## AI1110 Assignment 2

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Abstract—This document contains the solution for ICSE 2019 class 12 maths Q.15(a)

**Problem 15(a):** If a and b are perpendicular vectors,  $|\mathbf{a} + \mathbf{b}| = 13$  and  $|\mathbf{a}| = 5$ , find the value of  $|\mathbf{b}|$ . **Solution:** We know that

$$|\mathbf{a} + \mathbf{b}|^2 = |\mathbf{a}|^2 + |\mathbf{b}|^2 + 2\mathbf{a}.\mathbf{b}$$
 (1)

Given,  $\mathbf{a}$  and  $\mathbf{b}$  are perpendicular, hence  $\mathbf{a}.\mathbf{b} = 0$ , therefore substituting in (1),

$$|\mathbf{a} + \mathbf{b}|^2 = |\mathbf{a}|^2 + |\mathbf{b}|^2 \tag{2}$$

Given,

$$|\mathbf{a} + \mathbf{b}| = 13 \tag{3}$$

$$|\mathbf{a}| = 5 \tag{4}$$

Substituting (3) and (4) in (2),

$$13^2 = 5^2 + |\mathbf{b}|^2 \tag{5}$$

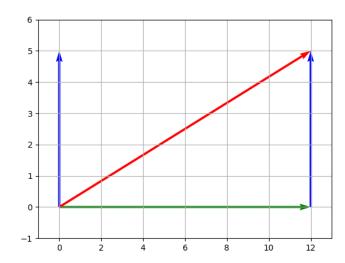
$$|\mathbf{b}|^2 = 13^2 - 5^2 \tag{6}$$

$$|\mathbf{b}|^2 = 169 - 25 \tag{7}$$

$$|\mathbf{b}|^2 = 144 \tag{8}$$

$$|\mathbf{b}| = \sqrt{144} \tag{9}$$

$$\therefore |\mathbf{b}| = 12 \tag{10}$$



1

In the figure, blue arrow with its tail at origin represents  $\mathbf{a}$ , which can also be displaced to have its tail at the coordinate (12,0) to complete the triangle. The red arrow represents  $\mathbf{a} + \mathbf{b}$  (by Triangle Law of Vector Addition) and green arrow represents  $\mathbf{b}$ . Vectors  $\mathbf{a}$  and  $\mathbf{b}$  are perpendicular,  $|\mathbf{a}| = 5$  and  $|\mathbf{a} + \mathbf{b}| = 13$ , hence by the diagram,  $|\mathbf{b}|$  should be 12 since by Baudhāyana Sulbasūtra, 5, 12, and 13 form a triplet which is quite famous  $(5^2 + 12^2 = 13^2)$ .

The output of the python code used for verification of the answer: