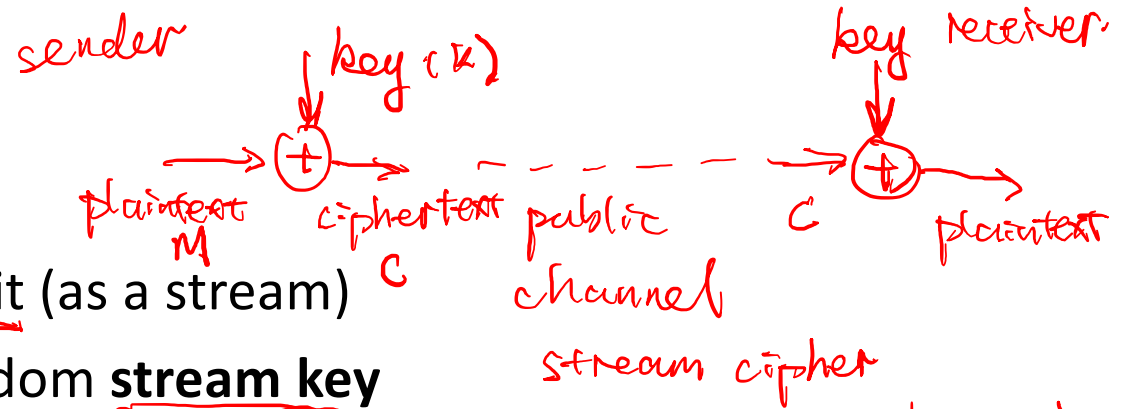


Stream Ciphers



- process the message bit by bit (as a stream)
- typically have a (pseudo) random stream key
- combined (XOR) with plaintext bit by bit
- randomness of **stream key** completely destroys any statistically properties in the message

$$C_i = M_i \text{ XOR } \boxed{\text{StreamKey}_i}$$

$C_i = M_i \oplus K_i$ ← as random as possible
 security ↑
 ideal case: truly random

- what could be simpler!!!!
- but must never reuse stream key ✓
- otherwise, can remove effect and recover messages, $M \oplus K \oplus K = M$

Associativity

$$M \oplus K \oplus K = M \oplus (K \oplus K)$$

DECRYPT = $M \oplus 0 = M$

$$M^1 = 1 \oplus 0 = 1$$

$$M^2 = 0 \oplus 0 = 0$$

Stream Cipher Properties

- some design considerations are:

- statistically random → key

- depends on large enough key → reuse and independent

- large linear complexity → increase input linear, running time $O(n)$,

- correlation immunity

- confusion

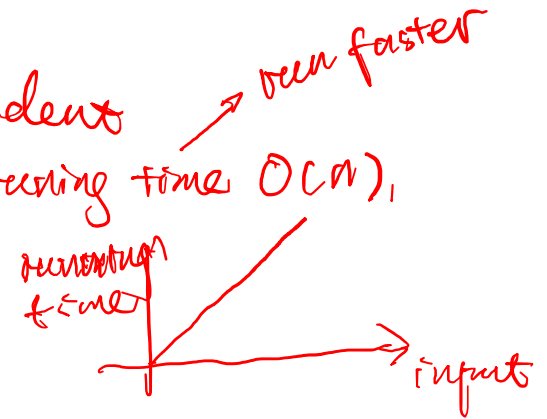
- diffusion

RC4 → WEP

swap ()

xor
swap

key { random
long



How to generate Stream Key?

- How to generate Stream Key?

PRNG

Stream Ciphers

- Idea: replace “rand” by “pseudo rand”
- Use Pseudo Random Number Generator
 - A secure PRNG produces output that looks indistinguishable from random
 - An attacker who can't see the internal PRNG state can't learn any output
- PRNG: $\{0,1\}^s \rightarrow \{0,1\}^n$ *small key s , $n \gg s$ state.*
 - expand a short (e.g., 128-bit) random seed into a long (typically unbounded) string that “looks random”
- Secret key is the seed
 - Basic encryption method: $E_{\text{key}}[M] = M \oplus \text{PRNG}(\text{key})$

