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~~Lab 5~~

S. Gary Wolf

Algorithm

Initialize the population of wolves (positions) randomly within the search space

Define the maximum number of iterations (T) and population size (N)

Define the fitness function to evaluate solutions

Evaluate the fitness of each wolf in the population
Identify the alpha (best solution), beta (second-best) and delta (third-best) wolves

For $t = 1$ to T :

For each wolf i in the population:

For each dimension d :

$$A_1 = 2 * a * \text{rand}() - a$$

$$C_1 = 2 * \text{rand}()$$

$$D_{\alpha} = |C_1 * X_{\alpha}[d] - x_i[d]|$$

$$x_1 = X_{\alpha}[d] - A_1 * D_{\alpha}$$

$$A_2 = 2 * a * \text{rand}() - a$$

$$C_2 = 2 * \text{rand}()$$

$$D_{\beta} = |C_2 * X_{\beta}[d] - x_i[d]|$$

$$x_2 = X_{\beta}[d] - A_2 * D_{\beta}$$

$$A_3 = 2 * a * \text{rand}() - a$$

$$C_3 = 2 * \text{rand}()$$

$$D_{\delta} = |C_3 * X_{\delta}[d] - x_i[d]|$$

$$x_3 = X_{\delta}[d] - A_3 * D_{\delta}$$

$$x_i[d] = (x_1 + x_2 + x_3) / 3$$

End For

End For

$$a = 2 - (2 * t / T)$$

Update alpha, beta and delta wolves based on fitness

End for

Program
import numpy as np

def grey_wolf_optimizer(fitness_function,
num_wolves, num_dimensions,
max_iterations, bounds):

lower_bound, upper_bound = bounds
wolves = np.random.uniform(lower_bound,
upper_bound, (num_wolves, num_dimensions))
alpha, beta, delta = None, None, None

fitness = np.array([fitness_function(wolf) for wolf
in wolves])

sorted_indices = fitness.argsort()

alpha, beta, delta = wolves[sorted_indices[:3]]

$\alpha = 2$

for iteration in range(max_iterations):

for i in range(num_wolves):

for d in range(num_dimensions):

$r1, r2 = np.random.rand(), np.random.rand()$

$A1 = 2 * \alpha * r1 - \alpha$

$C1 = 2 * r2$

$D_alpha = abs(C1 * alpha[d] - wolves[i, d])$

$X1 = alpha[d] - A1 * D_alpha$

$r1, r2 = np.random.rand(), np.random.rand()$

$A2 = 2 * \alpha * r1 - \alpha$

$C2 = 2 * r2$

$D_beta = abs(C2 * beta[d] - wolves[i, d])$

$X2 = beta[d] - A2 * D_beta$


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x1, x2 = np.random.randn(), np.random.randn()
A3 = 2 * a * x1 - a
C3 = 2 * x2
D_delta = abs(C3 * delta[d] - wolves[i, d])
x3 = delta[d] - A3 * D_delta

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wolves[i, d] = (x1 + x2 + x3) / 3

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wolves[i] = np.clip(wolves[i], lower_bound,
                    upper_bound)

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fitness = np.array([fitness_function(wolf) for
                    wolf in wolves])

```

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sorted_indices = fitness.argsort()

```

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alpha, beta, delta = wolves[sorted_indices[:3]]

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a = 2 - (2 * iteration / max_iterations)

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best_solution = alpha

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best_fitness = fitness_function(alpha)

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return best_solution, best_fitness

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if __name__ == "__main__":

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    def fitness_function(x)

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        return np.sum(x**2)

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    num_wolves = 30

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    num_dimensions = 5

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    max_iterations = 100

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    bounds = (-10, 10)

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    best_solution, best_fitness = grey_wolf_optimizer

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        (fitness_function, num_wolves, num_dimensions,
         max_iterations, bounds)

```

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print("Best solution:", best_solution)
print("Best Fitness:", best_fitness)
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Output

Best solution: $[-7.85e-12 \quad -7.36e-12, -8.765e-12]$
 $8.354e-12 \quad 8.366e-12]$

Best Fitness: $3.32219e-22$.