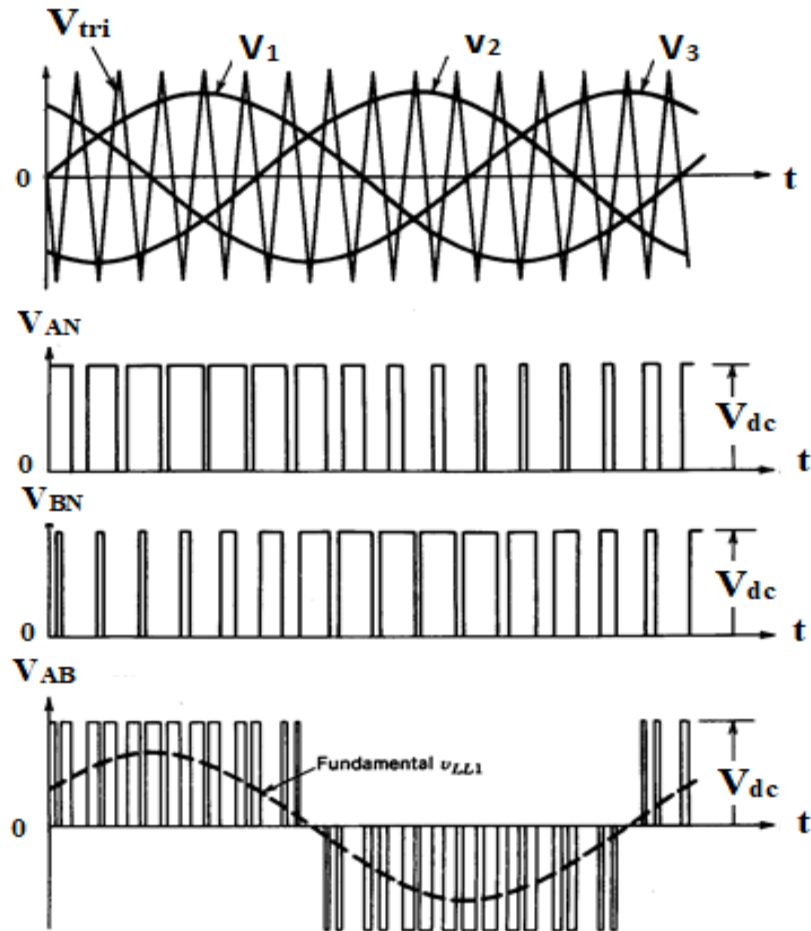
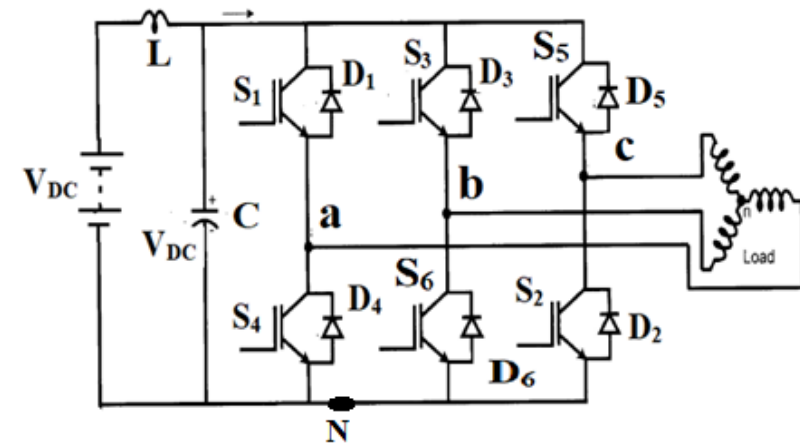
## ■ Node Voltages :





