

1. Application in Mechanics and dy/dx as a Rate Measure

1. Velocity and Acceleration in Rectilinear Motion

- Question: 1** The distance travelled s (in metre) by a particle in t second is given by $s = t^3 + 2t^2 + t$. The speed of the particle after 1 sec. will be
 (a) 8 cm/sec. (b) 6 cm/sec. (c) 2 cm/sec (d) None of these
- Question: 2** A particle moves in a straight line in such a way that its velocity at any point is given by $v^2 = 2 - 3x$, where x is measured from a fixed point. The acceleration is
 (a) Zero (b) Uniform (c) Non-uniform (d) Indeterminate
- Question: 3** The position of a point in time ' t ' is given by $x = a + bt - ct^2$, $y = a + bt^2$. Its acceleration at time ' t ' is
 (a) $b - c$ (b) $(b + c)$ (c) $2b - 2c$ (d) $2\sqrt{b^2 + c^2}$
- Question: 4** If the path of a moving point is the curve $x = at$, $y = bs \sin at$, then its acceleration at any instant [SCRA 1996]
 (a) Is constant (b) Varies as the distance from the axis of x
 (c) Varies as the distance from the axis of y (d) Varies as the of the point from the origin
- Question: 5** A stone thrown vertically upwards from the surface of the moon at velocity of 24 m/sec. reaches a height of $s = 24t - 0.8t^2$ m after t sec. The acceleration due to gravity in m/sec^2 at the surface of the moon is [MP PET 1992]
 (a) 0.8 (b) 1.6 (c) 2.4 (d) 4.9

2. Derivative as the Rate of Change

- Question: 6** The rate of change of the surface area of a sphere of radius r when the radius is increasing at the rate of 2 cm/sec is proportional to
 (a) $\frac{1}{r}$ (b) $\frac{1}{r^2}$ (c) r (d) r^2
- Question: 7** If the volume of a spherical balloon is increasing at the rate of 900 cm^3/sec . then the rate of change of radius of balloon at instant when radius is 15 cm [in cm/sec]
 (a) $\frac{22}{7}$ (b) 22 (c) $\frac{7}{22}$ (d) None of these
- Question: 8** A man of height 1.8 m is moving away from a lamp post at the rate of 1.2 m/sec. If the height of the lamp post be 4.5 meter, then the rate at which the shadow of the man is lengthening
 (a) 0.4 m/sec (b) 0.8 m/sec. (c) 1.2 m/sec. (d) None of these
- Question: 9** A 10 cm long rod AB moves with its ends on two mutually perpendicular straight lines OX and OY . If the end A be moving at the rate of 2 cm/sec. then when the distance of A from O is 8 cm, the rate at which the end B is moving, is [SCRA 1996]
 (a) $\frac{8}{3}$ cm/sec (b) $\frac{4}{3}$ cm/sec (c) $\frac{2}{9}$ cm/sec. (d) None of these

Assignment

Application in Mechanics

Basic Level

- The displacement of a particle in time t is given by $s = 2t^2 - 3t + 1$. The acceleration is
(a) 1 (b) 3 (c) 4 (d) 5
- A stone is falling freely and describes a distance s in t seconds given by equation $s = \frac{1}{2}gt^2$. The acceleration of the stone is
(a) Uniform (b) Zero (c) Non-uniform (d) Indeterminate
- The velocity of a particle at time t is given by the relation $v = 6t - \frac{t^2}{6}$. The distance travelled in 3 seconds is, if $s = 0$ at $t = 0$
(a) $\frac{39}{2}$ (b) $\frac{57}{2}$ (c) $\frac{51}{2}$ (d) $\frac{33}{2}$
- The equation of motion of a car is $s = t^2 - 2t$, where t is measured in hours and s in kilometers. when the distance travelled by the car is 15 km, the velocity of the car is
(a) 2 km/h (b) 4 km/h (c) 6 km/h (d) 8 km/h
- A particle is moving in a straight line according as $s = 45t + 11t^2 - t^3$, then the time when it will come to rest, is
(a) - 9 seconds (b) $\frac{5}{3}$ seconds (c) 9 seconds (d) $-\frac{5}{3}$ seconds
- If $t = \frac{v^2}{2}$, then $\left(-\frac{df}{dt}\right)$ is equal to (where f is acceleration) [MP PET 1991]
(a) f^2 (b) f^3 (c) $-f^2$ (d) $-f^3$
- A particle is moving in a straight line according to the formula $s = t^2 + 8t + 12$. If s be measured in meters and t be measured in seconds then the average velocity of the particle in third second is
(a) 14 m/sec (b) 13 m/sec (c) 15 m/sec (d) None of these
- If $2t = v^2$, then dv/dt is equal to
(a) 0 (b) $\frac{1}{4}$ (c) $\frac{1}{2}$ (d) $\frac{1}{v}$
- The equation of motion of a particle moving along a straight line is $s = 2t^3 - 9t^2 + 12t$, where the units of s and t are cm and sec. The acceleration of the particle will be zero after
(a) $\frac{3}{2}$ sec (b) $\frac{2}{3}$ sec (c) $\frac{1}{2}$ sec (d) Never
- A body moves according to the formula $v = 1 + t^2$, where v is the velocity at time t . The acceleration after 3 sec will be (v in cm/sec) [MP PET 1988]
(a) 24 cm/sec² (b) 12 cm/sec² (c) 6 cm/sec² (d) None of these
- A particle moves in a straight line so that its velocity at any point is given by $v^2 = a + bx$, where $a, b \neq 0$ are constant. The acceleration is
(a) Zero (b) Uniform (c) Non-uniform (d) Indeterminate

