

DC to DC Converter



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Introduction

Switched mode power supplies / Choppers.

→ High power → D.C. motor speed control

Calcutta metro : 750V DC

Bombay – Igatpuri : 1500V

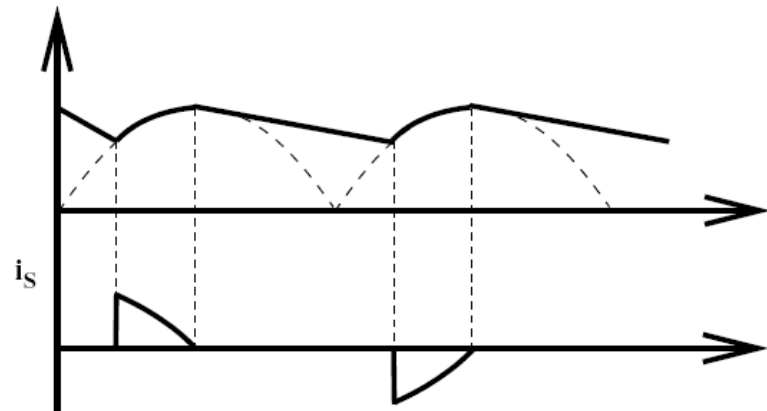
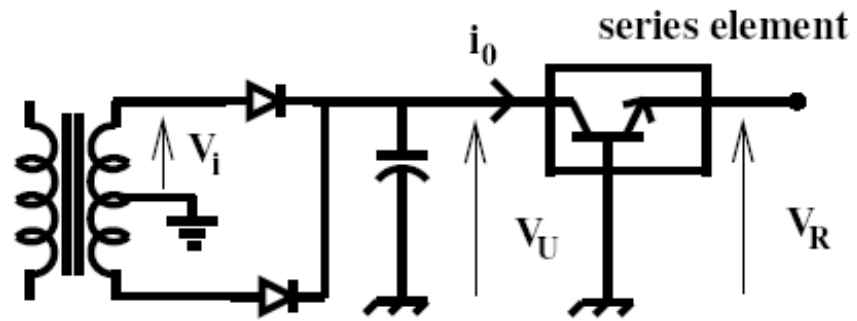
Power supplies : In computers, any electronic equipments.

Linear Regulated Power Supply

- Voltage across

$$C = V_U$$

- Out put voltage = V_R



Linear Regulated Power Supply

In order to get regulated power supply, use series regulator.

$$V_{SR} = V_U - V_R$$

As $V_U \uparrow$, $V_{SR} \uparrow$

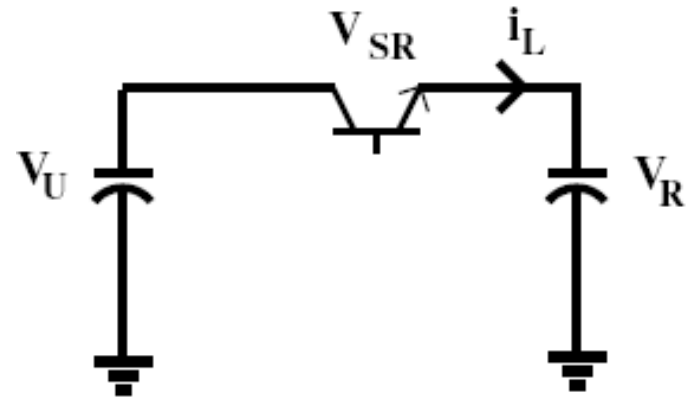
\Rightarrow 7805 Regulator

$$V_{U(\min)} = 7.5V$$

$$V_R = 5V$$

$$V_{U(\max)} = 35V$$

Power loss in the device = $V_{SR} * i_L$



Linear Regulated Power Supply

- **Disadvantages**
- Voltage is dropped across series element & hence efficiency is low
- Requires 50 Hz transformer
- Source current contains harmonics
- large size of the capacitor
- Heat sink size increases.

Switch Mode Power Supply

- DC to DC converter
- Operating at high frequency 100KHz
- Transformer operating frequency is high, so cost and weight is low
- As frequency increases, No. of turns decreases and core loss increase
- Ferrite core transformer is used. Operating flux density $\Rightarrow 0.2$ to 0.25 T
- Values of L and C required are less

DC to DC Converters

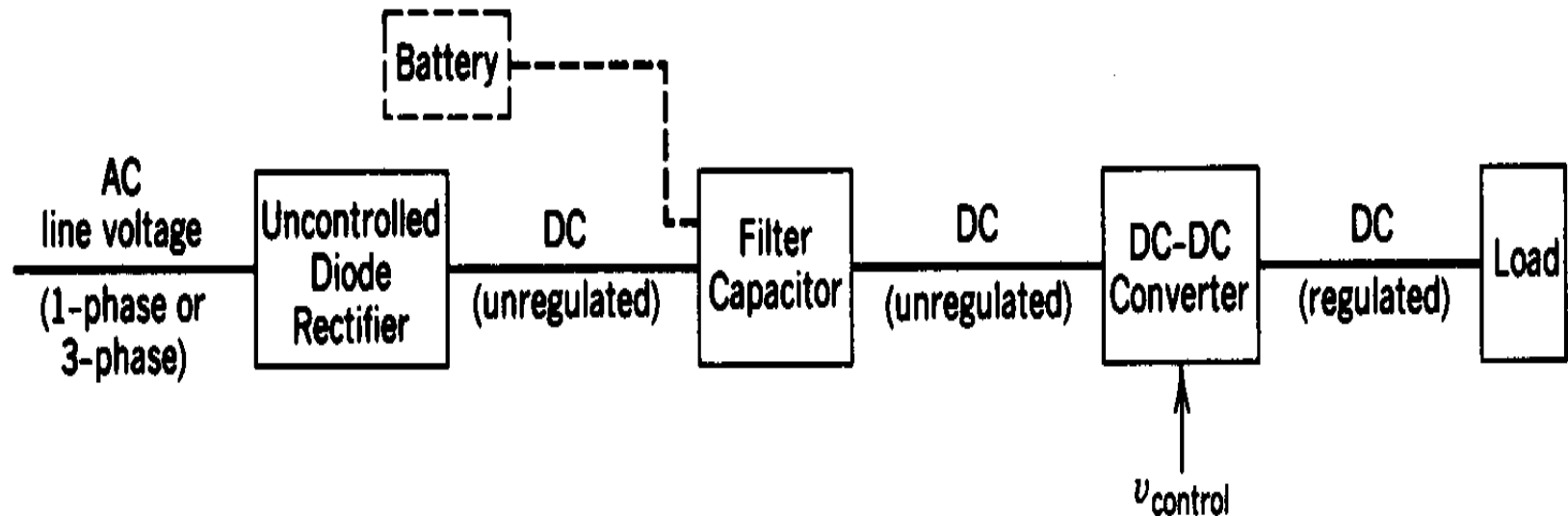


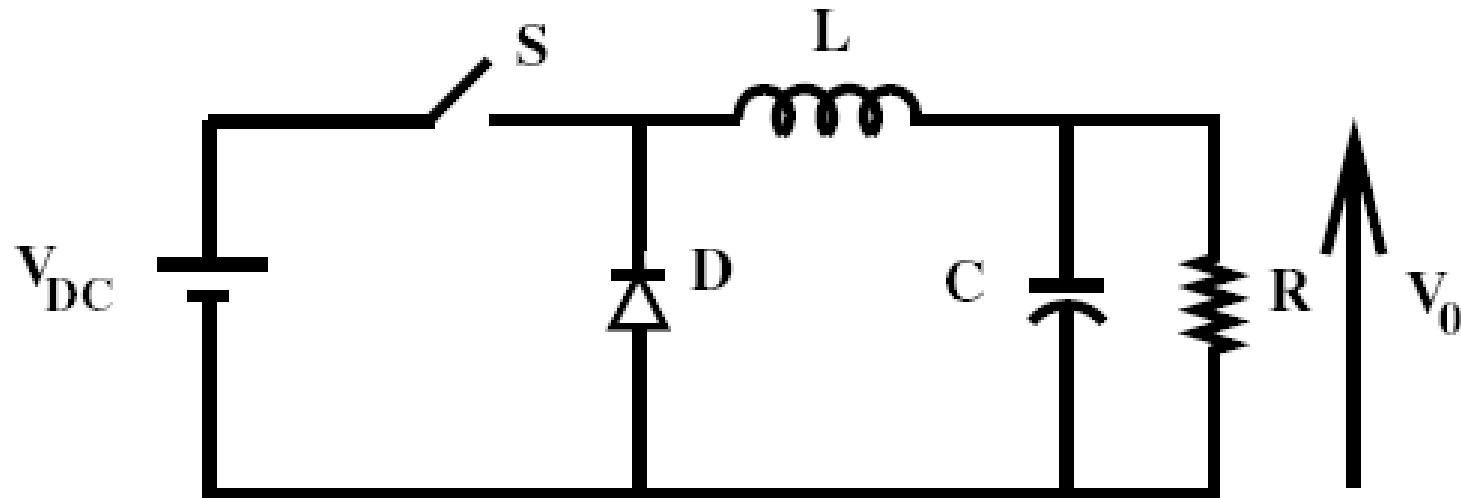
Figure 7-1 A dc–dc converter system.

DC to DC Converters-Classification

- Based on output voltage
 - 1) Buck / step- down
 - 2) Boost/ step-up
- Based on quadrant operation
 - 1) Single quadrant dc to dc converter
 - 2) Two quadrant dc to dc converter
 - 3) four quadrant dc to dc converter

DC to DC buck converter

- It is also called as step-down chopper
- Output voltage (V_O) is less than input voltage (V_{DC})
- Circuit components are S, D, L and C

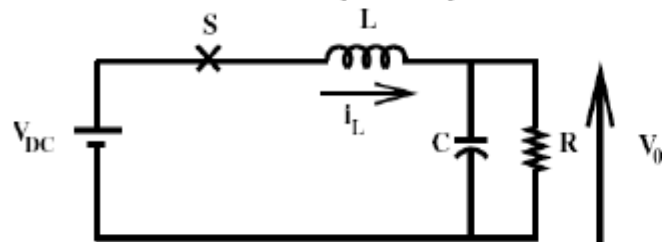


DC to DC Buck converter

'S' is switched at a very high frequency.

