

# Sliding Window Pattern



*Handwritten Notes*

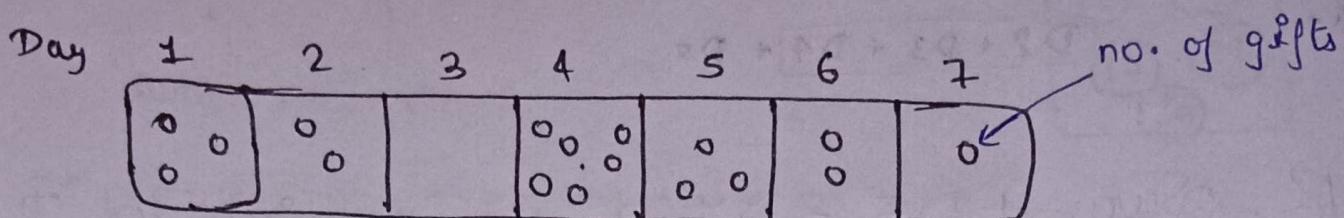
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learned from **CTO Bhaiya**

Day-12

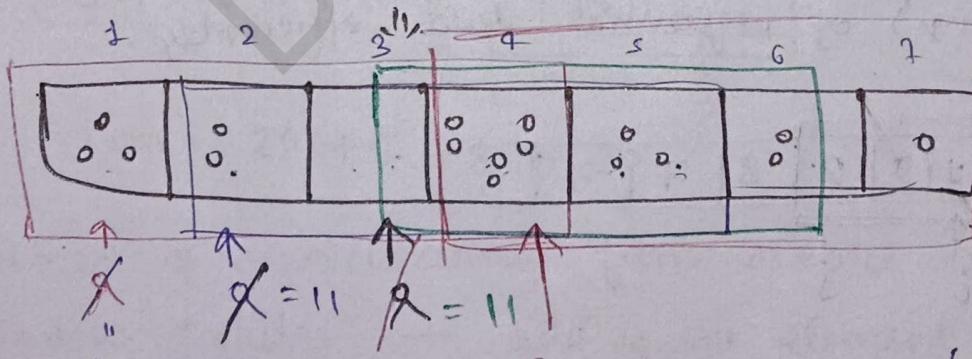
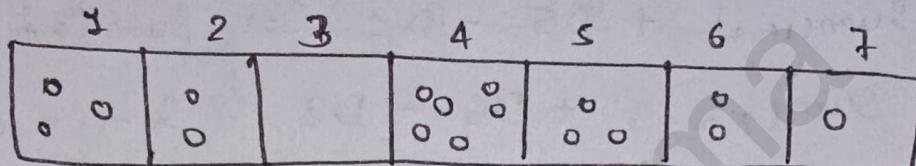
## Sliding Window Pattern

## ( Theory )



Boy ♂ ↑

( girl always ask → How many gift you have given  
to me during b/w 4 day )



$$R = 12$$

$$\text{Max} = 1/12$$

day b/w 4 to 7  
total gift = \$2

( ask in which  
4 days you give  
me max no. of  
gifts )

Problem: Boy check an

$$\begin{array}{l} \text{I. } D_1 + \boxed{D_2 + D_3 + D_4} \\ \text{II. } \boxed{D_2 + D_3 + D_4} + D_5 \end{array}$$

again - again  
calculate,

Iteration: Let

$$I \rightarrow \text{Sum} = D_1 + [D_2 + D_3 + D_4]$$

$$II \rightarrow [D_2 + D_3 + D_4] + D_5$$

$$\cancel{\text{Sum}} + D_5 - D_1 = \text{Total sum of II Iteration}$$

$$\text{Day 1 to 4} \Rightarrow D_1 + D_2 + D_3 + D_4 \Rightarrow \text{Sum}(1 \text{ to } 4)$$

$$\text{Day 2 to 5} \Rightarrow \text{Sum}(1 \text{ to } 4) + D_5 - D_1 \Rightarrow \text{Sum}(2 \text{ to } 5)$$

$$\text{Day 3 to 6} \Rightarrow \text{Sum}(2 \text{ to } 5) + D_6 - D_2 \Rightarrow \text{Sum}(3 \text{ to } 6)$$

$$\text{Day 4 to 7} \Rightarrow \text{Sum}(3 \text{ to } 6) + D_7 - D_3 \Rightarrow \text{Sum}(4 \text{ to } 7)$$

This is Sliding Window Concepts !!!

### → Sliding window Pattern

- A technique used to process contiguous chunks (subarrays or substrings) of sequential data efficiently.

e.g.,

1	9	2	8	7	7	6
i	j					

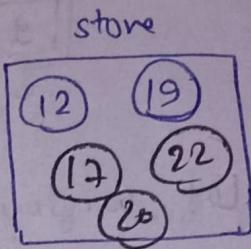
$$\text{sum} = 1 + 9 + 2$$

$$= 12$$

Ex.

1	9	2	8	7	7	6
i	j					

$$\text{sum} = 1 + 9 + 2 = 12$$



→

1	9	2	8	7	7	6
i	j					

$$\text{sum} = 12 + 8 - 1 = 19$$

{ 2 pointers  
on the  
boundary of window

→

1	9	2	8	7	7	6
i	j					

$$\text{sum} = 19 + 7 - 9 = 17$$

→

1	9	2	8	7	7	6
i	j					

$$\text{sum} = 17 + 7 - 2 = 22$$

→

1	9	2	8	7	7	6
i	j					

$$\text{sum} = 22 + 6 - 8 = 20$$

o Instead of recalculating from scratch everytime, the window "slides" — adding one element & removing an old element, so each update happen in constant time.

4	9	8	8	7	1	7	6
i		j					

Let window size =  $n/2$

So, in first iteration, i runs  $(n/2)$  times  
then  $j++$

in II iteration i runs  $(n/2)$  time

Brute Force

$$(n/2) \times (n/2) \Rightarrow TC = O(n^2)$$

But, In sliding window:

first sum calculate  $\rightarrow$  time =  $n/2$

and then,  $j++$  and  $j++$  one by one by  $(n/2)$

$$\frac{n/2 + n/2}{2} \Rightarrow TC \Rightarrow O(n)$$

→ Use two pointers (start, end) to represent the current window boundaries

As the window slides across the data:

- Add the new element that enters the window
- Remove the element that leaves the window

## Types of Sliding Window

### ① Fixed-size Window

- Window size K is constant
- Both pointers move together, maintaining a fixed distance
- Used when the number of consecutive elements is fixed (e.g. sum of three numbers).

Eg, Max<sup>n</sup> Sum of Subarray of size K=3

Brute Force

I.

0	1	2	3	4	5
2	1	5	1	3	2

$i \uparrow \quad j \uparrow \quad \uparrow$

Max =  $\emptyset$  8  
sum =  $2+1+5 = 8$

II.

0	1	2	3	4	5
2	1	5	1	3	2

$i \uparrow \quad j \uparrow \quad \uparrow$

Max = 8  
sum =  $1+5+1 = 7$

III.

0	1	2	3	4	5
2	1	5	1	3	2

$i \uparrow \quad \uparrow \quad \uparrow \quad j$

Max = 9  
sum =  $5+1+3 = 9$

Code

$$\max = 0$$

$$K = 3$$

for ( $i = 0$ ;  $j < n - K$ ;  $i++$ ) {

$$\text{sum} = 0$$

    for ( $j = i$ ;  $j <= i + K - 1$ ;  $j++$ ) {

$$\text{sum} = \text{sum} + \text{arr}[j]$$

}

$$\max = \text{MAX}(\max, \text{sum})$$

}

return max

'i' Kaha tak jaayega ?

0	1	2	3	4	5
2	1	5	1	3	2

$$\text{bcz, } K = 3$$

$$\text{So, } n = 6$$

$$K = 3$$

$$\therefore 6 - 3 = 3 = \text{index of last } i$$

$$\therefore [n - K]$$

'j' Kaha tak jaayega ?

0	1	2	3	4	5
2	1	5	1	3	2

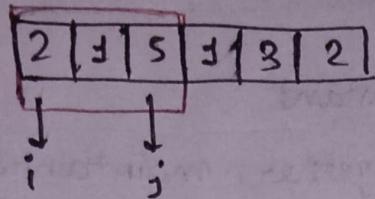
$$i = 3, j = 3 \quad \text{he searched to } 5^{\text{th}}$$

$$3 + 3 = 6 - 1 = 5 \quad \text{index}$$

$$\therefore [i + k - 1]$$

optimized

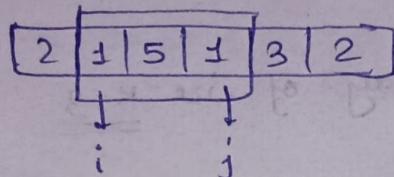
Max<sup>n</sup> sum of subarray of size K=3



$$\text{sum} = 8 \rightarrow \text{Max} = 8$$

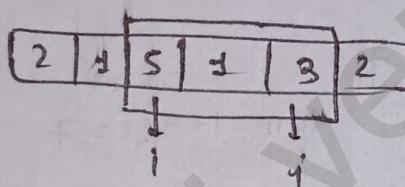
$i++$   
 $j++$

Next

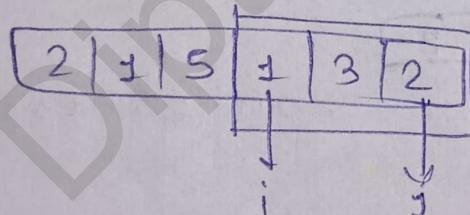


$$\text{sum} = 8 + \text{arr}[j] - \text{arr}[i-1]$$

$$= 8 + 1 - 2 = 7 \rightarrow \text{Max} = 8$$



$$\text{sum} = 7 + 3 - 1 = 9 \rightarrow \text{Max} = 9$$



$$\text{sum} = 9 + 2 - 5 = 6$$

$\Rightarrow \boxed{\text{Max} = 9}$

Code:

max = 0

sum = 0

K = 3

i = 0

for (j=0 ; j < k ; j++) {

    sum = sum + arr[j]

}

    max = Max(max, sum)

while (j < n):

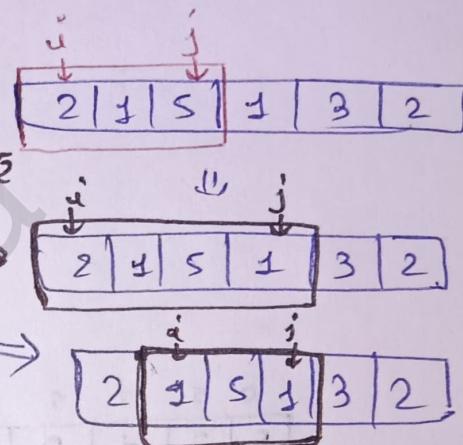
    sum = sum + arr[j] ~~else~~

    sum = sum - arr[i]

    i++

    j++

max = MAX(max, sum)



[TC = O(n)]

return max

②

## Dynamic (Variable-size) Window

- Windows expand or contract based on conditions
- Common for problems like:
  - Longest substring without repeating characters
  - Smallest subarray with sum  $\geq$  target.

