

## MEDIUM

(39)

2 SUM: check if a pair with given sum exists in Array.

arr = { 2, 6, 5, 8, 11 } target = 14

result = [ 1, 3 ]

## BRUTE

pick one element from the remaining array for (target - n). Repeat

for (i = 0 → n) {

for (j = i + 1 → n) {

if (arr[i] + arr[j] == target) {

return [i, j]

}

}

$O(n^2)$

## BETTER (Hashing)

arr = [ 2, 6, 5, 8, 11 ] target = 14

8 + (6) = 14

is there in map

(5, 2)
(6, 1)
(2, 0)

map

(elem, index)

map<int, int> mpp;

for (i=0 → n) {

int a = arr[i];

int more = target - a;

if (mpp.find(more) != mpp.end()) {

return [i, mpp.second];

}

else mpp.put[arr[i], i]

}

}

$O(n)$  - average

$O(n^2)$  - worst but rare

space complexity -  $O(n)$

**OPTIMAL** is space

arr[] = {2, 6, 5, 8, 11}

2 pointers

↓  
sort  
↓

arr[] = {2, 5, 6, 8, 11}

when (-8)

when (+)

i = 2

j = 11

2 + 11 = 13 less < 14 ∴

i++ = 5

j = 11

5 + 11 = 16 > 14 ∴

i = 5

--j = 8

5 + 8 = 13 < 14 ∴

++ i = 6

j = 8

6 + 8 = 14 ~~too~~ wow

```
for (i = 0 → n) {  
    sum += a[i];
```

calculating sum till i

```
    if (sum == k) {  
        maxlen = i + 1;  
    }  
}
```

if prefix sum is = k then max length would be that

```
long rem = sum - k;
```

```
if (presum.containsKey(rem)) {  
    int len = i - presum.get(rem);  
    maxlen = Math.max(maxlen, len);  
}
```

```
}
```

checking if (n-k) exist in map or not

```
if (!presum.containsKey(sum)) {  
    presum.put(sum, i);  
}
```

```
}
```

updating sum if it does not exists

Time complexity →  $O(n \times \log n)$

traversing

finding in ordered map

or  $O(n \times 1)$

traversing

finding in unordered map

but  $O(n \times n)$

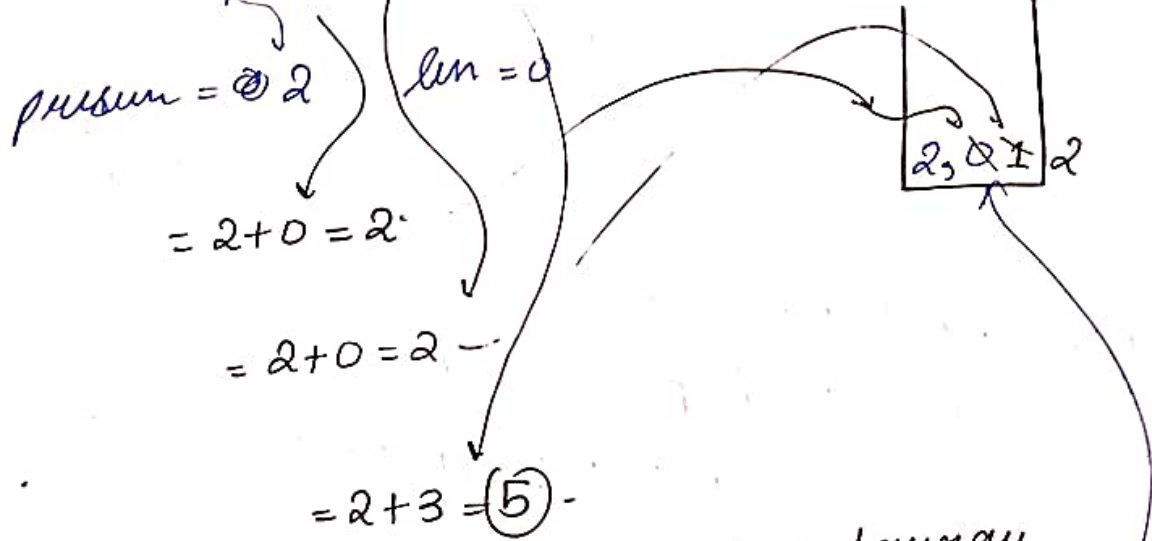
at worst case

space complexity:

Edge case

(42)

arr[]  $\rightarrow$  [2, 0, 0, 3]  $k=3$



$\therefore$  to have 3 as sum in subarray we need  $n-k \Rightarrow 5-3=2$  sum previously which exist in map but index "2" [2, 0, 0] [3]

$\therefore$  length of subarray is  $k$  sum whose sum is  $k = 1$  which is wrong as it gives minimum length but answer should be  $[0, 0, 3] = len=3$

$\therefore$  we should not update sum when going to new element which is zero gives same sum.

