

SQUARE ROOT OF NUMBER

Binary search way

BRUTE →

pick element from 1 to n linearly.

```
for (i = 1 → n) {  
    if (i × i ≤ n) {  
        ans = i;  
    }  
    else break;  
}
```

1	2	3	4	5	6	7	8	9	10
✓	✓	✓	✓	✓	✓	✗	✗	✗	✗

when $(n=36)$ 26×6

any no > 6 not an answer

So whenever we get situation in which we can eliminate certain possibilities then we can think of binary search

$$n = 28$$

$$\text{low} = 1$$

$$\text{high} = 28$$

$$\text{mid} = 14 \rightarrow 14 \times 14 > 28 \therefore \text{eliminate right half}$$
$$\therefore \text{new high} = \text{mid} - 1$$

$$\text{low} = 1 \quad \text{high} = 13 \quad \text{mid} = 7 \rightarrow 7 \times 7 > 28 \therefore \text{eliminate}$$

$$\text{low} = 1 \quad \text{high} = 6 \quad \text{mid} = 3 \rightarrow 3 \times 3 < 28 \text{ eliminate left half}$$

$$\text{low} = 4 \quad \text{high} = 6 \quad \text{mid} = 5 \rightarrow 5 \times 5 < 28$$

$$\text{same} = 5 \text{ eliminate left}$$

$$\text{low} = 6 \quad \text{high} = 6 \quad \text{mid} = 6$$

$$6 \times 6 > 28 \therefore 5 \text{ is answer}$$

floor value of $\sqrt{28}$

right eliminate

$$\text{low} = 6 \quad \text{high} = 5 \text{ (end)}$$

not possible
place
always

where answer
possible always

\therefore high will have
answer
always.

here
3 can be answer
if n is not perfect
square as 28 is
to look for min if
any other no satisfy
two (\leq) condition

$f(n) \{$

low = 1; high = n;

ans = 1;

while (low <= high) {

mid = (low + high) / 2;

if (mid * mid <= n) {

ans = mid;

low = mid + 1;

}

else high = mid - 1;

}

return (high or ans);

$\log_2(n)$

to identify pattern \rightarrow range would be known
and if max or min
we have to find then
think binary search
there max was $\sqrt{5 \times 5} < 28$
(max value of
in integers) $\sqrt{28}$

FIND N^{th} ROOT OF M

$$n=3 \quad M=27 \quad \sqrt[3]{27} = 3$$

return (-1) is not an integer.

same as previous but not taking floor

$f(n, m) \{$

low = 1, high = m

while (low <= high) {

mid = (low + high) / 2;

if (f(mid, n)

value = f(mid, n);

if (value == m) return mid;

else if (value < m) low = mid + 1;

else high = mid - 1;

}

return -1;

}

time complexity $O(\log_2(m) \times \log_2(n))$

$O(\log_2(m+n))$

edge case $n=10$ $m=10^9$

now \rightarrow mid $\approx \left(\frac{10^9}{2}\right)$

func $\left(\frac{10^9}{2}, 10\right) \rightarrow$ overflow

$O(\log_2(m))$

$O(\log_2 n)$

$O(n)$

if in built power function is used

if for loop is used.

therefore
do not actually calculate $\left(\frac{10^9}{2}, 10\right)$ 10 times

just store result and whenever it crosses "m"
stop as it will be sufficient for the if condition to
work

if $m = 16$

and $4 \times 4 = 16$ stop

$5 \times 5 = 25 \rightarrow$ stop do not multiply further
 $\therefore 25 > 16$

$f(\text{num}, \text{pow}, \text{mod})$

long ans = 1;

for ($i = 1 \rightarrow \text{pow}$) {

ans = ans \times mod;

if (ans > num) return 2;

if (ans == num) return 1;
return 0;

}

\therefore rewrite previous condition

value = $f(\text{mod}, n)$;

ans compare with 1, 0 and 2;

KOKO EATING BANANAS

piles $[7, 3, 6, 11]$ hours = 8

find min integer "K" such that Koko can eat all banana with hours given.

if Koko decided to eat 2 banana/hour

then $[7, 3, 6, 11]$

\downarrow
 $\frac{3}{2} = 1.5 \rightarrow (2)$ hours to complete eat 3 banana (we always take ceil value)

$$\frac{6}{2} = 3 \text{ hour}$$

$$\frac{7}{2} = 3.5 \rightarrow 4 \text{ hour}$$

$$\frac{11}{2} = 5.5 \rightarrow 6 \text{ hour}$$

$$\rightarrow 2 + 3 + 4 + 6 = (15) \text{ which is } > 8$$

\therefore not a solution

if 5 banana per hour

$$\frac{3}{5} = (1) \text{ hour}$$

$$\frac{6}{5} = 2 \text{ hour}$$

$$\frac{7}{5} = 2 \text{ hour}$$

$$\frac{11}{5} = 3 \text{ hour}$$

8 hour

\therefore 5 banana/hour is ~~answer~~

now if exact hours are not matching

we need to (taking less than 8 hours also are answer but we need to find closest to 8)

but if 4 banana per hour

$$\frac{3}{4} = 1$$

$$\frac{6}{4} = 2$$

$$\frac{7}{4} = 2$$

$$\frac{11}{4} = 3$$

(8) ans 4 is (4) x 5

4 is answer

as 3 banana per hour will not satisfy condition

OPTIMAL

Now $[3, 6, 7, 11]$

maximum rate can be (11) as after that same total hours

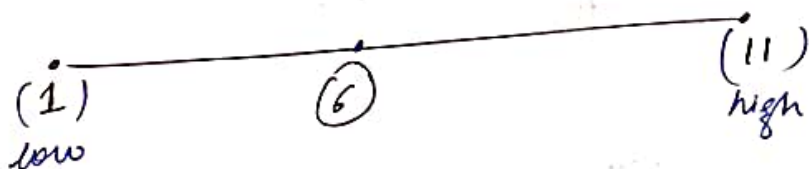
$[3, 6, 7, 11]$ (11)

$1+1+1+1 = 4$ hours

$1+1+1+1 = 4$ hours (12)

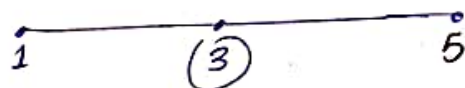
and minimum consumption = (1)
rate

answer will be in this range



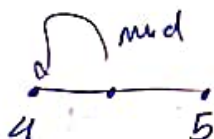
$6 \rightarrow 2 \times (1+1+2+2) = 6 < 8$ possible but does much smaller rate exist

\therefore
high = mid - 1;
ans = 6



$3(1+2+3+4) = 10 > 8$

\therefore we need to increase rate
 \therefore low = mid + 1;



$4(1+2+2+3) = (8)$

ans = ~~4~~ 4



$5(1+2+3) = 8$ but $5 > 4$

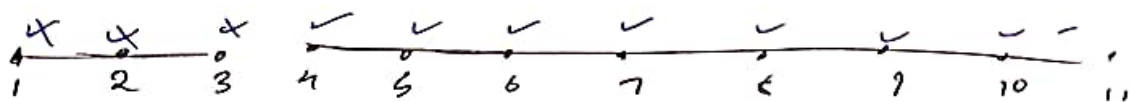
4 → 4

low = high = mid 4 satisfy

3 4 → low

high

break



low will eventually point to smallest (k)

∴ no extra element needed.

fun (arr, hours) {

low = 1; high = findMax(arr);

while (low <= high) {

int mid = (low + high) / 2;

int totalH = calculateTotalHours(arr, mid);

if (totalH ≤ hours) {

high = mid - 1;

else {

low = mid + 1;

}

}

return low;

}

$O(n)$

$\log_2(\text{max})$

0 "0" as better answer can exist as in case of 4 and 5

$O(n)$

time complexity → $O(n + n \times \log_2(\text{max}))$

type cast to double before dividing
if possible bug $\frac{\text{arr}[i] \text{ (double)}}{\text{mid} \text{ (double)}}$

AGGRESSIVE COWS

You are given an array 'arr' of size 'n' which denotes the position of stalls. You are also given an integer 'K' which denotes the no. of aggressive cows. You are given the task of assigning stalls to 'K' cows such that the minimum distance between any two of them is the maximum distance.

arr = [0 3 4 7 10 9] cows = 4

when dis = 1 ✓ sort array
 (1) $C_1 \leftrightarrow C_2 \leftrightarrow C_3 \leftrightarrow C_4$ ∴ min dis 1 possible

we have maintain
 min distance
 1 between cows

now when dis = 2

[0 3 4 7 9 10]

$C_1 \leftrightarrow C_2 \leftrightarrow C_3 \leftrightarrow C_4$

can't place here
 as dis = 1
 ∴ on 7 yes
 as $7 - 3 \geq 2$

when dis = 3

[0 3 4 7 9 10]

$C_1 \leftrightarrow C_2 \leftrightarrow C_3 \leftrightarrow C_4$ ✓

when $dis = 4$ $[0 \quad 3 \quad 4 \quad 7 \quad 9 \quad 10]$
 $c_1 \xrightarrow{4} c_2 \xrightarrow{4} c_3 \xrightarrow{4} c_4$ not possible

∴ minimum maximum distance is

(3)

BRUTE

sort(arr);

when two cows max possible min dist.

for ($i = 1$; $i \leq (man - min)$; $i++$) {

if (canplace(arr, i, cows) == true) continue;
 else return $i - 1$;

}

canplace(arr, i, cows) {

placing first cow at first index

countcows = 1; last = arr[0];

for ($i = 1$ → $(n - 1)$) {

if (arr[i] - last ≥ dist) {

last = arr[i];

countcows++;

}

can be here

if (countcows ≥ cows) return true

return false

}

TC → $O((man - min) \times O(n)) + n \log n$

sorting

SC → $O(1)$

OPTIMAL

$\begin{array}{cccccccccc} \checkmark & \checkmark & \checkmark & \times & \times & \times & \times & \checkmark & \times & \checkmark \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \end{array}$
 possible not possible

sorted ✓

possible not possible ✓

∴ Binary search

$\begin{array}{cccccccccc} 1 & 2 & 3 & 4 & (5) & 6 & 7 & 8 & 9 & 10 \\ \uparrow & & & & \times & & & & & \uparrow \end{array}$

$\begin{array}{cccccccccc} 1 & (2) & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \uparrow & \checkmark & & \uparrow & & & & & & \end{array}$

$\begin{array}{cccc} 1 & 2 & (3) & 4 \\ & & \uparrow & \uparrow \end{array}$

$\begin{array}{cccc} 1 & 2 & 3 & (4) \\ & & \uparrow & \uparrow \end{array}$

$\begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 & \% \text{ (ent)} \\ & & & \uparrow & \uparrow & \\ & & & \text{high} & \text{low} & \end{array}$
 answer

for (arr, rows) {

low = 0, high = arr[n-1] - arr[0];

sort(arr); $\rightarrow O(n \log n)$

while (low ≤ high) {

mid = (low + high) / 2;

if (can we place (over, mid, cows) == i) {

• low = mid + 1;

}

else high = mid - 1;

}

return high;

}

time complexity $\rightarrow O(n \log n) + O(\log_2(\text{max-min}) \times O(n))$

space $\rightarrow O(1)$

ALLOCATE BOOKS

arr = [25, 46, 28, 49, 24]

Student = 4

Given an array arr of integer where 'a[i]' represents the number of pages in the i-th book. There are a 'm' number of student and the task is to allocate all the books to the student

* Each student gets at least one book

* Each book should be allocated to only one student

* Book allocation should be in contiguous manner

* if allocation not possible return -1

25, 46, 28, 49, 24 m = 4

25 46 | 28 | 49 | 24

↳ this is maximum here

and we cannot get another maximum in any ~~last~~ arrangement that will be smaller than this maximum

∴ it is minimum maximum.

ans
OPTIMAL

arr = [25, 46, 28, 49, 24]

student = 4

if 49 (max of array)

then (1) \rightarrow 25

(2) \rightarrow 46

(3) \rightarrow 28

(4) \rightarrow 49

(5) \rightarrow 24

$\curvearrowright 5 > 4$

but we need to allocate to only 4 \therefore

we \uparrow 49 \rightarrow 50 \rightarrow 51

if 71

then

(1) \rightarrow 25,

(1) \rightarrow 25, 46

(2) \rightarrow 46

(2) \rightarrow 28

(3) \rightarrow 28

(3) \rightarrow 49, 2

(4)

(4) \rightarrow 24

\curvearrowright

4 = 4

answer

(we can do binary search from min)

when student = 1

* then the max allocation would be sum of array

No of s

Students (arr, pages) {

student = 1, pagesStudent = 0;

for (i = 0 → n - 1) {

if (pagesStudent + arr[i] ≤ pages) {

pagesStudent += arr[i];

}

else {

student++;

pagesStudent = 0;

}

return student;

}

fun (

low = min(arr);

high = sum(arr);

while (low ≤ high) {

mid = (low + high) / 2;

noStudents = students(arr, mid);

