

# Authenticated Encryption: Definition

- **Authenticated encryption (AE):** A scheme that simultaneously guarantees confidentiality and integrity (and authenticity, depending on your threat model) on a message
- Two ways of achieving authenticated encryption:
  - Combine schemes that provide confidentiality with schemes that provide integrity
  - Use a scheme that is designed to provide confidentiality and integrity MAC

# Scratchpad: Let's design it together

- You can use:
  - An encryption scheme:  $\text{Enc}(K, M)$  and  $\text{Dec}(K, M)$
  - An unforgeable MAC scheme (e.g. HMAC):  $\text{MAC}(K, M)$
- First attempt: Alice sends  $\text{Enc}(K_1, M)$  and  $\text{MAC}(K_2, M)$  ✗
  - Integrity? Yes, attacker can't tamper with the MAC
  - Confidentiality? No, the MAC is not secure  $M || \text{MAC}(K_2, M)$
- Idea 1: Let's compute the MAC on the ciphertext instead of the plaintext:  
 $\text{Enc}(K_1, M)$  and  $\text{MAC}(K_2, \text{Enc}(K_1, M))$   $\text{Enc}(K_1, M) || \text{MAC}$ 
  - Integrity? Yes, attacker can't tamper with the MAC
  - Confidentiality? Yes, the MAC might leak info about the ciphertext, but that's okay
- Idea 2: Let's encrypt the MAC too:  $\text{Enc}(K_1, M || \text{MAC}(K_2, M))$   ~~$M || \text{MAC}$~~   ~~$\text{MAC}$~~ 
  - Integrity? Yes, attacker can't tamper with the MAC
  - Confidentiality? Yes, everything is encrypted

# MAC-then-Encrypt or Encrypt-then-MAC?

- Method 1: Encrypt-then-MAC

- First compute  $\text{Enc}(K_1, M)$
- Then MAC the ciphertext:  $\text{MAC}(K_2, \text{Enc}(K_1, M))$

- Method 2: MAC-then-encrypt

- First compute  $\text{MAC}(K_2, M)$
- Then encrypt the message and the MAC together:  $\text{Enc}(K_1, M || \text{MAC}(K_2, M))$

- Which is better?

- In theory, both are secure if applied properly
- MAC-then-encrypt has a flaw: You don't know if tampering has occurred until after decrypting
  - Attacker can supply arbitrary tampered input, and you always have to decrypt it
  - Passing attacker-chosen input through the decryption function can cause side-channel leaks

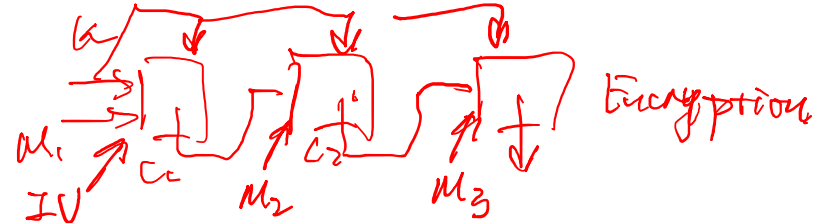
- **Always use encrypt-then-MAC** because it's more robust to mistakes

$M'$   
 $\text{Enc}(K_1, M')$   
trick Attacker  $M'$   
sender  
 $E(K_1, M' || \text{MAC}(K_2, M'))$

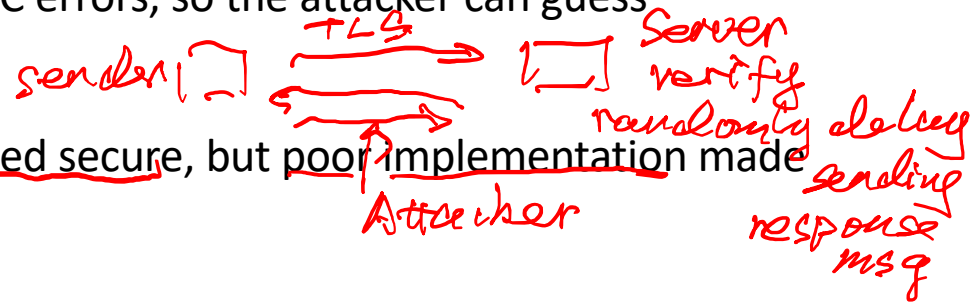
Decrypt

RSA timing attack

# TLS 1.0 “Lucky 13” Attack



- TLS: A protocol for sending encrypted and authenticated messages over the Internet
  - TLS 1.0 uses MAC-then-encrypt:  $\text{Enc}(k_1, M \parallel \text{MAC}(k_2, M))$  *1 bit*
    - The encryption algorithm is AES-CBC *Cypher Block Chain*
  - The Lucky 13 attack abuses MAC-then-encrypt to read encrypted messages
    - Guess a byte of plaintext and change the ciphertext accordingly
    - The MAC will error, but the time it takes to error is different depending on if the guess is correct *Wrong bit  $\rightarrow$  verification time long*
    - Attacker measures how long it takes to error in order to learn information about plaintext *timing attack*
    - TLS will send the message again if the MAC errors, so the attacker can guess repeatedly
  - Takeaways
    - Side channel attack: The algorithm is proved secure, but poor implementation made it vulnerable
    - Always encrypt-then-MAC
- 