CODE

```
int n = arr.length;
Map<Long, Integer> presum = new HashMap();
long sum = 0;
int maxLen = 0;
```



if (sum == k) {  
 maxlen = Math.max(maxlen, right - left + 1); (43)  
}

right++;  
 if (right < n) sum += a[right];  
}  
return maxlen;  
}

Now inner while loop will not run "n" times

as

1	2	3	4	5	6
↓	↓	↓	↓	↓	↓
0	0	0	3	0	2

= 5

as sometime while do not even get executed  
 ∴ it does not run n times for every  
 element but overall it runs n times (summation)  
 summation

∴  $O(n)$  &

∴  $O(n) + O(n) = O(2n)$

In case of (-) any run this

→ { 2, -1, 2, 3, -2, 4 } k=4

for optimal ~~x~~ and ~~trashing~~ solution

here if sum crosses k then  
 we have a solution to include  
 next number which can be  
 negative that will make the sum = k but in optimal approach we  
 just decrease the window  
 from left.

**OPTIMAL** when only +ve and 0s use prefix when ~~no~~ (-) included (42) (44)

2 pointer approach.

arr[] = [1, 2, 3, 1, 1, 1, 1, 3, 3] k = 6

(i) → (j)

count up till

increase upto k = 6

same length

now if sum > k then decrease length from left side

# increase from right to get to k and decrease from left to if sum > k

[1, 2, 3, 1]  
(i) → (j) sum = 7

[1, 2, 3, 1]  
(i) → (j) sum = 6

fun (int a[], k) {

int n = a.length;

int left = 0; right = 0;

long sum = a[0];

int maxLen = 0;

while (right < n) {

while (left ≤ right && sum > k) {  
sum -= a[left];  
left++

}

keep decreasing size as long as sum > k

O(n)

# MAJORITY ELEMENT ( $> n/2$ times)

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## BRUTE

arr = {2, 2, 3, 3, 1, 2, 2}

$$2 \geq (4 \text{ times} > \frac{7}{2})$$

pick element search the array increase count

for ( $i=0 \rightarrow n$ ) {

    cnt = 0;

    for ( $j=0 \rightarrow n$ ) {

        if (arr[j] == arr[i]) cnt++;

    }

    if (cnt >  $n/2$ ) return arr[i];

}

## BETTER (hashing)

arr = {2, 2, 3, 3, 1, 2, 2}

int n = arr.length;

HashMap mapp;

for ( $i=0 \rightarrow n$ ) {

    int value = mapp.get(arr[i]);

    mapp.put(arr[i], value + 1);

}

(1, 1)
(3, 2)
(2, 4)

(ele, count)

$O(n)$

when unordered map  
↓  
when sorted  
( $O(n \times \log n)$ )

but if you need index as answer then ... 46  
put each element in another data structure  
{ (2,0) (6,1) (8,3) } as index will be disturbed  
after sorting.  $\therefore$  only "yes" or "no" can be answered  
here.

```
quad ( ... ) {  
    int left = 0; right = n-1;  
    Arrays.sort(arr);  $\longleftarrow O(n \log n)$   
    while (left < right) {  
        int sum = arr[left] + arr[right];  
        if (sum == target) return "yes";  
        else if (sum < target) left++;  
        else right--;  $\longleftarrow O(n)$   
    }  
    return "NO";  
}
```

{  
 time complexity:  $O(n) + O(n \log n)$   
 space complexity:  $O(1)$



for (Map.Entry<Int, Int> it : map.entrySet()) {  
 if (it.getValue() > n/2) {  
 return it.getKey();  
 }  
}