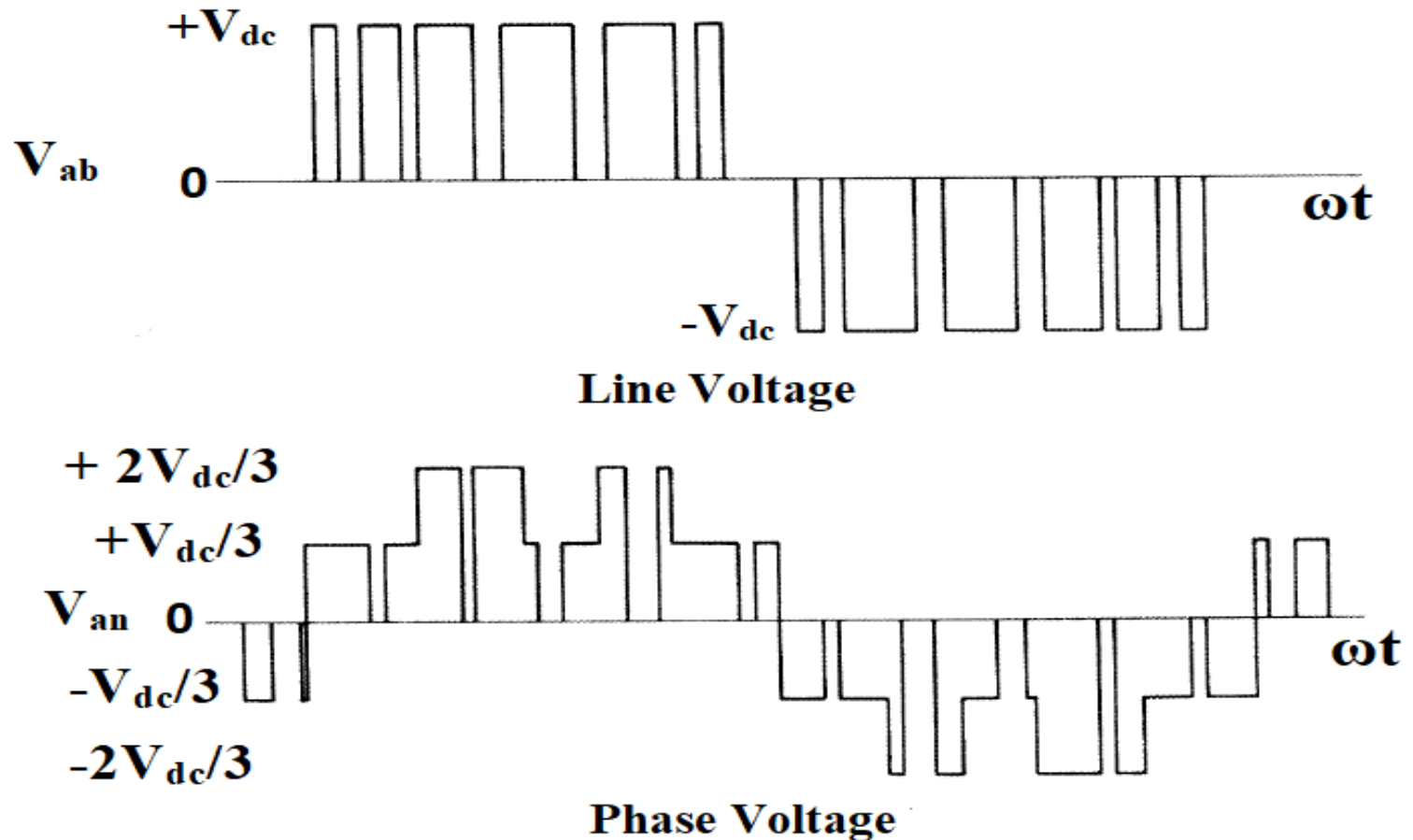
# Sinusoidal PWM

## ■ line voltage



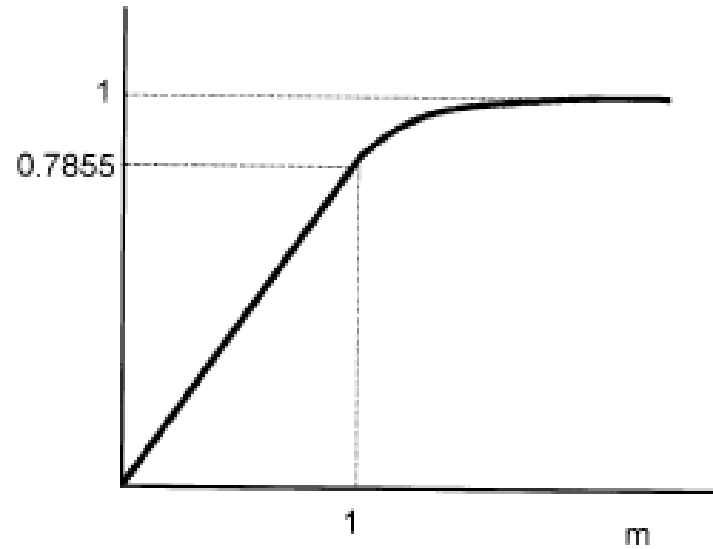
# Sinusoidal PWM

## ■ Phase and Line voltages



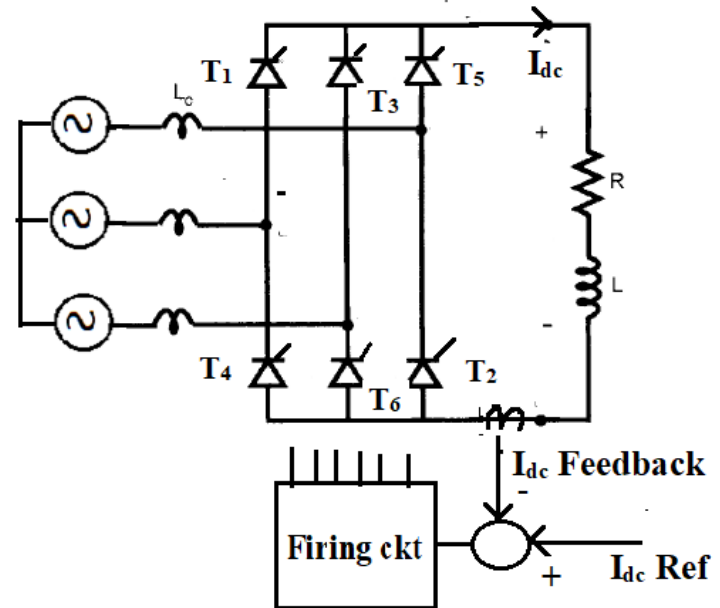
# Sinusoidal PWM

- Voltage Controlled by modulation Index ( $m$ )
- Linear modulation = O/P is proportional to  $m$
- Sinusoidal PWM provides 78.55% that of square wave Inverter
- Large value of  $m$  results into square wave inverter



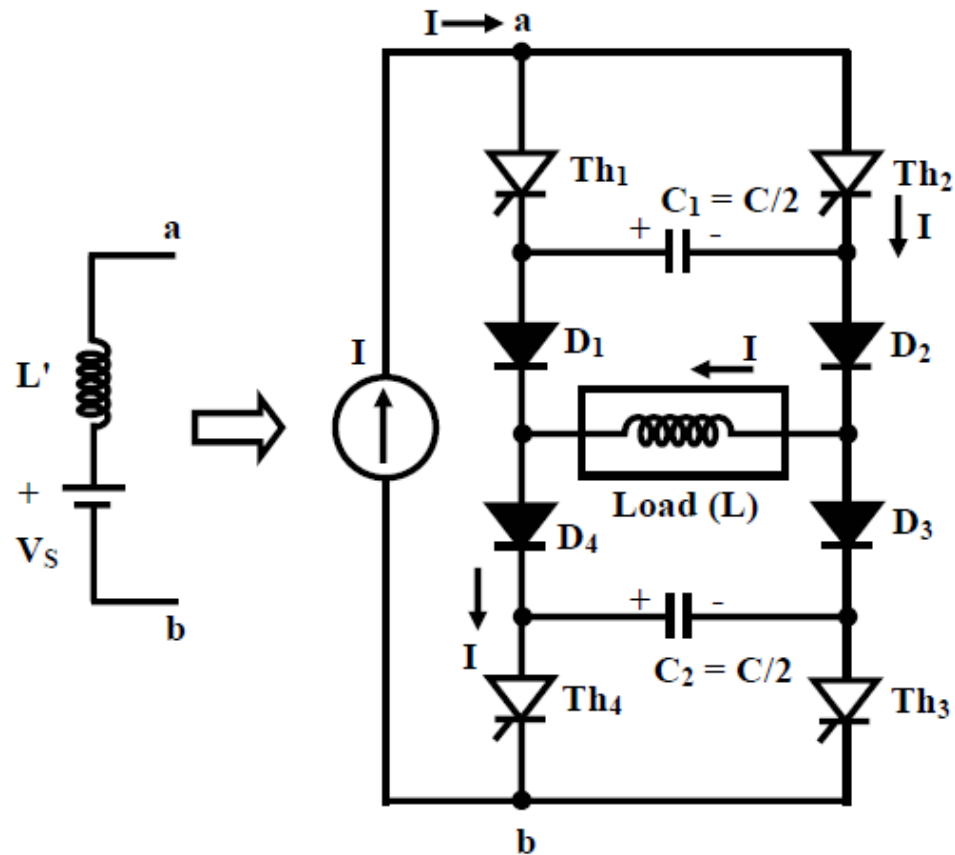
# DC Current Source

- Circuit diagram
- DC current source is obtained from AC to DC converter with closed loop current control
- $I_{dc}$  is always maintained to a set value by adjusting  $\alpha$  of the 6 pulse converter
- Voltage of the converter changes as per change in load to maintain  $I_{dc}$  constant