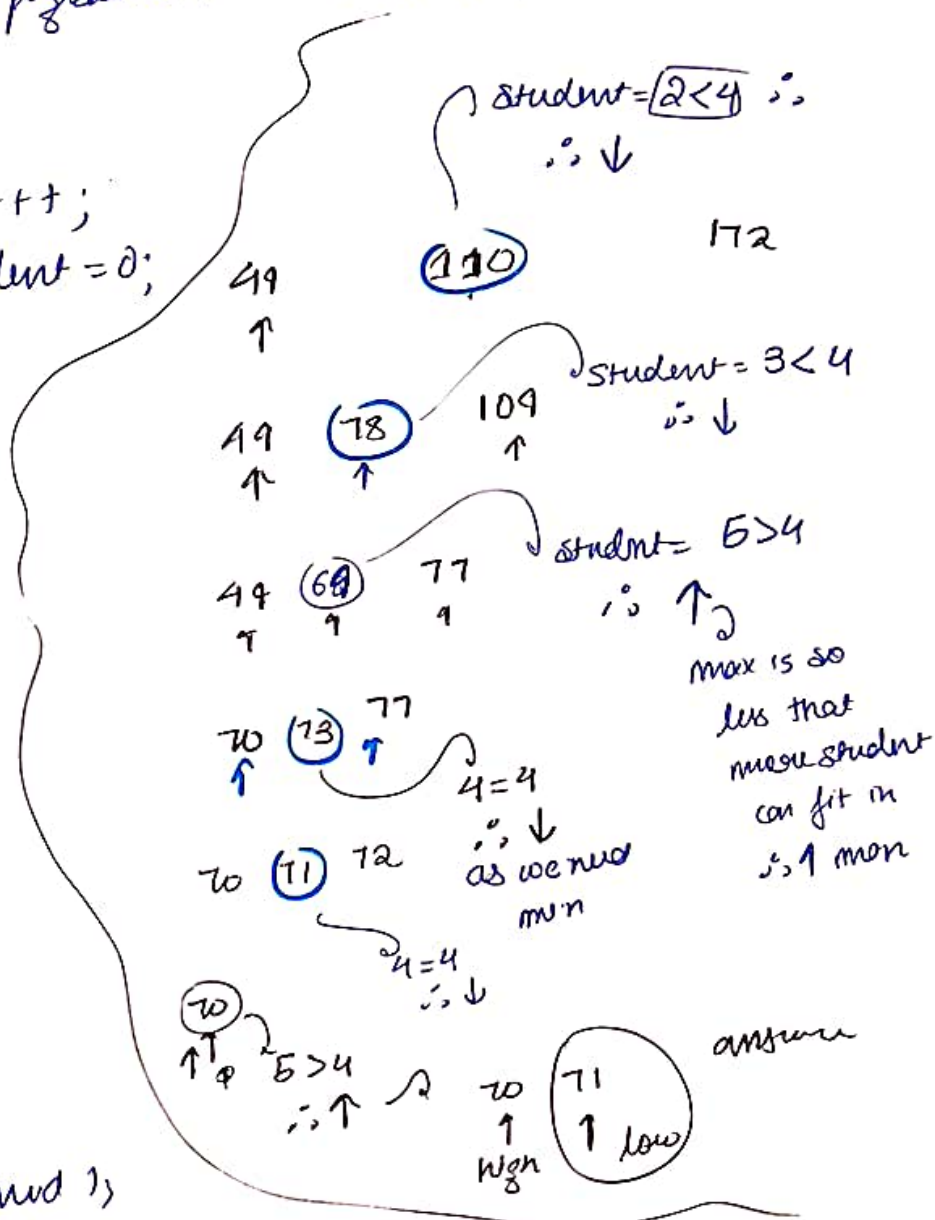
if (noStudents > m) low = mid + 1;

else high = mid - 1;

}

return low;

}



MINIMISE MAX DISTANCE BETWEEN GAS STATION

Problem: you are given a sorted array 'arr' of length 'n', which contains positive integer position of 'n' gas station. you are also given an integer 'k'. you have to place 'k' new gas station on the x-axis. you can place them anywhere on the non negative side of the x-axis even on non integer position. let 'dist' be maximum value of the distance between adjacent gas stations after adding k new gas stations. find minimum value of 'dist'.

arr = { 1, 2, 3, 4, 5 }

gas station
coordinate

$k = 4$

can be {13, 17, 23, 40}
but sorted

place k new gas station
so that you can minimize
max. two gas station
distance bet.

→ 1 2 3 4 5 6 7 8 9 (max = 1)

→ { 1 1.25 1.5 1.75 2 3 4 4.5 5 }
0.25 0.25 0.25 0.25 1 0.5 0.5
(max)

this is the
min
max.

→ 1 1.5 2 2.5 3 3.5 4 4.5 5
0.5 0.5 0.5 0.5 0.5 0.5 0.5
(max = 0.5)

→ ~~KTH MISSING NUMBER~~ ←

arr = {2, 3, 4, 7, 11} K = 5

Note: Answers within 10^{-6} of the actual answer will be accepted.

they (setter) do not want to that your code do not run for a long time on the server while calculating exact answer beyond 6 decimal places as it will result in "time limit exceeded" therefore it is said that do not calculate beyond 6 decimal places as only that will be compared.

arr = {1, 7} K = 2

↳

1 — . — . — 7

└──────────┘

$\frac{6}{3} = 2$

↳

1 — 3 — 5 — 7

placing gas station
between them
to minimize all
• (approach)

arr = {1, 13, 17, 23} K = 5

(12) (4) (6)

① → placing at max distance (12)

1 — 7 — 13 — 17 — 23

②nd

└──┘ └──┘ └──┘ └──┘

6 6 4 6

$$arr = \{1, 2, 3, 4, 5, 3\} \quad K=4$$

$0 \xrightarrow{\quad}$
 \uparrow
 ans can range from $0 \rightarrow$ when all the gas station are placed on same coordinate
 to $(1) \rightarrow$ which is current min distance between stations
 (yes we can do this)