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}

time -  $O(n) + O(n) = O(2n)$

space -  $O(n)$  - when unique elements

**OPTIMAL** (Moore's Voting Algorithm)

arr = [7, 7, 5, 7, 5, 1, 5, 7, 5, 5, 7, 7, 5, 5, 5, 5]

this works on logic that to <sup>cannot</sup> cancel out ~~no~~ a majority element ~~or~~ as consider arr = [1, 1, 1, 2, 2] =  $\frac{5}{2} = 2$

there majority element count is  $(3) > \frac{n}{2}$  therefore we need

③ element to cancel out of majority element but it is not possible as already majority covers more than  $\frac{n}{2}$  space of array, i.e. not other element combined can cancel out majority element  
 other element  $\neq 7 \therefore$  cancel out]

arr = [ 7 7 5  
           ↑ ↑  
 element = 7  
 count = 2 2 1

arr = [7, 7, 5, 7]  
 elem = 7  
 count = 1 + 1 = 2

when element = picked element (48)  
 ↓  
 increase count  
 else decrease count

arr = [7, 7, 5, 7, 5, 1, 7]  
 elem = 7  
 count = 2 - 1 = 1

we can say that in this subarray there is no majority element as the count becomes 0. which means no element have count  $> \frac{n}{2}$

Now  
 pick next element

arr = [7, 7, 5, 7, 5, 1, 5, 7, 5, 5, 7, 7, 5, 5, 5, 5]  
 element = 5  
 count = 1 - 0 = 1

element = 5  
 count = 1 + 2 + 1 = 4

element = 5  
 count = 1 + 2 + 3 + 4 = 10

as count  $\neq 0$  ∴ element = 5

will be majority element

kyunki bas aur main  
 den nahi use  
 maanne ha.

```
majority (arr) {  
    int n = arr.length  
    count = 0  
    el = 0
```

```
    for (i = 0 → n) {  
        if (count == 0) {  
            el = v[i];  
            count = 1;  
        }  
        else if (el == v[i]) count++;  
        else count--;  
    }
```

```
}  
int count1 = 0  
for (i = 0 → n) {  
    if (arr[i] == el) count1++;  
}  
if (count1 > (n/2)) return el;  
return -1;  
}
```

always ---  
 $O(n)$

check if  
that is majority  
element or not  
(case when there is  
no majority  
element)

$O(n)$

time -  $O(2n)$  when there can be or cannot  
be a majority element  
 $O(n)$  - when it exists always

space - ~~not~~  $O(1)$

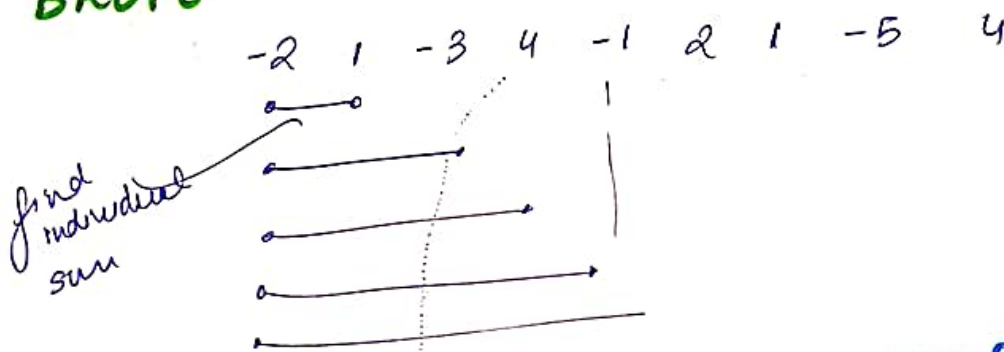
# MAXIMUM SUBARRAY

Given an integer array `nums`, find contiguous subarray which has largest sum and return its sum  
 (at least one number)

`nums = [-2, 1, -3, 4, -1, 2, 1, -5, 4]`

output: 6

## BRUTE



for ( $i = 0 \rightarrow n$ ) {

for ( $j = i \rightarrow n$ ) {

for ( $k = i \rightarrow j$ ) {

`sum += arr[i];`

}

`max = max(max, sum);`

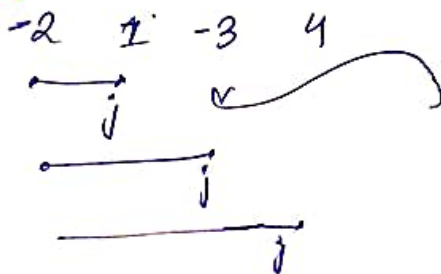
}

}

}

$O(n^3)$

## BETTER



time  $j$  is moving only one place but we are recalculating whole sum  
 $\therefore$  we can just add extra element only to existing sum



for (i = 0 → n) {

sum = 0;

for (j = 0 → n) {

sum += a[j];

}

max = Max(sum, max);

}

$O(n^2)$

## OPTIMAL (Kadane's Algorithm)

intuition: we carry a subarray sum as long as it gives us a (+) sum

-2 -3 4 -1 -2 1 5 -3  
sum = -2 max = -2

Now after going to another element we check if sum is <sup>before</sup> negative then we update (sum = 0) as