S – ON for DT

– OFF for $(1-D)T$

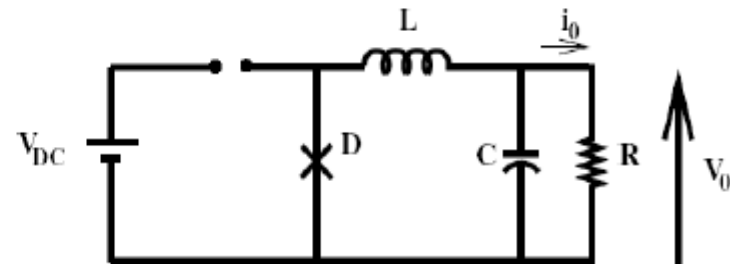


$$V_L = V_{DC} - V_0 \quad 0 < t < DT$$

= Constant

$i_L \uparrow$ Linearly

$$i_L = C \frac{dV_0}{dt} + \frac{V_0}{R}$$

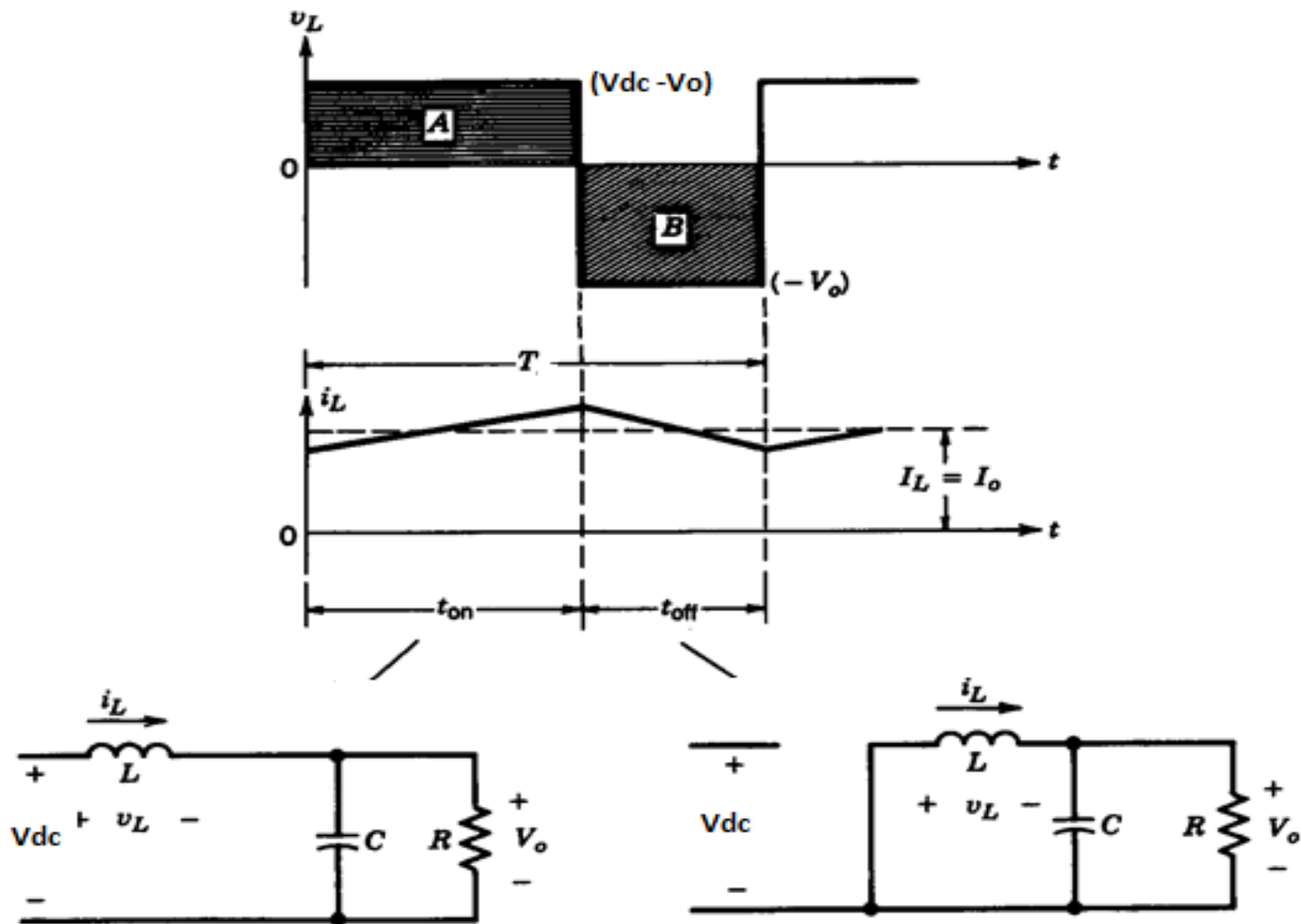


$$V_L = -V_0 \quad (1-D)T < t < T$$

$i_L \downarrow$ Linearly

$$i_L = C \frac{dV_0}{dt} + \frac{V_0}{R}$$

DC to DC buck converter

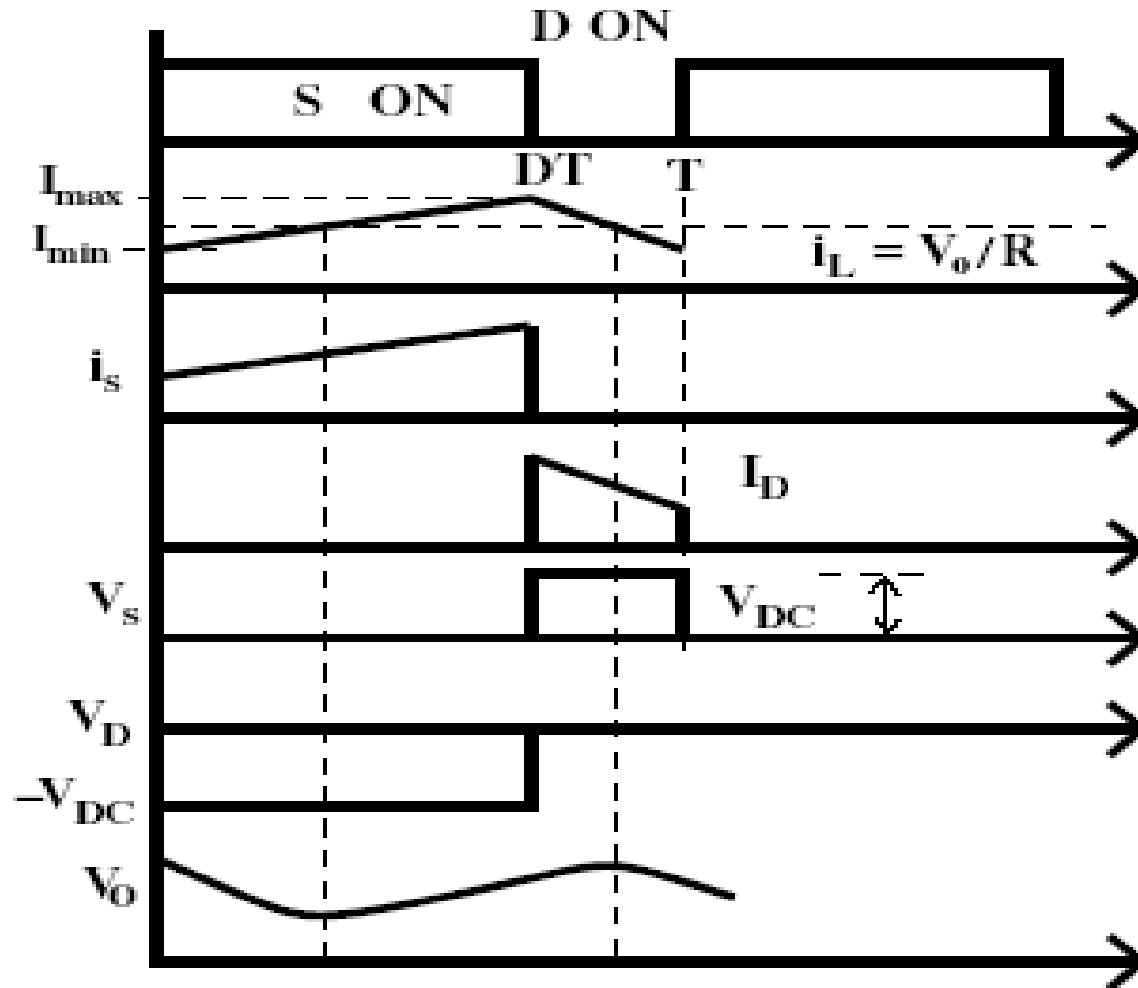


DC to DC buck converter

- Relationship between input and output voltage
- $D = T_{\text{on}} / T$
- Average voltage across inductor is zero.
- $(V_{\text{DC}} - V_{\text{O}}) DT = V_{\text{O}}(1 - D)T$
- $DV_{\text{DC}} - V_{\text{O}}D = V_{\text{O}} - V_{\text{O}}D$
- $V_{\text{O}} = D V_{\text{DC}}$

DC to DC Buck Converter

- Assume the inductor current (I_L) is continuous



DC to DC Buck converter

Neglect losses

Input power = Output power.

$$\begin{aligned} V_{DC} I_s &= V_o I_o \\ &= D V_{DC} I_o \end{aligned}$$

$$\therefore I_s = D I_o$$

Avg. source current < Avg. load current.

\Rightarrow Similar to step-down transformer.

Source current waveform jumps from peak to zero.

\Rightarrow peak value of $i_s > I_s$

\Rightarrow L-C filter at the input side.

DC to DC Buck converter

Discontinuous Conduction:

Inductor current ' i_L ' and NOT I_o .

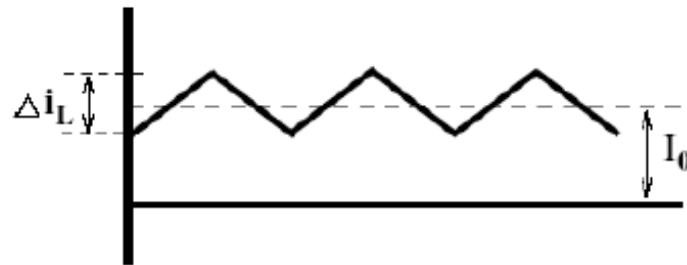
$$I_o = \frac{V_o}{R}.$$

Now i_L is continuous if

$$\frac{V_o}{R} \geq \frac{\Delta i_L}{2}$$

$$\frac{D V_{DC}}{R} \geq \frac{V_{DC}}{2L} (1-D) DT$$

$$\therefore R \leq \frac{2L}{(1-D)T} = R_{CR}$$



$$I_{max} = I_{min} + \frac{(V_{DC} - V_o) DT}{L}$$

$$I_{max} - I_{min} = \frac{(V_{DC} - V_o) DT}{L}$$

DC to DC Buck converter

If load $R > R_{CR}$,

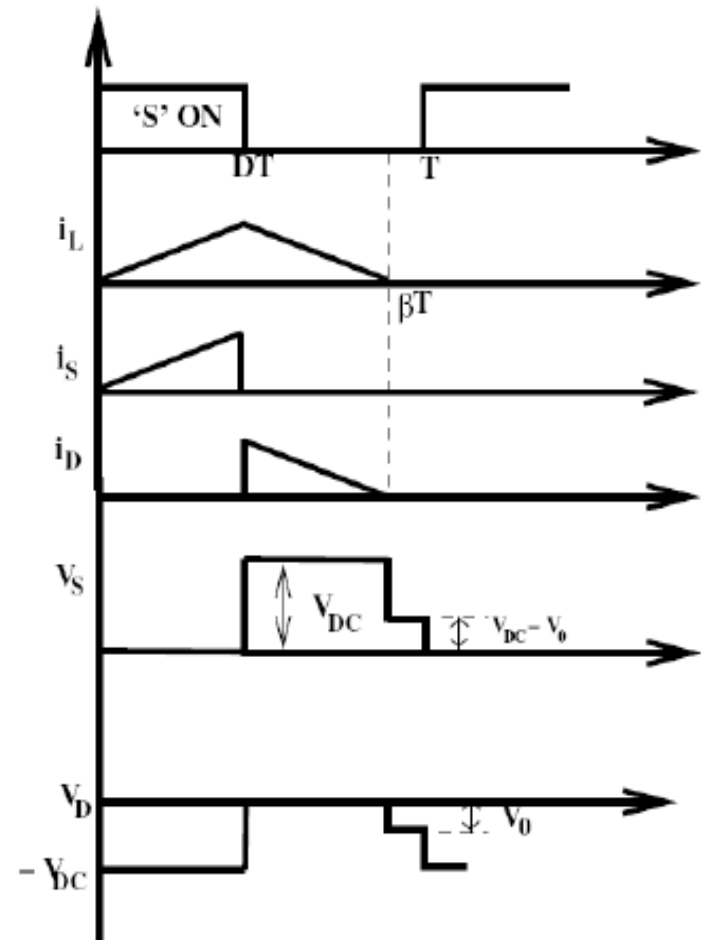
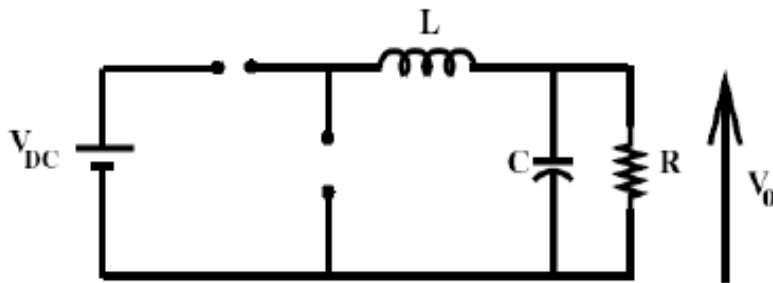
i_L is DISCONTINUOUS.

$\Rightarrow i_L = 0$ for finite time.

i_S starts from zero.

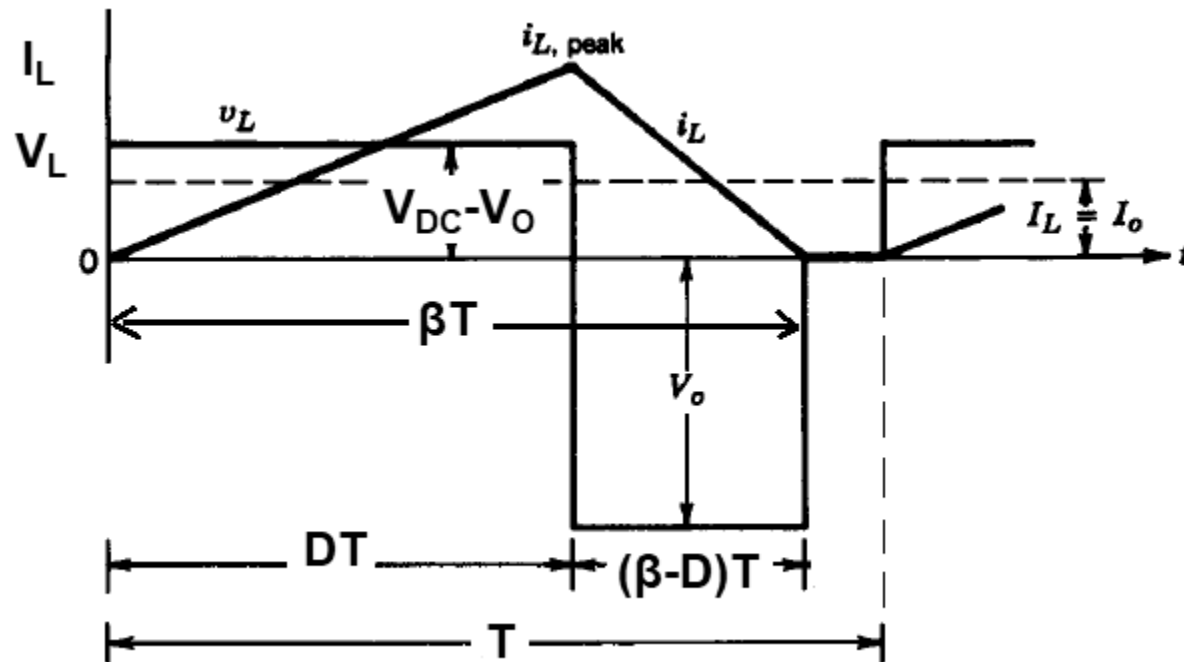
If i_L is continuous, $V_0 = D V_{DC}$

\Rightarrow Independent of I_0



DC to DC Buck converter

- o/p voltage with discontinuous conduction

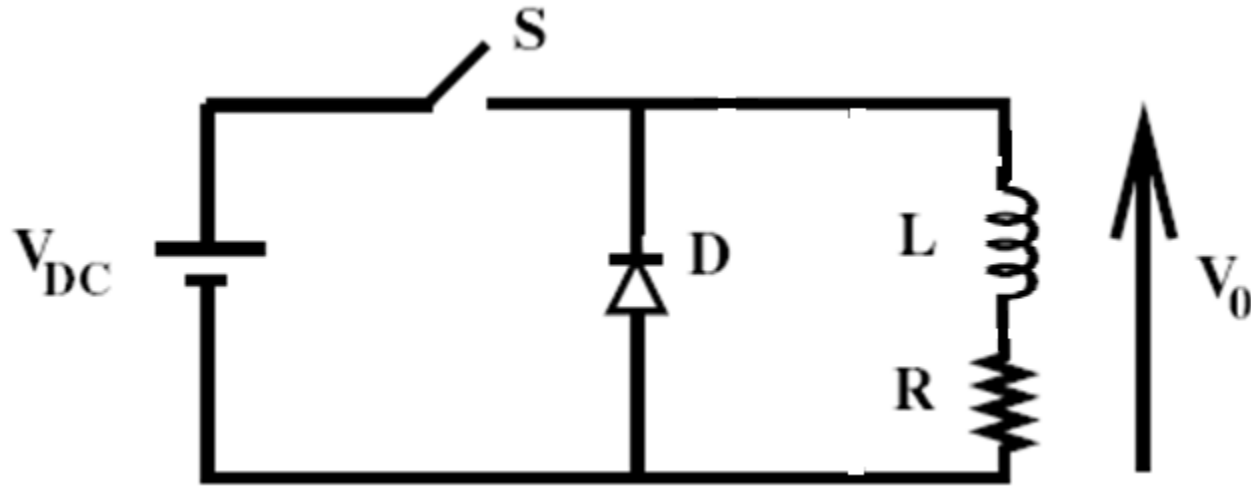


DC to DC Buck converter

- o/p voltage with discontinuous conduction
- $(V_{DC} - V_O) DT = V_O (\beta - D) T$
- $(V_{DC} - V_O) D = V_O (\beta - D)$
- $V_{DC} D = V_O \beta$
- $V_O = DV_{DC} / \beta$