Now linearly how this would work

$0 \quad 0.1 \quad 0.2 \quad 0.3 \quad \dots$
 \downarrow

to maintain a min min dis of 0 we need infinite 'K' station which is $\infty > 4$ \therefore not possible

Now

0.1

to maintain 0.1

$\{1, 1.1, 1.2, 1.3, 1.4, 1, 2, 3, 4, 5\}$

after using 4 station still we need more station as min min distance is still (1)

$\therefore \uparrow$ distance

0.3

$\{1, 1.3, 1.6, 1.9, 2, 2.3, \dots, 3, 4, 5\}$

here also need of gas station $> K$

~~line of gas~~

when 0.5

0 1 1.5 2 2.5 3 3.5 4 4.5 5

for 0.5 $K = \text{needed station count}$

this is answer but to find minimum we have to go left to minimize

← 0.5

no of gas $> K$ low = mid
else high = mid

0.4 1 2 3 4 5

$\frac{1}{0.4} = 2.5$ when in decimal

2 is no of station that we can place

but when $\frac{1}{0.5} = 2 \rightarrow$ only $2-1=1$ can be placed
 \therefore if exactly divisible then decrement.

→ 1 (7) 13 17 23

mom = 6

{ 1 13 17 23 }

2nd place

1 already placed
∴ dist
 $\frac{12}{2} = 6$

placing in between them

0	1	2
---	---	---

{ 1 13 17 23 }

keeping track of how many placed between them

0 1 2
[4 | | 1]

{ 1 13 17 23 }

3rd

$\frac{12}{2} = 6$

4

$\frac{6}{2} = 3$

Now mom = 6 ∴ to reduce we will place it there

all station equally = $13 - 1 = 12 = \frac{12}{3} = 4$ → 2 station to place ∴ 3 comparison
= (4) min new distance

0 1 2
[2 | 0 | 1]

{ 1 13 17 23 }

4th

$\frac{12}{3} = 4$

4

$\frac{6}{2} = 3$

Now mom = 4 ∴ place between (13, 17)

0	1	2
2	1	1

$\{ 1 \quad 13 \quad 17 \quad 23 \}$

now
 $5^{th} \quad \frac{12}{3} = 4 \quad \frac{4}{2} = 2 \quad \frac{6}{2} = 3$

$\therefore mom = 4$

\therefore place between them total $13-1 = \frac{12}{2+1+1} = \frac{12}{4} = 3$

already \nearrow new station \nearrow for comparison

$\{ 3 \quad 1 \quad 1 \}$ howMany

$\{ 1 \quad 13 \quad 17 \quad 23 \}$

$\frac{12}{4} = 3 \quad \frac{4}{2} = 2 \quad \frac{6}{2} = 3$

$\therefore mom\ min = 3$

for $(gas = 1 \rightarrow k)$

$momValue = -1, momIdx = -1;$

for $(i = 0 \rightarrow n-1)$

$diff = arr[i+1] - arr[i];$

$section\ length = diff / (howMany[i] + 1);$

if $(mom < section\ length)$

$mom = section\ length;$

$momIdx = i;$

}

}

$howMany[momIdx]++;$

}

minimize Max(distance (arr, k))

n = arr.length;

double low = 0;

double high = 0;

for (i = 0 → n - 1) { // defining range

high = Math.max(high, (double)(arr[i+1] - arr[i]));

}

double diff = 1e-6; $\sqrt{2} \cdot 10^{-6}$

while (high - low > diff) {

double mid = (low + high) / 2.0;

int cnt = numberOfCrossStationReq(mid, arr);

if (cnt > k) {

low = mid;

}

else {

high = mid;

}

}

return high;

}

we cannot do
mid + 1 as
there will be
lot of possible
answers that will
get missed as
answer is in double

```
numberofPairs (dist, arr) {
```

```
    n = arr.length;
```

```
    cnt = 0;
```

```
    for (i = 1 → n) {
```

```
        numberinbetween = (int) (arr[i] - arr[i-1] / dist);
```

```
        if ((arr[i] - arr[i-1]) == (dist * numberinbetween)) {
```

```
            numberinbetween --;
```

```
            cnt += numberinbetween;
```

```
        }  
    }  
    return cnt;
```

```
}
```

it means that
dist exactly
divides the
gap. i.e., -1 less
iteration

KTH MISSING POSITIVE NUMBER

you are given strictly increasing array 'arr' and a + int
K. find the Kth positive integer missing from 'arr'.

$$\text{arr} = \{4, 7, 9, 10\} \quad K = 4$$

missing no are 1, 2, 3, 5, 6, 8, 11, 12, ... K is 4 \therefore

4th missing no output

BRUTE

$$\text{arr} = \{2, 3, 4, 7, 11\} \quad K = 5$$

now 5 could be our answer but as 2, 3, 4 are present
 $\therefore 5 + 3 = \textcircled{8}$ can be our new answer

$$\text{arr} = \{2, 3, 4, \textcircled{7}, 11\} \quad K = \textcircled{5} \ 6 \ 7 \ 8$$

$\uparrow \quad \uparrow \quad \uparrow$

but 7 also present \therefore shift answer

$$8 + 1 = 9$$

now $11 > 9$ \therefore no shifting required as no ^{new} number is present before 9.

$\therefore \textcircled{9}$ solution

for ($i = 0 \rightarrow n - 1$) {

if ($\text{arr}[i] \leq K$) $K++$

else return K;

}

TC $\rightarrow O(n)$

OPTIMAL

arr = { 2, 3, 4, 7, 11 } K = 5

Now if no numbers were missing then the array would be

{ 1, 2, 3, 4, 5 }

Now ————— our original is (7) now $7 - 4 = 3$ ∴ there are 3 missing no before 7 that is why there is no 4 in its place

Similarly

$11 - 5 = 6$ ∴ there are 6 missing number to fill this place

{	2	3	4	7	11	}
	↓	↓	↓	↓	↓	
	1	1	1	3	6	

Now 5th missing would lie between

Now BINARY SEARCH

{	2	3	(4)	7	11	}
	↑		↓		↑	

missing number = $4 - 3 = 1$

as $5 > 1$ ∴ low = mid + 1;

{	2	3	4	(7)	11	}
				↑	↑	

$7 - 4 = 3$

as $5 > 3$ ∴ low = mid + 1;

{ 2, 3, 4, 7, (11) }

↑
↑ $11 - 5 = 6$

as $6 > 5$ ∴ high = mid - 1;

2, 3, 4, 7, 113

high ← 2
mid ← 3
low ← 4

(break)

Now

$arr[high] = 7$, $missing = 3$

but we need 5th missing $\therefore 5 - 3 = 2$ more missing

$\therefore arr[high] + more = 9$ answer

fun() {

low = 0, high = n-1;

while (low <= high) {

mid = (low + high) / 2;

missing = arr[mid] - (mid + 1);

if (missing < K) low = mid + 1;

else high = mid - 1;

}

(Problem)

high = -1

arr = {4, 7, 13} K=3
↑
low

\therefore is no \leq
 \therefore first occurrence

TC $\rightarrow O(\log n)$

now ans $\rightarrow arr[high] + more$

\downarrow
 $arr[high] + (K - missing)$

\downarrow
 $arr[high] + K - (arr[high] - high - 1)$

$arr[high] + K - arr[high] + high + 1$

$= (K + high + 1)$ answer

as low = high + 1

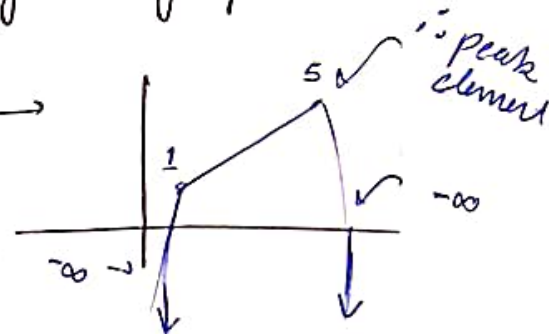
\therefore return (high + 1 + K) or (low + K)

FIND PEAK ELEMENT

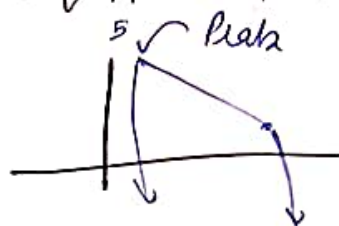
peak element $\rightarrow (arr[i-1] < arr[i] < arr[i+1])$

return index of peak element. if there are multiple peak numbers, return the index of any peak num.

also $\rightarrow arr[] = \{1, 2, 3, 4, 5\} \rightarrow$



$arr[] = \{5, 4, 3, 2, 1\}$



for the first element, the previous element should be considered as $-\infty$ as well as for the last element next element as $-\infty$ also.

BRUTE

for ($j=0$; $j < n$; $j++$) {

if ($(j == 0 \parallel arr[j-1] < arr[j]) \land$

$(j == n-1 \parallel arr[j] > arr[j+1])$) return j ;

}

if first element there is no previous $j=0$

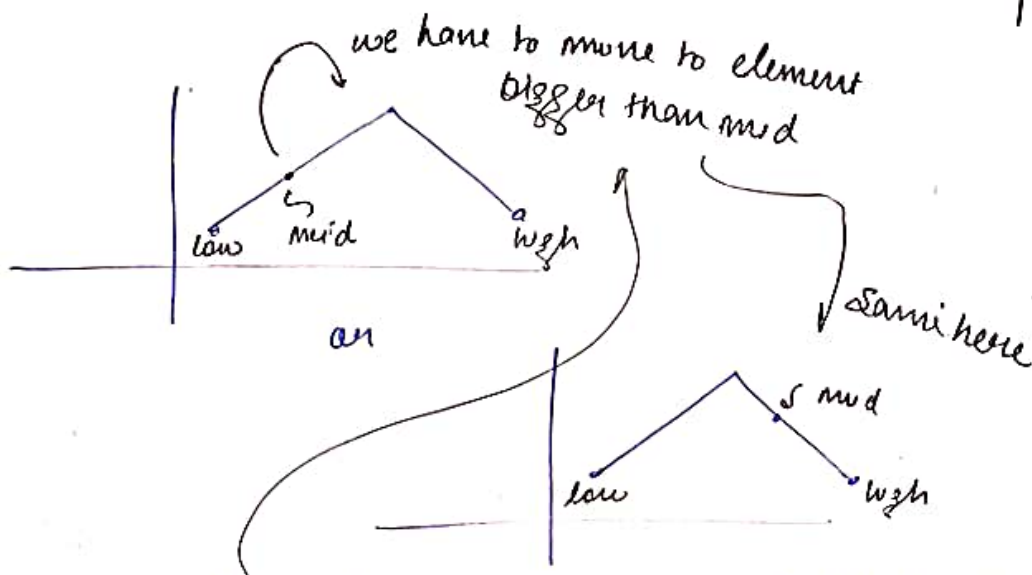
OPTIMAL

arr = { 1, 2, 3, 4, 5, 6, 7, 8, 5, 1 }

arr = { 2 } ← this is peak when one element

arr =

1 2 3 4 5 6 7 8 5 1



this is also followed when multiple peaks are there

1 2 3 4 (5) 6 7 8 5 1

4 < 5

but 5 < 6 ∴ not peak (check for peak)

∴ but 6 > 5 ∴ peak would be on right (low = mid + 1)
else (high = mid - 1)

fun(arr, n) {

if (n == 1) return 0;

if (arr[0] > arr[1]) return 1; ^{index of peak}

if (arr[n-1] > arr[n-2]) return n-1;

while (low = 1, high = n-2; ^{no including first and last}

while (low <= high) {

mid = (low + high) / 2;

if (arr[mid-1] < arr[mid] || arr[mid] > arr[mid+1])
return mid;

else if (arr[mid] > arr[mid-1]) low = mid + 1;

else high = mid - 1;

}

return -1;

}

MEDIAN OF TWO SORTED ARRAYS OF DIFFERENT SIZES

• return median of two sorted arrays.

arr1[] = {2, 4, 6}, arr2[] = {1, 3, 5}

Result → 3.5

as in sorted array

1	2	3	4	5	6
		↓			
		$\frac{3+4}{2}$			

= (3.5)

arr1[] = {2, 4, 6}, arr2[] = {1, 3}

Result → 3

{1, 2, 3, 4, 6}

BRUTE

arr1[] = {1, 3, 4, 7, 10, 12}, arr2[] = {2, 3, 6, 15}

space used
extra →

arr3[] = {1, 2, 3, 3, 4, 6, 7, 10, 12, 15}

$\frac{4+6}{2} = 5$

use merge
sort pointer
approach

i = 0 j = 0

while (i < n1 || j < n2) {

if (arr1[i] ≤ arr2[j]) arr3.add(arr1[i++]);

else arr3.add(arr2[j++]);

while (i < n1) arr3.add(arr1[i++]);

while (j < n2) arr3.add(arr2[j++]);

if $(n \% 2 == 1)$ return $arr3[n/2]$;
 else $\left(\frac{arr3[n/2] + arr3[n/2 - 1]}{2} \right)$;

BETTER in terms of space

$\{1, 2, 3, 4, 6, 7, 10, 12, 15\}$
 $\uparrow \quad \quad \uparrow$
 $idn1 \quad \quad idn2$

here we will not store the element in new array
 we will sort and move the pointer inside our
 $idn1$ value is sorted and $idn2$ also and will use
 that directly without storing

arr: $\{1, 2, 3, 4, 7, 10, 12, 15\}$
 $\downarrow \quad \downarrow \quad \uparrow$
 $\{1, 3, 4, 7, 10, 12, 15\}$
 \uparrow
 $\{1, 2, 3, 3, 4, 6\}$ (4) (6) \rightarrow got the mid + 1
 $\{1, 2, 3, 3, 4, 6\}$ (4) (6)
 $idn1$

for the code check vs code

OPTIMAL

Binary search

① arr1 $\rightarrow \{1, 3, 4, 7, 10, 12\}$

arr2 $\rightarrow \{2, 3, 6, 15\} \rightarrow 1, 2, 3, 3, 4 \mid 6, 7, 10, 12, 15$

as total 10 elements
 \therefore there will 5 elements each side
of median

Now how many element from array 1 can be
pick to make up the first half.