Eg Smallest subarray with sum  $\geq$  target

target = 7

Brute force

0	1	2	3	4	5
2	3	1	2	4	3

i j i j i j

start =

$$S = 2 + 3 = 5 + 1 = 6 + 2 = 8 > \text{target}$$

$$\text{Sum} = 8$$

$$\text{size} = (j - i + 1) = (3 - 0 + 1) = 4$$

$$\min\_size = \min(\min, \text{size}) = 4$$

0	1	2	3	4	5
2	3	1	2	4	3

i j i j i j

$$S = 0 + 3 + 1 + 2 + 4 + 2 = 6 + 4 = 10 > 7$$

$$\text{size} = 4$$

2	3	1	2	4	3
9	9	9	9	9	9

$$S = 0 + 1 + 2 + 3 + 4 = 7$$

$$\text{size} = 3$$

$$\min\_size = 3 \rightarrow \text{sum} = 7$$

2	3	1	2	4	3
---	---	---	---	---	---

i j i j i j

$$\text{sum} = 2 + 3 + 1 = 6$$

$$\text{size} = 3$$

Code:

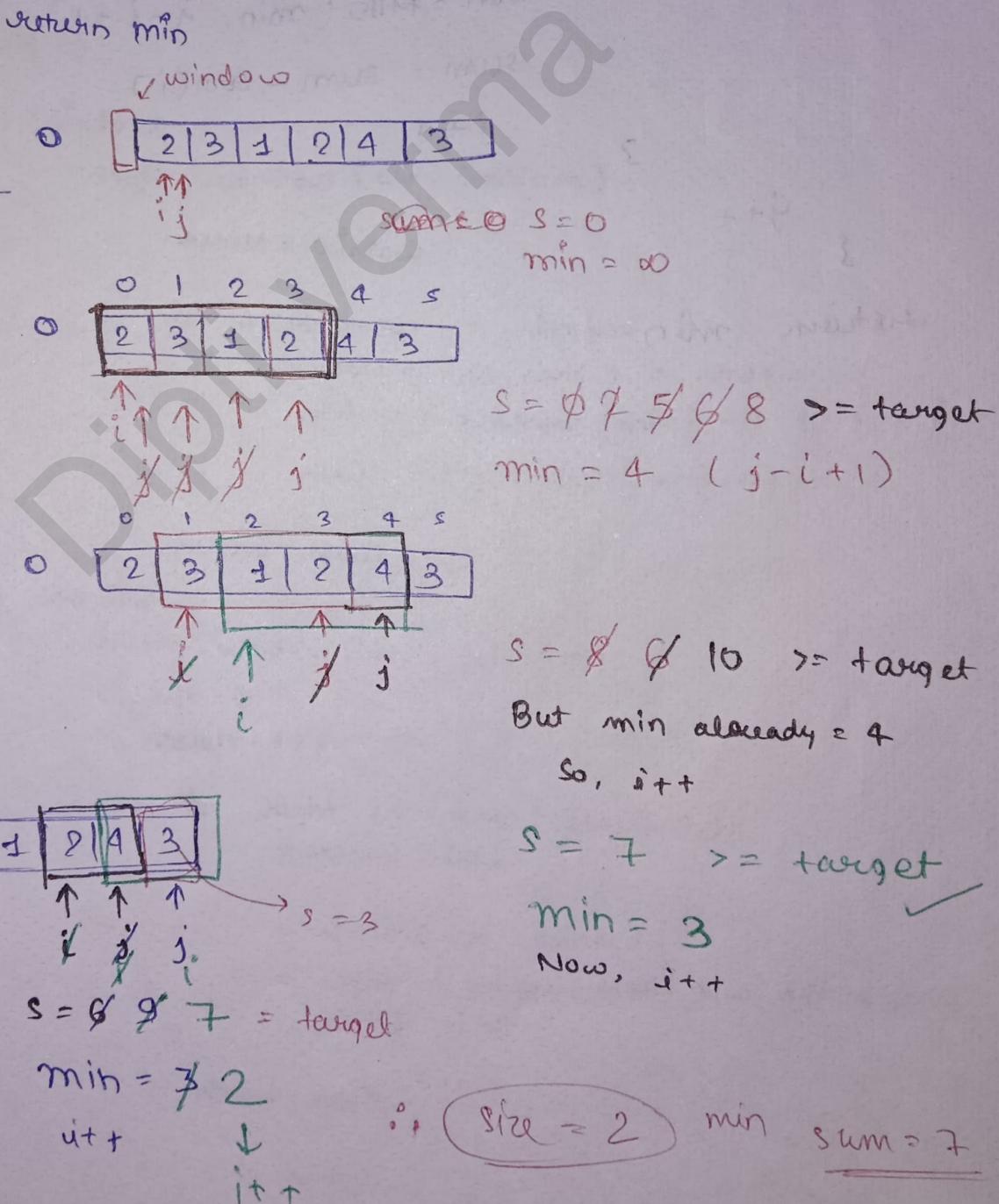
```

min = infinity
target = 7
for (i=0 ; i<n; i++) {
    break
    sum = 0
    for (j=i ; j<n; j++) {
        sum = sum + arr[j]
        if (sum >= target) {
            min = MIN(min, j-i+1)
            break
        }
    }
}
return min

```

Optimized

target = 7



code:

$\min = \text{infinity}$

$\text{target} = 7$

$\text{sum} = 0$

while ( $j < n$ ) {

$\text{sum} = \text{sum} + \text{arr}[j]$

while ( $\text{sum} \geq \text{target}$ ) {

$\min = \text{MIN}(\min, j - i + 1)$

$\text{sum} = \text{sum} - \text{arr}[i]$

$i++$

$j++$

}

return  $\min$

$\text{target} = 5$

$\text{target} = 0$

$\Rightarrow \min = 0$

$+ 7 = 0$

## → Identify Sliding Window

- The input is contiguous (array / string)
  - Question says "subarray" or "substring"
- def
- I. Try Brute Force
  - II. Check the condition of "Brute Force", convert into Sliding window or not.
- Asked for max/min/count with a contiguous range
  - You can express the problem as "window slides one step" each iteration

## ⇒ Template

### ◦ Fixed Window

sliding-window (arr, condition) :

result = window

for i in range (K, len(arr)):

window = add arr[i] to window

window = subtract arr[i-K] from window

result = best (result, window)

return result

### ◦ Dynamic Window

sliding - window ( arr, condition ) :

left = 0

result = ???

for right in range (len(arr)):

# expand window

while condition satisfied :

result = process result b/w left & right  
Shrink window

return result

Day-13

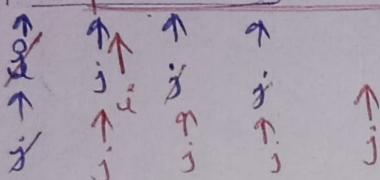
## Sliding Window Pattern

(Medium Level Question)

- Max sum subarray of size K (GFG)
- 2461. Max sum of Distinct Subarrays with length k (LC)
- 209. Min<sup>m</sup> size subarray sum (LC)

### Q. Max Sum Subarray of size K

Ex, [1, 4, 2, 10], 23, 3, 5, 0, 20]  $K=4$



$$\text{sum} = 1 + 4 + 2 + 10 = 17 \quad \text{sum} = 4 + 2 + 10 + 23 = 39$$

$$\text{Max} = \emptyset / 39$$

$$TC = O(n^2)$$

What we have observe?

$$\text{I. sum} = 1 + [4 + 2 + 10]$$

$$\text{II. sum} = [4 + 2 + 10] + 23$$

repeat the  
calculation

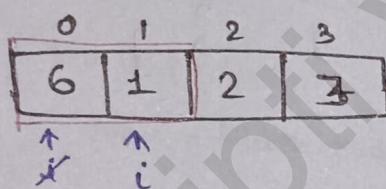
Optimized [ We get it as:  $(\underline{1+4+2+10}) + \underline{23} - \underline{1} = \text{II. sum}$  ]

Code :

```
public int maxSubarraySum( int arr[], int k) {  
    int sum=0, max=0;  
  
    for( int i=0; i<k; i++) {  
        sum = sum + arr[i];  
    }  
    max = Math.max( max, sum);  
  
    for( int i=k; i<arr.length; i++) {  
        sum = sum + arr[i];  
        sum = sum - arr[i-k];  
        max = Math.max( max, sum);  
    }  
    return max;  
}
```

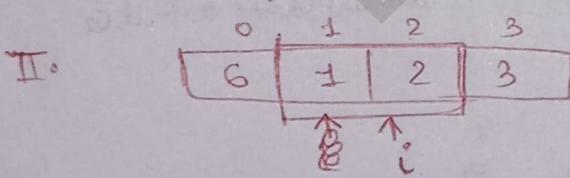
$$TC = O(K + K-1)$$

$\therefore \boxed{TC = O(n)}$   
 $SC = O(1)$



$$K=2$$

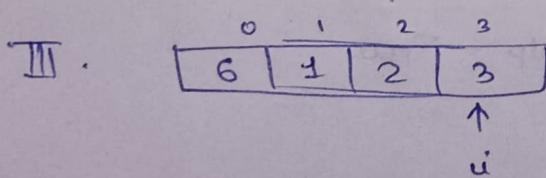
I.  $sum = \emptyset \oplus \boxed{7}$   
 $max = \emptyset \oplus \boxed{7}$



$$sum = 7 + 2 = 9$$

$$sum = 9 - arr[i-K] = 9 - 6 = 3$$

$$max = 7$$



$$sum = 3 + 3 = 6$$

$$sum = 6 - arr[i-K] = 6 - 1 = 5$$

$$max = 7$$

Ans = 7

## Q.(24G1) Max Sum of Distinct Subarrays with length K

num = [ 1, 2, 4, 2, 9, 9, 9 ]       $K = 3$

Valid

1 2 4	✓	{
2 4 2	✗	
4 2 9	✓	
2 9 9	✗	
9 9 9	✗	

[1 2 4]      [4 2 9]

sum = 7      sum = 15  
(Max)

### Brute Force

Ex,    [ 1, 2, 4, 2, 9, 9, 9 ]

I. Set = {1, 2, 4}  $\rightarrow$  No duplicate      inDulp = False  
 sum = 7  $\neq$  3  $\textcircled{7}$

Ex,    [ 1, 4, 4, 2, 9, 9, 9 ]

Set - [1, 4]      ✓ '4' already  $\rightarrow$  inDulp = True  
 sum = 5  $\neq$  7

max = 0

Check (inDulp = True) {

ignore

## Code:

```
public long maximumSubarraySum( int num[] , int k ) {  
    long max = 0 , sum = 0 ;  
    int n = num.length ;  
    for ( int i = 0 ; i <= n - k ; i++ ) {  
        Set< Integer > set = new HashSet<>();  
        boolean inDup = false  
        sum = 0 ;  
        for ( int j = i ; j <= i + k - 1 ; j++ ) {  
            if ( set.contains( num[j] ) ) {  
                inDup = true  
                break  
            }  
            set.add( num[j] )  
            sum = sum + num[j]  
        }  
        if ( ! inDup )  
            max = Math.max ( max , sum )  
    }  
    return max  
}
```

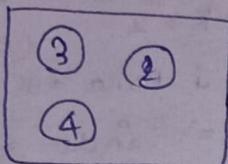
0 1 2 3 4  
⇒ 1 2 3 4 5  
K = 2 (end)  
i Kaha tak ga?  
⇒ index = 3  
n = 5  
and k = 2  
∴ ~~n~~  $n-k$

$$TC = O(n^2)$$
$$SC = O(n)$$

## Optimized

$\text{num} = [3, 2, 4, 3, 4, 3, 9]$   $K=4$

- Set



present  $\rightarrow$  invalid

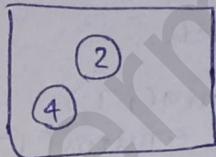
$$S = 12$$

$\max \Rightarrow$  no update  
(bcz. of dup)

- 3 remove and 4 add

[2, 4, 3, 4]

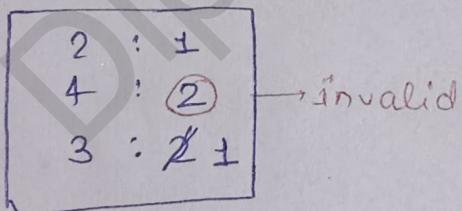
$\rightarrow$  remove '3' from set



but window  
show '3'

$\rightarrow$  and we delete ③

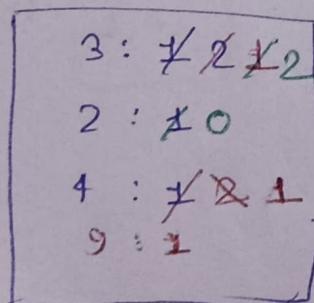
that's why we use Map, not set



Now, use Map:

$\text{num} = [3, 2, 4, 3, 4, 3, 9]$   $K=4$

- 0



Ex.  $[3, 2, 4, [3, 4], 3, 9]$  K = 4

Map

3 : ~~2~~ ~~2~~

2 : ~~0~~

4 : ~~1~~ ~~1~~

9 : 1

$$S = 3 + 2 + 4 + 3 = 12$$

Max = No update (~~3:2 (dup)~~)

$$S = 12 + 4 - 3 = 13$$

Max = No update (4:2 (dup))

$$S = 13 + 3 - 2 = 14$$

Max = X (3:2)

$$S = 14 + 9 - 4 = 19$$

Max = X (3:2)

In this case:

