

Lab-6 8-queens using A* and Hill Climbing Algorithms

1) 8-queens using A*:

Taking $f(x)$ as No. of empty spaces left
 $g(x)$ as No. of queens left to place
 Find state has $h(x) = 0$

~~Calculating functional values: Defining functional~~

1) ~~def emptySpaces(board):
 for i in range(8)
 for j in range(8):~~

Initial Setup:

Assuming an 8×8 array of integers representing the chessboard. 1 indicates queen placed on square, 0 indicates not placed

board = [[0 for _ in range(8)] for _ in range(8)]

Heuristic functional values:

1) ~~def emptySpaces(board):~~ \rightarrow $spaces = 0$
 for i in range(8)
 for j in range(8):
 row-check = set(board[i])
 col-check = set([board[k][j] for k in range(8)])
 diag-indexes = [(k, k+(j-i)) for k in range(8)]
 ~~diag-check =~~ \rightarrow $diag-check = [(k, k+(j-i)) for k in range(8)]$
 for ~~xi~~ i in diag-indexes:
 if $\min(i) < 0$ or $\max(i) > 7$:
 diag-indexes.remove(i)
 ~~diag-check~~ \rightarrow $diag-check = [board[i][0]] [i][7]$
 for i in diag-indexes:
 ~~diag-check~~ \rightarrow $diag-check = set(diag-check)$

```

if lenlen(row-check) == 1 == 1 and lenlen(col-check) == 1 == 1
    and lenlen(diag-check) == 1 == 1:
    spaces += 1
return spaces

```

```

2) def noOfQueensLeft(board):
    for row in board:
        if 1 in row:
            count += 1
    return 8 - count

```

General A* Algorithm:

Step 1: Initialize priority queue

Step 2: Push empty board state into queue

Step 3:

```
def astar(board):
```

```
    queue = []
```

```
    queue.append((board, 0))
```

```
    while queue:
```

```
        queue.append front = queue.pop(0)
```

```
        possible-move if front[1] == 8: return front
```

```
        for i in range(8):
```

```
            new-board = front[0]board[:]
```

```
            new-board[front[1]][i] = 1
```

```
            queue.pop queue.append((new-board, front[1] + 1))
```

```
            queue.sort key = (emptySpaces(x),  
                           noOfQueensLeft(x))
```

```
    return queue[0]
```

```
    if isSafe(board, front[1], i):
```

```
        queue.append((new-board,  
                      front[1] + 1))
```

```
    return
```

~~Process~~

→ Hill Climbing Algorithm:

Initial Setup:

Consider a mathematical expression which we have to attempt to maximise
def cost(x):

return math.cos(x)

```
def hill-climbing(initial-sol = 0, step = 0.01,
                  max-steps = 1000):
```

```
    current = initial-sol
```

```
    best = current
```

```
    for _ in range(max-steps):
```

```
        if neighbour = [current + step,
                        current - step]
```

```
        neighbours.sort(key = lambda x:
                        cost(x))
```

```
        current = neighbour[-1]
```

```
        if best cost(best) > cost(current):
            best = current
            current = best
```

```
        else:
```

```
            break
```

```
    return best
```

→ Initialization Code:

```
initial-sol = random.uniform(-10, 10)
```

```
steps = random.choice(0.01, 0.001)
```

```
print(hill-climbing(initial-sol, steps))
```

crossed

A* output:

Possible solution: (only col no.s)

(0, 4, 7, 5, 2, 6, 1, 3)

Hill Climbing output:

cost function: $\text{math.sin}(x)$

final solution: -4.71634

S
29/10/24