\rightarrow if we pick ① element from arr1 then

from arr1 $\rightarrow 1$

$\rightarrow 2, 3, 6, 15$

remaining 4 from
arr2

but

1 2 3 6 15 \mid 3 4 7 10 12

not correct configuration
as $15 < 3$

\therefore we cannot pick only 1 element from arr1

if we pick (4)
then

1	3	4	(7) l_1	10, q_1	12	still not valid
			2 l_2	(3) q_2	6 15	

here $l_1 > q_2$ \therefore we should pick less from array

if 3 pick

1	3	4		7	10	12	valid
	2	3		6	15		

if pick (2)

1	3	l_1		9(4)	7	10	12
2	3	(6) l_2		q_2	15		

$l_2 > q_1$ \therefore we should pick more from array

Now we have got the condition to eliminate halves right and left.

and also the range 0 — 6 \checkmark all of them from array

we will pick the array with less elements

$$\text{ans1} = \{7, 12, 14, 15\} \leftarrow \text{mod } 1$$
$$\text{arr}2 = \{1, 2, 3, 4, 9, 11\} \leftarrow \text{mod}2$$

low

② mid1

(4) wgh

∴, $mid2 = 5 - mid1 = 3$ (element to pick from arr2)

$$\begin{array}{ccc|cc} & 7 & 12 & (14) & 15 \\ & & & \nwarrow & \\ 1 & 2 & 3 & 4 & 9 \\ & & & \nearrow & \\ & & & & (mod 2) \end{array}$$

more $l_1 > l_2 \therefore \text{Wgh} = \text{mud} - 1;$

low
mid

① high

mid2 = 5

$12 = 5$
 l_1 | s mid 1
 7 12 14 15
 11 mid 2
 comparison does not matter

but $4 > 7$

$\therefore l_2 > r_1 \quad \therefore \text{low} = \text{mid} + 1$

Love

① high
low

$$m'v' = 1$$
$$\text{mid}2 = 4$$

				7	12	14	15
1	2	3	4		9	11	

here $9 \cdot 7 < 9 \cdot 49$ $49 < 12$

\therefore pick (1) only

if h_1 on q_2
does not exist
take
EPI
INI MIN

$$l_1 = arr1[mid1 - 1] \quad r_1 = arr1[mid1]$$

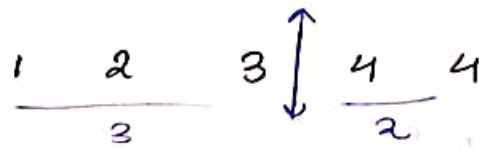
$$l_2 = arr2[mid2 - 1] \quad r_2 = arr2[mid2]$$
$$g_1 = a^{a-1} \pmod{a}$$
$$H_2 = \cos^2(\mu \theta^2)$$

$$\frac{\text{mem}(l_1, l_2) + \text{mem}(a_1, a_2)}{2}$$

but when odd element

arr1 = {2, 4}

arr2 = {1, 3, 4}



$$\text{partition} = \frac{n_1 + n_2 + 1}{2} = \frac{2 + 3 + 1}{2} = 3$$

on left

\Rightarrow mem(l1, l2) \hookrightarrow median

if

2	3
---	---

 then $\min(a_1, a_2)$

code

median(a, b) {

 n1 = a.size();

 n2 = b.size();

 if (n1 > n2) return median(b, a);

 int low = 0, high = n1;

 int left = (n1 + n2 + 1) / 2;

 while (low <= high) {

 int mid1 = (low + high) / 2;

 int mid2 = ~~int~~ left - mid1;

 int l1 = INT_MIN, l2 = INT_MIN;

 int r1 = INT_MAX, r2 = INT_MAX;

when we take all element from first array, mid points to index after array size

 if (mid1 < n1) r1 = a[mid1];

 if (mid2 < n2) r2 = b[mid2];

making sure to work on smaller array, calling same function again with smaller array in front. even and odd both

if (mid-1 ≥ 0) l1 = a[mid-1]; // l1 should exist.

if (mid2-1 ≥ 0) l2 = b[mid2-1]; // l2 " "

if (l1 ≤ n1 && l2 ≤ n2) {

if (n%2 == 1) return max(l1, l2);

return (double) (max(l1, l2) + min(n1, n2)) / 2

}

else if (l1 > n2) high = mid-1;

else low = mid+1;

}

return 0;

}

~~FAAD~~ !!
SOLUTION

~~O(n)~~
 $O(\log(\min(n_1, n_2)))$