We check the whole map again & again

$$\Rightarrow \underline{TC = O(n^2)}$$

\* How to optimised this map case? \*

Ex.  $[T, T, P, P]$

T : ~~2~~

P : ~~2~~

$T=2 > 1 \rightarrow \text{duplicate} = \emptyset$

$P=2 > 1 \rightarrow \text{duplicate} = \not 2$

-~~Opt.~~ in one window  $\Rightarrow \underline{\text{dup} = 2}$

eg. same  
In cases  $t \leq S$   
 $t < S$   
 $t > S$   
- max  
-- pos

E : E

★  $\text{num} = [3, 2, 4, 3, 4, 3, 9]$   $k=4$

I: Map:

- $\boxed{3 : 1}$

- Check count of 3:

$$1 = 1 \rightarrow \text{dup} = 0$$

- then, traverse  $i$  to 4 times

$\begin{matrix} 3 & 2 & 4 & 3 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ i & i & i & i \end{matrix}$	$\left[ \begin{array}{l} 3 : \cancel{1} \text{ } 2 \\ 2 : 1 \\ 4 : 1 \end{array} \right] \rightarrow \text{dup} = 1$
---	--

$$\text{sum} = 12$$

$$\text{max} = \text{no update} = 0$$

II: add 4 and remove 3

$\text{num} = [3, \boxed{2, 4, 3, 4}, 3, 9]$

$3 : \cancel{1}$
$2 : 1$
$4 : \cancel{2}$

- add 4 (freq)

$$\rightarrow \text{duplicate} = \cancel{2}$$

- remove 3

$$\rightarrow 3 \Rightarrow \text{count} = \cancel{2}$$

$$2 > 1$$

$$\text{duplicate} = \cancel{1}$$

freq --

$$\rightarrow 3 : 1$$

So, dup = 1  
 sum = 13  
 max = 0

III. num = [ 3, 2, 4, 3, 4, 3, 9 ]

• add 3

3 : 1	2
2 : 1	
4 : 2	

→ dup = 1

• remove 2

3 : 2	
2 : 0	
4 : 2	

→ dup = 2

sum = 14

max = 0

IV. num = [ 3, 2, 4, 3, 4, 3, 9 ]

• add 9

3 : 2	
2 : 0	
4 : 2	
9 : 1	

→ dup = 2

sum = 19

• remove 4

3 : 2	
4 : 1	
9 : 1	

→ dup = 1

sum = max = 0

V. num = [ 3, 2, 4, 3, 4, 3, 9, 6 ]

• add 6

3 : 2	
4 : 1	
9 : 1	
6 : 1	

→ dup = 1

• remove 3

3 : 1	
4 : 1	
9 : 1	
6 : 1	

→ dup = 0

sum = 19 + 6 - 3 = 22

max = 22

## Code:

```
public long maximumSubarraySum( int num[], int k ) {
    long sum = 0, max = 0;
    Map< Integer, Integer > counts = new HashMap<>();
    int dups = 0;

    for ( int i = 0; i < k; i++ ) {
        if ( ! map.containsKey( num[i] ) ) {
            map.put( num[i], 0 )
            3
            map.put( num[i], map.get( num[i] ) + 1 )
            sum = sum + num[i];
        } else if ( map.get( num[i] ) > 1 ) {
            dups = dups + 1
            3
        }
        if ( dups == 0 ) {
            max = Math.max( max, sum );
            3
        }
    }

    for ( int i = k; i < num.length; i++ ) {
        int numToAdd = num[i];
        int numToRemove = num[i - k];

        if ( ! map.containsKey( numToAdd ) ) {
            map.put( numToAdd, 0 )
            3
            map.put( numToAdd, map.get( numToAdd ) + 1 )
```

if( map.get( numToAdd ) > 1 ) {

    dups = dups + 1

}

    sum = sum + numToAdd

TC = O(n)

SC = O(n)

if( map.get( numToRemove ) > 1 ) {

    dups = dups - 1

}

    map.put( numToRemove, map.get( numToRemove ) - 1 )

    sum = sum - numToRemove

if( dups == 0 ) {

    maxSum = Math.max( sum, max )

}

3

return max

3

## $\Theta(209)$ . Min Size Subarray Sum

Eg target = 7

nums = [ 2, 3, 1, 6, 4, 3 ]

Brute force pattern always help to recognise the sliding window pattern.

Brute Force

[ 2, 3, 1, 6, 4, 3 ]

$\downarrow$

i  
j

$$TC = O(n^2)$$

$$SC = O(1)$$

I. [ 2, 3, 1, 6, 4, 3 ]

$\uparrow$   
i   i   i   j

$j=3$   
~~length = 6~~  
 $i=0$

$$S = 12 > \text{target}$$

$$\cancel{\text{size} = 6 - 3 + 1} \quad \text{size} = 4 \quad \text{size} = j - i + 1$$

II. [ 2, 3, 1, 6, 4, 3 ]

$\uparrow$   
i   i   i   j

$j=3$   
 $i=1$   
~~length = 6~~

$$\text{size} = 3 - 1 + 1$$

~~$S = 8 - 1 + 1$~~   
 $S = 10 > \text{target} = 3$   
 $\text{size} = 3$

III. [ 2, 3, 1, 6, 4, 3 ]

$\uparrow$   
i   i   j

$$S = 7 = \text{target}$$

$$\text{size} = 2$$

IV. [ 2, 3, 1, 6, 4, 3 ]

$\uparrow$   
i   j

$$S = 10 > \text{target}$$

$$\text{size} = 2$$

V. [ 2, 3, 1, 6, 4, 3 ]

$\uparrow$   
i   j

$$S = 7 = \text{target}$$

$$\text{size} = 2$$

VI. [ 2, 3, 1, 6, 4, 3 ]

$\uparrow$   
i   j

Stop.

Observations:

→ i loop stop →  
on a condition if  
'i' value  $\geq$  target hai  
toh stop  
bcz, bade no. min add  
karne pe bada hi hoga.

→ size value =  $j - i + 1$

→ Recognise: How sliding window applied?

Break condition → if ( $\text{sum} \geq \text{target}$ ) {

$\min = \text{Math.min}(\min, j-i+1)$

break;

$$\underline{\underline{[2, 3, 1, 6, 4, 3]}}$$

$$S = 2 + \boxed{3 + 1 + 6}$$

$$S = \boxed{3 + \boxed{1 + 6}}$$

$$S = \boxed{1 + 6}$$

\* Calculation

redundant (again-again)

What we do

- Sum get  $\rightarrow$  break  
 $i++$
- again calculate

In sliding window:

- Sum get  $\rightarrow$  remove one item & add one item

same

$$[2, 3, 1, 6, 4, 3]$$

$\overset{\uparrow}{i} \cdots \cdots \cdots \overset{\downarrow}{j}$

$$[2, 3, 1, 6, 4, 3]$$

$\overset{\uparrow}{i} \quad \overset{\uparrow}{j}$

$$S = 12 > \text{Target}$$

$$\text{Size} = 4$$

$$[2, 3, 1, 6, 4, 3]$$

$\overset{\uparrow}{i} \quad \overset{\uparrow}{j}$

$$S = 12 - 2 = 10 > \text{Target}$$

$$\text{Size} = 3$$

$$[2, 3, 1, 6, 4, 3]$$

$\overset{\uparrow}{i} \quad \overset{\uparrow}{j}$

$$S = 10 - 3 = 7 = \text{target}$$

$$\text{size} = ?$$

$$S = 7 - 1 = 6$$

$$S = 6 + 4 = 10 > \text{target}$$
$$\text{size} = 2$$

$$[2, 3, 1, 6, 4, 3]$$

$\overset{\uparrow}{i} \quad \overset{\uparrow}{j}$

$$S = 10 - 6 = 4$$

$$S = 4 + 3 = 7 = \text{target}$$

$$\text{size} = 2$$

$$\therefore \text{Answer} = 2$$

### Brute Force :

Code

```
sum = 0
min = Integer.MAX_VALUE

for ( i=0 ; i < num.length ; i++ ) {
    sum = 0
    for ( j=i ; j < num.length ; j++ ) {
        sum += num[j]
        if ( sum >= target ) {
            min = Math.min( min, j-i+1 )
            break
        }
    }
    return min == Integer.MAX_VALUE ? 0 : min;
}
```

### Sliding Window :

Code

TC = O(n)  
SC = O(1)

```
size = Integer.MAX_VALUE
sum = 0
i = 0, j = 0

while ( j < num.length ) {
    // expand window
    sum = sum + num[j]

    while ( sum >= target ) {
        size = Math.min( size, j-i+1 )
        sum = sum - num[i]
        i++
    }

    j++
}

return min == Integer.MAX_VALUE ? 0 : size
```

Day-14

## Sliding Window Pattern

(Med level Ques)

219. Contains Duplicate II (<sup>easy</sup>~~medium~~) LC

643. Max Average Subarray I (<sup>easy</sup>~~medium~~) LC

3. Longest substring without repeating characters (medium) LC

### Q. (219) Contains Duplicate II

Eg  $\text{num} = [1, 2, 3, 4, 2]$   $K=3$

olp = True

$\begin{bmatrix} 0 & 1 & 2 & 3 & 4 \\ 1, & 2, & 3, & 4, & 2 \end{bmatrix}$

$\text{num}[i] = 1$

$\text{num}[j] = 4$

no any dup

$\text{num}[i] = 2$   
 $\text{num}[j] = 2$

$\checkmark \rightarrow \text{True}$

Condition

$\text{num}[i] = \text{num}[j]$

$|i-j| \leq K$

Boundary

### Brute Force

$\bullet [0, 1, 2, 3, 4]$

(let)

$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

no dup

$\bullet [1, 2, 3, 4, 2]$

$\begin{bmatrix} 2 & 3 \\ 4 \end{bmatrix}$

already have  
→ dup

return True

Code :

```
for( i=0 ; i < num.length ; i++ ) {
```

```
    Set<Integer> set = new HashSet<>();
```

```
    for( j=i ; j <= (i+k) ; j++ ) {
```

if( set.contains( num[j] ) ) { error bcz  
of constraint }

```
    return true
```

$0 \leq K \leq 10^5$

3

```
    set.add( num[j] )
```

3

```
return false
```

TC =  $O(n^2)$   
SC =  $O(n)$

So, change condn!

CS :  $j \leq \min(i+k, \text{nums.length}) - 1$

e.g.  $i+k = 32$

length of array = 5

### Optimization

e.g. [ 1, 2, 3, 4, 2 ]       $K = 2$

( 1, 2, 3, 4 ) + ( 2, 3, 4, 2 ) ] Window concept

fixed slider

Let's check, fixed size window concept fitted or not  $\Rightarrow$

- O  $[1, 2, 3, 4, 2]$   $K = 3$

set

1	2
3	

$$\text{abs } |j - i| \leq K$$

You have to check  
4 elements at  
a time

But  
here  $= 3$

$$(0 - 3) \leq 3$$

$$= \text{size} = 4$$

so,

- $\Rightarrow [1, 2, 3, 4, 2], K = 3$

$j.$

then, what we do in fixed size  $\Rightarrow i = K \rightarrow$  then check

- $[1, 2, 3, 4, 2]$

$i$

check ④ in in set or not

$\rightarrow$  that means window  $\Rightarrow \text{size} = 4$  (4 elements  
process at a  
time)

1	4
3	2

- O Now, add and remove element

- $[*, 2, 3, 4, 2]$

$i$

$j$

$\Rightarrow$  check ② in in set or not

• Yes

• True

*	4
2	3

Code:

```
Set<Integer> set = new HashSet<>()
```

```
for (i=0; i < Math.min(k, num.length); i++) {
```

```
    if (!set.contains(num[i])) {
```

```
        return true
```

```
}
```

```
    set.add(num[i])
```

```
}
```

$$TC = O(n)$$

$$SC = O(n)$$

```
for (i=k; i < num.length; i++) {
```

```
    if (!set.contains(num[i])) {
```

```
        return true
```

```
,
```

```
    set.add(num[i])
```

```
    set.remove(num[i-k])
```

```
}
```

return false

e.g.,      0    1    2    3  
             ↓    ↓    ↓    ↓  
0    1    2    3    1

K = 2

ret = [1, 2]

then, [1    2    3    1 ]

↓  
i

ret = [1, 2, 3]

remove 1

ret = [2, 3]

0    1    2    3    1  
↓

ret = [2, 3]

add 1

~~remove~~

remove = 2

ret = [3, 1]

→ False

On this  
eg, duplicate  
is present ←  
but on In the  
range of  
 $\text{abs}(j-i) \leq k$

## Q (643) Maximum Average Subarray I

Eg,  $\text{num} = [1, 12, -5, -6, 50, 3]$   $K=4$

(Which 4 nos. have average num in Max)

Max' Subarray sum

concept =

Max Average subarray

How?

