

The governing equation is $\frac{\partial T}{\partial t} = \alpha \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right)$ and for steady state, we have $\frac{\partial T}{\partial t} = 0$

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In[*]:= nx = 21; ny = 21;
Δx =  $\frac{1}{nx - 1}$ ; Δy =  $\frac{1}{ny - 1}$ ;
k = 1; h = 10; T0 = 300; Tleft = 350; α = 1;
u = 1; v = 2;
T = Array["T", {nx, ny}];

In[*]:= discreteEqns = Table[
  u  $\frac{T[[i, j]] - T[[i - 1, j]]}{\Delta x}$  + v  $\frac{T[[i, j]] - T[[i, j - 1]]}{\Delta y}$  ==
  α  $\left( \frac{T[[i + 1, j]] - 2 T[[i, j]] + T[[i - 1, j]]}{\Delta x^2} + \frac{T[[i, j + 1]] - 2 T[[i, j]] + T[[i, j - 1]]}{\Delta y^2} \right)$ ,
  {i, 2, nx - 1}, {j, 2, ny - 1}];

In[*]:= leftBoundary = Table[T[[1, j]] == Tleft, {j, 2, ny - 1}];
topBoundary = Table[T[[i, ny]] == T[[i, ny - 1]], {i, 1, nx}];
bottomBoundary = Table[T[[i, 1]] == 280, {i, 1, nx}];
rightBoundary =
  Table[ $\frac{-k}{\Delta x} (T[[nx, j]] - T[[nx - 1, j]]) == h (T[[nx, j]] - T_0)$ , {j, 2, ny - 1}];

In[*]:= eqns = Join[Flatten[discreteEqns],
  leftBoundary, topBoundary, rightBoundary, bottomBoundary];

In[*]:= sol = NSolve[eqns, Flatten[T]];

In[*]:= TVals = T /. sol // #[[1]] &;

In[*]:= ListContourPlot[Transpose[TVals], PlotLegends → Automatic]

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