DC to DC Buck converter

- Type A chopper
- In some applications LC filter is not required



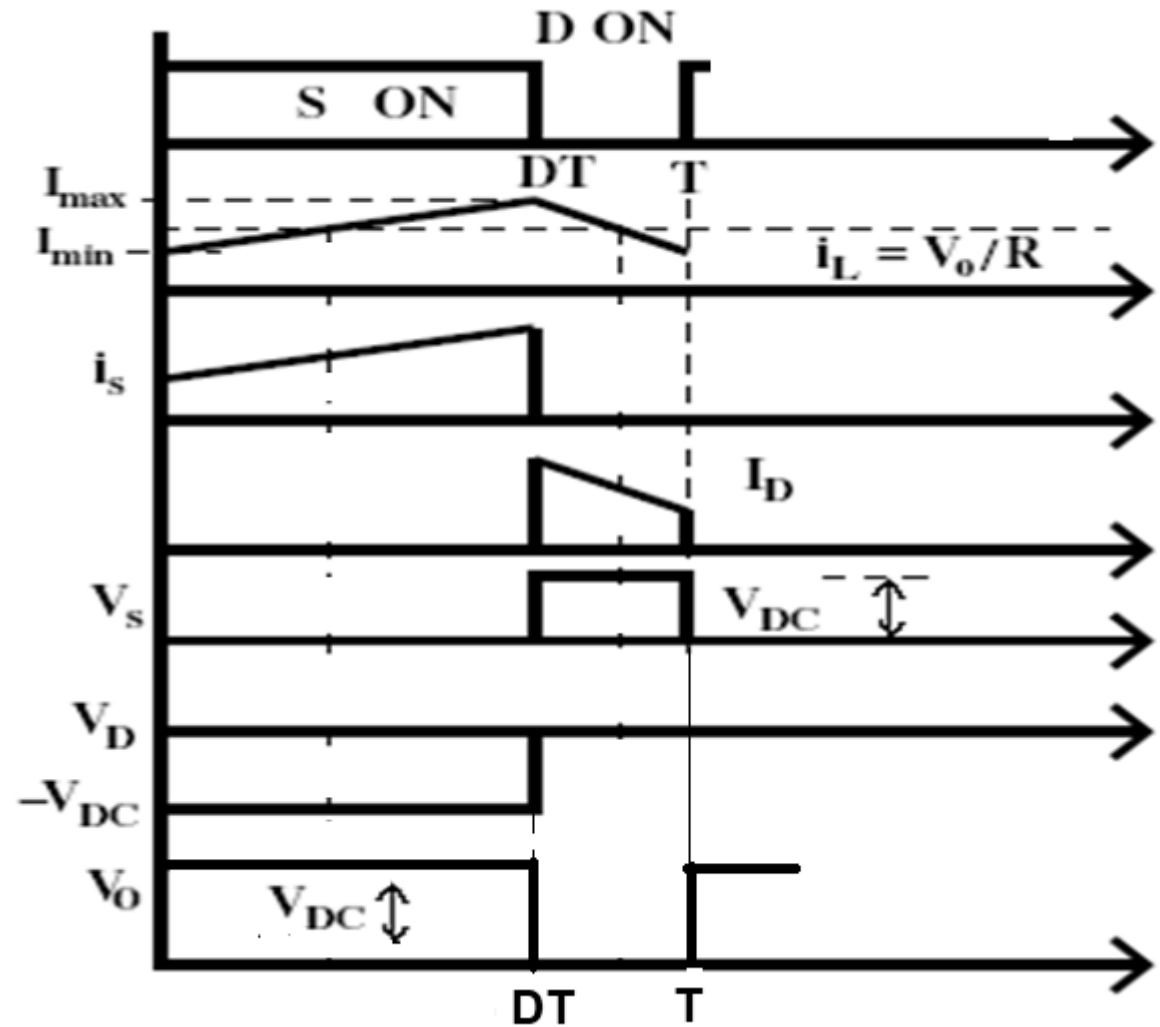
- In this case load is RL load

Type A chopper

■ Waveforms

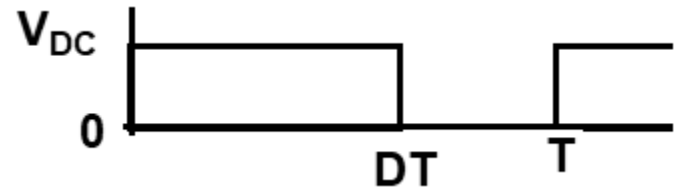
$$V_O = \frac{D T V_{DC}}{T}$$

$$V_O = D V_{DC}$$



Type A chopper : Numerical Problem

- Type A chopper is supplied from 100 V DC supply and is connected to $R = 10 \Omega$ and operating at 0.7 duty cycle. Determine i) average DC voltage ii) Power dissipated in R load and iii) ripple content in DC O/P voltage.
- Average voltage = 70 V
- Rms voltage = 83.66 V
- Form factor = $83.66/70 = 1.195$
- Ripple content = $\sqrt{1.195^2 - 1} = 0.6542$
- % ripple = 65.42%
- Power dissipated in R Load = $V_{dc(rms)}^2/R$
- Power dissipated in R load = 699.89 W



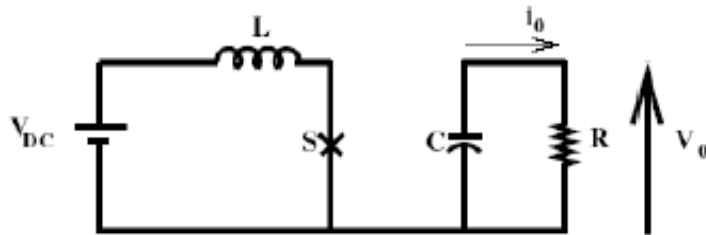
Boost Converter : Continuous Mode

Boost Converter

All components are ideal.

V_0 & V_{DC} are constant and ripple free.

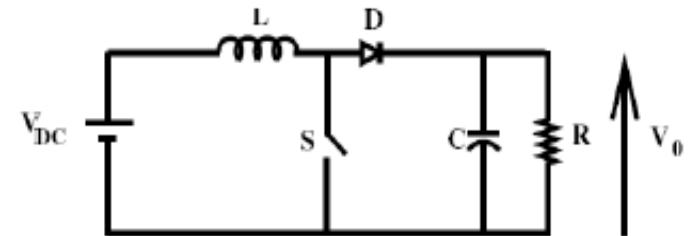
Close S : for DT



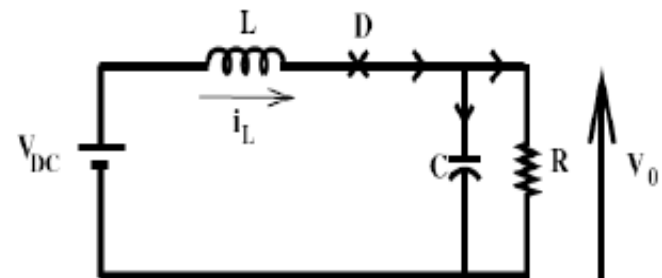
$$V_L = V_{DC}$$

$\therefore i_L \uparrow$ linearly.

$$i_0 = -C \frac{dV_0}{dt} = \frac{v_0}{R}$$



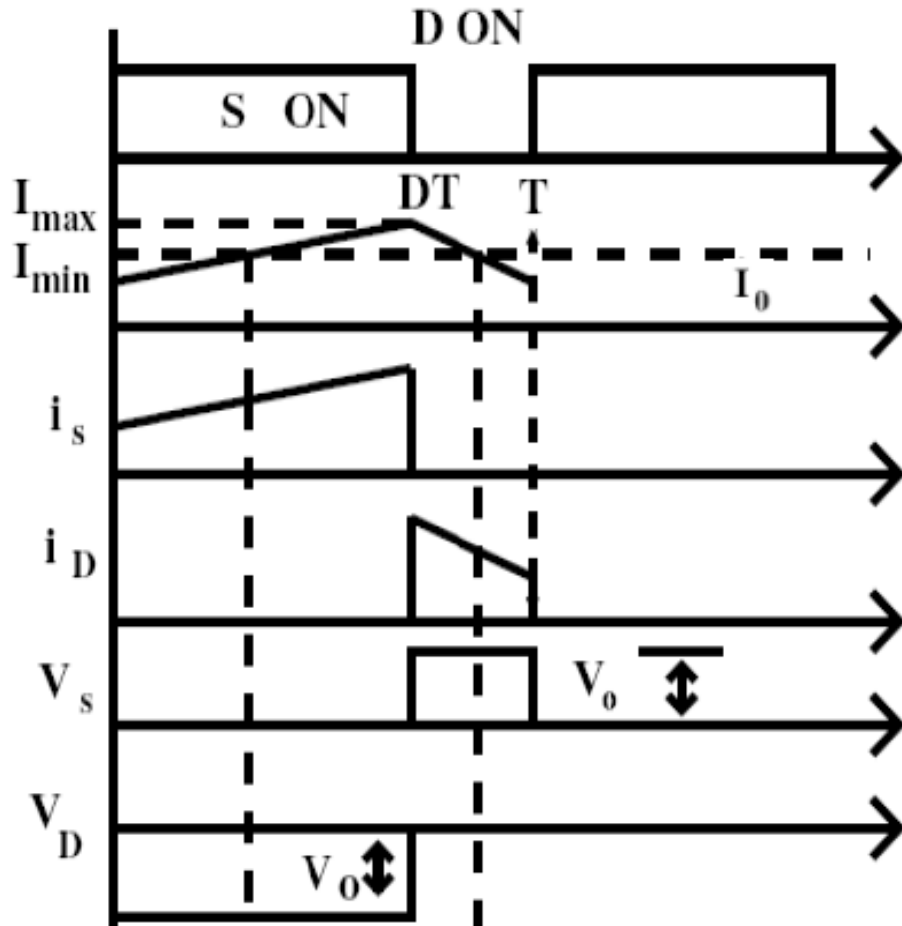
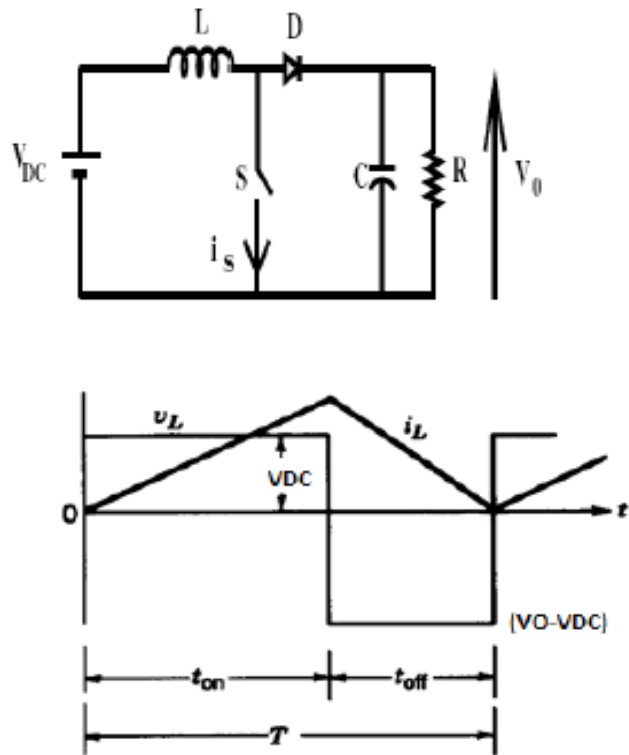
Open S



$$v_L = V_{DC} - V_0$$

$$C \frac{dV_C}{dt} + \frac{V_0}{R} = i_L$$

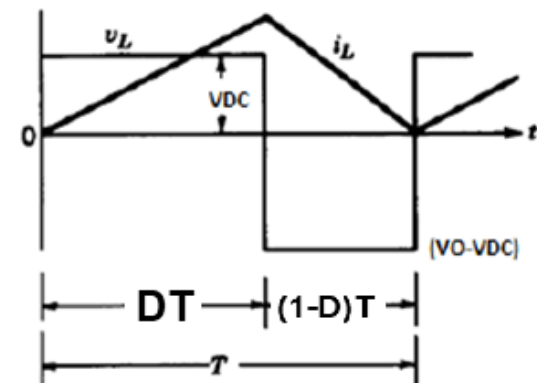
Boost Converter : Continuous mode



Source current and Inductor current is same

Boost Converter : continuous Mode

- Average Voltage drop across L is zero
- $V_{DC} DT = (V_O - V_{DC})(1-D)T$
- $V_{DC} D = (V_O - V_{DC})(1-D)$
- $V_{DC} D = V_O (1-D) - V_{DC} + V_{DC} D$
- $V_O (1-D) = V_{DC}$
- $V_O = V_{DC} / (1-D)$



Boost Converter : Continuous Mode

Capacitor supplies power to the load.

$$V_s = 0$$

$$V_D = -V_0$$

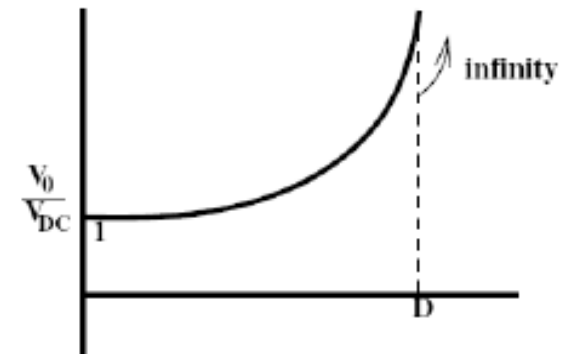
avg. voltage across 'L' = 0.

$$V_0 = \frac{V_{DC}}{(1-D)}$$

System is loss-less.