$K=2$

[1 2 3 4] 2

Max sum = [3, 4]

= 7

Max avg =

$$7/2 = 3.5 \text{ Max}$$

Max sum = Max Avg

[1, 12, -5, -6, 50, 3]

first 4 elements =  $\frac{1+12-5-6}{4} = 0.5$

$$\frac{51}{4} = 12.75$$

$$\frac{42}{4} = 10.50$$

$$\text{Max} = \underline{\underline{12.75}}$$

Brute Force

num = 0  
max = 0

[1, 12, -5, -6, 50, 3]

$$\text{sum} = 1 + 12 - 5 - 6 = 2$$

$$\text{max} = 2$$

$$\rightarrow \text{max} = \frac{51}{4} = \underline{\underline{12.75}}$$

## Optimized

- $\text{num} = [3, 12, -5, -6, 50, 3] \quad k=4$   
 $\downarrow$   
i is pointing to max element in array

$$\text{sum} = \emptyset \neq 13 \otimes 2$$

$$\max = \emptyset 2$$

- $[3, [12, -5, -6, 50], 3]$   
 $\downarrow$   
i

$$\text{sum} = 2 52 51$$

$$\max = 2 51$$

- $[3, [12, [-5, -6, 50, 3]]]$   
 $\downarrow$   
i

$$\text{sum} = 51 54 42$$

$$\max = 51$$

Now,  $\frac{\max}{4} = 12.75 //$

## Code 11 :

double max = 0, sum = 0

for (int i=0; i<k; i++) {

3

sum = sum + num[i]

$$TC = O(n)$$

$$SC = O(1)$$

max = Math.max(max, sum) - sum

for (int i=k; i<num.length; i++) {

// expand window

sum = sum + num[i]

// contract window from left

sum = sum - num[i-k]

max = Math.max(max, sum)

3

return max/k

Error of case : num = [-1] and k = 1

expected  $\Rightarrow -1.0000$

o/p get  $\Rightarrow 0.0000$

Why,

bcz. of max = Math.max(max, sum)

Update :

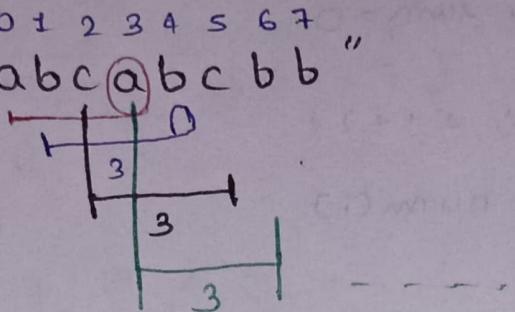
max = sum

Learn how we update max once.

## Q (3) Longest Substring, Without Repeating Characters

Eg  $s = "abc@abcbb"$

len = 3



### Brute Force

max = 0

for ( i=0 ; i < s.length() ; i++ ) {

    Set<Character> set = new HashSet<()>

    for ( j=i ; j < s.length() ; j++ ) {

        char c = s.charAt( j )

        if ( set.contains( c ) ) {

            break

        set.add( c )

    max = Math.max( max, j-i+1 )

}

}  
return max

TC = O(n<sup>2</sup>)

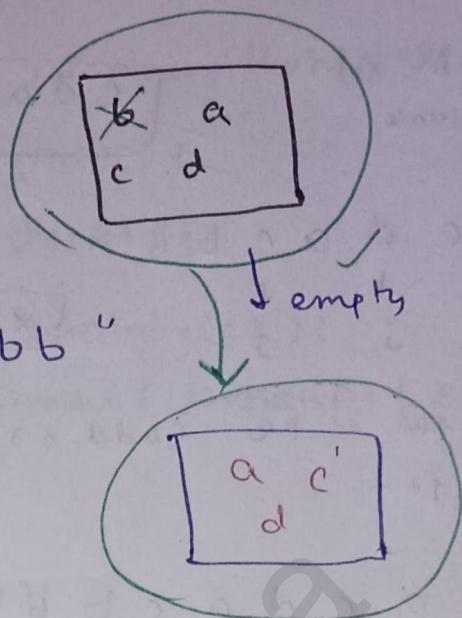
SC = O(n)

Optimized

#dynamic - window

o  $s = "bacdaca\text{bb}"$

i i i i i



repeating char  
add in  
ret

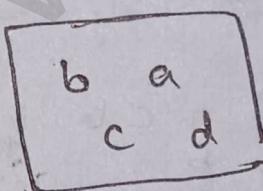
↓  
redundant  
↓  
sliding  
window

o  $s = "bacdaca\text{bb}"$

i i i i

o  $s = bacda\text{c}\text{bb}$

i i i i i



$G_{\max}^{(\text{len})} = 284$

o  $s = bacdaca\text{c}\text{bb}$

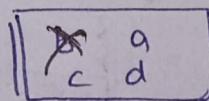
i j

same (no, again add  $\rightarrow$  deleted)

remove 'b'

• Check again 'a' in ret  
→ Yes

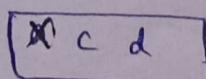
j++



o  $s = \overset{0}{b} \overset{1}{a} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{c} \overset{6}{b} \overset{7}{b}$

remove 'a'

• check 'a' → No



No  $\text{len} = j - i = 2$

→  $\max = 4$

•  $s = b a c d a c b b$

$\downarrow$   
 $i$        $\downarrow$   
 $j$

$\rightarrow c$  in set  
break

cda

•  $s = b a c d a c b b$

$\downarrow$   
 $i$        $\downarrow$   
 $j$

\* da

$\rightarrow c$  in set  $\rightarrow$  No (add c)

~~i++~~  $i++$

$s = b a c d a c b b$

$\downarrow$   
 $i$        $\downarrow$   
 $j$

$\rightarrow b$  in set  $\rightarrow$  No (add b)

$i++$

len = 4

\* d a c b

$s = b a c d a c b b$

$\downarrow$   
 $i$        $\downarrow$   
 $j$

b in set  $\rightarrow$  Yes

$i++$

d a c b

•  $s = b a c d a c b b$

$\downarrow$   
 $i$        $\downarrow$   
 $j$

\* d a c b

'remove' d'

check 'b' in set  $\rightarrow$  Yes,  
again if +

Code :

max = 0

i = 0, j = 0

Set<Character> set = new HashSet<>()

while (j < s.length()) {

char c = s.charAt(j)

while (set.contains(c)) {

set.remove(s.charAt(i))

i++

}

set.add(c)

max = Math.max(max, j - i + 1)

j++

}

return max

TC = O(n)

SC = O(n)

Day - 15

## Sliding Window Pattern

(Rabin Karp Algo)

187. Repeated DNA Sequences    Leetcode    ~~Medium~~ (Medium)

- DNA sequence composed of 'A', 'C', 'G' and 'T'

Eg, "ACGAATTCCG"

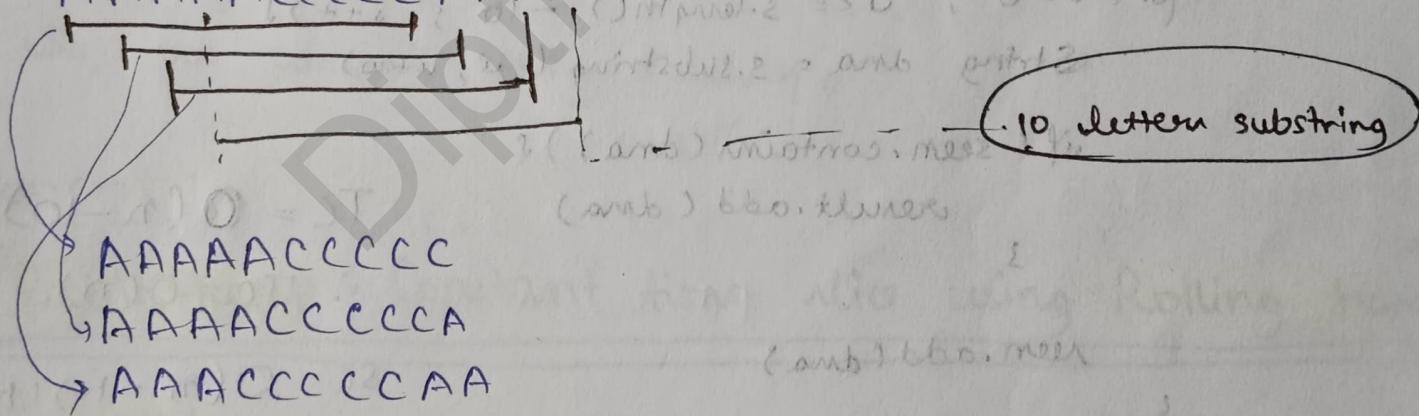
- Repeated sequences

- return all the **10-letter** long sequences that occur more than once in a DNA molecule.

Eg, "AAAAAACCCCCCAAAAAACCCCCAAAAAGGGTTT"  
some (repeated)

→ O/p = "AAAAACCCCC" and "CCCCCAAAAA"

Eg, "AAAAACCCCCAAAAACCCCCAAAAAGGGTTT"

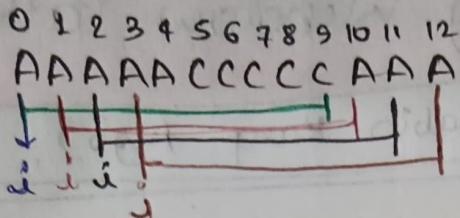


Logic:

0 1 2 3 4 5 6 7 8 9 10 11  
"AAAAACCCCCAAAAACCCCCAAAAAGGGTTT"

- $s.substring(i, i+10)$  → inclusive → substring from(index 0 to 9)
- Check the string contain in set  
if it already in set, then add in result ~~set~~ set

$\Rightarrow$   $i$  kaha tak jayega?



In this case,  $i$  moves 0 to 3

We have,

$$\text{length} = 13$$

$$\text{size} = 10 \text{ (window)}$$

Same chahiye.  $i$  moves to '3' but no matter

$$i = 0$$

$$i \leq (\text{length} - \text{size})$$

Code: `Set<String> seen = new HashSet<>();`

`Set<String> result = new HashSet<>();`

`for (i = 0; i <= s.length() - 10; i++) {`

`String dna = s.substring(i, i+10)`

`if (!seen.contains(dna)) {`

`seen.add(dna)`

$3$

$$TC = O(n-10)(10)$$

$$\therefore TC = O(n)$$

`seen.add(dna)`

$3$

$$SC = O(n-10)(10)$$

$$\therefore SC = O(n)$$

`return new ArrayList<String>(result)`

## Optimized

$S = "AAAAA CCCCC AAAAA CCCC AAAAA GGG TTT"$

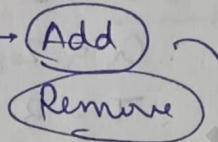
~~Without using extra space~~

AAAAA CCCC ↳ repeated calculation

AAAACCCCCA

(use sliding window as):

$$\begin{aligned} & \text{AAAACCCC} + A - A \\ &= \text{AAAACCCCCA} \end{aligned}$$

★ We have string →  give new string

So, we don't have constant time on these operations  
bcz of string.

So, we convert string → ??

Concept:

Rabin-Karp : Constant time slice using Rolling Hash

Prerequisites :

Base 10 → means no. bin to 10 to 3

Eg. 950

320

329

4 digit →

0000 - 9999

0368

3980

9210

Unique (each digit in a no. are unique)

→ Relate this with DNA sequence:

DNA → 10 len  
which only have 4 characters

A, C, G, T

Let,

Base 4 → 0, 1, 2, 3

Assume A = 0

C = 1

G = 2

T = 3

Eg,

AACG → 0012

mean, all length of string represent in no.