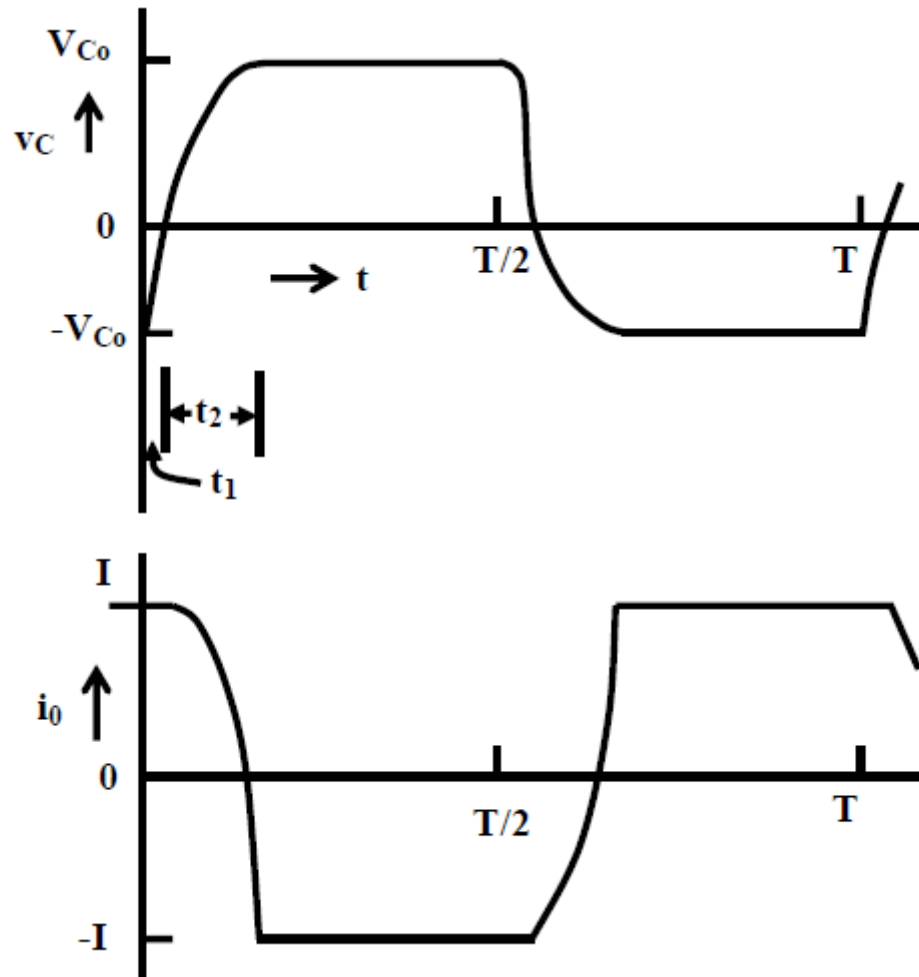
# 1 $\phi$ CSI

## ■ Circuit diagram

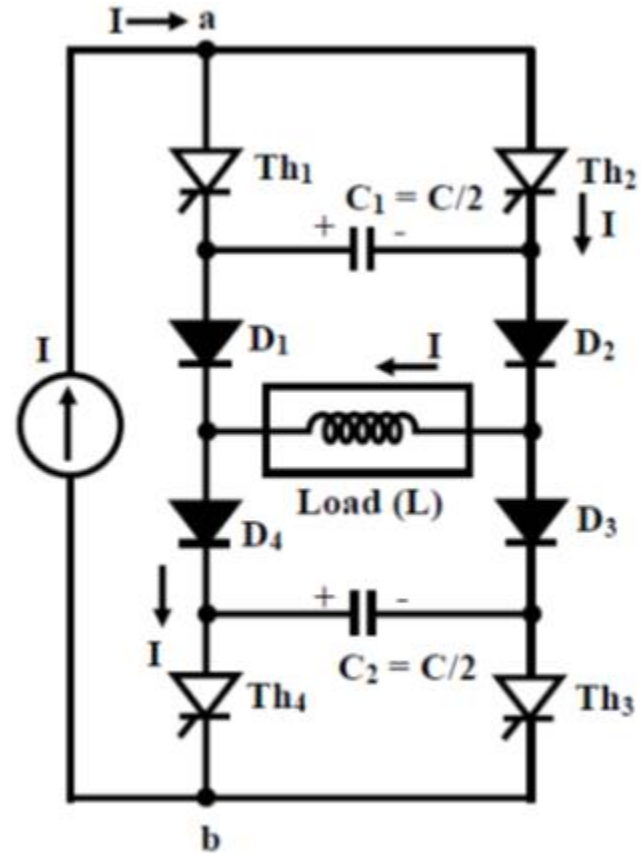
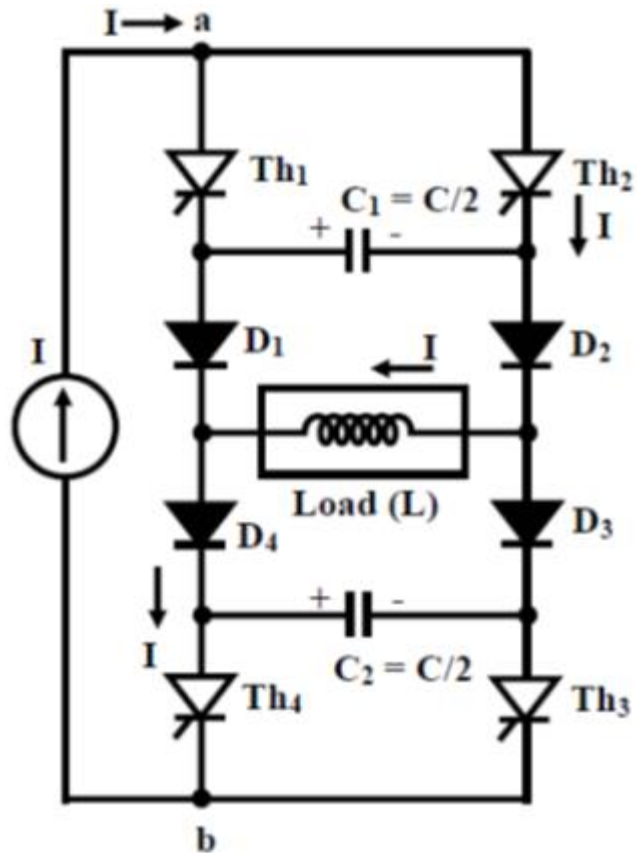


