

Problem 5: Dry Run & Analyze - Time and Space Complexity

1. Function: printTriangle(int n)

```
void printTriangle(int n) {  
    for (int i = 0; i < n; i++)  
        for (int j = 0; j <= i; j++)  
            System.out.print("*");  
}
```

Dry Run for n = 4:

- $i = 0 \rightarrow j = 0 \rightarrow$ print 1 star
- $i = 1 \rightarrow j = 0, 1 \rightarrow$ print 2 stars
- $i = 2 \rightarrow j = 0, 1, 2 \rightarrow$ print 3 stars
- $i = 3 \rightarrow j = 0, 1, 2, 3 \rightarrow$ print 4 stars

Total stars printed = $1 + 2 + 3 + 4 = 10$

Time Complexity: $O(n^2)$

Space Complexity: $O(1)$

2. Function: printPattern(int n)

```
void printPattern(int n) {  
    for (int i = 1; i <= n; i *= 2)  
        for (int j = 0; j < n; j++)  
            System.out.println(i + "," + j);  
}
```

Dry Run for n = 8:

- $i = 1 \rightarrow j = 0 \text{ to } 7 \rightarrow 8 \text{ iterations}$
- $i = 2 \rightarrow 8 \text{ iterations}$
- $i = 4 \rightarrow 8 \text{ iterations}$
- $i = 8 \rightarrow 8 \text{ iterations}$

Total Iterations = $4 \text{ (outer)} \times 8 \text{ (inner)} = 32$

Time Complexity: $O(n \log n)$

Space Complexity: $O(1)$

3. Function: `recHalf(int n)`

```
void recHalf(int n) {
    if (n <= 0) return;
    System.out.print(n + " ");
    recHalf(n / 2);
}
```

Dry Run for n = 20:

- `recHalf(20)` → print 20
- `recHalf(10)` → print 10
- `recHalf(5)` → print 5
- `recHalf(2)` → print 2
- `recHalf(1)` → print 1
- `recHalf(0)` → return

Printed values: 20 10 5 2 1

Total recursive calls = 6

Time Complexity: $O(\log n)$

Space Complexity: $O(\log n)$

4. Function: `fun(int n)`

```
void fun(int n) {
    if (n == 0) return;
    fun(n - 1);
    fun(n - 1);
}
```

Dry Run for n = 3:

- $T(3) = 2 \times T(2) = 2 \times (2 \times T(1)) = 2 \times 2 \times (2 \times T(0)) = 2^3 = 8$ total calls

Total calls = 8

Time Complexity: $O(2^n)$

Space Complexity: $O(n)$

5. Function: `tripleNested(int n)`

```
void tripleNested(int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            for (int k = 0; k < n; k++)
                System.out.println(i + j + k);
}
```

Dry Run for n = 3:

- i: 0 to 2 → 3 iterations
- j: 0 to 2 → 3 iterations
- k: 0 to 2 → 3 iterations

Total Iterations = $3 \times 3 \times 3 = 27$

Time Complexity: $O(n^3)$

Space Complexity: $O(1)$