$$V_{DC} I_s = V_0 I_0$$

$$\therefore I_s = \frac{V_0}{V_{DC}} * I_0 = \frac{I_0}{(1-D)}$$



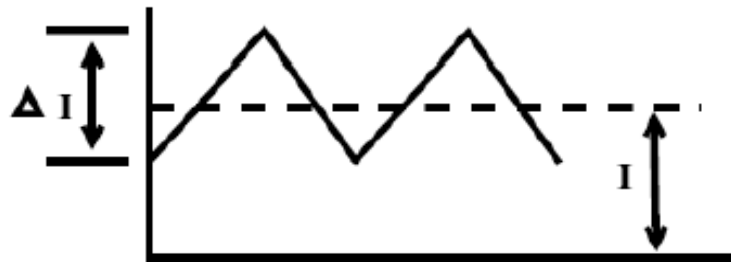
Boost Converter : Critical load Resistance

- $I_s = I_o / (1-D)$
- $I_o = V_o / R = V_{DC} / [(1-D)R]$
- $I_s = V_{DC} / [(1-D)^2 R]$
- $I_{\max} = I_{\min} + (V_{DC}/L) DT$
- $I_{\max} - I_{\min} = (V_{DC}/L) DT$
- $\Delta I_L = (V_{DC}/L) DT$

Boost Converter : Critical load Resistance

Discontinuous current:

Av. value of source I = inductor I = $\frac{V_{DC}}{R(1-D)^2}$



The above I is always + ve

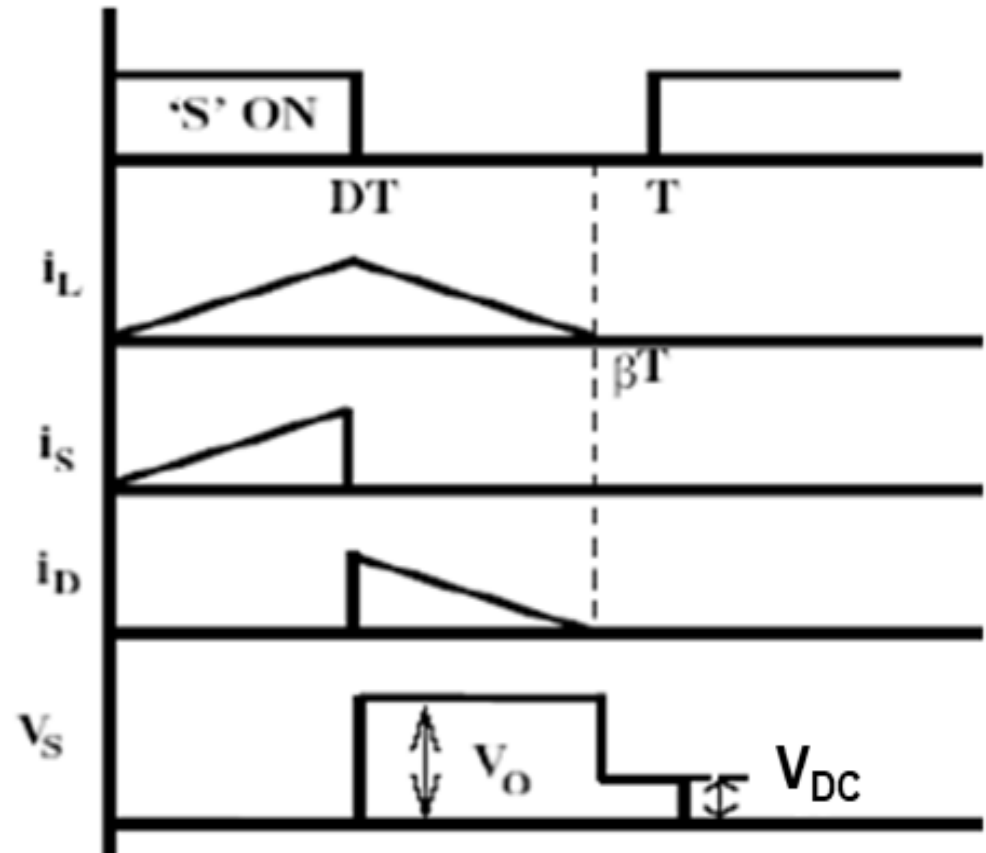
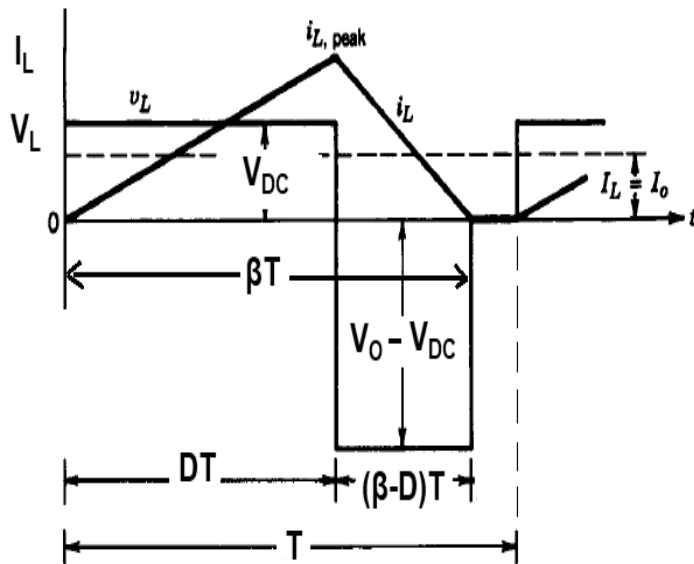
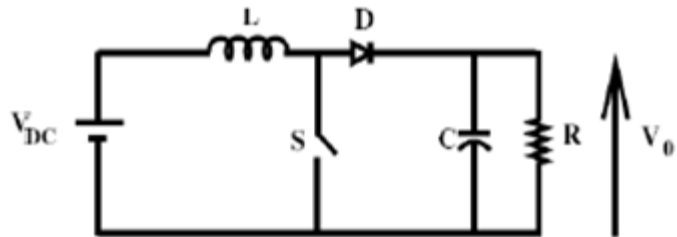
$$\text{if } \begin{aligned} &> \frac{\Delta I}{2} \\ &> \frac{V_{DC}}{2L} DT \end{aligned}$$

$$\therefore R_{CR} \leq \frac{2L}{(1-D)^2 DT}$$

If load $R > R_{CR}$

Inductor I \Rightarrow Discontinuous

Boost Converter : Discontinuous mode

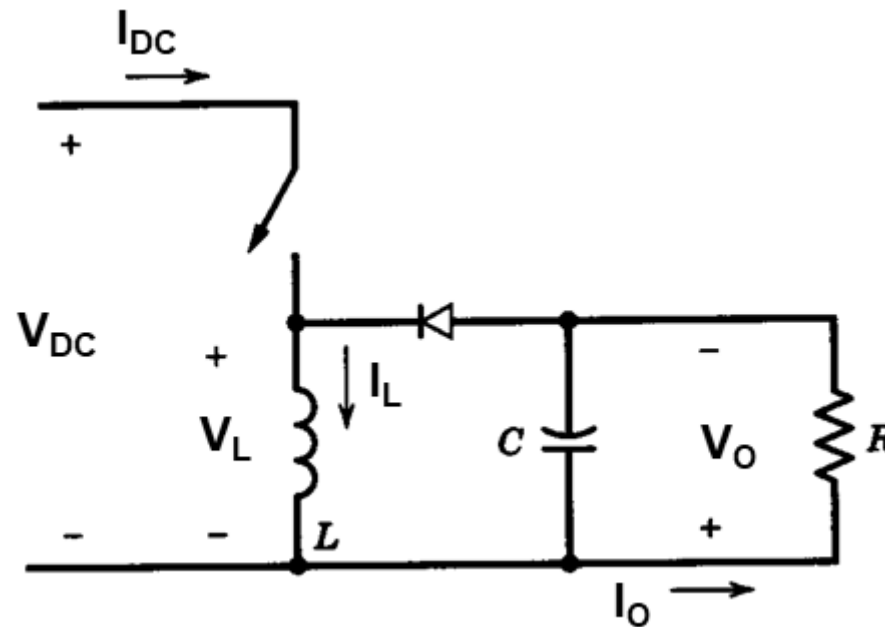


Boost Converter : Discontinuous Mode

- Average Voltage drop across L is zero
- $V_{DC} DT = (V_O - V_{DC})(\beta - D)T$
- $V_{DC} D = (V_O - V_{DC})(\beta - D)$
- $V_{DC} D = V_O (\beta - D) - \beta V_{DC} + V_{DC} D$
- $V_O (\beta - D) = \beta V_{DC}$
- $V_O = \beta / (\beta - D) V_{DC}$

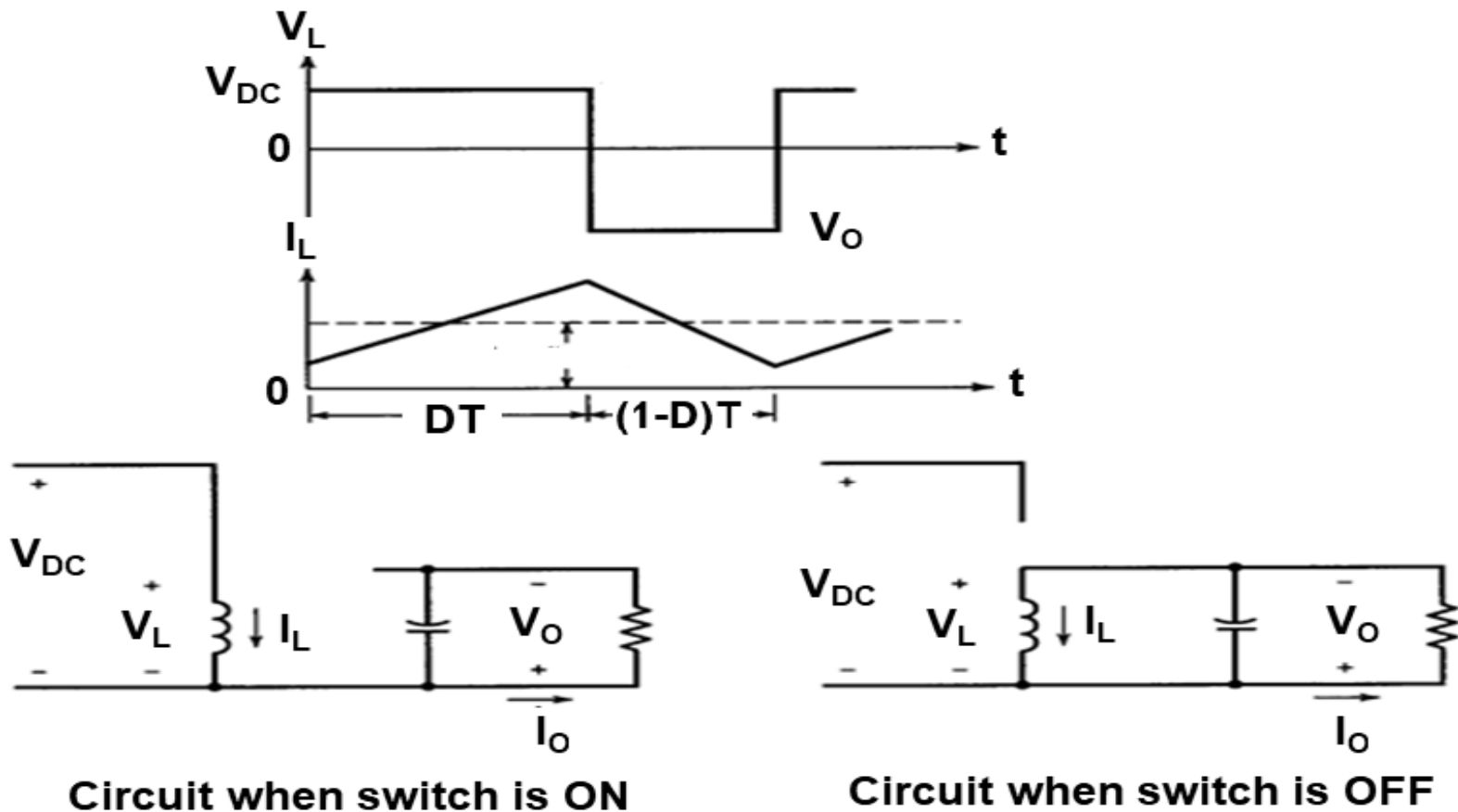
Buck-boost DC to DC Converter

- Output voltage can be higher or lower than input voltage
- Provides $-V_e$ polarity O/P



Buck-boost DC to DC Converter

■ Continuous conduction mode

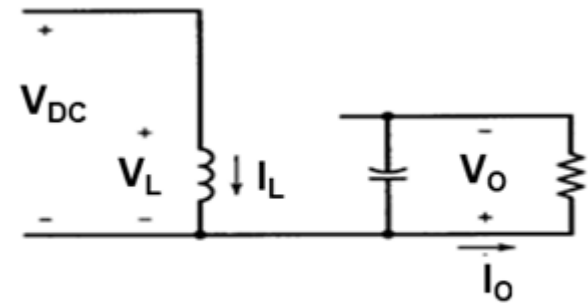
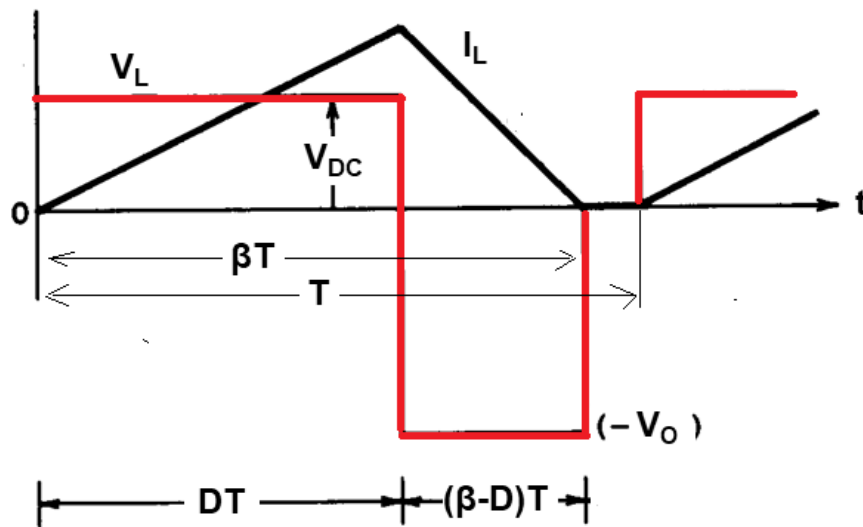