computational indistinguishability

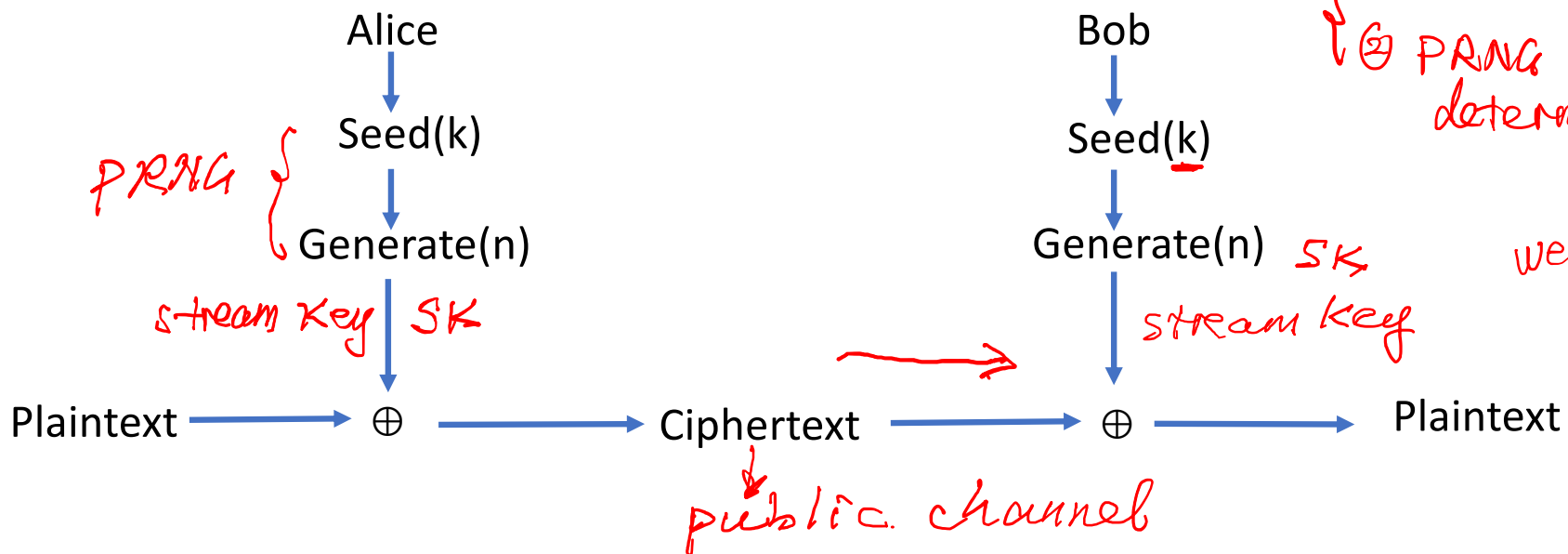
s

PRNG { (1) seed, (2) Generator }

$$= M \oplus \text{Key}$$

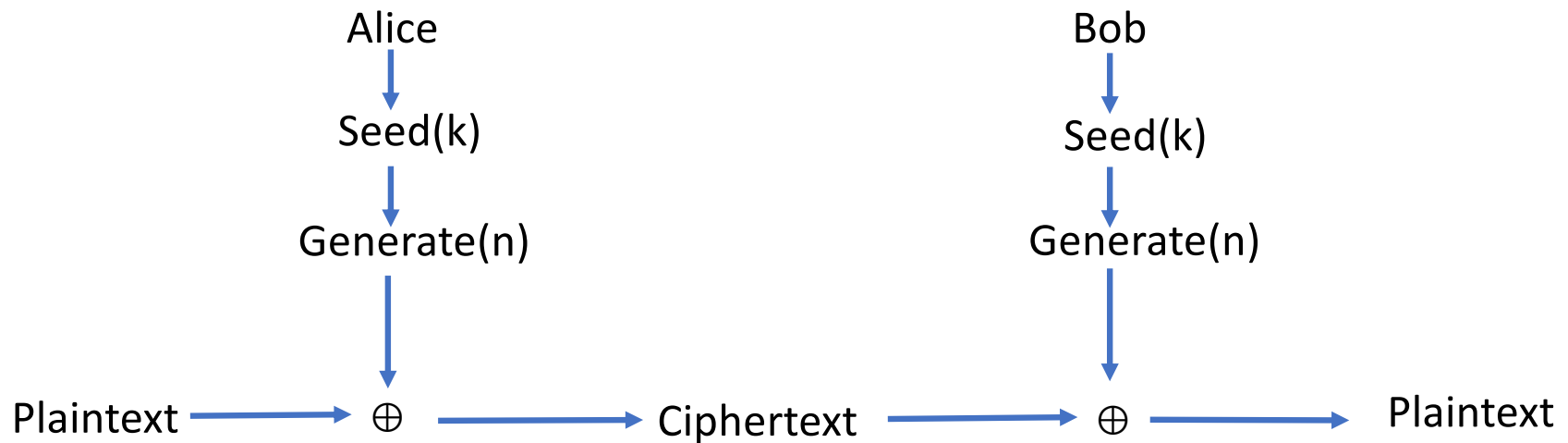
Stream Ciphers

- Protocol: Alice and Bob both seed a secure PRNG with their symmetric secret key, and then use the output as the key for stream key