12. The distance in seconds, described by a particle in t seconds is given by $s = ae^t + \frac{b}{e^t}$. The acceleration of the particle at time t is
 (a) Proportional to t (b) Proportional to s (c) s (d) Constant
13. A stone thrown vertically upwards rises ' s ' metre in t seconds, where $s = 80t - 16t^2$, then velocity after 2 seconds is [SCRA 1996]
 (a) 8 m per sec. (b) 16 m per sec. (c) 32 m per sec. (d) 64 m per sec.
14. If the distance ' s ' travelled by a particle in time t is $s = asint + b\cos 2t$, then the acceleration at $t = 0$ is
 (a) a (b) $-a$ (c) $4b$ (d) $-4b$
15. If the distance travelled by a point in time t is $s = 180t - 16t^2$, then the rate of change in velocity is
 (a) $-16 t$ unit (b) 48 unit (c) -32 unit (d) None of these
16. The motion of stone thrown up vertically is given by $s = 13.8t - 4.9t^2$, where s is in metres and t is in seconds. Then its velocity at $t = 1$ second is
 (a) 3 m/s (b) 5 m/s (c) 4 m/s (d) None of these
17. A particle is moving in a straight line. Its displacement at time t is given by $s = -4t^2 + 2t$, then its velocity and acceleration at time $t = \frac{1}{2}$ second are
 (a) $-2, -8$ (b) $2, 6$ (c) $-2, 8$ (d) $2, 8$
18. A ball thrown vertically upwards falls back on the ground after 6 seconds. Assuming that the equation of motion is of the form $s = ut - 4.9t^2$, where s is in metres and t is in seconds, find the velocity at $t = 0$
 (a) 0 m/s (b) 1 m/s (c) 29.4 m/s (d) None of these
19. A particle is moving in a straight line according as $s = \sqrt{1+t}$, then the relation between its acceleration (a) and velocity (v) is
 (a) $a \propto v^2$ (b) $a \propto v^3$ (c) $a \propto \frac{1}{v^3}$ (d) $a \propto v$
20. The distance travelled by a particle moving in a straight line in time t is $s = \sqrt{at^2 + bt + c}$. Acceleration of the particle is
 (a) Proportional to t (b) Proportional to s (c) Proportional to s^{-3} (d) None of these

[Kerala (Engg.) 2002]

Advance Level

21. A particle is moving along the curve $x = at^2 + bt + c$. If $ac = b^2$, then the particle would be moving with uniform [Orissa JEE 2002]
 (a) Rotation (b) Velocity (c) Acceleration (d) Retardation
22. The equations of motion of two stones thrown vertically upwards simultaneously are $s = 19.6t - 4.9t^2$ and $s = 9.8t - 4.9t^2$ respectively and the maximum height attained by the first one is h . When the height of the first stone is maximum, the height of the second stone will be
 (a) $h/3$ (b) $2h$ (c) h (d) 0
23. A particle is moving on a straight line, where its position s (in metres) is a function of time t (in seconds) given by $s = at^2 + bt + 6$, $t \geq 0$. If it is known that the particle comes to rest after 4 seconds at a distance of 16 metres from the starting position ($t = 0$), then the retardation in its motion is
 (a) -1 m/sec^2 (b) $\frac{5}{4} \text{ m/sec}^2$ (c) $-\frac{1}{2} \text{ m/sec}^2$ (d) $-\frac{5}{4} \text{ m/sec}^2$
24. A point moves in a straight line during the time $t = 0$ to $t = 3$ according to the law $s = 15t - 2t^2$. The average velocity is

[MP PET 1992]

SPECTRUM CAREER INSTITUTE

AOD-1

- (a) 3 (b) 9 (c) 15 (d) 27
25. The equation of motion of a stone, thrown vertically upwards is $s = ut - 6.3t^2$, where the units of s and t are cm and sec . If the stone reaches at maximum height in $3sec$. then $u =$
- (a) 18.9 cm/sec (b) 12.6 cm/sec (c) 37.8 cm/sec (d) None of these