Buck-boost DC to DC Converter

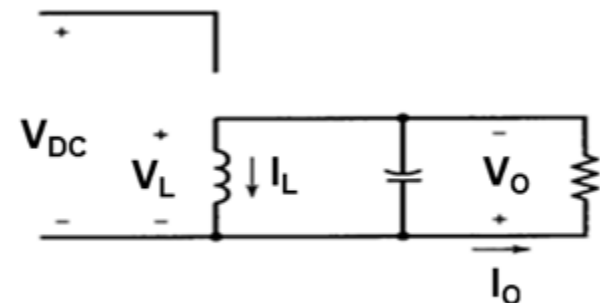
- Average voltage across inductor is zero.
- $V_{dc} D T = V_o (1-D) T$
- $V_o = D/(1-D) V_{dc}$
- $V_o/V_{dc} = D/(1-D)$
- $I_o/I_d = (1-D)/D$
- Source current is discontinuous

Buck-boost DC to DC Converter

■ Discontinuous conduction



Circuit when switch is ON



Circuit when switch is OFF

Buck-boost DC to DC Converter

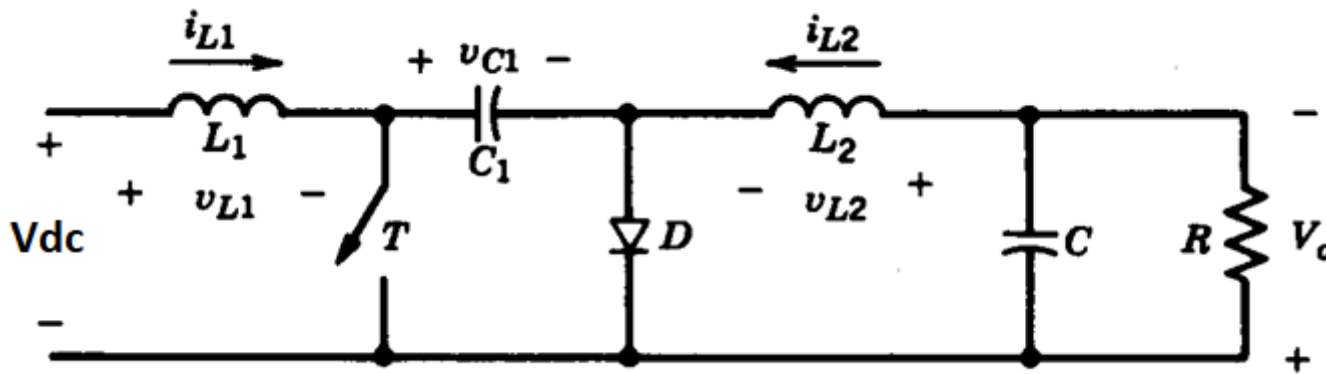
- Average voltage across inductor is zero.
- $V_{DC} D T = V_O (\beta - D) T$
- $V_{DC} D = V_O (\beta - D)$

$$V_O = \frac{D}{(\beta - D)} V_{DC}$$



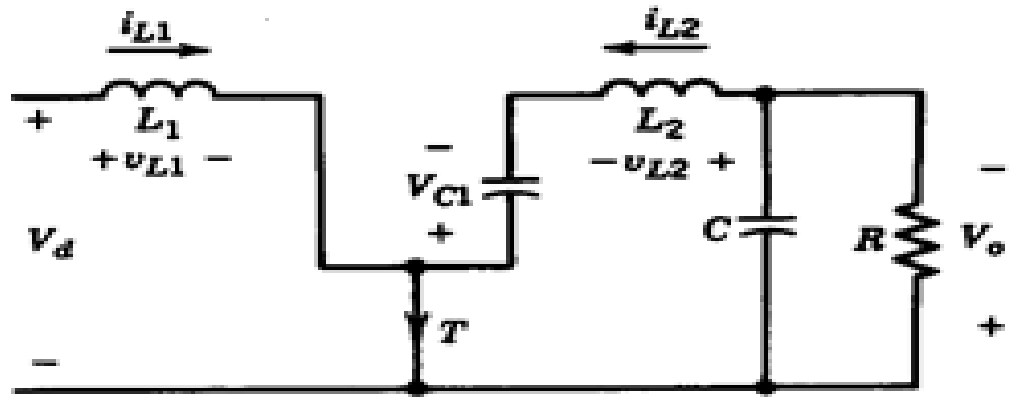
Cuk Converter

- Output voltage can be lower or higher than input voltage
- It provides negative polarity output
- Average voltage V_{L1} and $V_{L2}=0$
- $V_{C1} = V_{DC} + V_O$
- V_{C1} remains approximately constant



Cuk Converter

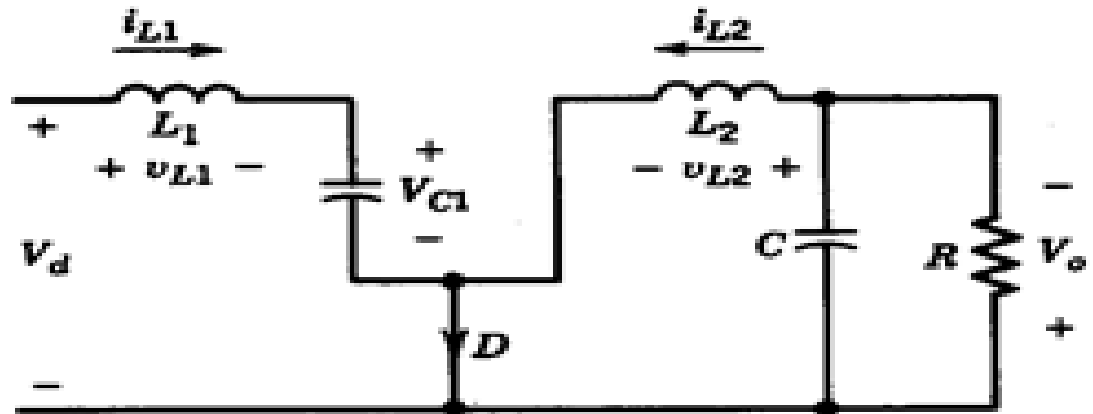
- When switch is on



- Current through L_1 will increase. $V_{L1} = V_d$
- V_{C1} is greater than V_o hence current through L_2 also increases. $V_{L2} = V_{C1} - V_o$
- L_1 receives energy from source
- C_1 will supply energy to load and L_2

Cuk Converter

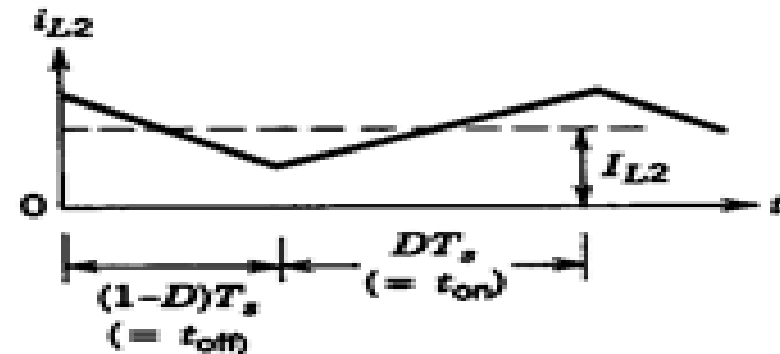
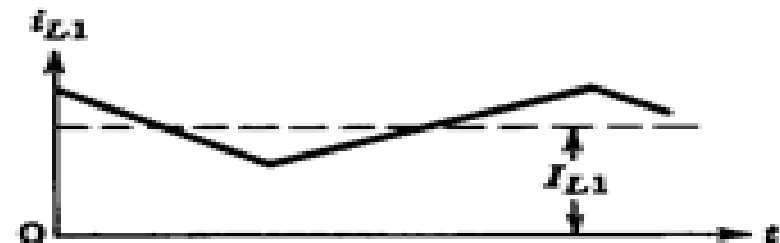
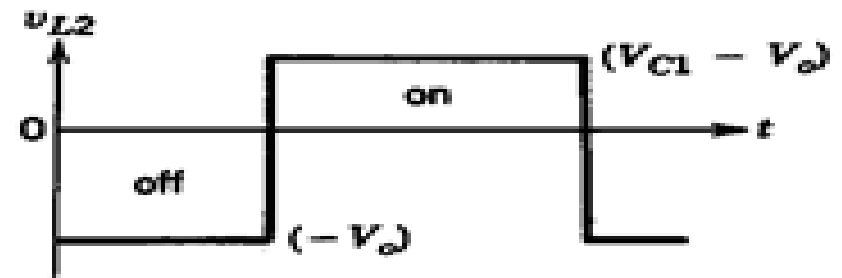
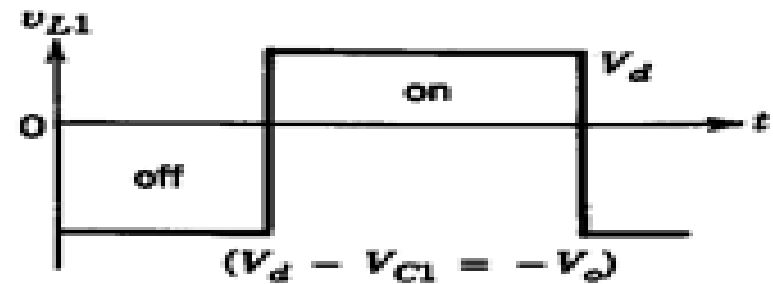
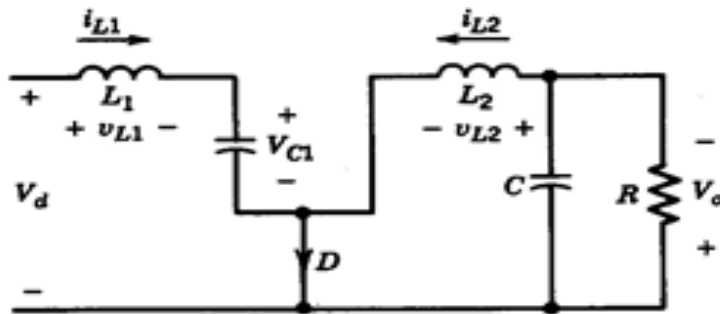
- When switch is off



- L_1 will charge to C_1 , i_{L1} decreases
- Voltage across $L_1 = -(V_d - V_{C1})$
- L_2 provides energy to load
- Voltage across $L_2 = -V_o$

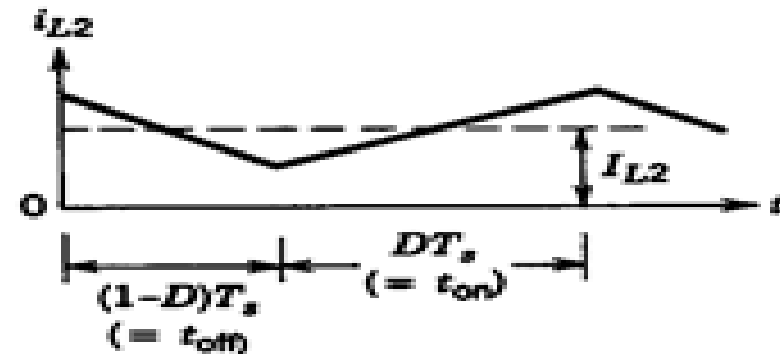
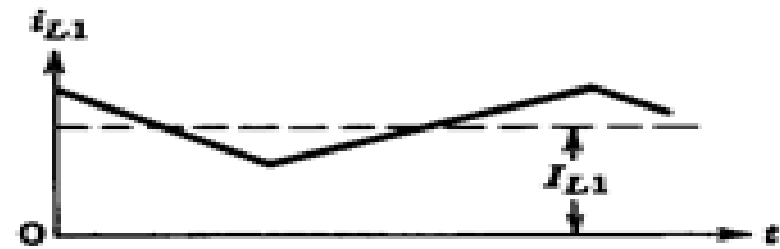
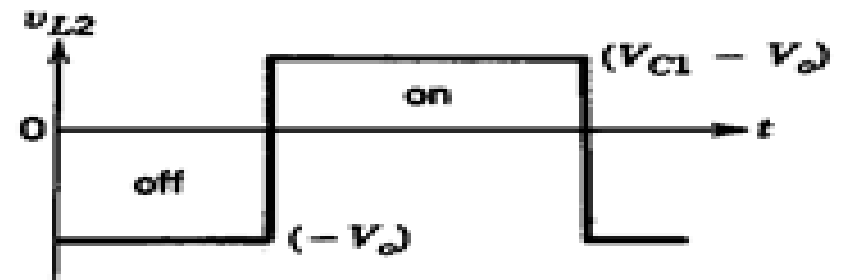
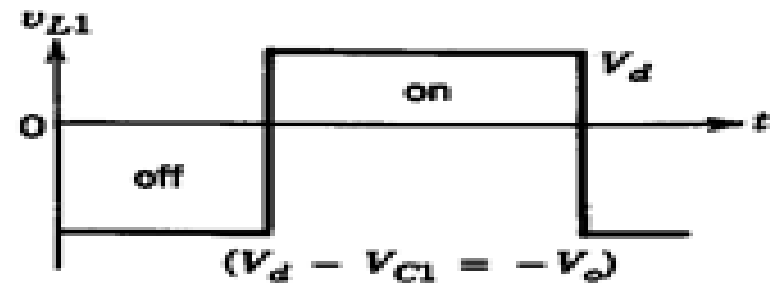
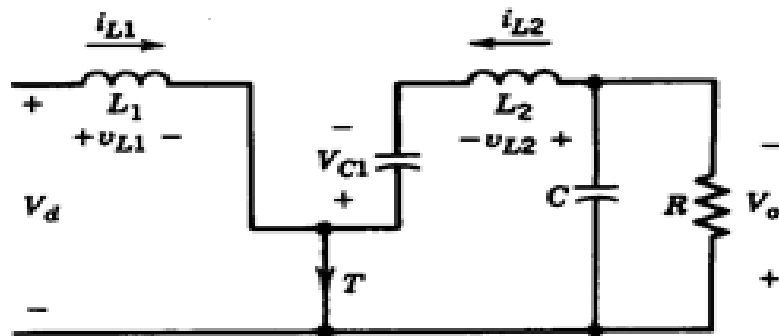
Cuk Converter