-2 -3 (4) -1 -2 1 5 -3  
sum = 0 + -3 = -3  
update  
= 0 + 4 = 4  
keep as (+)  
= 4 - 1 = 3  
3 - 2 = 1  
1 + 1 = 2 → 2 + 5 = 7 - 3 = 4  
max = -2  
max = 4  
max = 7

maxSubarray (arr) {

int sum = 0;  
int maxSum = 0;

for (i = 0 → n) {

sum += arr[i];

maxSum = max(sum, maxSum);

if (sum < 0) sum = 0;

}

return maxSum;

}

if we need index of array to print <sup>mem</sup>

maxSubarray (arr) {

int sum = 0; int ansStart; int ansEnd;

int maxSum = 0;

for (i = 0 → n) { <sup>local variable</sup>

if (sum == 0) start = i

sum += arr[i];

if (sum > maxSum) {

ansStart = start;

ansEnd = i;

maxSum = sum;

}

if (sum < 0) sum = 0;

}

# SORT ARRAY OF 1s, 0s AND 2s.

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**BRUTE** - sort  $\rightarrow$  T.C

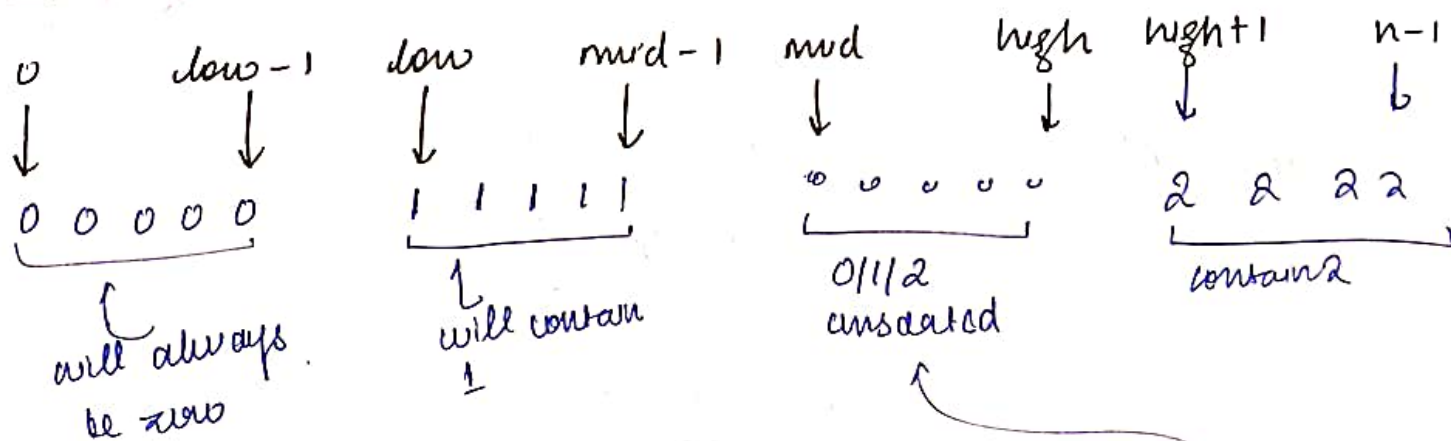
**BETTER** - keep count of all these no  $\rightarrow$  0 count  
1's count  
2's count

if make array count  
if reiterate array and overwrite  
 $O(2N)$

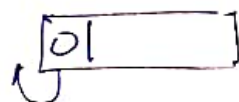
**OPTIMAL** - Dutch National Flag Algorithm.

arr = 0 1 1 0 1 2 1 2 0 0 0

rules

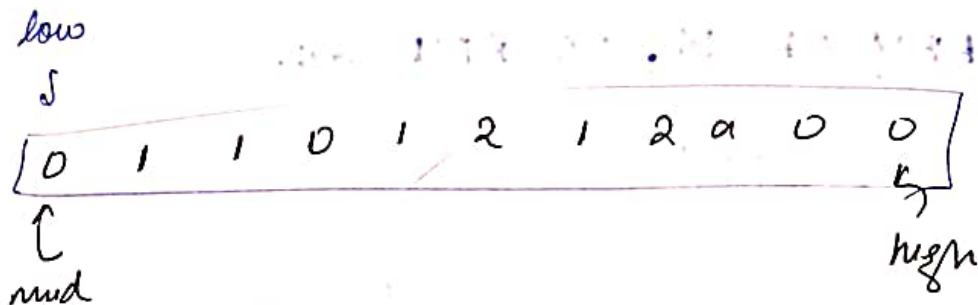


point to point should move array unsorted  
when we discover any 0 from array  
using low and high pointer we place them there