# 1 $\phi$ CSI

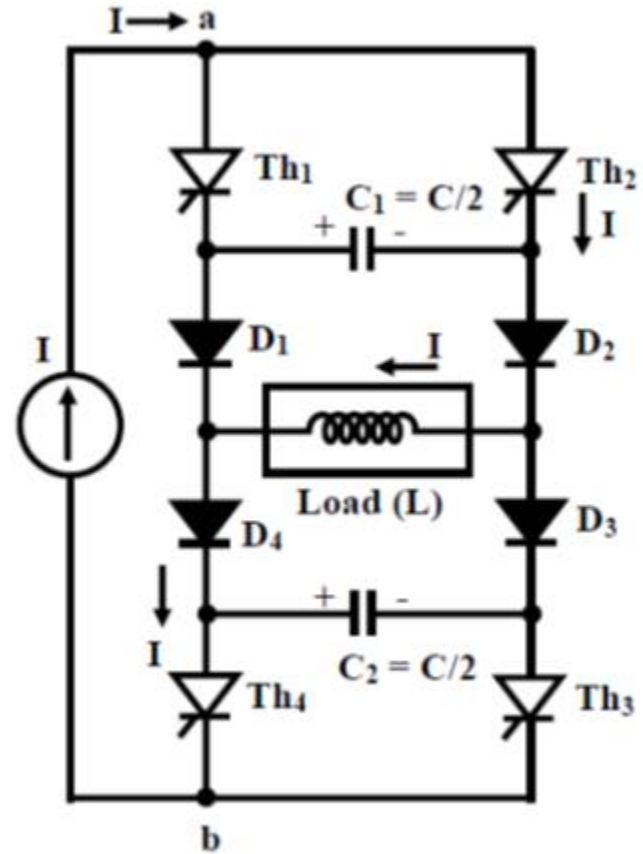
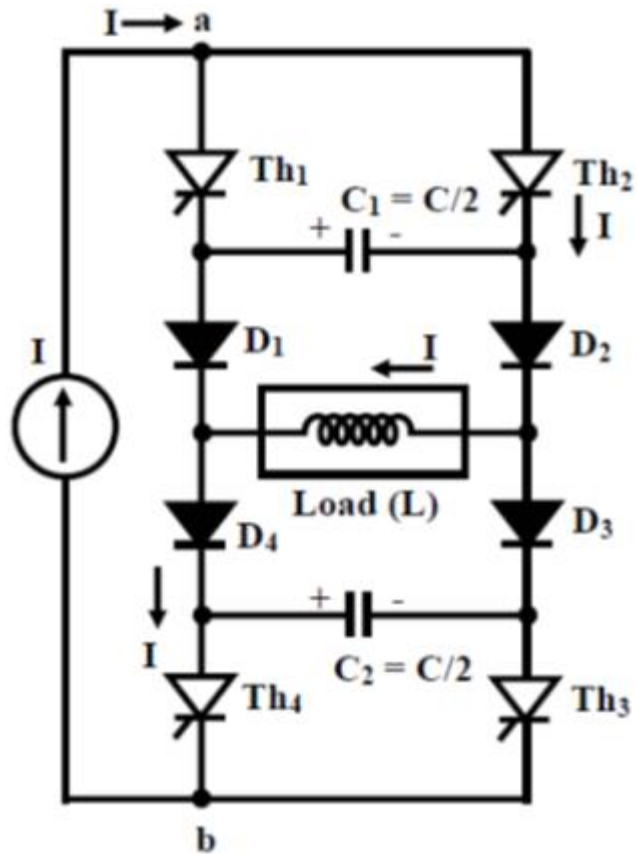
## ■ Wave forms



# 1 $\phi$ CSI



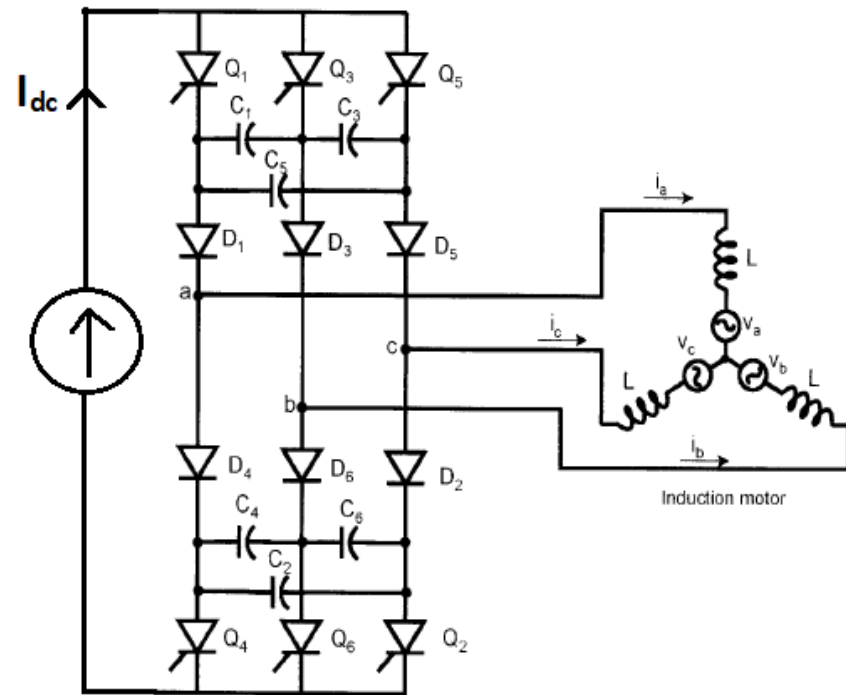
# 1 $\phi$ CSI





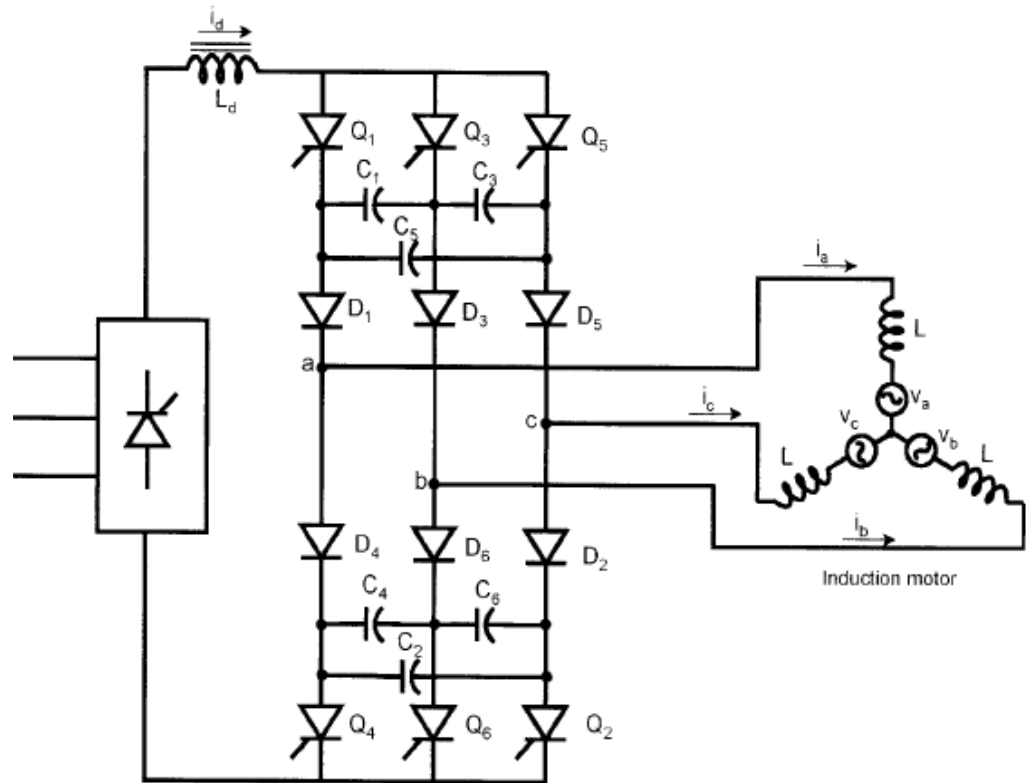
# 3 $\phi$ ASCI

- Auto sequentially current fed Inverter (ASCI)
- It consists of current source and force commutated inverter
- Each Thyristor conducts for  $120^\circ$ .
- Capacitors are used for commutation and diodes are used to isolate capacitors from load



# 3 $\phi$ ASCI

- Thyristors Q1 Q3 and Q5 forms one group
- Thyristors Q2 Q4 and Q6 forms other group
- Commutation takes place within a group.
- Nature of load current is quasi square wave.