- When S is OFF
- Capacitor voltage is assumed constant



Cuk Converter

- When S is ON
- Capacitor voltage is assumed constant



Cuk Converter

- It provides negative polarity output
- When switch is on
- $V_{L1} = V_d$ and $V_{L2} = V_{C1} - V_O$
- When switch is off
- $V_{L1} = V_{C1} - V_d$ and $V_{L2} = V_O$
- Average voltage drop across L_1 is zero
- $V_d D T = (V_{C1} - V_d)(1-D) T$
- $V_{C1} = V_d / (1-D)$

Cuk Converter

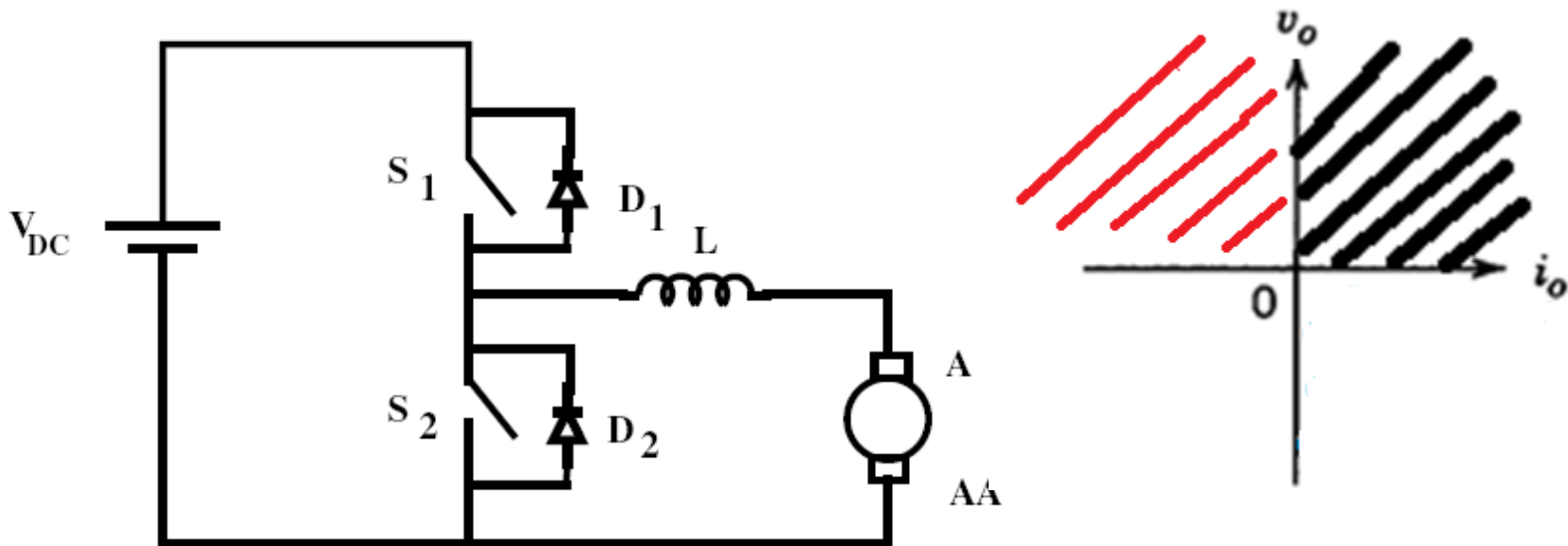
- Average voltage drop across L_2 is zero
- $(V_{C1} - V_O) DT = V_O(1-D) T$
- $V_O = D V_{C1}$
- Substituting value of V_{C1}

$$V_O = \frac{D}{(1-D)} V_d$$

- It is a buck boost converter

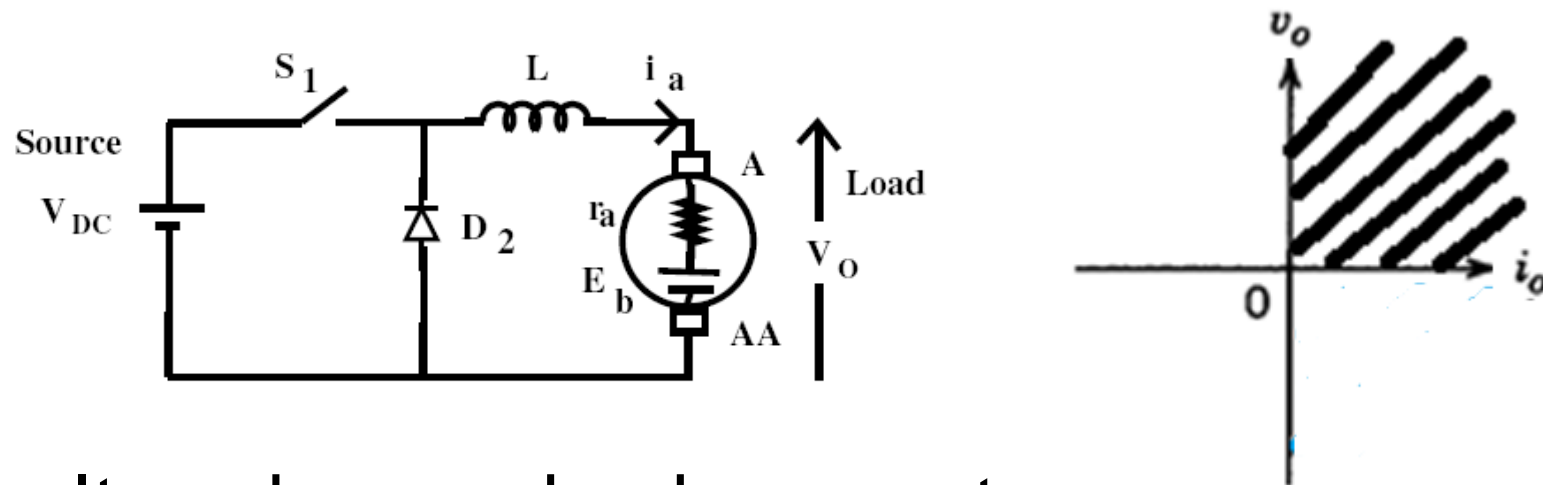
Two quadrant DC to DC Converter

- Two quadrant operation



Two quadrant DC to DC Converter

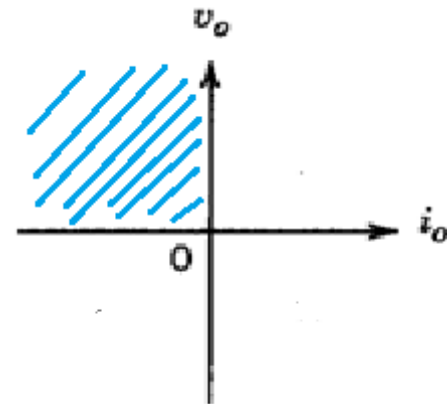
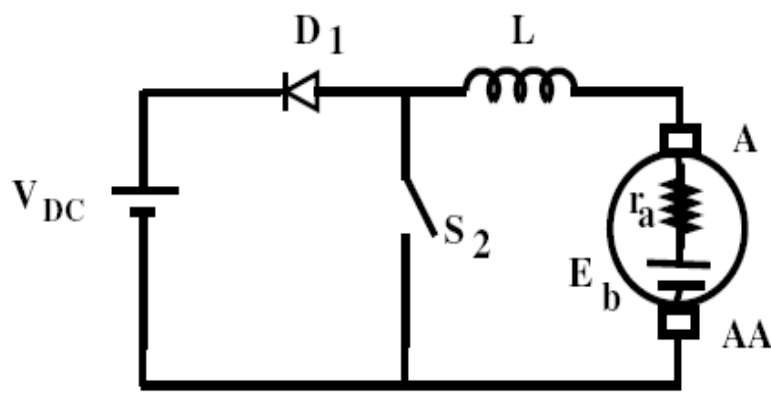
- First quadrant operation
- S_2 is kept off and S_1 is controlled



- It works as a buck converter.
- Output voltage supplied to armature of motor is controlled by controlling duty ratio.

Two quadrant DC to DC Converter

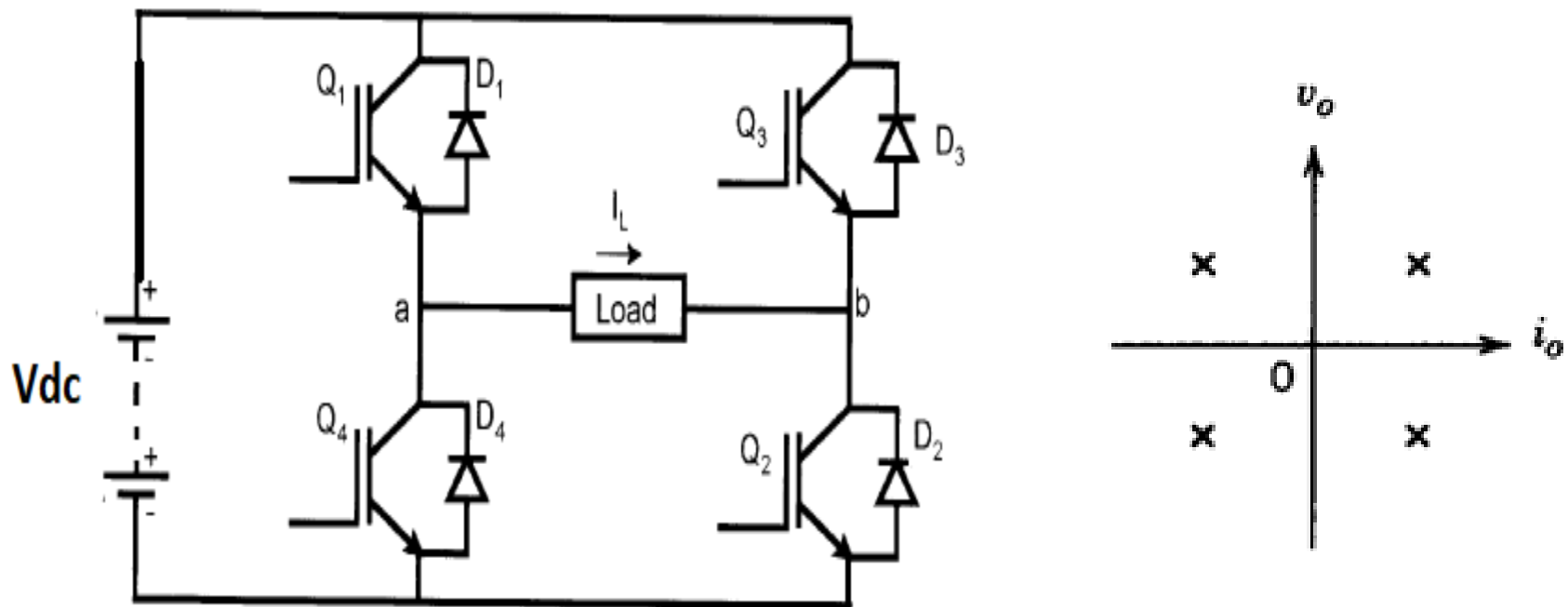
- Second Quadrant operation
- S_1 is kept off and S_2 is controlled



- It works as a boost converter, providing regenerative braking of separately excited DC Motor

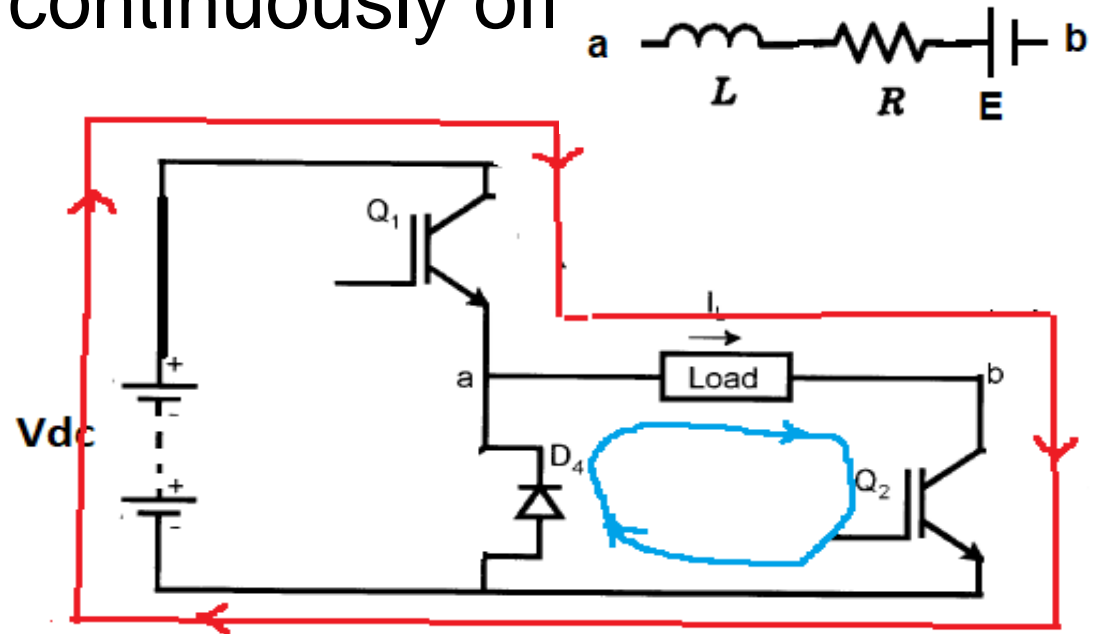
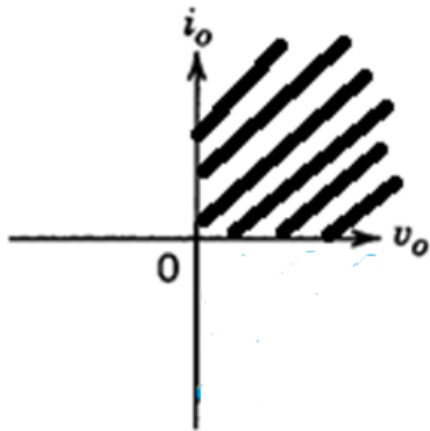
Four quadrant DC to DC Converter

