

Data Structures & Algorithms Notes

Comprehensive Reference Guide

This document provides an overview of fundamental data structures and algorithms, including definitions, properties, and example use cases. Suitable for students and interview preparation.

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1. Arrays

Definition: An array is a collection of items stored at contiguous memory locations. The idea is to store multiple items of the same type together.

Properties:

- Fixed size
- $O(1)$ access by index
- $O(n)$ search (if unsorted)

Example:

```
int arr[5] = {1, 2, 3, 4, 5};
```

Use Cases:

- Storing lists of items
- Implementing other data structures (heaps, hash tables)

2. Linked Lists

Definition: A linked list is a linear data structure where each element is a separate object, called a node, which contains data and a reference to the next node.

Types:

- Singly Linked List
- Doubly Linked List
- Circular Linked List

Properties:

- Dynamic size
- $O(1)$ insertion/deletion at head
- $O(n)$ search

Example Node (C++):

```
struct Node {  
    int data;  
    Node* next;  
};
```

Use Cases:

- Implementing stacks and queues
- Memory management

3. Stacks

Definition: A stack is a linear data structure that follows the Last In First Out (LIFO) principle.

Operations:

- push(x): Add x to the top
- pop(): Remove and return the top
- peek(): Return the top without removing

Properties:

- $O(1)$ push/pop

Use Cases:

- Function call management
- Undo operations
- Expression evaluation

4. Queues

Definition: A queue is a linear data structure that follows the First In First Out (FIFO) principle.

Operations:

- enqueue(x): Add x to the rear
- dequeue(): Remove and return the front

Types:

- Circular Queue
- Priority Queue
- Deque (Double-ended queue)

Use Cases:

- Scheduling
- Buffer management

5. Trees

Definition: A tree is a hierarchical data structure consisting of nodes, with a single root node and potentially many levels of additional nodes.

Types:

- Binary Tree
- Binary Search Tree (BST)
- AVL Tree
- Heap

Properties:

- Recursive structure
- Used for hierarchical data

Use Cases:

- File systems
- Databases (B-trees)
- Expression parsing

6. Graphs

Definition: A graph is a collection of nodes (vertices) and edges connecting pairs of nodes.

Types:

- Directed/Undirected
- Weighted/Unweighted

Representations:

- Adjacency Matrix
- Adjacency List

Use Cases:

- Social networks
- Routing algorithms
- Network analysis

7. Sorting Algorithms

Common Algorithms:

- Bubble Sort: $O(n^2)$
- Selection Sort: $O(n^2)$
- Insertion Sort: $O(n^2)$
- Merge Sort: $O(n \log n)$
- Quick Sort: $O(n \log n)$ average
- Heap Sort: $O(n \log n)$

Use Cases:

- Data organization
- Searching optimization

8. Searching Algorithms

Common Algorithms:

- Linear Search: $O(n)$
- Binary Search: $O(\log n)$ (sorted arrays)

Use Cases:

- Data retrieval
- Database queries

9. Hash Tables

Definition: A hash table is a data structure that implements an associative array, a structure that can map keys to values using a hash function.

Properties:

- $O(1)$ average-case lookup, insert, delete
- Collisions handled by chaining or open addressing

Use Cases:

- Caches
- Symbol tables
- Sets and maps

10. Recursion

Definition: Recursion is a method of solving problems where a function calls itself as a subroutine.

Properties:

- Base case and recursive case
- Used in divide and conquer algorithms

Examples:

- Factorial
- Fibonacci sequence
- Tree traversals

11. Dynamic Programming

Definition: Dynamic programming is a technique for solving problems by breaking them down into simpler subproblems and storing the results of subproblems to avoid redundant computation.

Properties:

- Overlapping subproblems
- Optimal substructure

Examples:

- Fibonacci sequence
- Knapsack problem
- Longest common subsequence