↑ big data transmission

# Authenticated Encryption: Summary

- Authenticated encryption: A scheme that simultaneously guarantees confidentiality and integrity (and authenticity) on a message
- First approach: Combine schemes that provide confidentiality with schemes that provide integrity and authenticity
  - MAC-then-encrypt:  $\text{Enc}(K_1, M \parallel \text{MAC}(K_2, M))$
  - Encrypt-then-MAC:  $\text{MAC}(K_2, \text{Enc}(K_1, M))$  ✓
  - Always use Encrypt-then-MAC because it's more robust to mistakes

↗ no group key,

Computation Time       $\text{MAC} < \text{Symmetric Encryption} < \text{Asymmetric Encryption}$

Defense:  
Add randomness

↑  
fixing attack  
Big data input

# Digital Signature

# Digital Signatures

- NIST FIPS PUB 186-4 - the result of a cryptographic transformation of data that, when properly implemented, provides a mechanism for verifying origin authentication, data integrity, and signatory non-repudiation
- Based on asymmetric keys

~~no confidentiality~~

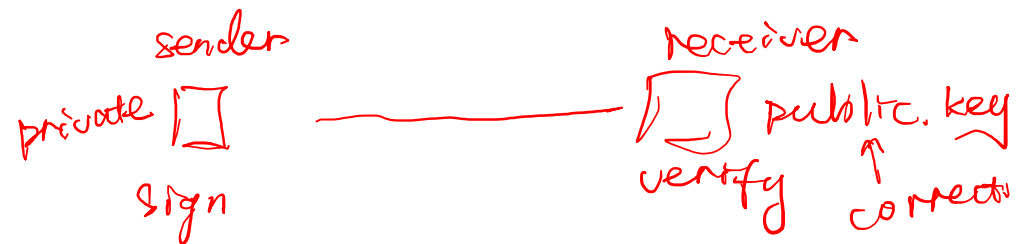
# Digital Signatures

$H = \dots$

- Asymmetric cryptography is good because we don't need to share a secret key
- Digital signatures are the asymmetric way of providing integrity/authenticity to data
- Assume that Alice and Bob can communicate public keys without David interfering

PKI  
Third Authority Party  
certificate  
↓  
Sig (K, SK)  
#

correct





# Digital Signatures: Definition

- Three parts:
  - $\text{KeyGen}() \rightarrow PK, SK$ : Generate a public/private keypair, where  $PK$  is the verify (public) key, and  $SK$  is the signing (secret) key
  - $\text{Sign}(SK, M) \rightarrow sig$ : Sign the message  $M$  using the signing key  $SK$  to produce the signature  $sig$
  - $\text{Verify}(PK, M, sig) \rightarrow \{0, 1\}$ : Verify the signature  $sig$  on message  $M$  using the verify key  $PK$  and output 1 if valid and 0 if invalid
- Properties:
  - **Correctness**: Verification should be successful for a signature generated over any message
    - $\text{Verify}(PK, M, \text{Sign}(SK, M)) = 1$  for all  $PK, SK \leftarrow \text{KeyGen}()$  and  $M$
  - **Efficiency**: Signing/verifying should be fast *1st 2.*
  - **Security**: Same as for MACs except that the attacker also receives  $PK$ 
    - Namely, no attacker can forge a signature for a message *without private key*

# RSA Signature

- KeyGen(): *Same as RSA Encryption*

- Randomly pick two large primes,  $p$  and  $q$
- Compute  $n = pq \rightarrow$  *large number, public.*
  - $n$  is usually between 2048 bits and 4096 bits long

- Choose  $e$

- Requirement:  $e$  is relatively prime to  $(p-1)(q-1)$

- Requirement:  $2 < e < (p-1)(q-1) = \phi(n)$

- Compute  $d = e^{-1} \bmod (p-1)(q-1)$

- **Public key:**  $n$  and  $e$   $\rightarrow \phi(n)$   $\rightarrow$  *public*
- **Private key:**  $d$

$$\gcd(e, \phi(n)) = 1$$

# A Short Quiz

- We will have a short quiz on Wednesday, Oct. 30, in class
- A short quiz will cover the materials taught that day.