- It is also called as class E chopper



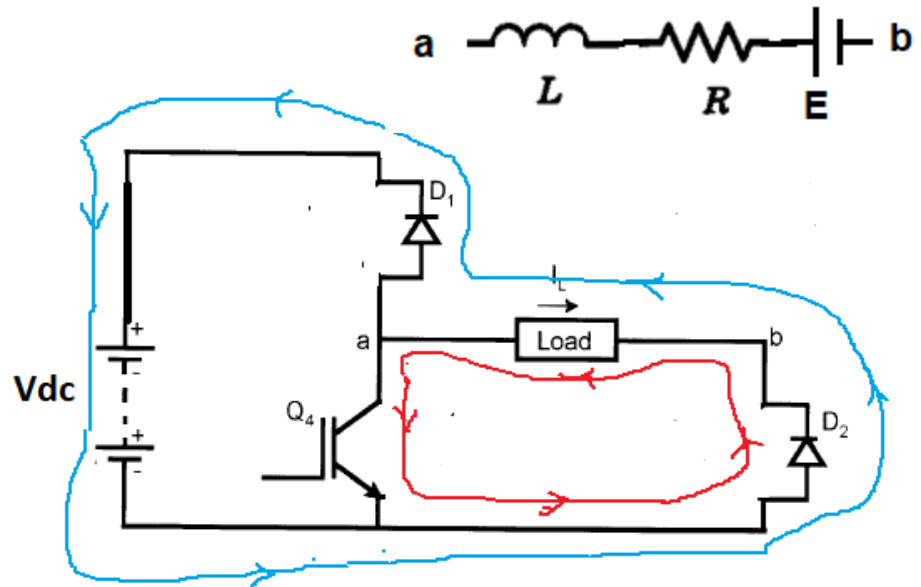
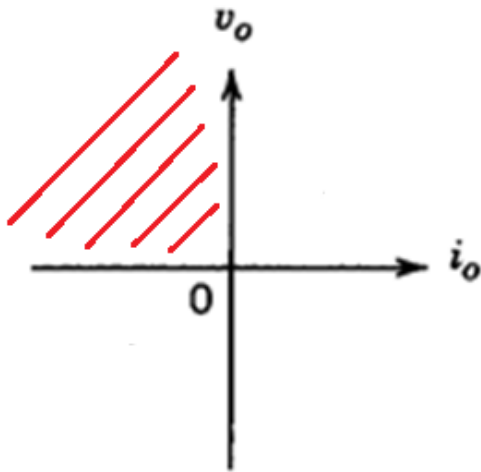
Four quadrant DC to DC Converter

- First quadrant operation
- Works as buck converter
- Q2 is continuously on , Q1 is controlled
- Q3 and Q4 are continuously off



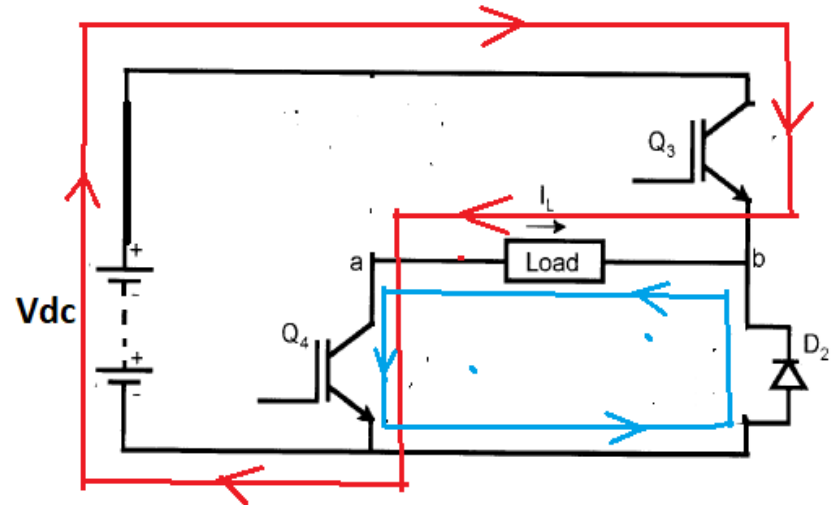
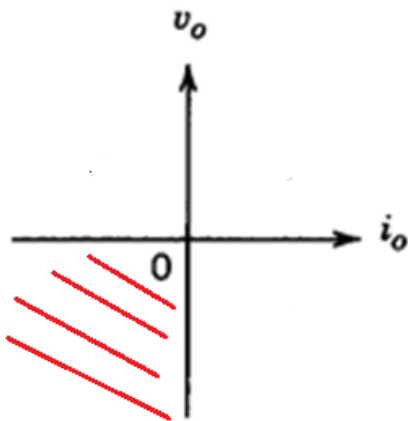
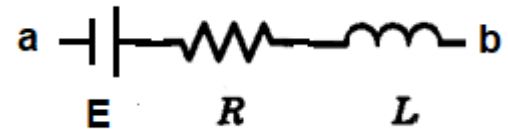
Four quadrant DC to DC Converter

- **Second quadrant operation**
- Load should be RLE type
- Q4 is controlled, Q1, Q2, Q3 continuously off
- Works as boost converter. feeding power back to supply



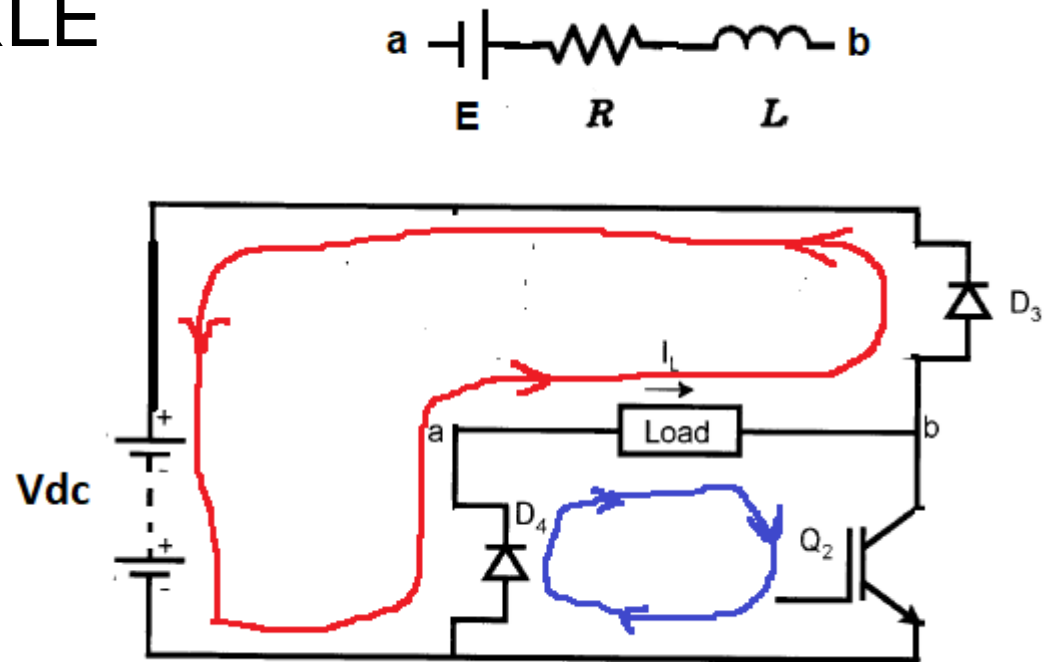
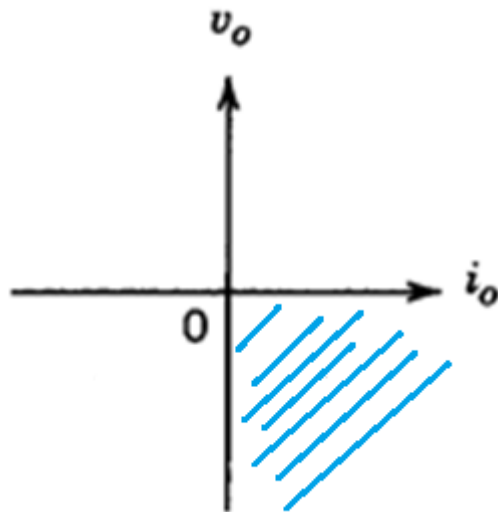
Four quadrant DC to DC Converter

- Third quadrant operation
- Works as buck converter
- Q4 is continuously on, Q3 is controlled
- Q1 and Q2 are continuously off.



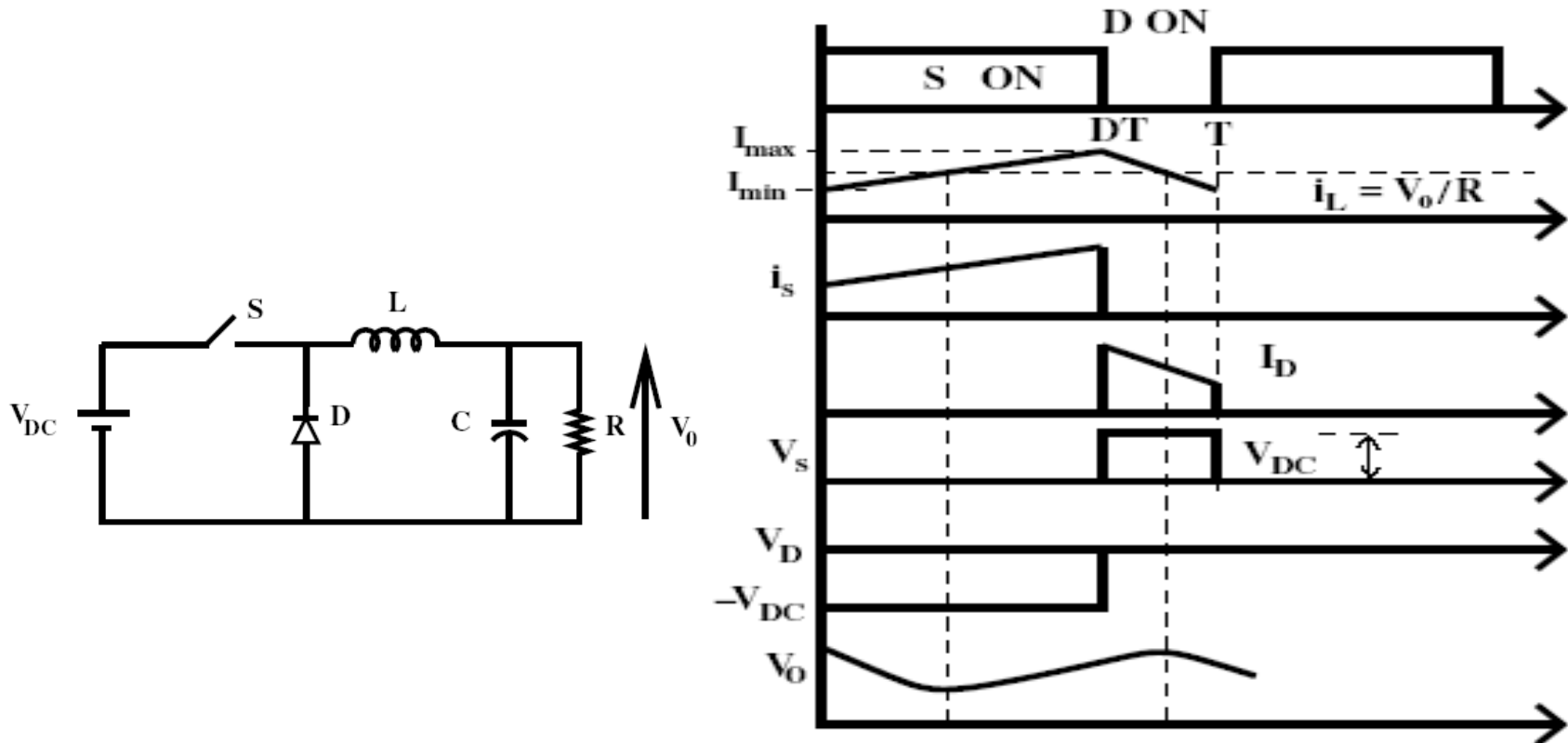
Four quadrant DC to DC Converter

- fourth quadrant operation
- Works as boost converter
- Q2 is controlled. Q1, Q3 and Q4 are off.
- Load should be RLE