As we know, Binary to Decimal

$$(\text{binary no}) \quad 101 = 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 = 5 \quad (\text{decimal no.})$$

So, For Base 4

AACG → 0012

$$\begin{array}{r} 0012 \\ 4^3 \ 4^2 \ 4^1 \ 4^0 \\ \hline = 6 \end{array}$$

AACG = 6 (this string represent with unique value)

Ex. AACGAC

We know,

$$AACG = 6$$

$A \rightarrow 0$
$C \rightarrow 1$
$G \rightarrow 2$
$T \rightarrow 3$

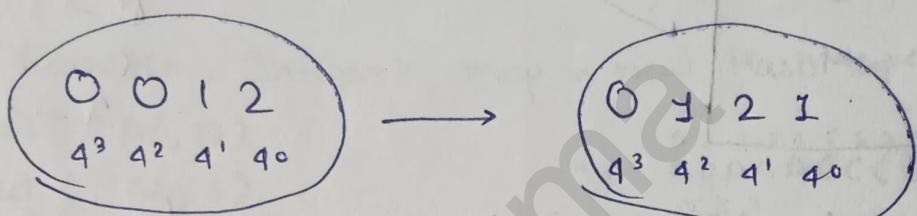
We want,

$$AACG + C - A = ACCGC$$

So

Before : AACG (0012)

After : ACCGC (0121)



Let

$$\begin{array}{l} a \ b \ c \ d \\ 0 \ 0 \ 1 \ 2 \\ \hline 4^3 \ 4^2 \ 4^1 \ 4^0 \end{array}$$

$$\begin{array}{l} b \ c \ d \ e \\ 0 \ 1 \ 2 \ 1 \\ \hline 4^3 \ 4^2 \ 4^1 \ 4^0 \end{array}$$

$$\Rightarrow 4^3 \cdot a + 4^2 \cdot b + 4^1 \cdot c + 4^0 \cdot d$$

$$= 4^3 \cdot b + 4^2 \cdot c + 4^1 \cdot d + 4^0 \cdot e$$

power + 1

$$\text{So, } 4^3 \cdot a + 4^2 \cdot b + 4^1 \cdot c + 4^0 \cdot d = \text{Sum}$$

$$\Rightarrow (\text{Sum} - 4^3 \cdot a) 4 + e$$

$$= 4^3 \cdot b + 4^2 \cdot c + 4^1 \cdot d + e$$

~~Sum always unique~~

For  
understand  
binary to  
decimal  
always unique

Eg,

$$S = \text{AAAAAACC} \overset{0}{\text{C}} \text{CCCC} \overset{1}{\text{A}} \text{AAAAAACC} \overset{2}{\text{C}} \text{CCCC} \overset{3}{\text{A}} \text{AAAAAAGGAGTTT} "$$

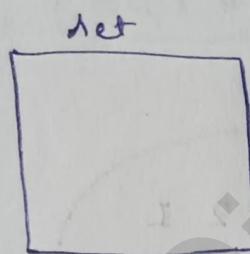
$$\begin{array}{l} A \rightarrow 0 \\ C \rightarrow 1 \end{array}$$

$$\begin{array}{l} G \rightarrow 2 \\ T \rightarrow 3 \end{array}$$

$$\text{AAAAAACC} \overset{0}{\text{C}} \text{CCCC}$$

= Sum

$$4^9 4^8 4^7 \dots 4^0$$



$$\begin{array}{l} A \rightarrow 0 \\ C \rightarrow 1 \\ G \rightarrow 2 \\ T \rightarrow 3 \end{array}$$

$$\text{Formula: } (S - 4^9 \cdot A) 4 + A = [S - 4^9 \cdot (0)] 4 + 0$$

Their

Symmetry

String  $\rightarrow$  Numerical representation  
in constant time

Code:

```
public List<String> findRepeatDnaSequences(String s) {
    int k = 10;
```

```
    if (s.length() <= k) {
```

```
        return new ArrayList<>();
```

$$Tc = O(m)$$

```
    Set<Integer> seen = new HashSet<>();
    Set<String> result = new HashSet<>()
```

~~if k=10~~

```
    int rep = 0 //sum / representation of sub-string
```

```
    Map<Character, Integer> map = new HashMap<>();
```

```
    map.put('A', 0)
```

```
    map.put('C', 1)
```

```
    map.put('G', 2)
```

```
    map.put('T', 3)
```

$$\text{eg, } \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ \text{A} & \text{A} & \text{A} & \text{A} & \text{A} & \text{A} & \text{C} & \text{C} & \text{C} & \text{C} \\ 4^9 & 4^8 & 4^7 & 4^6 & 4^5 & 4^4 & 4^3 & 4^2 & 4^1 & 4^0 \end{matrix}$$

$$\text{rep} = 4^9 \times 0 + 4^8 \times 0 + \dots$$

```
for (int i = 0; i < k; i++) {
```

```
    int pow = k - i - 1
```

```
    rep = rep + (int)(Math.pow(4, pow) * map.get(s.charAt(i)))
```

```
seen.add(rep)
```

$$\text{rep} = 4^9 \times 0 + \dots + 4^0 \times 1$$

```
for (i = k; i < s.length(); i++) {
```

```
    rep = rep - (int)(Math.pow(4, k - 1) * map.get(s.charAt(i - k)))
```

```
    rep = 4 * rep
```

```
    rep = rep + map.get(s.charAt(i))
```

```
    if (seen.contains(rep)) {
```

```
        result.add(s.substring(i - k + 1, i + 1));
```

```
        seen.add(rep)
```

3

```
return new ArrayList<String>(result);
```

Day-16

## Sliding Window Pattern

(2 simple Interview Ques)

3. Longest Substring Without Repeating Characters HARD

904. Fruit Into Baskets Medium-Hard

Q. (3) Longest Substring Without Repeating Characters

# More Optimized

Previous logic:

b a c d a  
↑ ↑ ↑ ↑ ↑  
i j i j i

in case of jumps

b a c d a  
↑ ↑ ↑ ↑ ↑  
i j i j i

> b not in set → add  
then  $j++$

> again a not in set  
 $j++$

b a c

b a c d

> a in set  
→ remove 'b'  
 $j++$

b a c  
d

b a c d a  
↑ ↑  
i j

> a in set  
→ remove 'a'  
 $i++$

a c d

( (i) + A.size - 1 ) : max + len = 90%

( (j) + A.size - 1 ) : min + len

return ③

= 3

max = 4 - 2 + 1

= 3

stop

return ③

Anituation:

be f a c d a

What we do?

> remove one-one element from set and check.

See:

b e f a c d a  
 [ ] [ ]  
 i j

o:d

a ko remove karne se 'c' repeat nhi kar diha hai set mein.

Toh, kya ham

a ko add karne ne 'a' repeat kar diha hai  
 "toh ham direct 'a' ke aage hi jump kar lette hai" → isse hamne extra remove 'b' 'e' 'f' karne hi need nhi hoti!!!  
 → Use Map !!

Code:

int i=0, j=0, max = 0

Map<Character, Integer> map = new HashMap<>();

while (j < s.length()) {

char c = s.charAt(j)

if (map.containsKey(c)) {

i = map.get(c) + 1

map.put(c, j)

max = Math.max(max, j - i + 1)

j = j + 1

}

return max.

Eg. befacda

0 1 2 3 4 5 6	befacda
↑ i ↑ j	

- $j = b \rightarrow$  not in map
- $\rightarrow b \rightarrow$  not in map

b: 0

$$\rightarrow \max = 0 + 1$$

$\uparrow \uparrow$   
 $i \quad j$

- $\rightarrow j = e \rightarrow$  not in map

b, e

$$\max = 2 \\ \uparrow \uparrow$$

$\uparrow \uparrow$   
 $i \quad j$

- $\rightarrow j = f \rightarrow$  not in map

b e f

$$\max = 3 \\ \uparrow \uparrow$$

$\uparrow \uparrow$   
 $i \quad j$

- $\rightarrow j = a \rightarrow$  not

b e f a

$$\max = 4 \\ \uparrow \uparrow$$

~~$j = b$~~  befacda

↑ i ↑ j	↑ j
------------------	--------

$\rightarrow j = c \rightarrow$  x

b e f a c

$$\max = 5$$

$\uparrow \uparrow$   
 $i \quad j$

$$\rightarrow j = d \rightarrow$$

$$\max = 6 \\ \uparrow \uparrow$$

b e f a c d

$\uparrow \uparrow$   
 $i \quad j$

$$j = 3 + 1 = 4$$

b: 0 d: 5  
e: 1  
f: 2  
c: 4

$\uparrow \uparrow$   
 $i \quad j$

$$\max = (3, 6)$$

$\uparrow \uparrow$   
atop

return  $\underline{\underline{\max = 6}}$

befacda

but that code not seem for this case

- $s = "abba"$
- $i = 0$ ,  $j = 3$
  - $i = 1$ ,  $j = 2$
  - $i = 2$ ,  $j = 1$
  - $i = 3$ ,  $j = 0$

$s = "abba"$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

$j = a \rightarrow x$

a: 0
------

$\max = 1$   
 $j++$

$s = "abba"$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

a: 0
b: 2

$\max = 2$

$s = "abba"$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

$j = b \rightarrow x$

a: 0
b: 1

$\max = 2$   
 $j++$

$s = "abba"$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

$j = a \checkmark$

a: 0
b: 2

$i = 0 + 1 = 1$

"a again go on i index"

$s = "abba"$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

$j = b \checkmark$

so,  $i = j + 1 - 2$

$\max = 2$

Toh ham :

$ab \boxed{b} a$  and b is  
not exist in  
the window

$s = "abba"$

$\begin{matrix} \uparrow \\ i \\ j \end{matrix}$

$i = 1 + 1 = 2$

again

a: 0
b: 1

3  
like value chahi hai agar  
current i se toh ignore

if (map.containsKey(c)) {  
if (map.get(c) >= i) {  
j = map.get(c) + 1

### Updated code :

```

int i = 0, j = 0, max = 0
Map<Character, Integer> map = new HashMap<>;
while (j < s.length ()) {
    char c = s.charAt (j)
    if (map.containsKey (c)) {
        if (map.get (c) >= i) {
            i = map.get (c) + 1
        }
    }
    map.put (c, j)
    max = Math.max (max, j - i + 1)
    j = j + 1
}
return max

```

$$TC = O(n)$$

$$SC = O(n)$$

### O-(904) Fruit into Baskets

- Trees are represented by array `fruits[]` where `fruits[i]` = type of fruit tree the  $i^{th}$  tree produces.
- We want to collect as much fruit as possible with strict rules :
  - Only 2 baskets, each basket can hold a single type of fruit. No limit on amount.
  - We must pick exactly one fruit from every tree
  - Once you reach a tree with fruit that cannot fit in your baskets, **stop**.
  - Return, the max no. of fruits you pick.

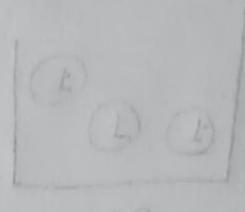
Eg, [ 0, 1, 2, 2, 1, 1, 3, 2, 2, 1 ]

Assume: 0 → type of tree of  $\Delta$  fruit

1 → type of tree of  $\square$  "

2 → " " " " "  $\circlearrowleft$  "

3 → " " " "  $\circlearrowright$  "



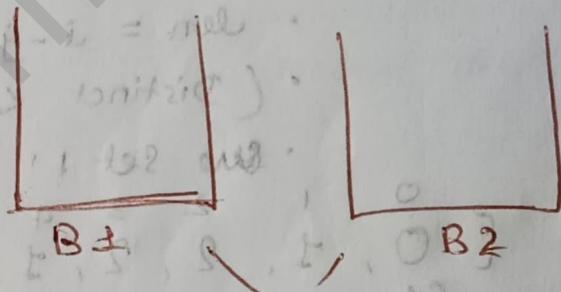
[ 0, 1, 2, 2, 1, 1, 3, 2, 2, 1 ]

[  $\Delta$ ,  $\square$ ,  $\circlearrowleft$ ,  $\circlearrowright$ ,  $\square$ ,  $\square$ ,  $\circlearrowleft$ ,  $\circlearrowright$ ,  $\square$  ]

> B1 basket mein ek hi type ka fruit unlimited dal sakte hai

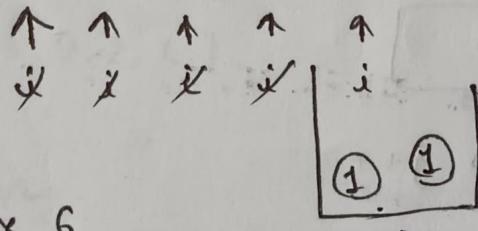
> same for B2 basket

> but, jese hi 3rd type of fruit milega, toh ham B1 & B2 basket mein nahi dal skte hain → Stop and count the no. of fruits in B1 and B2.



Eg, [ 0, 1, 2, 2, 1, 1, 3, 2, 2, 1 ]

Let j on index 2



on index 6

j get 3 fruits

→ Stop bcz, B1 have ①

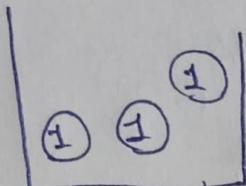
B2 have ②

→ count = 4 fruits

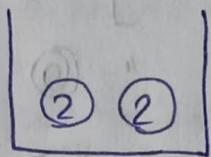
Ex.  $[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]$ , O/P = 5

How? ; O/P = 5

↑  
↑  
↑  
↑  
↑  
↑  
↑  
↑  
↑  
↑  
stop



B1



B2

$$\text{count} = \underline{\underline{5}}$$

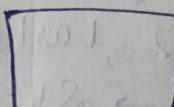
$$\text{len?} \rightarrow i=5 \rightarrow 8 \cdot (i-j+1) = \underline{\underline{5}}$$

### Initiation:

- move until we have 2 type of distinct fruits
- len =  $i-j+1$
- (Distinct  $\leq 2$ )  $\rightarrow$  move ~~size~~ out input
- ~~the set!~~

Ex.  $[0, 1, 2, 2, 1, 3, 2, 2, 1]$

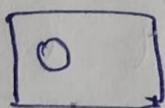
↑  
↑  
j      max = 0



•  $[0, 1, 2, 2, 1, 3, 2, 2, 1]$

↑  
j

> 0  $\rightarrow$  put in set



> ask, element in set

= 1  $\rightarrow$  ok  $\rightarrow$   $j++$

> size =  $j-i+1 = 1$

> max = 1

not tel  
strategic

- $[0, 1, 2, 2, 1, 1, 3, 2, 2, 1]$

$\uparrow \uparrow$   
 $i; j$

>  $i \rightarrow$  put in set  $\boxed{0, 1}$

> ask, size of set = 2  $\rightarrow$  ok  $\rightarrow j++$

> size = 2

> max = 2

- $[0, 1, 2, 2, 1, 1, 3, 2, 2, 1]$

$\uparrow \uparrow$   
 $i; j$

>  $i \rightarrow$  set  $\boxed{0, 1, 2}$

> size of set = 3  $\times \rightarrow j++$

and  $j = i$  and reset the set

(sm)  $O = ST$

(L)  $O = T^2$

- $[0, 1, 2, 2, 1, 1, 3, 2, 2, 1]$

$\uparrow$   
 $i \uparrow$   
 $j$

>  $i \rightarrow$  set  $\boxed{1}$

> size = 1  $\checkmark \rightarrow j++$

- $[0, 1, 2, 2, 1, 1, 3, 2, 2, 1]$

$\uparrow \uparrow$   
 $i; j$

>  $i \rightarrow$  set  $\boxed{1, 2}$

> size = 2  $\checkmark \rightarrow j++$

- $[0, 1, 2, 2, 1, 1, 3, 2, 2, 1]$

$\uparrow \uparrow \uparrow \uparrow \uparrow$   
 $i; j; j; j; j$

$\rightarrow i \rightarrow$  set already

$\rightarrow$  size = 2  $\rightarrow j++$

$\max = 2 \neq 4 \neq 5 \quad (j - i + 1)$

- $[0, 1, 2, 2, 1, 1, 3, 2, 2, 1]$

$\uparrow \uparrow$   
 $i; j$

$\rightarrow i \rightarrow$  set  $\boxed{1, 2, 3}$

$\rightarrow$  size of set = 3  $\rightarrow x \rightarrow j++$  ~~size~~  $\max = 5 \neq$

$O = n \cdot m \rightarrow$  slow

(sm)  $O = ST$

(L)  $O = T^2$

time complexity =  $T^2$  or  $m^2$

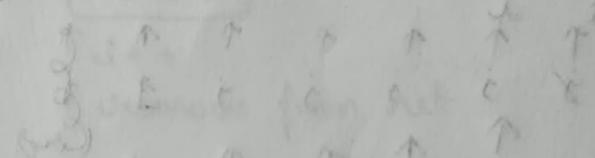
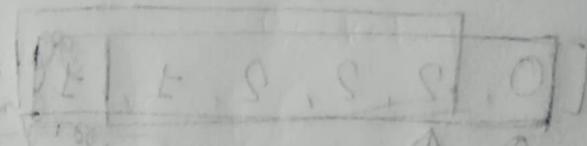
if the max. size

then step or 3 below

(not same point)

same result

barrier of O



max = 5

if all elements

max = 5

Code:

max = 0

for ( i=0 ; i< fruit.length ; i++ ) {

    Set<Integer> set = new HashSet<>()

    for ( j=i ; j< fruit.length ; j++ ) {

        set.add( fruit[j] )

TC = O(n<sup>2</sup>)

SC = O(A)

if ( set.size() > 2 ) {

    break

}

Here, SC = constant

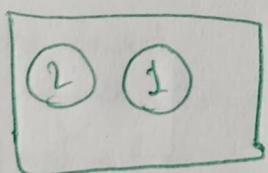
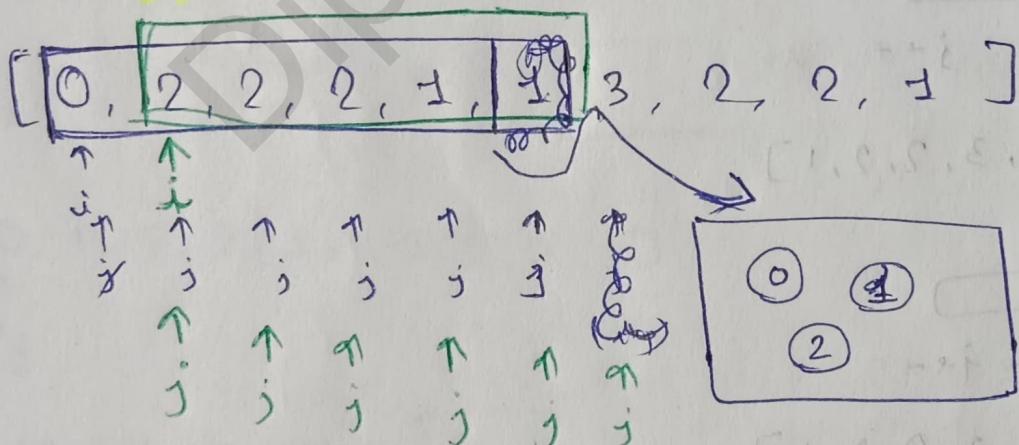
b/c, ham set ki

value 2 se jada <sup>3</sup> nahi kar sake.

between max

    max = Math.max( max , j-i+1 )

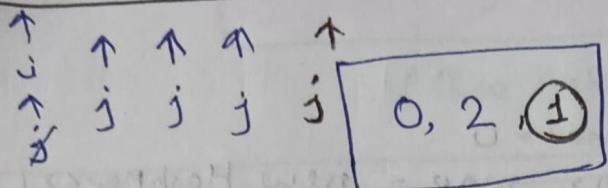
Optimized



repeating !!

{ 0 2 2 2 1   
        2   
 2 2 2 1 - - -

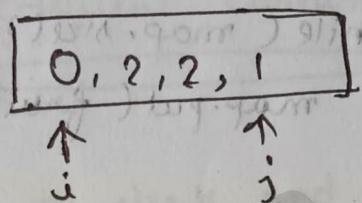
Ex.  $[0, 0, 2, 2, 1, 1, 3, 2, 2, 1]$



$$\max = \emptyset \neq 2 \neq 4$$

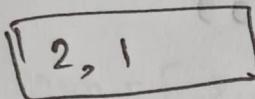
$\downarrow$   
size > 2

- $i++$
- remove 0 from set



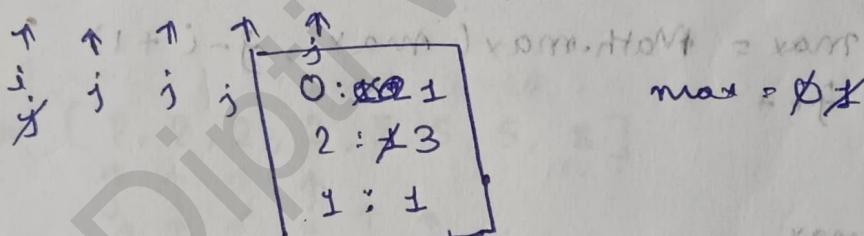
But, this window

is not represent  
by set



\* That's why we don't use Set  
→ Use Map (that store count)

Ex.  $[0, 2, 2, 2, 1, 1, 3, 2, 2, 1]$

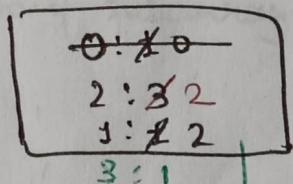
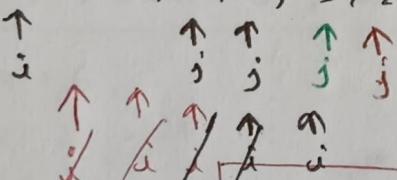


$$\max = \emptyset \neq 2 \neq 4$$

$\downarrow$   
size > 2

- $i++$
- remove from set

$[0, 2, 2, 2, 1, 1, 3, 2, 2, 1]$

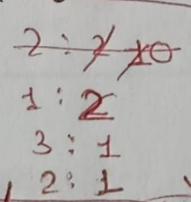


$$\max = 5$$

③

$\downarrow$   
 $i \geq 2$

$i++$   
1: 2 X 0  
3: 1  
2: 1



$\downarrow$   
size > 2  
•  $i++$

①

again size > 2  
→  $j++$

$$\max = 5$$

$\downarrow$   
now, size = 2  
 $j++$

Code :

```
int i = 0, j = 0, max = 0
Map<Integer, Integer> map = new HashMap<>()
while (j < fruit.length) {
    map.put(fruit[j], map.getOrDefault(fruit[j], 0) + 1)
    while (map.size() > 2) {
        map.put(fruit[i], map.get(fruit[i]) - 1)
        if (map.get(fruit[i]) == 0) {
            map.remove(fruit[i])
        }
        i++
    }
    max = Math.max(max, j - i + 1)
    j++
}
return max
```

$$\begin{aligned}TC &= O(n) \\SC &= O(1)\end{aligned}$$

$i < j$

Day - 17

## Sliding Window Pattern

(Two Interview Ques)

Q343. No. of sub-arrays of size k and average greater than or equal to threshold (Medium)

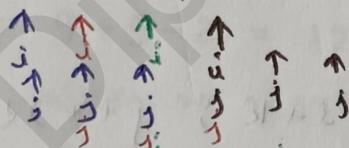
Q338. Frequency of the most frequent element (medium-hard)

Q (Q343). No of sub-arrays of size k and average greater than or equal to threshold

Eg, arr = [ 2, 2, 2, 2, 55, 5, 8 ]    K=3    threshold = 4

Brute Force:

arr = [ 2, 2, 2, 2, 5, 5, 5, 8 ]



> sum = 6     $6/3 = 2 \geq 4$  X  
> sum = 2 + 5 + 5 = 12     $12/3 = 4 \geq 4$  ✓  
> i++, sum = 0, i = j    > No. of subarray = 1  
else.

> sum = 6     $6/3 = 2 \geq 4$  X  
> i++, sum = 0, i = j

> sum = 9     $9/3 = 3 \geq 4$  X  
> i++, sum = 0, i = j

Let a car can hold maximum vehicles (length)

arr = [ 2, 2, 2, 3, 5, 5, 5, 8]      K=3      threshold = 4

$$\text{Sum} = 10 \rightarrow \frac{10}{3} = 3.3333 \geq 4$$

Let  $\frac{x}{y} \geq t$

$$\rightarrow x \geq (t \times y) \quad \begin{array}{l} \text{[No need to use]} \\ \text{float data type} \end{array}$$

~~10~~  $\geq (3 \times 4)$

Code:

int maxT = K \* threshold

int count = 0

for ( i=0 ; i < arr.length - K ; i++ ) {

    int sum = 0

    for ( j=i ; j < i+k ; j++ ) {

        sum = sum + arr[j]

TC = O(n<sup>2</sup>)

SC = O(1)

    if ( sum >= maxT ) {

        count = count + 1

}

return count

## Optimization :

$$\text{arr} = [ \underline{\underline{2, 2, 2, 2}}, 5, 5, 5, 8 ]$$

$$\begin{matrix} 2+2+2 \\ 2+2+2 \\ 2+2+5 \end{matrix}$$

repetition calculation !!!