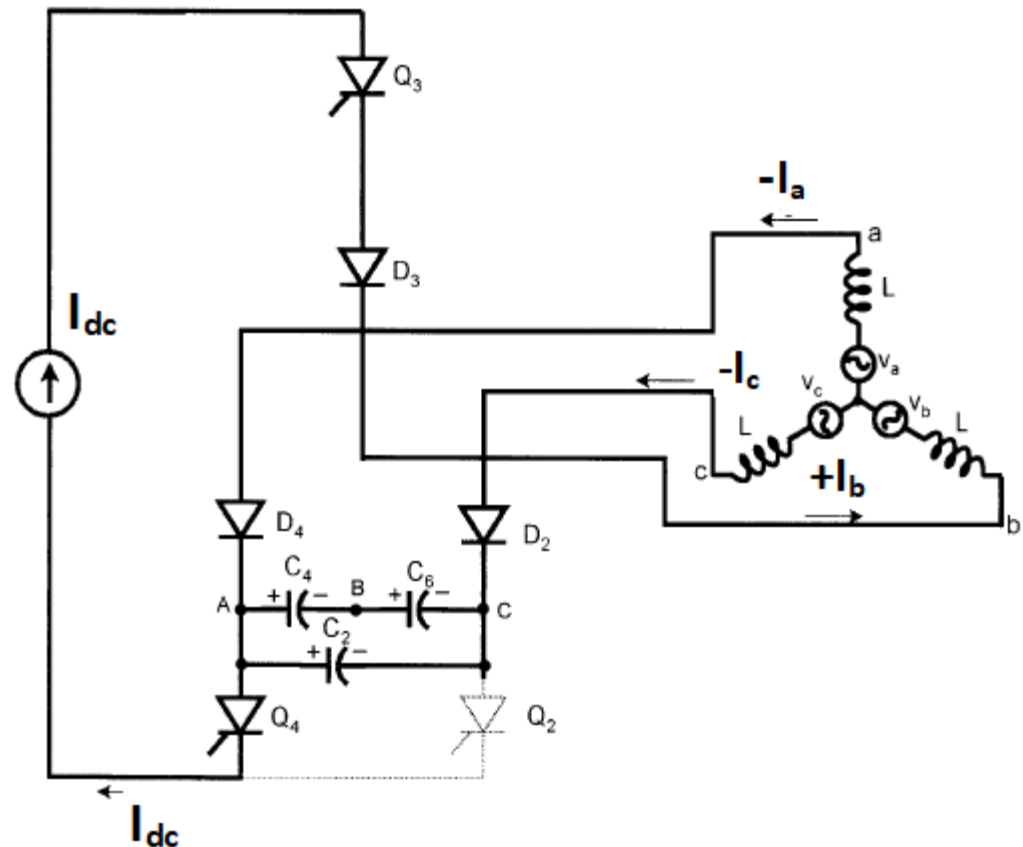


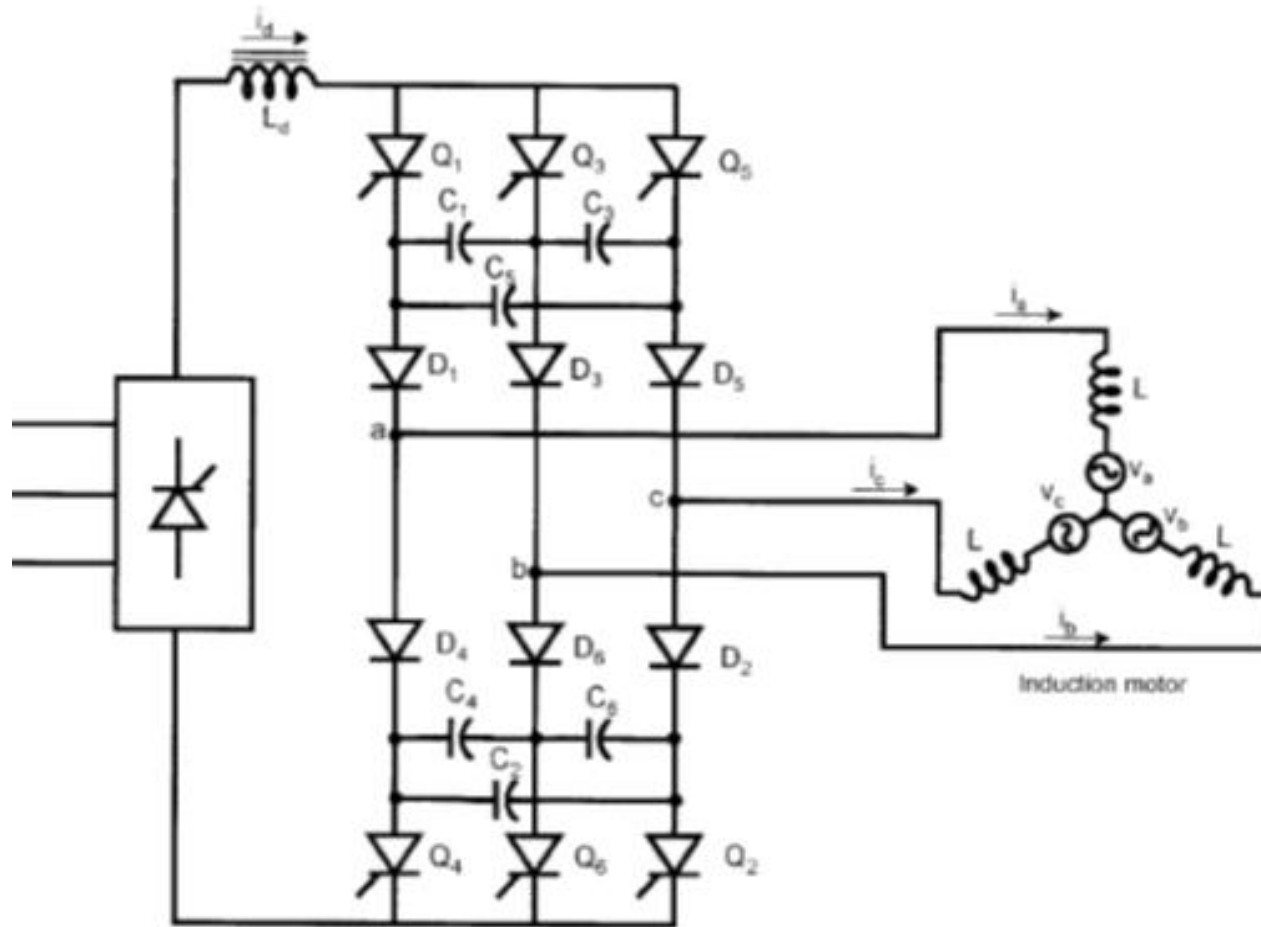
# 3 $\phi$ ASCI

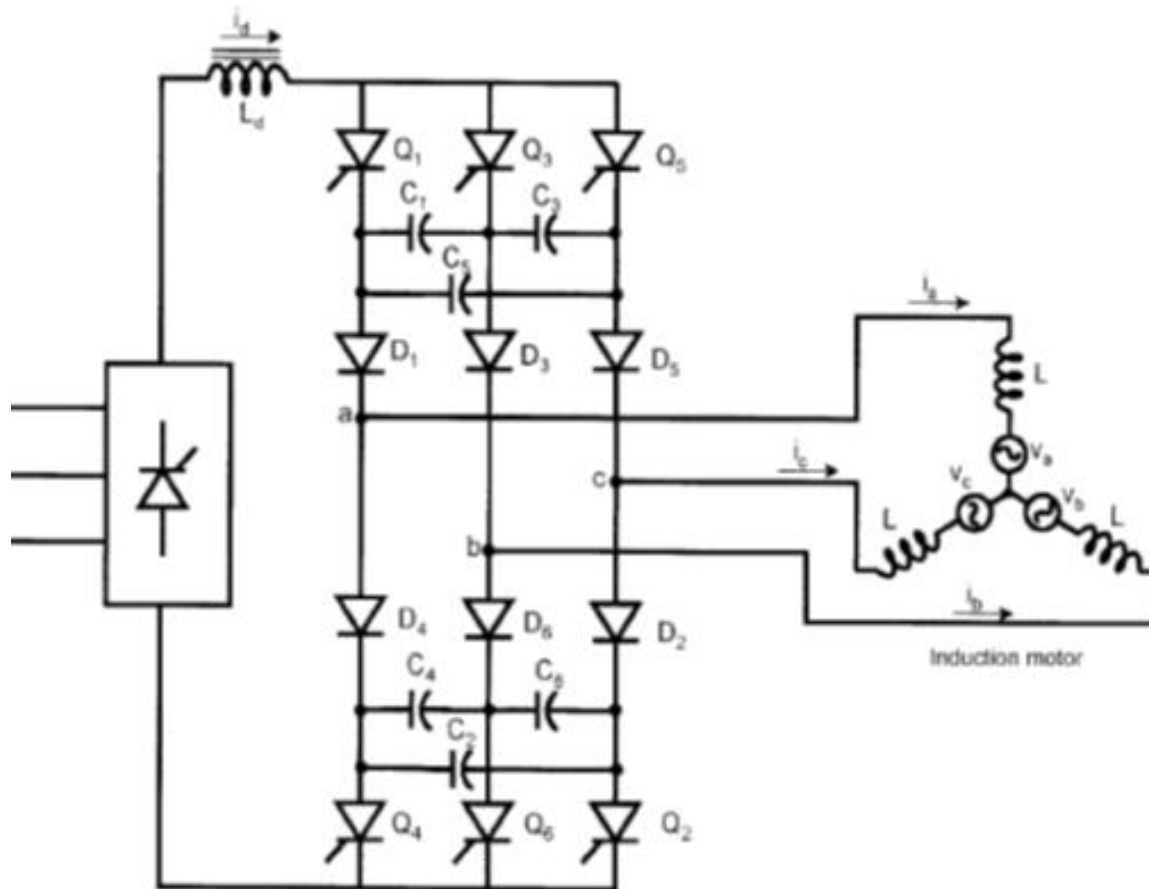
- Commutation from  $Q_2$  to  $Q_4$

- When  $Q_2$  is ON the capacitors  $C_2$ ,  $C_4$  &  $C_6$  will charge as shown polarity
- When  $Q_4$  is turned ON capacitor voltage is applied across  $Q_2$  to turn it off