0  $\rightarrow$  for low to pass go  
1  $\rightarrow$  for mid-1 to pass  
2  $\rightarrow$  high to pass go

if  $> 0$   
 $arr =$



$arr[mid] == 0$  { if  $mid == 0$  then we have to put in place of low which contains "1";  $\therefore$  we do

$swap(arr[mid], arr[low])$

$low++$ ; as it is sorted

$mid++$ ; as 1 is there and array sorted upto 1

$\therefore$  unsorted array after  $mid-1$ ;

}

$arr[mid] == 1$  {  $mid++$ ; as 1 is at correct place  
 $\therefore$  unsorted array is after 1 }

$arr[mid] == 2$  {  $swap(arr[mid], arr[high])$ ;

$\therefore$  upto up high to  $n-1$  sorted

$\therefore$   $high--$ ;

and whatever value comes to  $arr[mid]$  after swapping is unsorted  
 $\therefore$  no change;

}



arr = [0, 1, 1, 0, 1, 2, 1, 2, 0, 0, 0]

mid points to 0 and 2

swap arr[mid] == 0 case.

arr = [0, 1, ...]

mid points to 1

arr[mid] = 1

arr = [0, 1, 1, ...]

mid points to 2

arr = [0, 1, 1, 0]

low points to 1, mid points to 0

swap 1 and 0

arr = [0, 0, 1, 1]

low points to 1, mid points to 0

arr = [0, 0, 0, 1, 1, 2]

low points to 1, mid points to 2

high and mid swapped

arr = [0, 0, 0, 1, 1, 0, 1, 2, 0, 0, 2]

low points to 1, mid points to 0, high points to 2

check mid apply rule

arr = [0, 0, 0, 0, 1, 1, 1, 2, 0, 0, 2]

low points to 1, mid points to 2, high points to 0

arr = [0, 0, 0, 0, 1, 1, 1, 0, 0, 2, 2]

low points to 1, mid points to 0, high points to 2

arr = [0 0 0 0 0 1 1 1, 0, 2, 2, 2]

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low high mid mid

arr = [0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 2, 2, 2]

low high

{

low = 0, high = n-1; mid = 0;

while (mid <= high) {

if (arr[mid] == 0) {

swap(arr[mid], arr[low]);

mid++;

low++;

}

else if (arr[mid] == 1) { mid++; }

else { swap(arr[mid], arr[high]);

high--;

}

}

$O(n)$

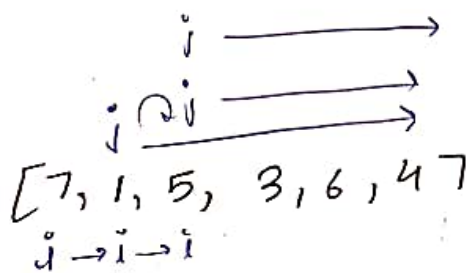
# STOCK BUY AND SELL

you want to maximize your profit by choosing a single day to buy on stock and choosing a different day in the future to sell stock. Return max profit if you cannot make profit return 0;

int prices = [7, 1, 5, 3, 6, 4]

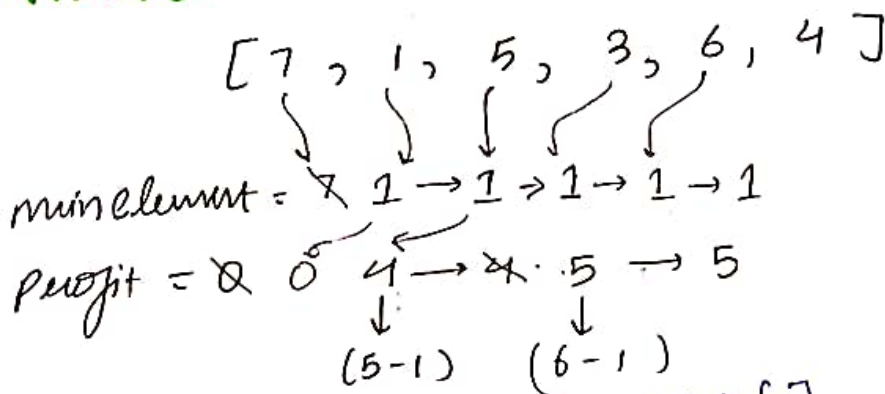
output = 5

## BRUTE



$O(n^2)$

## OPTIMAL



maxProfit ( ) {

minPrice = 0

minPrice = INT\_MAX;

for (i = 0 -> n) {

minPrice = min(minPrice, prices[i]);

maxProfit = max(maxProfit, prices[i] - minPrice);

