

The result of the tensor product is following:

$$\begin{aligned}
 & H \otimes I \otimes I \\
 & \downarrow \\
 & \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 \end{bmatrix} \times \begin{bmatrix} \frac{a}{\sqrt{2}} \\ \frac{b}{\sqrt{2}} \\ 0 \\ 0 \\ \frac{a}{\sqrt{2}} \\ \frac{b}{\sqrt{2}} \\ 0 \\ 0 \end{bmatrix} = \frac{1}{\sqrt{2}} \begin{bmatrix} \frac{a}{\sqrt{2}} \\ \frac{b}{\sqrt{2}} \\ \frac{b}{\sqrt{2}} \\ \frac{a}{\sqrt{2}} \\ \frac{a}{\sqrt{2}} \\ \frac{b}{\sqrt{2}} \\ -\frac{b}{\sqrt{2}} \\ -\frac{a}{\sqrt{2}} \end{bmatrix} = \frac{1}{2} \begin{bmatrix} \frac{a}{\sqrt{2}} |000\rangle \\ \frac{b}{\sqrt{2}} |001\rangle \\ \frac{b}{\sqrt{2}} |010\rangle \\ \frac{a}{\sqrt{2}} |011\rangle \\ \frac{a}{\sqrt{2}} |100\rangle \\ \frac{b}{\sqrt{2}} |101\rangle \\ -\frac{b}{\sqrt{2}} |110\rangle \\ -\frac{a}{\sqrt{2}} |111\rangle \end{bmatrix}
 \end{aligned}$$

Another way (ket notation) to write the above state is:

$$\begin{aligned}
 & \Rightarrow \frac{1}{2} [a|000\rangle + b|001\rangle + b|010\rangle + a|011\rangle + a|100\rangle - b|101\rangle - b|110\rangle + a|111\rangle] \\
 & \Rightarrow \frac{1}{2} [|00\rangle (a|0\rangle + b|1\rangle) + |01\rangle (a|1\rangle + b|0\rangle) + |10\rangle (a|0\rangle - b|1\rangle) + |11\rangle (a|1\rangle - b|0\rangle)]
 \end{aligned}$$

This is the final state of all 3 qubits. We measure the qubits α & β now. The result will be either of the four states which are:

$$|00\rangle, |01\rangle, |10\rangle, |11\rangle$$

If its $|00\rangle$ we apply the I transformation which means we don't do anything to γ . Following are the operations that we in all 4 cases.

$ \alpha\beta\rangle$	$ \gamma\rangle$	operator
$ 00\rangle$	$a 0\rangle + b 1\rangle$	I
$ 01\rangle$	$a 1\rangle + b 0\rangle$	X
$ 10\rangle$	$a 0\rangle - b 1\rangle$	Y
$ 11\rangle$	$a 1\rangle - b 0\rangle$	Z