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Assignment-3

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Download all latex codes from:

https://github.com/PrasannaLanka/Assignment3/blob/main/Assignment3/codes/Assignment3.tex

and python codes from

https://github.com/PrasannaLanka/Assignment3/blob/main/Assignment3/codes/Assignment3.py

PROBLEM: GATE 2002(CS)-Q.41

Four fair coins are tossed simultaneously. The probability that at least one head and one tail turn up is

- a) $\frac{1}{16}$
- b) $\frac{1}{8}$
- c) $\frac{7}{8}$
- d) $\frac{15}{16}$

SOLUTION

Let $Y \in \{0, 1\}$ be the random variable such that 1 represents occurrence of tail,0 represents occurrence of head when coin is tossed.

TABLE I: Probability distribution for values of Y

Y	P(Y)
1	$\frac{1}{2}$
0	$\frac{1}{2}$

Let the discrete random variable x is following bernoulli distribution with parameters n, p where n = 4, $p = \Pr(Y = 0) = \frac{1}{2}$ and $q = \Pr(Y = 1) = \frac{1}{2}$ Probability mass function of x successes in n trials is given by

$$Pr(X = x) = {}^{n}C_{x}p^{x}q^{n-x}$$
 (0.0.1)

$$\sum_{j=1}^{3} \Pr(X = j) = {}^{4}C_{1}(1/2)^{1}(1/2)^{3} + {}^{4}C_{2}(1/2)^{2}(1/2)^{2}$$

$$(0.0.2)^{3} + {}^{4}C_{3}(1/2)^{3}(1/2)^{4}$$

$$(0.0.3)^{3}$$

$$\sum_{j=1}^{3} \Pr(X = j) = \frac{7}{8}$$
 (0.0.4)

The required probability is $\frac{7}{8}$ \therefore **Option C is true**