}

return maxProfit;

## REARRANGE BY SIGN

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Array with equal number of +ve and -ve elements.  
without changing the relative order of +ve and -ve numbers  
return an array of alternate +ve and -ve

$$\text{arr}[ ] = \{1, 2, -4, -5\} \quad n=4$$
$$\hookrightarrow \{1, -4, 2, -5\}$$

## BRUTE

Take +ve array

Take array for -ve number

fill by pointing through array  $\hookrightarrow O(n)$

overwrite original array.

$\rightarrow$  even index = +ve

$\rightarrow$  odd index = -ve

$$\text{for } (i=0 \rightarrow \frac{n}{2}) \{$$

$$\text{arr}[2 \times i] = \text{pos}[i];$$

$$\& \text{arr}[2 \times i + 1] = \text{neg}[i];$$

}

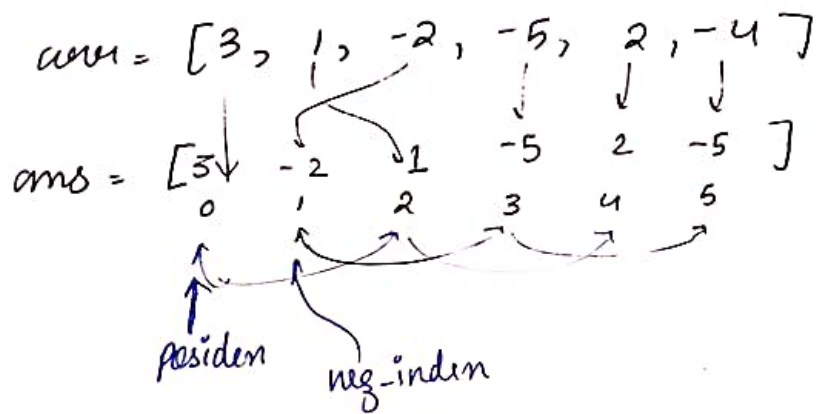
$$\hookrightarrow O\left(\frac{n}{2}\right)$$

filling array

$$\text{time} - O\left(n + \frac{n}{2}\right)$$

$$\text{space} \rightarrow O(n)$$





# when we will encounter an element put elements on respective index and increment appropriately in ans array

return ans array.

TC  $\rightarrow O(N)$

Space  $\rightarrow O(N)$

rearrange (nums) {

int ans[nums.length];

int posIndex, negIndex;

for (i = 0  $\rightarrow$  n) {

if (nums[i] < 0) {

ans[negIndex] = nums[i];

negIndex += 2;

}

else {

ans[posIndex] = nums[i];

posIndex += 2;

}

}

}

**Observation** - if some elements are left put them in end without altering the order.

answer = fall back to brute force method.

```
ArrayList<Integer> pos = new ArrayList<>();  
ArrayList<Integer> neg = new ArrayList<>();
```

```
for (i = 0; i < n; i++)
```

```
if (arr[i] > 0) pos.add(arr[i]);  
else neg.add(arr[i]);
```

```
if (pos.size() < neg.size())
```

```
for (i = 0; i < pos.size(); i++)
```

```
arr[i * 2] = pos.get(i);
```

```
arr[2 * i + 1] = neg.get(i);
```

```
int index = pos.size() * 2;
```

iden from where to fill remaining element

```
for (i = pos.size(); i < neg.size(); i++)  
arr[index++] = neg.get(i);
```

else {

$O(\text{sumarrng})$

$\therefore O(n) + O(\text{Min}(\text{pos}, \text{neg})) + O(\text{sum})$

when all +ve or -ve then  $O(n)$

$\therefore O(n) + O(n) = O(2n)$

# NEXT PERMUTATION

$$Arr = \{1, 3, 2\}$$

output  $\rightarrow \{2, 1, 3\} \leftarrow$  next permutation after above

## # BRUTE

Generate all permutation find next permutation using linear search.

$$arr[] = [3, 1, 2]$$

1	2	3
1	3	2
2	1	3
2	3	1
3	1	2
3	2	1

Just learn how to find using recursion

$$\# \text{ Number} = 3! = 6$$

$$O(n! \times n)$$

permutation

every permutation of  $n$  size

## # OPTIMAL

$$arr = [2, 5, 1, 5, 4, 3, 0, 0]$$

for next permutation this is sorted in descending order  
 $\therefore$  arranging these would not help in getting next bigger number than current.

$\therefore$  step 1: find a  $a[i] < a[i+1]$  because if we are arrange now we can make the next greater number

Step 2: find  $num > 1$  out smallest one. now if any element is picked eg 2 5 but 2 3 will should come before  $\therefore$  we need to find next greater no than 1 in right part

Step 3: Now arrange the remaining in ascending order  
 so that ~~the~~ next number can be formed by  
 arranging inner element first (63)

indm = -1;

for (j = n-2; i >= 0; i--) {

if (a[i] < a[i+1]) {

indm = i; break

}

[2, 1, 5, 4, 3, 0, 0]  
 indm

if (indm == -1) reversearray(arr); return;

as reached as last one  
 i.e array already in  
 descending order.

for (j = n-1; i >= indm; i--) {

if (arr[i] > arr[indm]) {

swap(arr[i], arr[indm]);

}

[2, 1, 5, 4, 3, 0, 0]  
 [2, 3, 5, 4, 1, 0, 0]

reverse(arr, indm+1, n-1); [2, 3, 0, 0, 1, 4, 5]  
 reverse:



# LEADERS IN AN ARRAY

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- A leader is an element that is greater than all of the elements on its right side in the array.
- rightmost element is always the leader.
- print all leaders.

## OPTIMAL

• ~~can~~ instead of comparing an element with max element of right side instead of all elements on right update max when a lead leader is found.

arr = [10, 22, 12, 3, 0, 6]

max → 10 22 22 22 22

leaders = [12, 6, 22]

```
int max = arr[n-1];
```

```
print(max);
```

```
for (i = n-2 → 0) {
```

```
    if (arr[i] > max) {
```

```
        max = arr[i];
```

```
        print(arr[i]);
```

```
    }
```

←  $O(n)$

# BRUTE (FIND LONGEST UNSEQUENTIVE SQU) 64

sequence

arr = [100, 200, 1, 3, 2, 4]

length = 4

arr = [3, 8, 5, 7, 6]

length = 4 as [5, 7, 6, 8] rearrangement can be done.

arr[] = [102, 4, 100, 1, 101, 3, 2, 1, 1]

Pick one do linear search for next consecutive element  
increas count if any (repeat)

for (i = 0 → n) {

n = arr[i];

count = 1;

mem = 01;

while (linearSearch(arr, n+1) == true) {

n = n + 1;

count = count + 1;

}

mem = Mem(count, mem);

}

## BETTER

Sort element first then count:

sort(arr); →  $O(n \log n)$

longest = 1; lastSmaller = INT\_MIN, count = 0

for (i = 0 → n)

if (arr[i] - 1 == lastSmaller) {

count = count + 1;

lastSmaller = arr[i];

}

else if (arr[i] != lastSmaller) {

count = 1;

lastSmaller = arr[i];

}

longest = max(longest, count)

}

time -  $O(n) + O(n \log n)$

but we are modifying array.

∴

## OPTIMAL

arr = [102, 4, 100, 1, 101, 3, 2, 1, 1]

→ use set

102
4
100
1
101
3
2

Set

now iterate element by element

→ 102 now do not start from here as 102 is 400

∴ search for next smaller consecutive

∴ move one step down

we shall start from here

→ 4 now 3 exist in set ∴ no right element to start ∴ counting with 0's move down

→ 100 now 99 do not exist ∴ start with 100 and count

$\left. \begin{array}{l} 100 \\ 101 \\ 102 \end{array} \right\} \text{count} = 3$

∴ Repeat:

$\rightarrow \begin{array}{c} 1 \\ \downarrow 2 \\ \downarrow 3 \\ \downarrow 4 \end{array} \left. \right\} 4$

∴ 100  
101 → go down

∴ 302 → go down

∴ 201 → go down

→ `int n = a.length;`

`if (n == 0) return;`

`int longest = 1;`

`Set<Integer> set = new HashSet<>();`

`for (i = 0 → n) { set.add(a[i]); }`

`for (int j = 1; j ≤ n; j++)`

`if (!set.contains(j-1)) {`

`int cnt = 1;`

`int n = j;`

`while (set.contains(n+1)) {`

`n = n + 1;`

`count = count + 1;`

`}`

`longest = Math.max(longest, count);`

$O(n)$

if it contains previous one or not

$O(2N)$

element

as  $N + N$

(7+7)

another iteration

for sequence length

(1, 2, 3, 4), (2, 3, 4, 5)