Ex.  $\text{arr} = [ \underbrace{2, 2, 2}, 2, 5, 5, 5, 8 ] \quad k=3, \underline{t=4}$

$$\rightarrow \text{sum} = 6 \quad \text{maxT} = 12$$

$$\text{sum} >= \text{maxT} \times$$

$$\rightarrow \text{sum} = 6 + 2 - 2 = 6 \quad \text{maxT} = 12$$

$$\text{sum} >= \text{maxT} \times$$

$$\rightarrow \text{sum} = 9 \quad \text{maxT} = 12$$

$$\text{sum} >= \text{maxT} \times$$

$$\rightarrow \text{sum} = 9 + 5 - 2 = 12 \quad \text{maxT} = 12$$

$$\text{sum} >= \text{maxT} \checkmark$$

$$\text{Count} = 1$$

Code:

```
int sum = 0
```

```
int maxT = k + threshold
```

```
for (i=0 ; i < k ; i++) {
```

```
    sum = sum + arr[i]
```

```
}
```

```
int count = 0
```

```
if (sum >= threshold maxT) {
```

```
    count++
```

```
}
```

```
sum = sum + arr[i]
```

```
sum = sum - arr[i-k]
```

```
if (sum >= maxT) {
```

```
    count++
```

```
}
```

$T.C = O(n)$

$S.C = O(1)$

## Q. (1838) Frequency of the Most Frequent Element

Eg.  $\text{num} = [1, 2, 4]$   $K = 5 \rightarrow$  operation  
on index 0  $\rightarrow$  do 3 operations  
it becomes 4  
on index 1  $\rightarrow$  do 2 operations it becomes 4  
 $\therefore \text{num} = [4, 4, 4] \rightarrow \text{op} = \underline{\underline{3}}$

### Approach - 1

Eg.  $\text{num} = [1, 10, 19, 17, 16] \quad K = 5$

$\rightarrow$  let we take 17

- 17 is chota 16
- ab 16 + 1  $\rightarrow$  1 operation = 17 ✓

$\rightarrow$  let we take 19

- 19 is chota 17
- ab 17 + 2  $\rightarrow$  2 operations = 19 ✓
- 19 is chota 16
- ab 16 + 3  $\rightarrow$  3 operations = 19 ✓

• 0 operation left

• we get 19  $\rightarrow$  frequency =  $\underline{\underline{3}}$

for this, we want sorting

Let  $\text{num} = [1, 10, 16, 17, 19]$

$\text{numu} = [1, 10, \underbrace{16, 17, 19}]$

Let take subarray =  $[16, 17, 19] \Rightarrow \text{Operation} = 5$

$+2$   
 $+3$

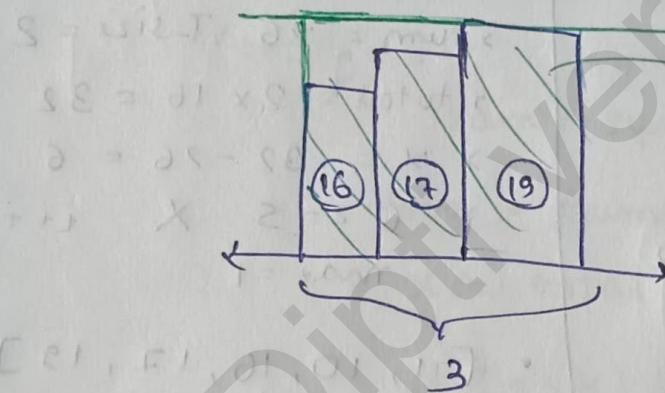
Let take subarray =  $[10, \underbrace{16, 17}] \Rightarrow \text{Operation} = 8$

$+1$   
 $+7$

Means, if we analysis all subarray after sorting, and check the no. of operation  $\leq k$ , then count frequency.

$\Sigma$  of subarray  $\rightarrow \geq ??$  (no. of operations)

Let subarray =  $[16, 17, 19]$



$$\begin{aligned} & 19 \times 3 = 57 \\ & \text{but actually} = 16 + 17 + 19 \\ & = 53 \end{aligned}$$

$$\text{and, } 57 - 53 = 4$$

• we have

$$\Sigma = 4 \text{ and } k = 5$$

$$4 \leq 5 \quad \checkmark$$

- o sorted
- o Take subarray and calculate sum
- o take last element of subarray (let e)  $\times$  size
- o  $\text{Sum} - (e \times \text{size}) = \Sigma$
- o Check ( $\Sigma \leq k$ )
  - Valid subarray
  - calculate Frequency

size	calculate?
1	2 3
1	16 18 19
	↑ ↑ ↑
i	j
3	
$j - i + 1 = \text{size}$	

Eg,  $\text{numu} = [1, 10, 19, 17, 16]$        $k=5$   
 $\begin{array}{ccccc} & 0 & 1 & 2 & 3 & 4 \\ \text{sort} \rightarrow & [1, 10, 16, 17, 19] & \uparrow & \downarrow & \downarrow & \end{array}$

$$\text{max} = 0$$

$$\text{sum} = 0$$

•  $[1, 10, 16, 17, 19]$

↑

ij

$$> \text{sum} = 1, \text{total size} = 1$$

$$> \text{total} = 1 - 1 = 0$$

$$> 0 <= 5 \checkmark \quad i++$$

$$> \text{max} = 1$$

•  $[1, 10, 16, 17, 19]$

↑

ij

$$> \text{sum} = 11, \text{total size} = 2$$

$$> \text{total} = 2 \times 10 = 20$$

$$> x = 20 - 11 = 9$$

$$> 9 <= 5 \times \rightarrow i++$$

$$\text{max} = 1$$

•  $[1, 10, 16, 17, 19]$

↑  
ij

$$> \text{sum} = 10, \text{total size} = 1$$

$$> \text{total} = 2 \times 10 = 20$$

$$> x = 20 - 10 = 0$$

$$> 0 <= 5 \checkmark \quad i++$$

$$\text{max} = 1$$

$$\frac{\text{total}}{\text{size}} = j-i+1$$

$$\text{total} = \frac{\text{total size} \times \text{last element}}{size}$$

$$x? \rightarrow \text{total} - \text{sum}$$

•  $[1, 10, 16, 17, 19]$

↑  
ij  
1  
2

$$> \text{sum} = 26, \text{T-size} = 2$$

$$> \text{total} = 2 \times 16 = 32$$

$$> x = 32 - 26 = 6$$

$$> 6 <= 5 \times \rightarrow i++$$

$$\text{max} = 1$$

•  $[1, 10, 16, 17, 19]$

↑  
ij

$$> \text{sum} = 16, \text{T-size} = 1$$

$$> \text{total} = 2 \times 16 = 32$$

$$> x = 32 - 16 = 16$$

$$> 0 <= 5 \checkmark \quad \text{max} = 1$$

•  $[1, 10, 16, 17, 19]$

↑  
ij

$$> \text{sum} = 33, \text{T-size} = 2$$

$$> \text{total} = 2 \times 17 = 34$$

$$> x = 34 - 33 = 1$$

$$> 1 <= 5 \checkmark \quad \text{max} = 2$$

•  $(1, 10, 16, 17, 19)$

↑ ↑  
i j

> sum =  $\$2$ ,  $T_{size} = 3$

> total =  $3 \times 19 = 54$

>  $k = 54 - \$2 = \$2$

>  $2 < 5 \rightarrow \max 3, j++$

Stop.

return = 3

Code:

max = 0

Array.sort(nums)

for ( $i=0$ ;  $i < \text{num.length}$ ;  $i++$ ) {  
 sum = 0

for ( $j=i$ ;  $j < \text{num.length}$ ;  $j++$ )  
 sum = sum + num[j]

total = num[j] \* ( $j-i+1$ )

if ( $total > k$ )  
 break

max = Math.max(max,  $j-i+1$ )

return max

berimdego

$Tc = O(n^2)$

$Sc = O(\text{sorting space complexity})$

$O(n \log n)$

anobisimayda

## Optimized

$\text{nums} = [1, 10, 1, 19, 17, 16]$

Sort  $\rightarrow$   $[1, 1, 10, 16, 17, 19]$

$\text{sum} = \emptyset \neq 12$

$\text{max} = 2$

$K = 5$

$\text{if } (\text{nums}[j] \times (j-i+1) - \text{sum} > K) \text{ break}$

2

(sum)  $\neq 102, 100, 104$

Check: totals  $(10 \times 3) - 12 \neq 5$  ✓

break  $i++ \text{ max}$

window =  $[1, 1, 10]$

sum =  $(1 \times 3) - 10 \neq 2$

and, in 2nd iteration:

$\boxed{1} \boxed{1 \quad 10}$  16  $\neq 7 \neq 19$

# Dynamic size window

Simply: sum - 1 =

(NO need to again)  
calculation

now move

Eg,  $\text{numu} = [1, 10, 1]$   $K = 5$

sort  $\rightarrow [1, 1, 10]$   $\leftarrow \text{function name}$   
 $\uparrow \quad \uparrow \quad \uparrow$   $\uparrow \quad \uparrow \quad \uparrow$   $\uparrow \quad \uparrow \quad \uparrow$   
 $i \quad j \quad i \quad j \quad i \quad j$   $\leftarrow \text{0} = \text{max} - \text{first element}$   
 $\leftarrow \text{0} = i, \text{0} = j$

- sum = 1

$$\text{total} = 1 \times (\text{input} + \text{max}) = \text{max}$$

$$x = 0$$

$$0 > K \times$$

$$(0 < \text{max} - (\text{input} - 1)) \times (1) \text{ input} \rightarrow \text{break}$$

$$j++ \quad \text{max} = 1$$

$$(\text{total}) \times 0 = 0$$

$$(\text{total}) \times 0 = 0$$

- sum = 2

$$\text{total} = 2 \times 1 = 2$$

$$x = 0$$

$$0 > K \times$$

$$j++ \quad \text{max} = 2$$

- sum = 12

$$\text{total} = 3 \times 10 = 30$$

$$x = 30 - 12 = 18$$

$$18 > 5 \checkmark \rightarrow \text{break}$$

$$j++ \quad \text{max} = 2$$

- sum =  $12 - 1 = 11$

$$\text{total} = 2 \times 10 = 20$$

$$x = 20 - 11 = 9$$

$$9 > 5 \checkmark \rightarrow \text{break}$$

$$j++ \quad \text{max} = 2$$

- sum =  $11 - 1 = 10$

$$\text{total} = 1 \times 10 = 10$$

$$x = 0$$

$$0 \leq 5 \rightarrow x$$

$$j++ \quad \underline{\text{stop}}. \quad \text{max} = 2 //$$

Code:

```
int max = 0
    . Array.sort(num)
long int sum = 0
int i=0, j=0

while ( j < num.length ) {
    sum = sum + num[j]
    while ( num[j] * (j-i+1) - sum > k ) {
        sum = sum - num[i]
        i++
    }
    max = Math.max(max, j-i+1)
    j++
}

return max
```

TC =  $O(n \log n + n^2)$   
SC =  $O(n \log n)$

This code little bit wrong bcz of constraint:

$i \leq num.length \leq 10^5$

$y \leq num[i] \leq 10^5$

$num.length = 100000$

$element = 100000$

$sum = 10000000000 (10^{10})$

But max int value =  $2147483647$   
→ which is smaller than  $10^{10}$

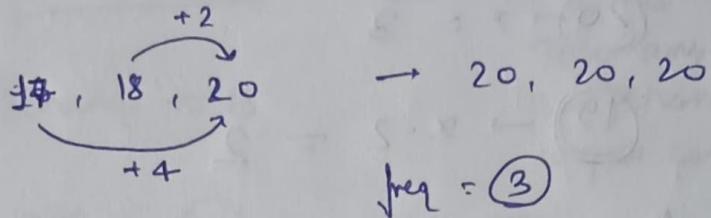
So, change the data type.

