

The governing equation is  $\frac{\partial T}{\partial t} = \alpha \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right)$  and for steady state, we have  $\frac{\partial T}{\partial t} = 0$

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In[*]:= nx = 21; ny = 21;
        Δx =  $\frac{1}{nx - 1}$ ; Δy =  $\frac{1}{ny - 1}$ ;
        k = 1; h = 10; T0 = 300; Tleft = 350;
        T = Array["T", {nx, ny}];

In[*]:= discreteEqns = Table[
         $\frac{T[[i + 1, j]] - 2 T[[i, j]] + T[[i - 1, j]]}{\Delta x^2} + \frac{T[[i, j + 1]] - 2 T[[i, j]] + T[[i, j - 1]]}{\Delta y^2} == 0,$ 
        {i, 2, nx - 1}, {j, 2, ny - 1}];

In[*]:= leftBoundary = Table[T[[1, j]] == Tleft, {j, 2, ny - 1}];
        topBoundary = Table[T[[i, ny]] == T[[i, ny - 1]], {i, 1, nx}];
        bottomBoundary = Table[T[[i, 1]] == T[[i, 2]], {i, 1, nx}];
        rightBoundary =
        Table[ $-\frac{k}{\Delta x} (T[[nx, j]] - T[[nx - 1, j]]) == h (T[[nx, j]] - T_0),$  {j, 2, ny - 1}];

In[*]:= eqns = Join[Flatten[discreteEqns],
        leftBoundary, topBoundary, rightBoundary, bottomBoundary];

In[*]:= sol = NSolve[eqns, Flatten[T]];

In[*]:= TVals = T /. sol // #[[1]] &;

In[*]:= ListContourPlot[Transpose[TVals], PlotLegends → Automatic]

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Out[\*] =