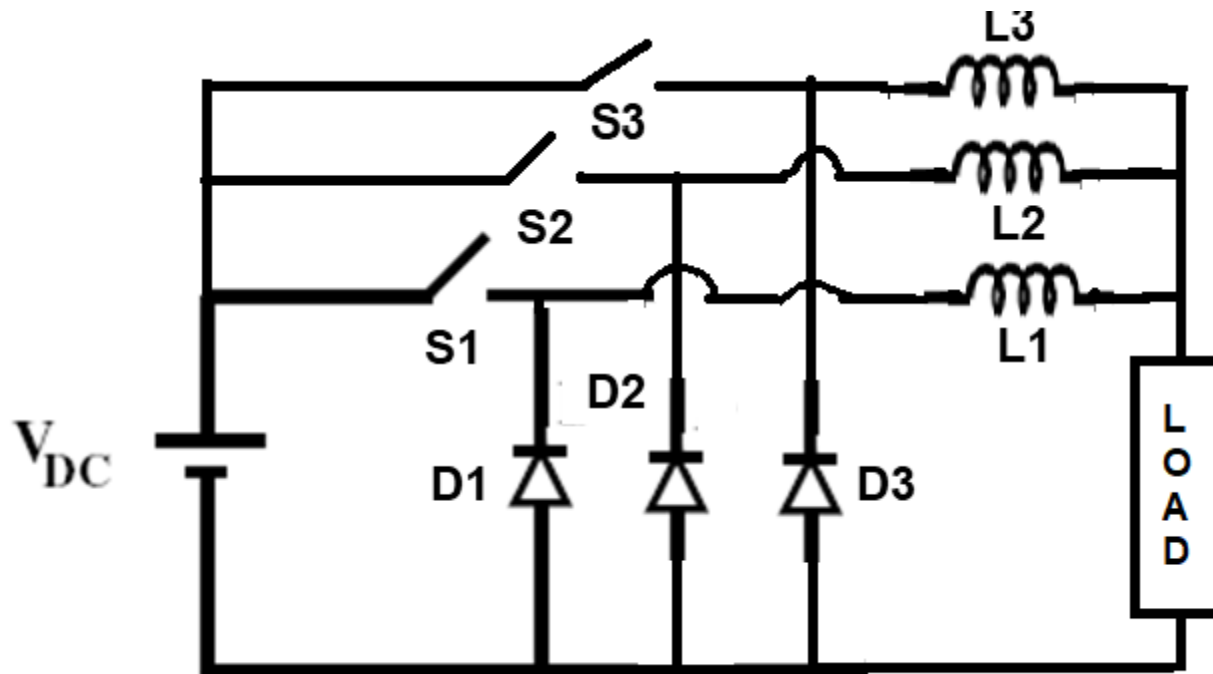
DC to DC Buck Converter

- Assume the inductor current (I_L) is continuous



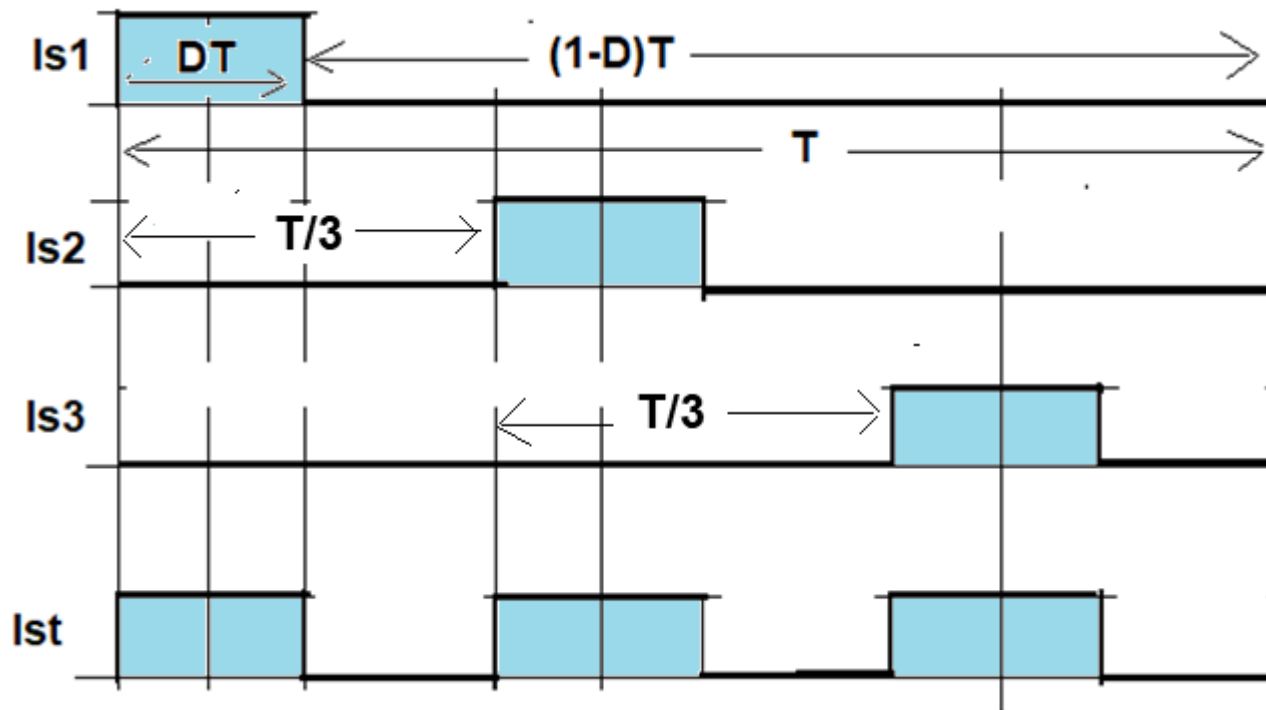
Multi Phase choppers

- Type A chopper connected in parallel to supply a common load
- Any numbers of type A can be connected in parallel



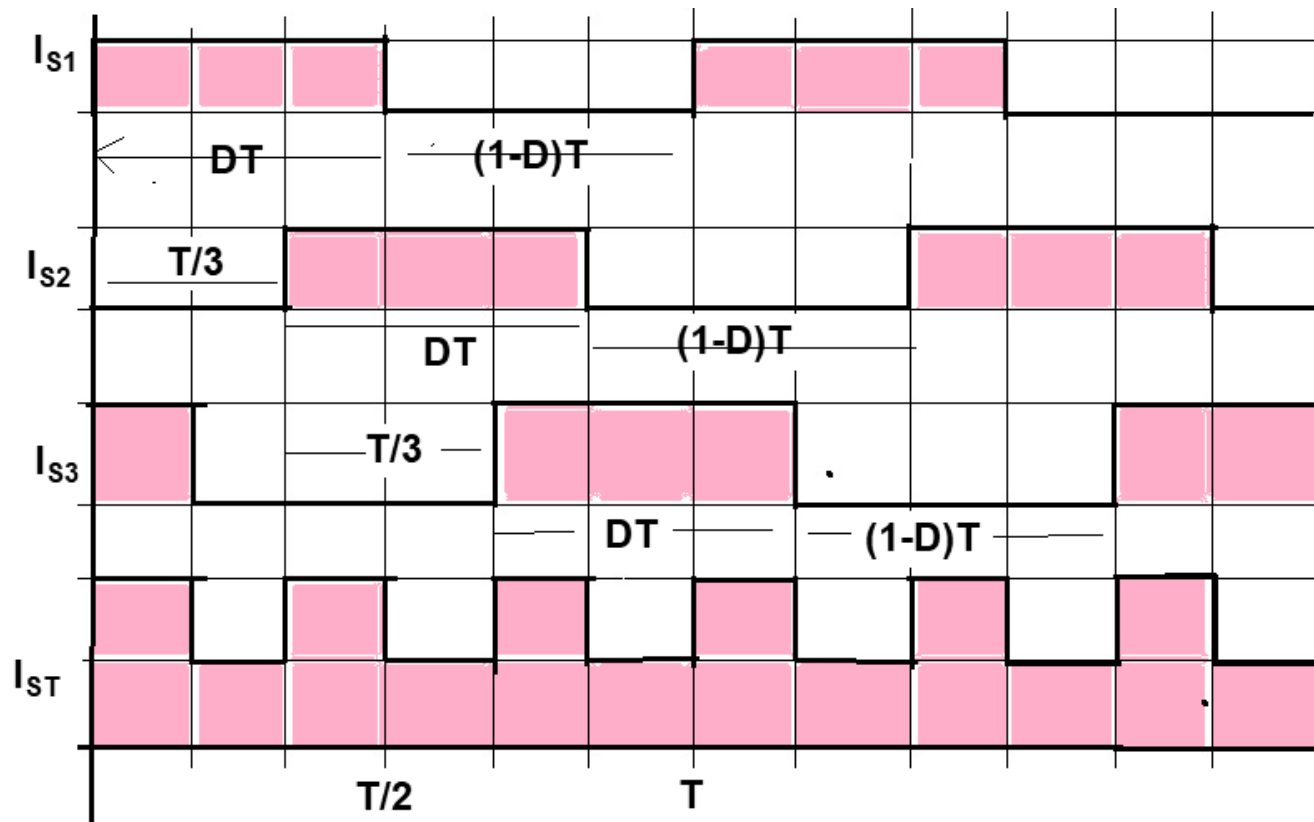
Multi Phase choppers : Operating Modes

- In-phase operation
- Phase shifted operation $D = 0.15$



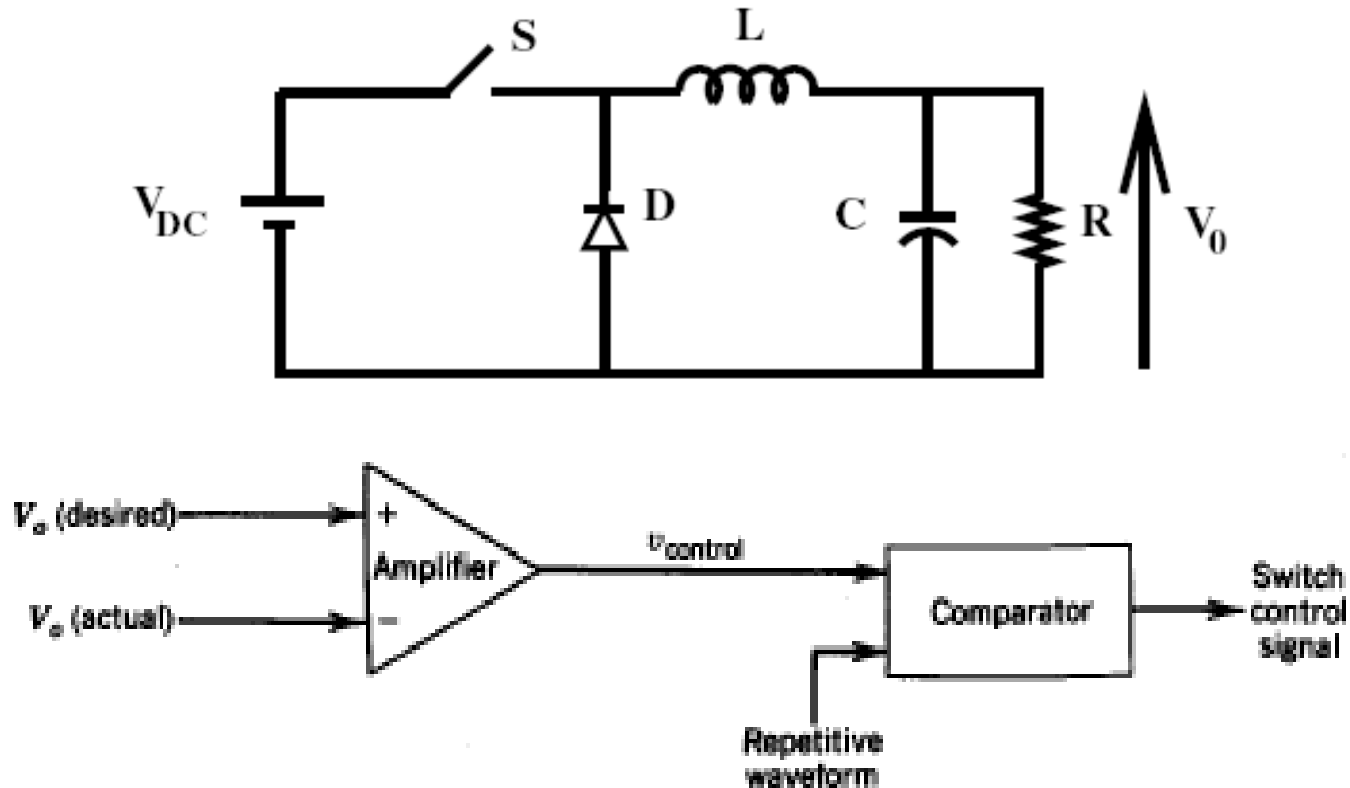
Multi Phase choppers : Operating Modes

■ Phase shifted operation $D=0.5$



Close loop control

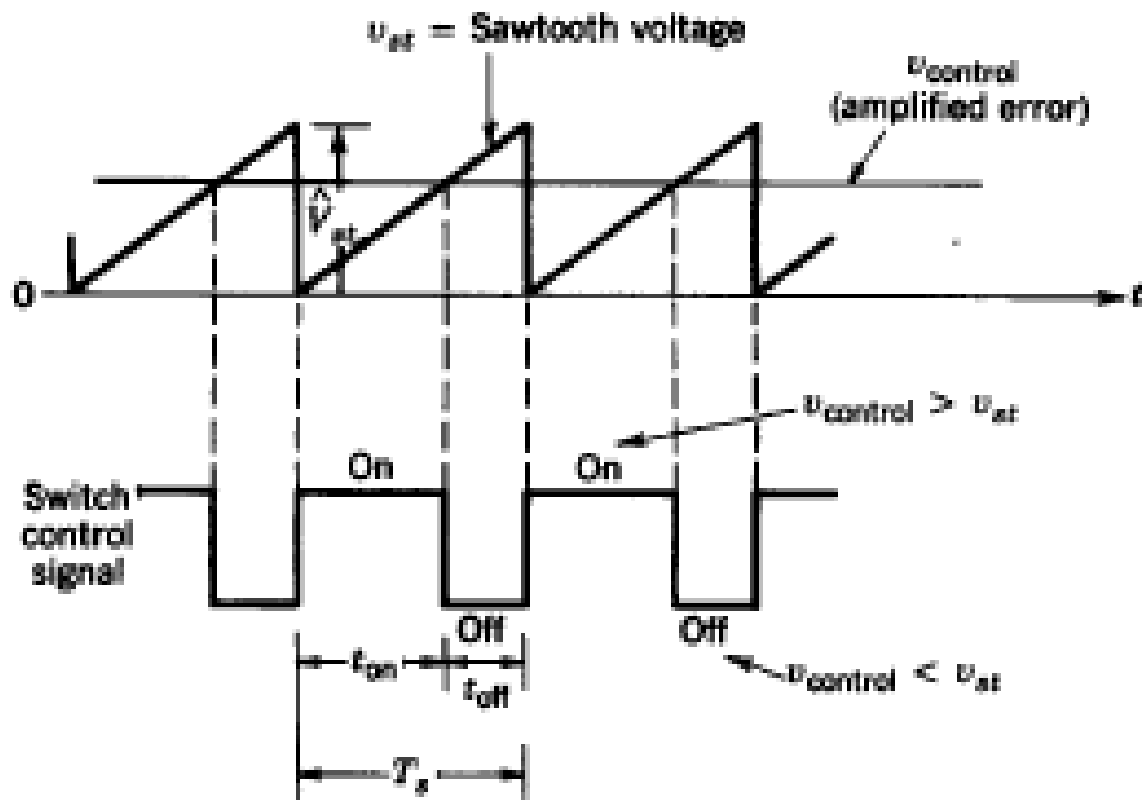
■ Buck Converter



■ Amplifier => PI OR PID controller

Close loop control

■ Buck Converter



Conclusion

- DC to DC converter should be operated at high switching frequency to reduce the size of L and C
- DC to DC converters finds the application in dc servo drives which requires very fast response.
- DC servo drives finds applications in robotics and position control.

THANKS !

Any Questions?

Close loop control

- V_L I_L V_{DC} V_O I_O βT $(\beta-D)T$ $D1$ $D2$ $D3$ $S1$ $S2$ $S3$
- DT
- $(1-D)T$ $L1$ $L2$ $L3$ $T/3$ I_{S1} I_{S2} I_{S3} I_{ST}
- 0 I_{DC}
- T $T/2$ DT $(1-D)T$
- Circuit when switch is ON

- Circuit when switch is OFF