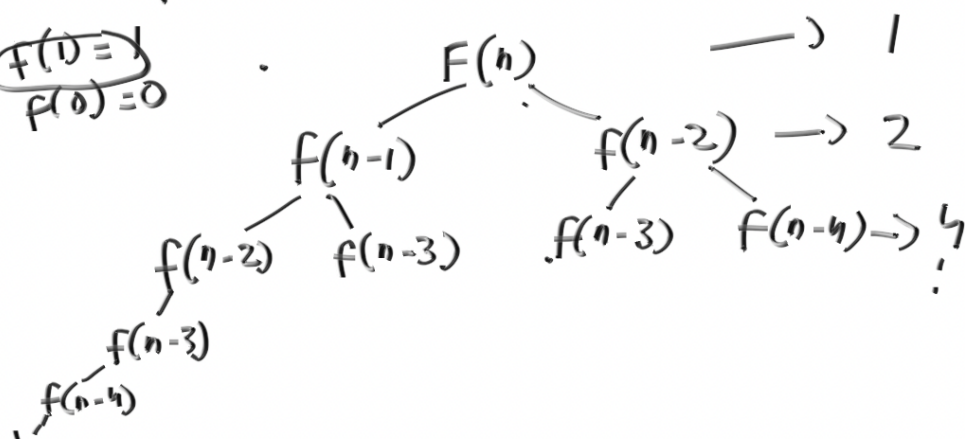


$$F(n) = F(n-1) + F(n-2)$$

$$\begin{aligned} f(1) &= 1 \\ f(0) &= 0 \end{aligned}$$



Big-O

Theta

Ω

$\Theta(n)$

O

$$n = 1000$$

(3)

$$n^2 \quad n^{\log n}$$

$$1 < \log n < \underbrace{n}_{\Omega(n)} < \underbrace{n \log n}_{\Theta(n)} < \underbrace{n^2}_{O(n^2)} \dots$$

$$\begin{array}{ccc}
 2^{2n} & & 2^n \\
 \underline{\underline{2^{2n}}} & & \underline{\underline{2^n}} \\
 \textcircled{2^n} & & \underline{\underline{2^n}} \\
 2^n \times 2^n \times 2^n & \text{---} & n \text{ times} \\
 \underline{\underline{2^{n+1}}} & & \underline{\underline{2^{2n+1}}} \\
 \downarrow & & \downarrow \\
 2 \times 2^n & & 2 \times 2^{2n}
 \end{array}$$

$$\begin{array}{ccc}
 \underline{n^2} & \frac{n^3}{n^2 \times n} & \frac{2n}{1} \quad \frac{3n}{1} \\
 & \uparrow & \uparrow
 \end{array}$$

$$\begin{aligned}
 \bigcirc \quad \left(\overset{n}{\uparrow} f(n) + \overset{n^2}{\uparrow} g(n) \right) &= O(\underline{\underline{\max(f(n), g(n))}}) \\
 \bigcirc \quad \underline{(n + n^2)} &= O(\underline{\underline{n^2}})
 \end{aligned}$$

Example 1:**Input:**

N = 5

arr[] = {1,2,3,4,5}

Output: 6**Explanation:** Smallest positive missing number is 6.**Example 2:****Input:**

N = 5

arr[] = {0,-10,1,3,-20}

Output: 2**Explanation:** Smallest positive missing number is 2.

$[0, -10, \underline{1}, 3, -20]$

$\underline{1}, 2, 3, 4, \dots \quad \underline{\underline{O(n)}}$

$[\underline{1}, \underline{\underline{n+1}}]$

$$\begin{array}{r} [1, 2, 3, -2, 5] \\ \hline 6 \\ \hline \boxed{9} \end{array}$$
$$[1, 2, -10, \underline{1, 5}]$$
$$\begin{array}{ccccccc} 1 & 2 & 3 & \dots & n \\ \hline n & n-1 & n-2 & \dots & 1 \end{array}$$

$O(n^2)$

max. til. here:

	0	1	2	3	4
	1	2	-10	1	5
		3	-7	1	6

$$\text{mth}[0] = \text{arr}[0]$$

i > 1 :

$$mth[i] = mth[i-1] + arr[i]$$
$$\text{if } mth[i-1] > 0$$
$$mth[i] = arr[i] \text{ otherwise}$$

$nth[i] = \text{maximum sum of any subarray ending EXACTLY at index } i.$

TC: $O(n)$ Aux space = $O(n)$

	0	1	2	3	4	5
arr:	1	2	-1	1	3	-2
<u>nth:</u>	1	3	<u>2</u>	<u>3</u>	<u>6</u>	<u>4</u>

Input : arr[] = {1, 3, 5, 5, 5, 5, 67, 123, 125}
x = 5

Output : First Occurrence = 2
Last Occurrence = 5

Input : arr[] = {1, 3, 5, 5, 5, 5, 7, 123, 125 }
x = 7

Output : First Occurrence = 6
Last Occurrence = 6

0	1	2	3	4	5	6	7
1	3	5	5	5	5	67	123
			<u>5</u>				

x = 5

low = 0 high = 7

mid = $\frac{0+7}{2} = 3$ first_occ = 3
 \swarrow
arr[mid] = 5

low = 0 high = 2

mid = $\frac{0+2}{2} = 1$ (arr[mid] < x)

low = 2 high = 2

mid = $\frac{2+2}{2} = 2$

first_occ = 2

$$\checkmark \quad \text{ans[mid]} == x$$

(low = 2 high = 1) STOP!

~~X~~ 0 0 ~~X~~ 0

1 ~~X~~ 0 1

1 ~~X~~ 0 1

	0	1	2
0	X 0	0	X 0
1	1	X 0	1
2	1	X 0	1



rows: $\begin{bmatrix} \overset{0}{T} & \overset{1}{F} & \overset{2}{F} \end{bmatrix}$ cols: $\begin{bmatrix} \overset{0}{F} & \overset{1}{T} & \overset{2}{F} \end{bmatrix}$

$\underline{\underline{O(n)}}$ $\underline{\underline{(n \times m)}}$ TC: $O(n \times m)$

Aux Space: $O(n + m)$

	0	1	2
0	1	0X	1
→ 1	1	X0	1
→ 2	X0	0	0X

i = 1, j = 1

	0	1	2
0	X0	0	X0
1	1	X0	1
2	X0	0	0X

1	0	1
1	0	1
0	0	0

bool first_row = T TC: $O(n \times m)$
 bool first_col = F Aux space: $O(1)$