- After  $Q_4$  turns ON, capacitors charge with reverse polarity

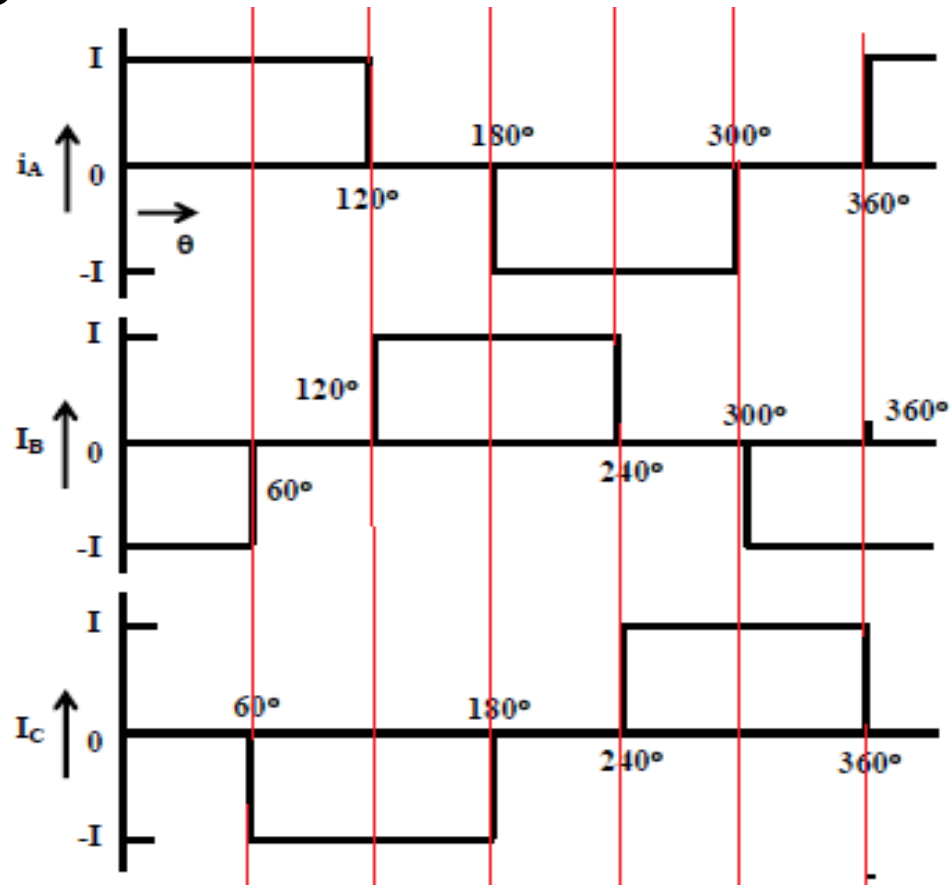






# 3 $\phi$ ASCI

## ■ Waveforms



# 3 $\phi$ ASCI

## ■ Advantages

- Converter grade thyristors are used
- Thyristor have high voltage blocking capability and sustain large voltage and current spikes.
- Current source converter inverter combination can work in four quadrant for Large IM drive.

