91)  $T(n) = 3T (n/2) + n^2$   $T(n) = aT(n/6) + f(n^2)$  a > 1, b > 1On compaining  $a = 3, b = 2, f(n) = n^2$ Now, C = log a = log 3 = 1.584  $n^2 = n^{1.584} \le n^2$   $f(n) > n^2$   $f(n) > n^2$   $f(n) > n^2$  $f(n) > n^2$ 

93)  $T(n)_2 T(n/2) + 2^n$  A = 1 b = 2  $f(n)_2 2^n$  C = log a = log c = 0  $h^c = h^o = 1$   $f(n) > h^c$   $T(n)_2 \delta(2^n)$ 

91)  $T(n)_2 2^n T(n/2) + n^n$   $\rightarrow a = 2^n$  b = 2,  $f(n) = n^2$   $c = \log_2 a = \log_2 2^n$  e = n  $n^2 + n^n$   $f(n) = n^2$ f(n) = 0 ( $n^2 \log_2 n$ )

95) T(n) = 16 T(n/4) + n  $\rightarrow a = 16, b = 4$  f(n) = n  $c = \log 16 = \log (4)^2 = 2\log 4$   $= 2^{16} = \log (4)^2 = 2\log 4$   $n^c \ni n^2$   $f(n) \in n^c$   $f(n) \in n^c$   $f(n) \in n^c$ 

Jo)  $T(n)=2T(n/2)+n \log n$   $\rightarrow a=2, b=2$   $f(n)=n \log n$   $c=\log z=1$   $n^c=n^c=n$   $n \log n > n$   $f(n) > n^c$   $f(n) > n^c$  $f(n) = 0 (n \log n)$ 

X

g7) T(n)2 2T(n/2) + n/lagn > a=2, b=2, f(n)= n/logn C= lag 2 = 1 nc=n1=n log n < n · . f(n) < nc :. T(n) = 0 (n) 98) T(n)=2T(n/4)+n0.51 → a=2, b=4, f(n)= n0.51  $C = \log_{10} a = \log_{10} 2 = 0.5$   $n^{c} = n^{0.5}$   $n^{0.5} < n^{0.5}$ f(n)>nc .. T(n) = 0 (nº.51) 99) T(n) 2 0.5 T (n/2) + 1/n -> a=0.5, b=2 a 1/1 but here a is 0.5 so me cannot apply Master's Theorem. 910) T(n)= 16T(n/4)+n! -> a=16, b=4, f(n)=n!

So we cannot apply Master Theorem. g(0) T(n) = 16T(n/4) + n!  $\Rightarrow a = 16, b = 4, f(n) = n!$   $\therefore c = lag_a = lag_{16} = 2$   $n^c = n^2$ As  $n! > n^2$   $\therefore T(n) = \theta(n!)$ 

911) 4T(n/2) + lag n -, a=4, b=2, f(n)=lagn C = lega . leg 4 = 2 ne = n2 1(n). legn : logn < n2 f(n) (n° T(n): 0 (nc) = 0 (n2) Q12) T(n) 2 squt(n) T(n/2) + logn -, a= In, b=2 C= logo a = log In = 1 log n · · - Legen < leg(n) ,. f(u)>uc T(n) = 0 (f(n)) = 0 (leg (n)) (13) T(n)=3T(n/2)+n  $\rightarrow$  a=3; b=2; f(n)=n $C = log \alpha = log 3 = 1.5849$   $nc = n^{1.5489}$ n< n1.5849 > f(n) < nc T(n) = 0 (n 1.5841) Q14) T(n) = 3T(n/3) + sgrt(n)  $\rightarrow a=3, b=3$ C = lega = leg3 = 1  $n^{c} = n^{2} = n$ As sgut (n) < n f(n) (nc T(n) 20(n)

X

$$g(15) T(n) = 4T(n/2) + n$$
 $\rightarrow a = 4, b = 2$ 
 $C = lag_a = lag_2 = 2$ 
 $h^c = n^2$ 
 $n < n^2$  (for any constant)

 $f(n) < n^c$ 
 $f(n) = 0 (n^2)$ 

$$g_{16}$$
)  $T(n)=3T(n/4)+n \log n$   
 $\rightarrow a=3, b=4, f(n)=n \log n$   
 $C=\log_{b}a=\log_{4}3=0.792$   
 $n^{c}=n^{0.792}$   
 $n^{0.792} < n \log n$   
 $T(n)=0 (n \log n)$ 

$$g_{17}$$
)  $T(n)=3T(n/3)+n/2$   
 $\rightarrow a=3;b=3$   
 $c=laga=lag_3=1$   
 $f(n)=n/2$   
 $n^c=n'=n$   
 $As n/2 < n$   
 $f(n) < nc$   
 $f(n) < nc$   
 $f(n) < nc$   
 $f(n) = 0 < n$ 

$$g_{18}$$
)  $T(n) = GT(n/3) + n^2 \log n$   
 $\rightarrow a = G; b = 3$   
 $C = \log_b a = \log_3 G = 1.6309$   
 $n^c = n^{1.6309}$   
As  $n^{1.6309} \le n^2 \log n$   
 $\therefore T(n) \ge 0 (n^2 \log n)$ 

```
g19) T(n)=4T(n/2) mby + n/loga
 -> a=4,b=2,f(n)=n
  C= loga = log4 = 2 logn
     lagn (n²
     T(n) = 0 (n2)
820) T(n) = 64T(n/8) - n2 logn
-> a=64 b=8
 C = log a = log 64 = log (8)2
    nc = n2
  ... n^2 \log n > n^2
    T(n) = 0 (n2 logn)
(21) T(n)= 7T (n/3)+n2
-> a=7; b=3; f(n)=n2
```

$$\begin{array}{c} g_{21} \\ T(n) = 7T (n/3) + n^2 \\ \rightarrow a = 7; b = 3; f(n) = n^2 \\ C = log_a = log_3 7 = 1.7712 \\ n^c = n^{1.7712} \\ n^{1.7712} < n^2 \\ T(n) = 0 (n^2) \end{array}$$

Do