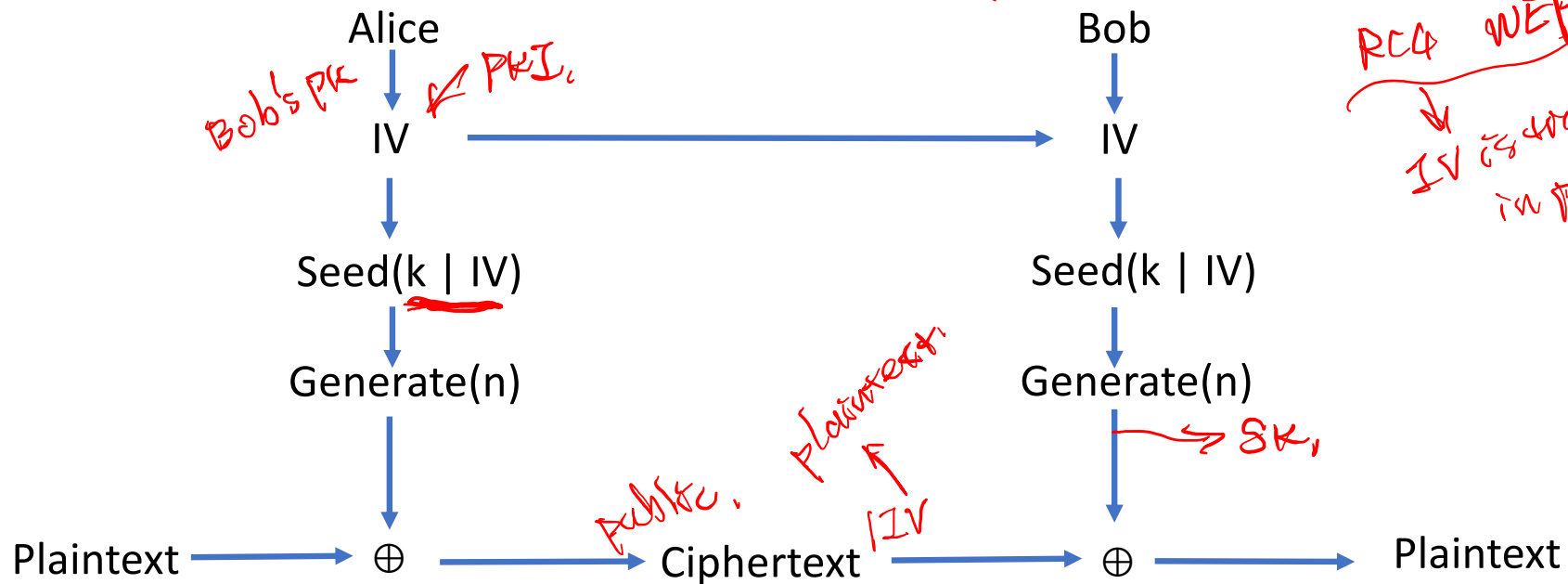
Stream Ciphers: Encrypting Multiple Messages

- How do we encrypt multiple messages without key reuses?