## ■ Disadvantages

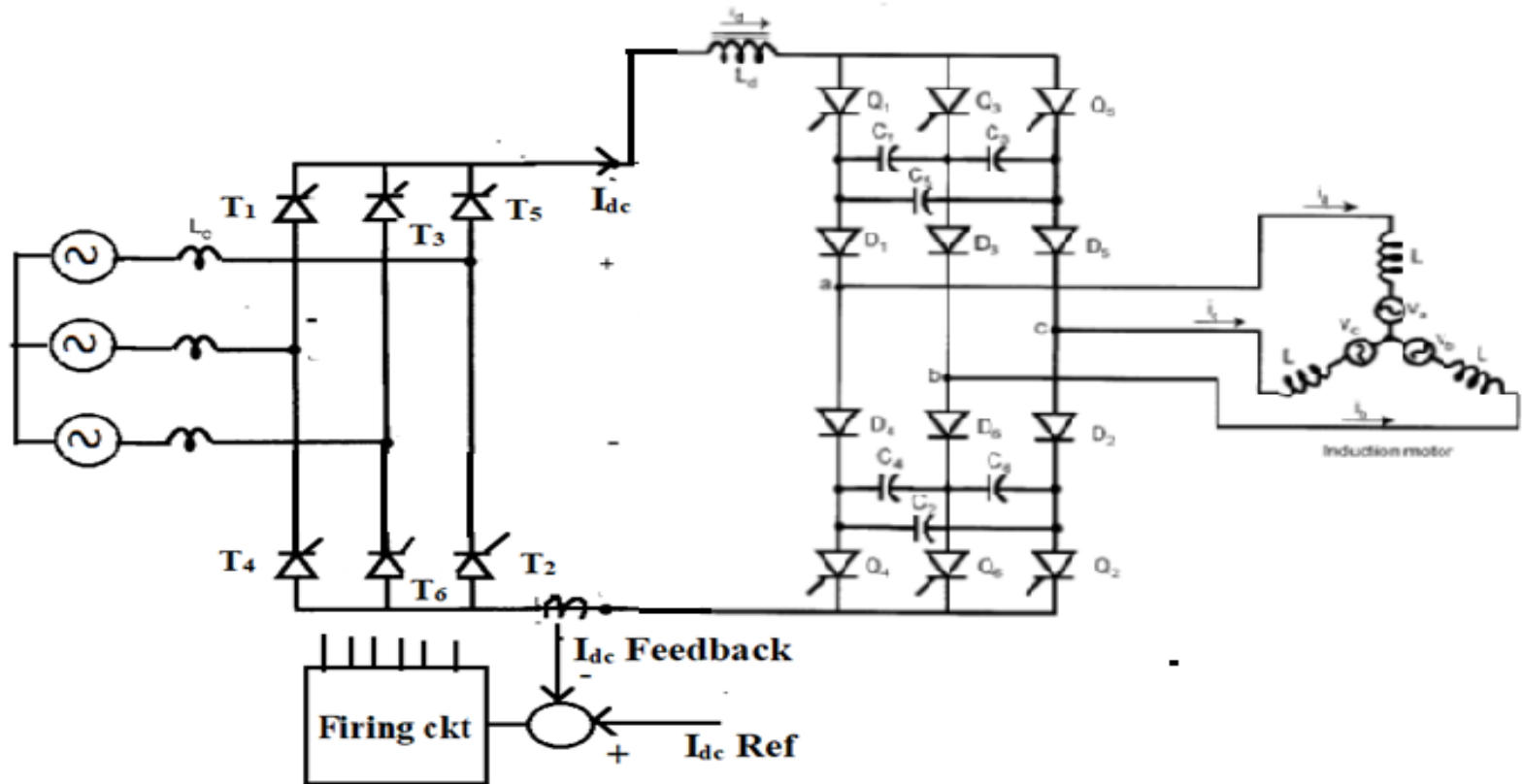
- Minimum load is required as commutation depends upon load
- High frequency light load, stability problem

# 3 $\phi$ ASCI

- Applications
- This inverter is used in large capacity AC drives
- Load current is quasi square wave
- It is desirable to design motor with low leakage inductance to reduce voltage spikes



# Auto sequentially commutated CSI for IM

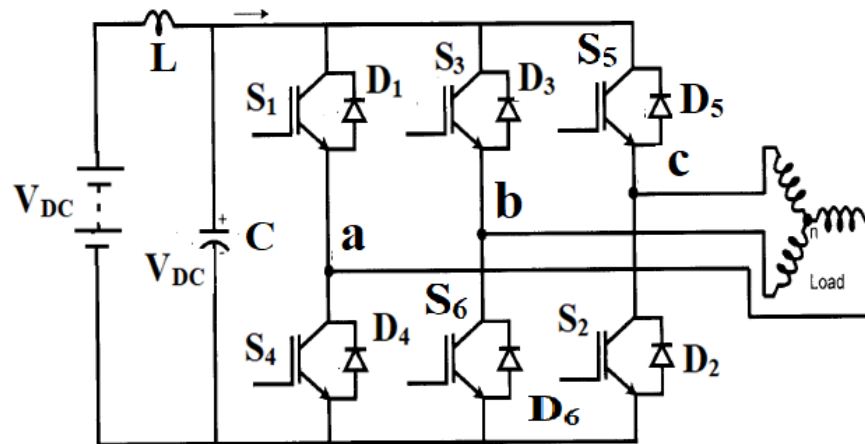


# Conclusion

- Voltage source Inverters are widely used for speed control of Induction motor and synchronous motor
- Normally PWM technique is used to control voltage and frequency.
- Switching frequency is kept high to reduce harmonics in the load current

# Numerical Problem - $120^\circ$ mode

- A star connected load of 15 ohm per phase is fed from 550 V DC source through a three-phase bridge inverter. For  $120^\circ$ -degree mode of conduction, determine i) power dissipated in resistive load, ii) RMS value of fundamental component of phase and line voltage, iii) average and rms current through the devices.

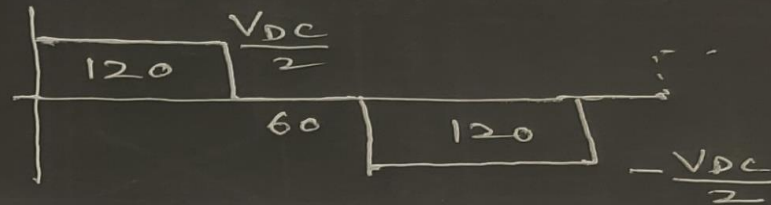


# Numerical problem - 120° mode

120 Degree Mode of conduction

Power dissipated in R-load

V<sub>ph</sub> wave form



$$V_{ph(rms)} = \sqrt{\frac{2}{3}} \cdot \frac{V_{dc}}{2} = \sqrt{\frac{2}{3}} \times \frac{550}{2} \\ = 224.53 \text{ V}$$

Power dissipated in 3φ load

$$= \frac{3 \cdot V_{ph(rms)}^2}{R} = \frac{3 \times (224.53)^2}{15} \\ = 10,083.33 \text{ W} = 10.083 \text{ kW}$$