## Follow up Question

freq of the most frequent element

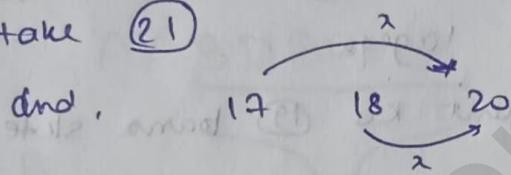
3, 3, 10, 17, 18, 20, 29

$K = 6$



But, here we take assumption that last element of subarray is present in the main array (eg. 20)

Let take ②1

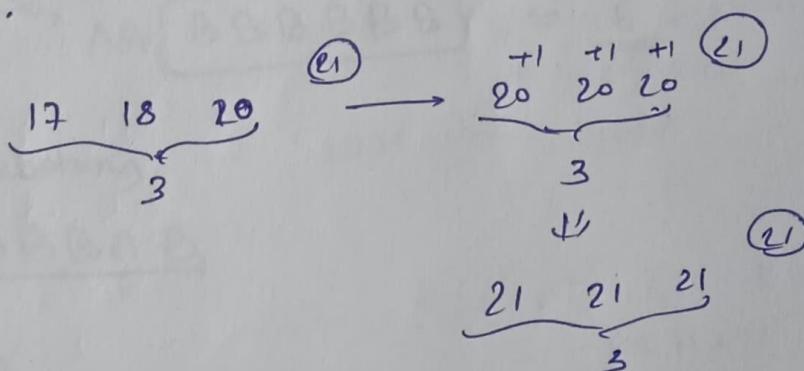


$$x \text{ operation} = 5$$

take  $x+1$  which is not exists (eg. 21)

→ Hamne tin element ko 20 kiya tha with 5 operation

→ Toh hamne only 3 more operation se ham 21 bana skte hain.



Ex. [1, 1, 10, 17, 18, 20, 29]  $K=5$

freq = 3

19

$$20 \rightarrow x = 3$$

$$19 \rightarrow x-2 = 2$$

- Agar hum 20 ko banane mein x operation lag raha hai.
- Toh hum 20 se chota set 19 ko banaye, toh hume x operation se bhi kam lagega.
- Toh hum aur bhi element ko 19 bana skte hain.

But, But, But ----

- Agar 19 se already chota element array mein exist karta hai, toh hum simply bol slore hui ki hume hamara frequent element apne array mein hi milega.

Day - 18

## Sliding Window Pattern

### B. (424) Longest Repeating Character Replacement (Medium)

e.g.,  $s = "AABDBBAAB"$   $K = 2$  Operation

If, D and A change to B  
then,

$AABBBB BBBB = 6$

Take any character,  
and change it to diff  
upper case character

opposite of beer on  
the

c : A

$s = 3 \times am$

$s = 1 + 3 - i = 5 \times 2$

$O = S - s$

or  $BDBBAAB$

$S = 3 \times am$

$E = 3 \times am$

$L = 3 \times am$

$H = 3 \times am$

$T = 3 \times am$

$R = 3 \times am$

$I = 3 \times am$

$O = 3 \times am$

$D = 3 \times am$

$S = 3 \times am$

$E = 3 \times am$

$L = 3 \times am$

$H = 3 \times am$

$T = 3 \times am$

$R = 3 \times am$

#### Brute Force :

o  $AABDBBAAB$   
 $D, A \rightarrow B$   
substring →  $B = 4$  max char in substring  
 $\downarrow$   
length = 6

$6 - 4 = 2$  and  $2 = K \checkmark$  (valid)

then, ② char to convert into B

So,

AA,  $\boxed{BBB BBB}$

o Let another substring:  $S = 3 \times am \longrightarrow tilov$

$AABDBBAAB$

length = 7

max value char (B) = 4

$7 - 4 = 3$

but  $3 > k$  ( Invalid Substring )

$2 \times am$

Eg.  $S = "AABDBBABA"$  K=2

$\max C = 0 \uparrow \uparrow \uparrow \uparrow \uparrow j$

- $A: 1$   
 $\max C = 0 \uparrow$   
 $\text{and size} = j-i+1 = 1$   
 $\max C - \text{size} = 1 - 1 = 0$
- $\{A: 2, B: 2, D: 1\}$   
 $\max C = 2$   
 $\text{size} = j-i+1 = 2$   
 $2-2=0$

No need to change

$j++$

- $A: 2$

$\max C = 2$

$\text{size} = j-i+1 = 2$

$2-2=0$

- $\{A: 2, B: 1\}$

$\max C = 2$

$\text{size} = 3$

$3-2=1$

mean, 1 operation we can do

and  $1 < K$

valid  $\rightarrow \max = 3$

$j++$

- $\{A: 2, B: 1, D: 1\}$

$\max C = 2$

$\text{size} = 4$

$4-2=2$

$2 = K(2)$  operation

valid  $\rightarrow \max = 4$  ( $j-i+1$ )

$j++$

- $\{A: 2, B: 2, D: 1\}$   
 $\max C = 2$   
 $\text{size} = 5$   
 $\text{no. of operations} 5-2 = 3 > K \rightarrow \text{invalid}$

$\max = 4$

$j++ \text{ and } j=i$

$\uparrow$   
 $A A B D B B A B$   
 $\uparrow$   
 $j \uparrow \uparrow \uparrow \uparrow \uparrow j$

- $A: 1$   
 $\max C = 1$   
 $\text{size} = 1$   
 $1-1=0 \checkmark j++$

- $\{A: 1, B: 1\}$   
 $\max C = 1, \text{size} = 2$   
 $2-1=1 < K \checkmark$

- $\{A: 1, B: 1, D: 1\}$   
 $\max C = 1, \text{size} = 3$   
 $3-1=2 < K \checkmark$

- $\{A: 1, B: 2, D: 1\}$   
 $\max C = 2, \text{size} = 4$   
 $4-2=2 = K \checkmark$

- $\{A: 1, B: 3, D: 1\}$   
 $\max C = 3, \text{size} = 5$   
 $5-3=2 < K \checkmark \max = 5$

- $\{A: 2, B: 3, D: 1\}$   
 $\max C = 3, \text{size} = 6$   
 $6-3=3 > K \rightarrow X$

$\boxed{\max = 5}$

Code:

max = 0

for (j=0; j < s.length(); j++) {

    maxC = 0

    int[] counts = new int[26]

    for (j=i; j < s.length(); j++) {

        char c = s.charAt(j)

        counts[c - 'A'] = counts[c - 'A'] + 1

convert

A → 0

B → 1

C → 2

D → 3

    maxC = Math.max(maxC, counts[c - 'A'])

    ops = (j-i+1) - maxC

    if (ops > k) {

        break

TC = O(n<sup>2</sup>)

SC = O(1)

    max = Math.max(max, j-i+1)

3

return max

Eg. ABCB, k=1  
 ↑↑  
 i j  
 max = 0  
 maxC = 0

• A: 1 maxC = 1

ops = 1 - 1 = 0

0 > 1 X

max = 1

• {A:1, B:1} maxC = 1

ops = 2 - 1 = 1

j > 1 X break X

max = 1

• {A:1, B:1, C:1} maxC = 1

ops = 3 - 1 = 2

2 > 1 ✓ break  
i++

• B:1 maxC = 1

ops = 0

No break, Max = 1

• {B:1, C:1} maxC = 1

ops = 1

• {B:2, C:1} maxC = 2

ops = 1

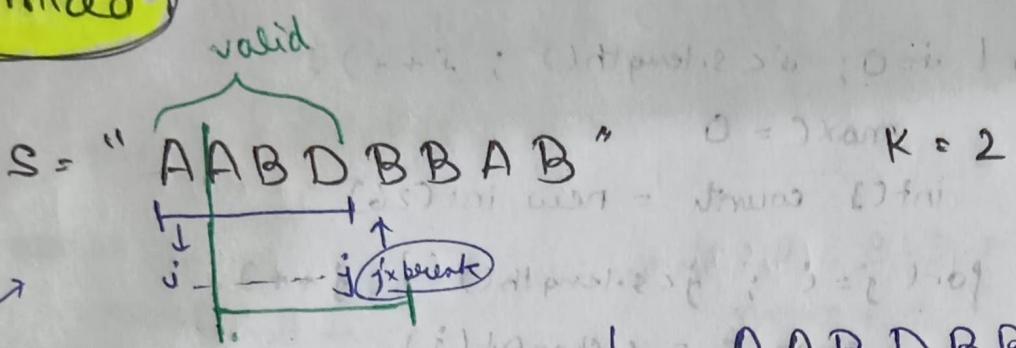
else valid

max = 2

Max = 2

## Optimized

in  
brute  
force



we get,

$$\max C = 2$$

$$\{A: 2, B: 1, D: 1\}$$

$$\max = 2$$

$AABDBBABA$

recalculate

$$(1+1+1) = 390$$

(sm)  $O = ST$   
 $O = 32$

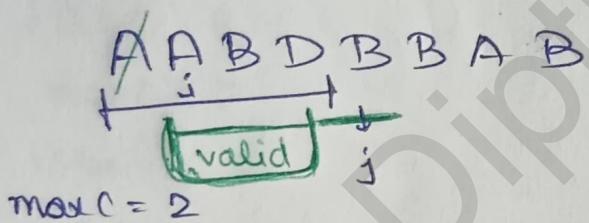
~~err → AABD → valid~~

~~if AABD (remove)~~

~~ABD~~

~~valid ✓~~

# Variable - size sliding window



$$\max C = 2$$

$$\{A: 2, B: 1, D: 1\}$$

$$\max \geq 2$$

$$OPI = 4 - 2 = 2 = K \rightarrow \text{valid}$$

$BDBA$ ,  $O = ?$

$$O = \text{sum}$$

$$O = 390$$

$\uparrow$   
 $\uparrow$   
 $\uparrow$   
 $\uparrow$   
 $\uparrow$

$$I = \text{sum} \quad I : A$$

$$O - E - E = 390$$

$$X 1 \leq 0$$

$$E = \text{sum}$$

$$I - I - S = 390$$

$$X \text{ valid } X E \leq E$$

$$E = \text{sum}$$

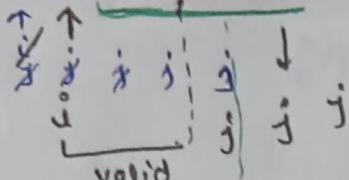
$$I - I - S = 390$$

$$S - I - S = 390$$

$$\text{valid} \sim I \leq S$$

Ex,  $s = "AABDBBAAB"$ ,  $K=2$

$\max = 0$   
 $\max C = 0$



$\{A: 2, B: 3, D: 1\}$

$\max C = 3$

$$OPI = 6 - 3 = 3 > K \checkmark$$

break,  $i++$

$\boxed{ABDBB}$  valid

remove A: 1

$\max C = 1$

$$OPI = 0 > K \times$$

$\max = 1$

$\{A: 2\}$

$\max C = 2$

$$OPI = 2 - 2 = 0 > K \times$$

$\max = 2$

$\{A: 2, B: 1\}$

$\max C = 2$

$$OPI = 3 - 2 = 1 > K \times$$

$\max = 2$

$\{A: 2, B: 1, D: 1\}$

$\max C = 2$

$$OPI = 4 - 2 = 2 > K \times$$

$\max = 2$

$\{A: 2, B: 2, D: 1\}$

$\max C = 2$

$$OPI = 5 - 2 = 3 > K \checkmark$$

break,  $i++$

$\boxed{AABD}$  valid

and, ABD after removing 'A'  
is also valid !!

> remove from freq map

$\{A: 1, B: 2, D: 1\}$

$\max C = 2$

$$OPI = 4 - 2 = 2 > 2 \times$$

$\{A: 1, B: 3, D: 1\}$

$\max C = 3$

$$OPI = 5 - 3 = 2 > 2 \times$$

$\{A: 2, B: 3, D: 1\}$

$\max C = 3$

$$OPI = 6 - 3 = 3 > K \times$$

$\{A: 1, B: 4, D: 1\}$

$\max C = 4$

$$OPI = 6 - 4 = 2 > K \times$$

$\boxed{BDBBAB}$

valid

How we terminate?

$s = "AABDBBAAB"$

$\boxed{j j j j j j j j j j}$

ab agar ham i ko ++ kiye toh  
bhi kya valid substring with max  
value mileage  $\rightarrow$  Never.

bcz, length toh chota hote jaa  
raha hai.

Isliye, termination depend on

job j end min jayega  $\rightarrow$  stop.