Stream Ciphers: Encrypting Multiple Messages

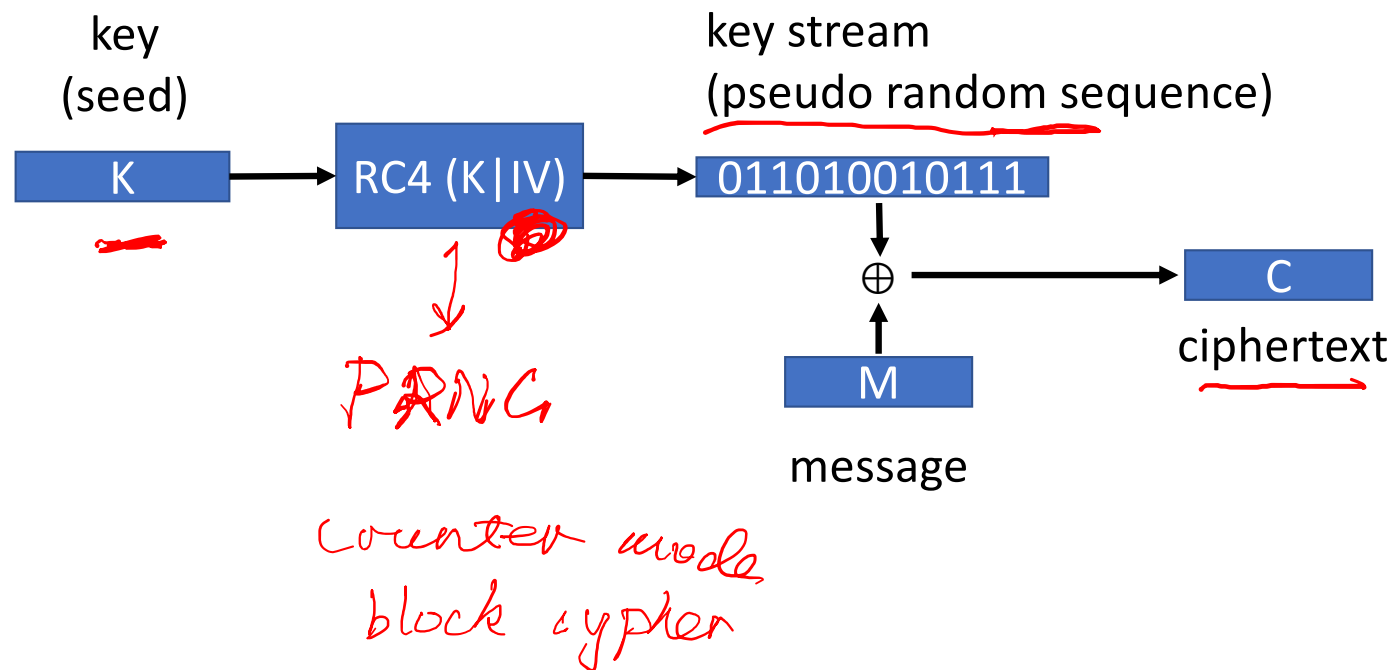
- Solution: For each message, seed the PRNG with the key and a random IV, concatenated(" | "). Send the IV with the ciphertext



Real-world example: RC4

- a proprietary cipher designed in 1987
- Extremely simple but effective! *→ fast.*
- Very fast - especially in software
- Easily adapts to any key length, byte-oriented stream cipher
- widely used (web SSL/TLS, *→ transport* wireless WEP, WAP)
- A trade secret by RSA Security *1994 leaked to public.*
- uses that permutation to scramble input info processed a byte at a time
*↓
swaps*

RC4 Stream Cipher



① RC4 Key Schedule

② Encryption

- starts with an array S of numbers: 0...255
- use key to well and truly shuffle
- S forms internal state of the cipher
- given a key k of length l bytes

```
/* Initialization */  
for i = 0 to 255 256 do  
    S[i] = i;  
    T[i] = K[i mod keylen];  
/* Initial Permutation of S */  
j = 0;  
for i = 0 to 255 do  
    j = (j + S[i] + T[i]) mod 256;  
    Swap (S[i], S[j]); → diffusion
```

Throw away ~~T & K~~, retain S

$$T[i] = K[i \bmod \text{keylen}] \quad K = [1, 2, 3, 4] \quad \text{keylen} = 4$$

If $\text{keylen} > i$; $T[i] = [1, 2, 3, 4]$

$\begin{array}{cccc} \uparrow & \uparrow & \uparrow & \uparrow \\ 0 & 1 & 2 & 3 \end{array}$

$0 \bmod 4 = 0 \Rightarrow K[0]$
 $1 \bmod 4 = 1 \Rightarrow K[1]$

$T[i] = K[i]$

If $\text{keylen} \leq i$

$T[4] = K[4 \bmod 4] = K[0] = 1$

$T[5] = K[5 \bmod 4] = K[1] = 2$

$T = [1, 2, 3, 4, 1, 2, 3, 4, 1, 2, 3, 4]$

$\underbrace{\hspace{1.5cm}} \quad \underbrace{\hspace{1.5cm}}$
 \downarrow
 repeat pattern, \Rightarrow reuse key

\therefore add IV to be large enough