```
MATRIX_MULTIPLY(A, B):

if columns(A) ≠ rows(B):

raise ValueError("Matrix multiplication is not defined.")

rows_A ← number of rows in A

cols_A ← number of columns in A

cols_B ← number of columns in B

result ← matrix of size rows_A x cols_B filled with zeros

for i from 1 to rows_A do:
    for j from 1 to cols_B do:
        sum ← 0

    for k from 1 to cols_A do:
        sum ← sum + A[i][k] * B[k][j]

result[i][j] ← sum return result
```

- 1. if columns(A)  $\neq$  rows(B): This is a conditional check which takes constant time, O(1).
- 2. rows\_A = number of rows in A, cols\_A = number of columns in A, cols\_B = number of columns in B: These operations involve reading the size details of matrices and hence, take constant time which is O(1).
- 3. result = matrix of size rows\_A x cols\_B filled with zeros: Creating a matrix of certain size can be seen as an operation that operates on every cell once, hence it can be seen as a O(rows\_A \* cols\_B) operation.
- 4. Three nested loops each of which ranges from the number of elements:

```
for i from 1 to rows_A do:
for j from 1 to cols_B do:
sum = 0
for k from 1 to cols_A do:
```

These loops indicate that for every element in the resulting matrix, we do a constant amount of work (multiplication operation). Hence, this

takes O(rows\_A \* cols\_B \* cols\_A) time.

5. sum = sum + A[i][k] \* B[k][j]: Constant time, but this operation runs once for each loop iteration described above, hence its time complexity is included in the triple nested loop's complexity.

6. result[i][j] = sum: Constant, but this runs once for each double-loop iteration described above, hence its time complexity is included in the double loop's complexity.

Adding all these, the total time complexity would be  $O(1) + O(1) + O(rows_A * cols_B) + O(rows_A * cols_B * cols_A) = O(rows_A * cols_B * cols_A)$  as this term will dominate the overall time complexity for large matrices.