Rate Measures

Basic Level

26. Radius of a circle is increasing uniformly at the rate of 3 cm/sec . The rate of increase of area when radius is 10 cm , will be
- (a) $\pi\text{ cm}^2/\text{s}$ (b) $2\pi\text{ cm}^2/\text{s}$ (c) $10\pi\text{ cm}^2/\text{s}$ (d) None of these
27. A 10 cm long rod AB moves with its ends on two mutually perpendicular straight lines OX and OY . If the end A be moving at the rate of 2 cm/sec , then when the distance of A from O is 8 cm , the rate at which the end B is moving, is [SCRA 1996]
- (a) $\frac{8}{3}\text{ cm/sec}$ (b) $\frac{4}{3}\text{ cm/sec}$ (c) $\frac{2}{9}\text{ cm/sec}$ (d) None of these
28. If $y = x^3 + 5$ and x changes from 3 to 2.99 , then the approximate change in y is
- (a) 2.7 (b) $-.27$ (c) 27 (d) None of these
29. The volume of a spherical balloon is increasing at the rate of 40 cubic centimetre per minute. The rate of change of the surface of the balloon at the instant when its radius is 8 centimetres, is
- (a) $\frac{5}{2}\text{ sq cm/min.}$ (b) 5 sq cm/min. (c) 10 sq cm/min. (d) 20 sq cm/min.
30. A ladder 5 m in length is resting against vertical wall. The bottom of the ladder is pulled along the ground away from the wall at the rate of 1.5 m/sec . The length of the highest point of the ladder when the foot of the ladder is 4.0 m away from the wall decreases at the rate of
- (a) 2 m/sec (b) 3 m/sec (c) 2.5 m/sec (d) 1.5 m/sec
31. If the rate of increase of area of a circle is not constant but the rate of increase of perimeter is constant, then the rate of increase of area varies
- (a) As the square of the perimeter (b) Inversely as the perimeter (c) As the radius (d)

Advance Level

32. Gas is being pumped into a spherical balloon at the rate of $30\text{ ft}^3/\text{min}$. Then the rate at which the radius increases when it reaches the value 15 ft is
- (a) $\frac{1}{30\pi}\text{ ft/min.}$ (b) $\frac{1}{15\pi}\text{ ft/min.}$ (c) $\frac{1}{20}\text{ ft/min.}$ (d) $\frac{1}{25}\text{ ft/min.}$
33. On dropping a stone in stationary water circular ripples are observed. Rate of flow of ripples is 6 cm/sec . When radius of the circle is 10 cm , then fluid rate of increase in its area is
- (a) $120\pi\text{ cm/sec}$ (b) 120 sq cm/sec (c) $\pi\text{ sq cm/sec}$ (d) $120\pi\text{ sq cm/sec}$
34. If the edge of a cube increases at the rate of 60 cm per second , at what rate the volume is increasing when the edge is 90 cm
- (a) $486000\text{ cu cm per sec}$ (b) $1458000\text{ cu cm per sec}$ (c) $43740000\text{ cu cm per sec}$ (d) None of these
35. If a spherical balloon has a variable diameter $3x + \frac{9}{2}$, then the rate of change of its volume with respect to x is
- (a) $27\pi(2x+3)^2$ (b) $\frac{27\pi}{16}(2x+3)^2$ (c) $\frac{27\pi}{8}(2x+3)^2$ (d) None of these
36. Two cyclists start from the junction of two perpendicular roads, their velocities being $3v$ metres/minute and $4v$ metres/minute. The rate at which the two cyclists are separating is
- (a) $\frac{7}{2}v\text{ m/min}$ (b) $5v\text{ m/min}$ (c) $v\text{ m/min}$ (d) None of these

SPECTRUM CAREER INSTITUTE

AOD-1

37. A stick of length a cm rests against a vertical wall and the horizontal floor. If the foot of the stick slides with a constant velocity of b cm/s then the magnitude of the velocity of the middle point of the stick when it is equally inclined with the floor and the wall, is
- (a) $\frac{b}{\sqrt{2}}$ cm/s (b) $\frac{b}{2}$ cm/s (c) $\frac{ab}{2}$ cm/s (d) None of these
38. If $y = \int_0^x \frac{t^2}{\sqrt{t^2+1}} dt$ then the rate of change of y with respect to x when $x=1$, is
- (a) $\sqrt{2}$ (b) $1/2$ (c) $1/\sqrt{2}$ (d) None of these



Dr. ANOOP DIXIT @ SPECTRUM CAREER INSTITUTE

Contact: 9810683007, 9811683007, 9810283007, www.spectrumanoop.in

Centres: 1. Shipra Suncity Indirapuram Gzb 2. Sector 122 Noida 3. Sector 49 Noida