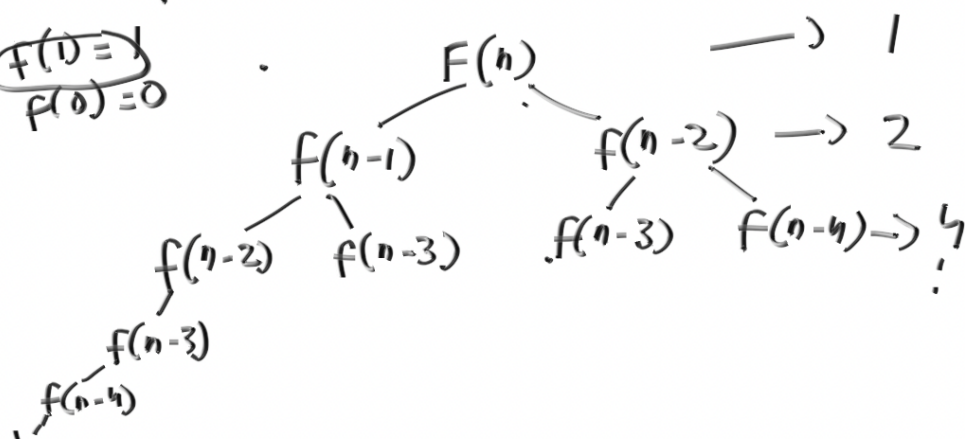


$$F(n) = F(n-1) + F(n-2)$$

$$\begin{matrix} f(1) = 1 \\ f(0) = 0 \end{matrix}$$



Big-O

Theta

Ω

$\Theta(n)$

O

$$n = 1000$$

(3)

$$n^2 \quad n^{\log n}$$

$$1 < \log n < \underbrace{n}_{\Omega(n)} < \underbrace{n \log n}_{\Theta(n^2)} < \underbrace{n^2}_{\Omega(n^2)} \dots$$

$$\begin{array}{ccc}
 2^{2n} & & 2^n \\
 \underline{\underline{2^{2n}}} & & \underline{\underline{2^n}} \\
 \textcircled{2^n} & & \underline{\underline{2^n}} \\
 \underline{\underline{2^n}} \times \underline{\underline{2^n}} \times \underline{\underline{2^n}} & \text{--- n times ---} &
 \end{array}$$

$$\begin{array}{ccc}
 2^{n+1} & & 2^{2n+1} \\
 \underline{\underline{2^{n+1}}} & & \underline{\underline{2^{2n+1}}} \\
 \downarrow & & \downarrow \\
 2 \times 2^n & & 2 \times 2^{2n}
 \end{array}$$

$$\begin{array}{ccc}
 \underline{\underline{n^2}} & \frac{n^3}{n^2 \times \underline{\underline{n}}} & \frac{2n}{1} \quad \frac{3n}{1} \\
 & \downarrow & \downarrow
 \end{array}$$

$$\begin{aligned}
 \bigcirc \quad \left(\overset{n}{\uparrow} f(n) + \overset{n^2}{\uparrow} g(n) \right) &= O(\underline{\underline{\max(f(n), g(n))}}) \\
 \bigcirc \quad \underline{(n + n^2)} &= O(\underline{\underline{n^2}})
 \end{aligned}$$

Example 1:**Input:**

N = 5

arr[] = {1,2,3,4,5}

Output: 6**Explanation:** Smallest positive missing number is 6.**Example 2:****Input:**

N = 5

arr[] = {0,-10,1,3,-20}

Output: 2**Explanation:** Smallest positive missing number is 2. $[0, -10, \underline{1}, 3, -20]$ $\underline{1}, 2, 3, 4, \dots \quad \underline{\underline{O(n)}}$
↑ $[\underline{1}, \underline{\underline{n+1}}]$

Input:
 $N = 5$
 $Arr[] = \{1, 2, 3, -2, 5\}$
Output:
 9
Explanation:
 Max subarray sum is 9
 of elements $(1, 2, 3, -2, 5)$ which
 is a contiguous subarray.

$$\begin{array}{c}
 [1, 2, 3, -2, 5] \\
 \hline
 6 \\
 \hline
 \boxed{9}
 \end{array}$$

Example 2:

Input:
 $N = 4$
 $Arr[] = \{-1, -2, -3, -4\}$
Output:
 -1
Explanation:
 Max subarray sum is -1
 of element (-1)

$$\begin{array}{c}
 [1, 2, -10, 1, 5] \\
 \hline
 6 \\
 \hline
 \boxed{9}
 \end{array}$$

$\begin{array}{ccccccc} 1 & 2 & 3 & & & & n \\ n & n-1 & n-2 & \dots & & & 1 \end{array}$
 $\underline{\underline{O(n^2)}}$

$$\begin{array}{cccccc}
 & 0 & 1 & 2 & 3 & 4 \\
 [& 1 & 2 & -10 & 1 & 5] \\
 \text{max-till-here:} & 1 & 3 & \underline{\underline{-7}} & \underline{\underline{1}} & \boxed{6}
 \end{array}$$

$$mth[0] = arr[0]$$

$$\begin{aligned}
 i \geq 1 : \quad mth[i] &= mth[i-1] + arr[i] \\
 &\quad \text{if } mth[i-1] > 0 \\
 mth[i] &= arr[i] \quad \text{otherwise}
 \end{aligned}$$

$mth[i]$ = maximum sum of any subarray
 ending EXACTLY at index i .

$$TC: O(n) \quad Aux \text{ space} = \underline{\underline{O(n)}}$$

	0	1	2	3	4	5
arr:	1	2	-1	1	3	-2
<u>nth:</u>	1	3	<u>2</u>	<u>3</u>	<u>6</u>	<u>4</u>

Input : arr[] = {1, 3, 5, 5, 5, 5, 67, 123, 125}
x = 5

Output : First Occurrence = 2
Last Occurrence = 5

Input : arr[] = {1, 3, 5, 5, 5, 5, 7, 123, 125 }
x = 7

Output : First Occurrence = 6
Last Occurrence = 6

0	1	2	3	4	5	6	7
1	3	5	5	5	5	67	123
			<u>5</u>				

x = 5

low = 0 high = 7

mid = $\frac{0+7}{2} = 3$ first_occ = 3
 \swarrow
arr[mid] = 5

low = 0 high = 2

mid = $\frac{0+2}{2} = 1$ (arr[mid] < x)

low = 2 high = 2

mid = $\frac{2+2}{2} = 2$

first_occ = 2

$$\checkmark \quad \text{ans[mid]} == x$$

(low = 2 high = 1) STOP!