

MFE 409 LECTURE 8

LIQUIDITY RISK

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LECTURE OBJECTIVES

- Market liquidity
- Funding liquidity
- How to measure them?
- Liquidity crises

LIQUIDITY

- Liquidity: ability to make payments when they are due
- Two dimensions to liquidity:
 - ① **Market liquidity**, or trading liquidity
 - ② **Funding liquidity**
- The two dimensions interact

OUTLINE

① MARKET LIQUIDITY

② FUNDING LIQUIDITY

③ LIQUIDITY CRISES

MARKET LIQUIDITY

- **Market liquidity:** Ability to sell an asset on short notice
- Price received for an asset depends on:
 - ▶ Mid-market price
 - ▶ How much is to be sold
 - ▶ How quickly it is to be sold
 - ▶ The economic environment

BID-ASK SPREAD

- Ask price (or offer price): price at which one can buy
- Bid price: price at which one can sell
- Role of *size*



COST OF LIQUIDATION

- Proportional bid-ask spread:

$$s = \frac{\text{Ask Price} - \text{Bid Price}}{\text{Mid-market Price}}$$

- Cost of liquidating a portfolio with positions α_i right now:

$$\sum_{i=1}^n \frac{1}{2} |\alpha_i| s_i(\alpha_i)$$

- Stressed conditions: replace s_i by extreme historical value, e.g. 1% largest
- *Liquidity-adjusted VaR*: If portfolio is likely liquidated in extreme bad performance, add liquidation cost to VaR calculation

ROLE OF TIME

- Role of *time*
 - ▶ Example: selling a house tomorrow vs over the next month
- Trade-off for executing a trade:
 - ▶ Selling slowly avoids large trading costs
 - ▶ Selling slowly increases the risk of adverse price movement

OPTIMAL EXECUTION

- You want to sell S shares over the next n days
- The bid-ask difference is $p(q)$ where q is the quantity sold on that day
- The daily standard deviation of price changes is σ
- Formalize the problem of optimal execution

$$\begin{aligned} \min_{\{q_t\}} \quad & \lambda \sqrt{\sum_{t=1}^n \sigma^2 x_t^2} + \sum_{t=1}^n \frac{1}{2} |q_t| p(q_t) \\ \text{such that} \quad & \sum_{t=1}^n q_t = S \\ & x_1 = S \\ & x_t = x_{t-1} - q_{t-1} \end{aligned}$$

- Solve it for $p(q) = 0.1 + 0.05 \exp(0.03 \times q)$, $S = 100$, $n = 5$, $\sigma = 0.1$

FIRE SALES

- Bid-ask spread might be the tip of the iceberg for illiquidity
- **Fire sale:** In periods of deep market distress, many investors might want to sell, and few are ready to buy, so the whole price is lower
- Fire sales are difficult to tell apart from justified low prices
 - ▶ Chodorow-Reich, Ghent, Haddad (2020): *Asset insulators*: Valuation of institutions that sit out the fire sale should not respond to the drop in prices

OUTLINE

① MARKET LIQUIDITY

② FUNDING LIQUIDITY

③ LIQUIDITY CRISES

FUNDING LIQUIDITY

- **Funding liquidity:** Ability to maintain sources of funding for running the firm's activities
- Sources of funding liquidity:
 - ▶ Cash and Treasury holdings
 - ▶ Ability to borrow
 - ▶ Retail and wholesale deposits
 - ▶ Central bank borrowing

QUANTIFYING LIQUIDITY RISK

- Difficult to quantify liquidity risk
- Some measures from Basel III:
 - ▶ *Liquidity coverage ratio*: designed to make sure that the bank can survive a 30-day period of acute stress
 - ▶ *Net stable funding ratio*: a longer term measure designed to ensure that stability of funding sources is consistent with the permanence of the assets that have to be funded

OUTLINE

① MARKET LIQUIDITY

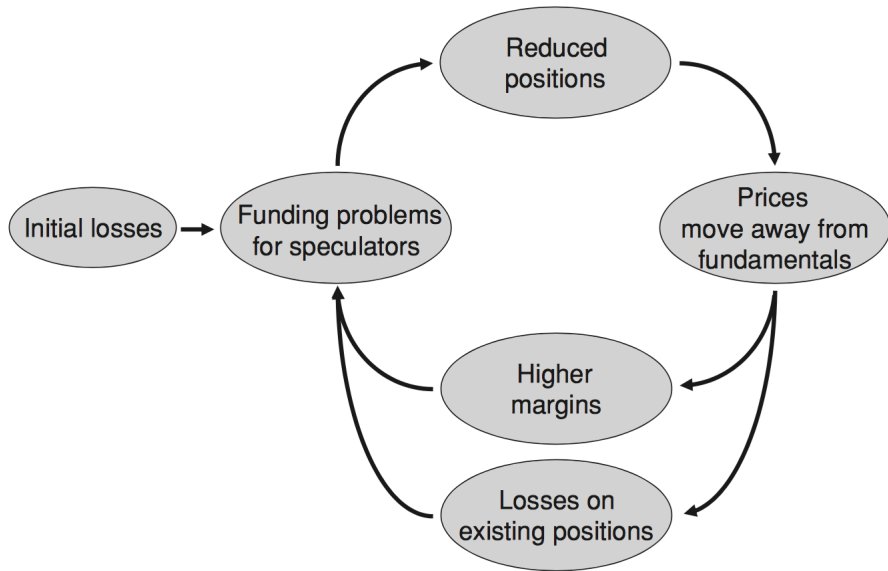
② FUNDING LIQUIDITY

③ LIQUIDITY CRISES

LIQUIDITY CRISES

- In a simple view of markets, trading stabilizes prices
 - ▶ If somebody gets in trouble and has to liquidate some assets ...
 - ▶ Somebody else sees this as a buying opportunity
 - ▶ *Negative feedback trading*: price drop creates buying, which pushes price up
- But market frictions can lead to unstable prices: positive feedback trading
 - ▶ Remember LTCM

LIQUIDITY SPIRALS



PREPARING FOR LIQUIDITY CRISES

- Fatalist view: when everything goes bad, there is nothing to do
- Some useful steps:
 - ▶ Plan for the lifetime of the strategy
 - ▶ Analyze correlation of strategy performance and funding conditions
 - ▶ Understand behavior of other participants in the markets: if everybody does the same thing, everybody will fall at the same time
- Even risk management regulations could generate liquidity crises!

TAKEAWAYS

- Liquidity problems can prevent ability to run a strategy or a business
- Stem from limited ability to:
 - ▶ Sell assets: market liquidity
 - ▶ Borrow to finance trade: funding liquidity
 - ▶ Both
- Liquidity risk is difficult to quantify ...
- But being aware of sources of liquidity and market environment can help