Assignment-1

Lanka Prasanna - CS20BTECH11029

Problem:

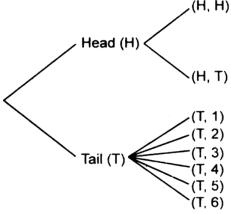
Consider the experiment of tossing a coin. If the coin shows head, toss it again but if it shows tail, then throw a die. Find the conditional probability of the event that "the die shows a number greater than 4" given that "there is at least one tail".

Solution:

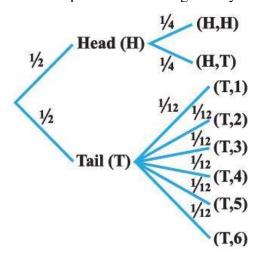
Given that a coin is tossed.

If coin shows head, it is tossed again.

If it shows tail, then a die is thrown.



Different probabilities are given by



Probabilities				
Event	Probability			
(H,H)	$\frac{1}{2}.\frac{1}{2} = \frac{1}{4}$			
(H,T)	$\frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$			
(T,1)	$\frac{1}{2}.\frac{1}{6} = \frac{1}{12}$			
(T,2)	$\frac{1}{2}.\frac{1}{6} = \frac{1}{12}$			
(T,3)	$\frac{1}{2}.\frac{1}{6} = \frac{1}{12}$			
(T,4)	$\frac{1}{2}.\frac{1}{6} = \frac{1}{12}$			
(T,5)	$\frac{1}{2}.\frac{1}{6} = \frac{1}{12}$			
(T,6)	$\frac{1}{2}.\frac{1}{6} = \frac{1}{12}$			

Let $X \in \{0,1\}$ be the random variable such that 1 represents occurrence of tail,0 represents occurrence of head when coin is tossed.

TABLE I: Probability distribution for values of X

X	P(X)			
1	$\frac{1}{2}$			
0	$\frac{1}{2}$			

Let Y denotes the getting a number on the die thrown, then the probability distribution is

TABLE II: Probability distribution for values of Y

Y	1	2	3	4	5	6
P(Y)	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	$\frac{1}{6}$

$$\begin{aligned} &\Pr(X=1) \\ &= \Pr(H,T) + \Pr(T,1) + \Pr(T,2) + \Pr(T,3) + \Pr(T,4) + \Pr(T,5) + \Pr(T,6) \\ &= \frac{1}{4} + \frac{1}{12} + \frac{1}{12} + \frac{1}{12} + \frac{1}{12} + \frac{1}{12} + \frac{1}{12} \\ &= \frac{1}{4} + \frac{6}{12} \\ &= \frac{3}{4} \end{aligned}$$

$$Pr(X = 1, Y > 4)$$
=Pr(T, 5)+Pr(T, 6)
=\frac{1}{12} + \frac{1}{12}
=\frac{1}{6}

We need Pr(Y > 4|X = 1)We know that

$$Pr(Y > 4|X = 1) = \frac{Pr(Y > 4, X = 1)}{Pr(X = 1)}$$
 (0.0.1)

$$\Pr(Y > 4|X = 1) = \frac{\frac{1}{6}}{\frac{3}{4}} = \frac{2}{9}$$
 (0.0.2)

 \therefore The required probability is $\left[\frac{2}{9}\right]$

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