# Numerical Problem - 120° mode

RMS Value of fundamental component of phase voltage:

$$a_n = \frac{8}{T} \int_0^{T/4} f(\omega) \cos n\omega \cdot d\omega = \frac{8}{2\pi} \int_0^{\pi/3} \frac{V_{dc}}{2} \cos n\omega \cdot d\omega$$

$$\therefore a_n = \frac{2 V_{dc}}{\pi} \frac{\sin n\pi/3}{n}$$

$$a_1 = \frac{2 V_{dc}}{\pi} \times \frac{\sqrt{3}}{2} = \frac{\sqrt{3} V_{dc}}{\pi}$$

$$V_{1ph(rms)} = \frac{\sqrt{3} V_{dc}}{\sqrt{2} \pi} = 214.41V$$

$$V_{Lph(rms)} = \sqrt{3} \times 214.41 = 371.369V$$

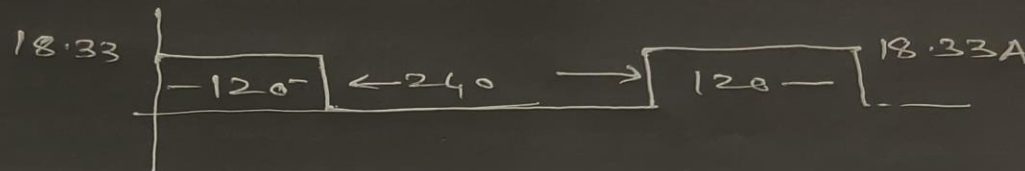
# Numerical Problem - 120° mode

Current through the Device



current (Peak) through switch  
$$= \frac{550}{2 \times 15} = 18.33 \text{ A}$$

Current through switch



Average current through switch

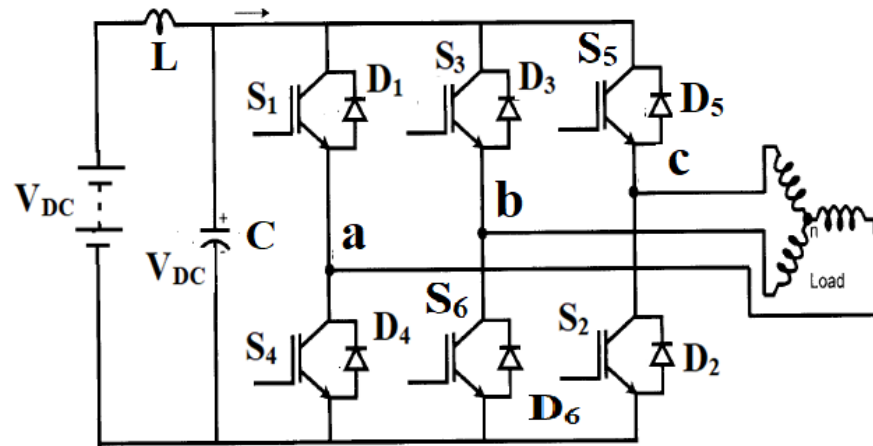
$$I_{av(th)} = 18.33 \times \frac{120}{360} = 6.11 \text{ A}$$

RMS current through switch

$$I_{rms(th)} = 18.33 \times \sqrt{\frac{120}{360}} = 10.58 \text{ A}$$

# Numerical Problem – 180° mode

A three phase bridge inverter deliver the power to the resistive load from a 600 V DC source. For a star connected load of 20 ohm per phase. Determine for 180 degree mode of conduction i) RMS value of load current, ii) RMS value of device current, iii) power dissipated in resistive load. iv) Fundamental component of output voltage.



# Numerical Problem – 180° mode

180° mode of conduction.

$$\begin{aligned} \text{RMS value of line voltage} &= \sqrt{2/3} V_{dc} \\ &= \sqrt{2/3} \times 600 = 489.89 \text{ V} \end{aligned}$$

$$\text{RMS value of phase voltage} = \frac{489.89}{\sqrt{3}}$$

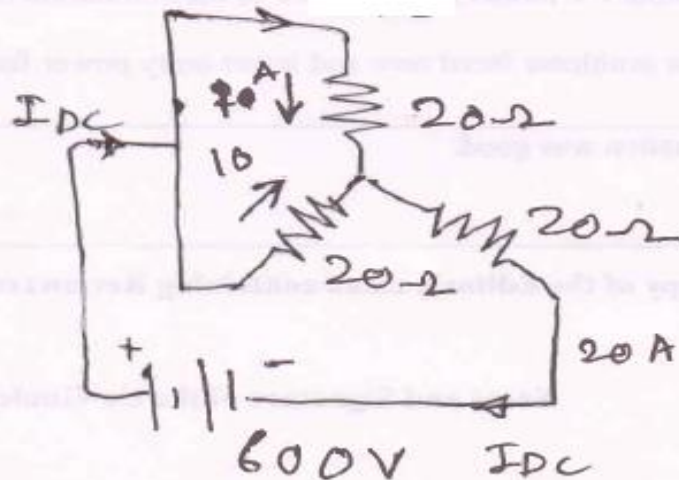
$$\therefore V_{ph}(\text{rms}) = 282.84 \text{ V}$$

$$\therefore I_{\text{rms}}/\text{ph} = \frac{V_{ph}(\text{rms})}{R} = \frac{282.84}{20}$$

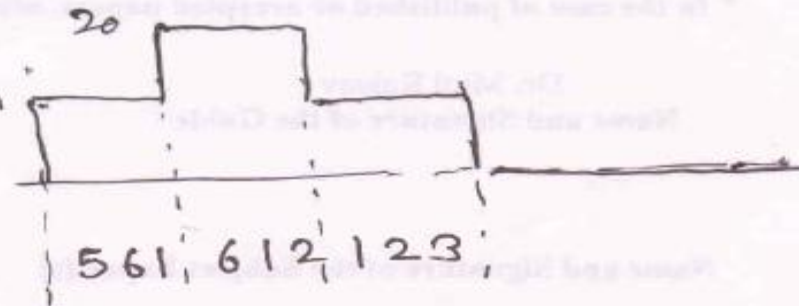
$$\therefore I_{\text{rms}}/\text{ph} = 14.142 \text{ A}$$



# Numerical Problem – 180° mode



$$I_{DC} = \frac{600}{20 + 10} = 20 \text{ A}$$



$$I_{rms \text{ device}} = \sqrt{\frac{10^2 \times 120 + 20^2 \times 60}{360}}$$

$$\text{device } I_{rms} = 10.0 \text{ Amps}$$

# Numerical Problem – 180° mode

$$\text{Power dissipated in R load} \\ = 3 V_{ph(rms)} \times I_{ph(rms)}$$

$$= 3 \times 282.84V \times 14.142$$

$$= 11999.76 \approx 12000W$$

$$= 12 \text{ KW}$$

$$V_{l(rms)} \text{ line} = \frac{\sqrt{6}}{\pi} \cdot V_{dc}$$

$$\text{RMS value of fun. comp. (line)} = \frac{\sqrt{6}}{\pi} \times 600 = 467.81V$$

$$\text{RMS value of fundamental component of phase voltage} = 467.81/\sqrt{3} = 270.09V$$

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THANKS !

Any Questions?