$O(3N) \rightarrow$  time

$O(N) \rightarrow$  space

## SET MATRIX ZEROS

# Given a matrix if an element in the matrix is 0 then you will have to set its entire column and row to 0

ex

1	1	1		→	1	0	1
1	0	1			0	0	0
1	1	1			1	0	1

## BRUTE

1	1	1	1
1	0	0	1
1	0	1	1
1	1	1	1

→

**STEP 1**

mark row and column value as (-1) whenever we find 0 and do not change 0 to -1 in between

1	-1	-1	1
-1	0	0	-1
-1	-1	0	-1
1	-1	-1	1

↓

**STEP 2**

matrix change -1 to 0 in next iteration

for (i → n) {

for (j → m) {

if (arr[i][j] == 0) {

markRow(i);

markCol(j);

}

}

}

$O(n \times m)$

$O(mn)$

markRow(i) {

for (j = 0 → m) {

if (arr[i][j] != 0) {

arr[i][j] = -1;

}

markCol(j) {

for (i = 0 → n) {

if (arr[i][j] != 0) {

arr[i][j] = -1;

}

$O(n)$

for (i → n) {

for (j → m) {

if (arr[i][j] == -1) arr[i][j] = 0; }

}

}

$O(m \times n)$

∴ time -  $O((n \times m) \times (n + m) + m \times n) \approx \text{cubic}$

## BETTER

now we are running mark function for some row and column every time we encounter a zero in that row/column

for mark function array

0 then mark that column and row

1	1	1	1	1	0	1	1	1	1
1	0	1	1	1	1	0	1	1	1
1	1	0	1	1	1	1	0	1	1
1	0	0	1	1	1	1	0	0	1

→ now → but not whenever we will get a 0 we will only mark that column to set it to 0 at end

in the end the marked column/row will be set to 0

col[m] = {0}, row[n] = {0}

for (i=0 → n) {

for (j=0 → m) {

if (arr[i][j] == 0) {

row[i] = 1;

col[j] = 1;

}

}

✓  $O(n \times m)$

for (i=0 → n) {

for (j=0 → m) {

if (row[i] || col[j]) arr[i][j] = 0

}

✓  $O(n^2)$

}

$O(n \times m)$

time -  $O(2(n \times m))$

space →  $O(n) + O(m)$

## OPTIMAL

Thought process → how to reduce the space complexity  
we will store the array in the matrix itself.

→ eliminate

this will be used to mark column

1	1	1	1	
1	0	1	1	
1	1	0	1	
0	1	1	1	

these extra variables used as there will be overlap between row 0 and column 0 tracking

as

1	1	1	1
1			
1			
0			

This is 0's will be zero and this column will be zero if no extra

navable then the matrix will look like

mean  
for  
column = 0  
only

0	1	1	1
1			
1			
0			

for row  
zero only

but when we will get to  
this element it will look  
here as it is 0 it will turn  
to 0 which should not be  
done as it was meant for  
column not row.  
∴ extra navable

0			
1	0	0	
0	1	1	1
0	1	0	1
0	1	1	1

itself  
will work  
for row  
but for column

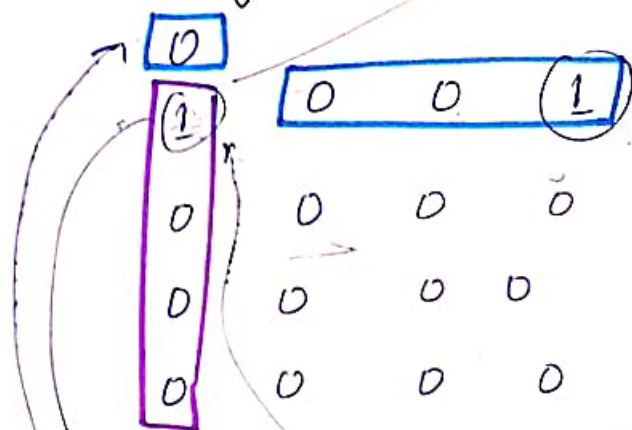
0			
1	0	0	1
0	0	1	1
0	1	0	1
0	1	0	1

now we will  
start iterating  
from the inner elements  
only as iterating  
through array stored  
as matrix would  
disturb its own element  
therefore making unnecessary  
elements 0

0			
1	0	0	1
0	0	0	0
0	0	0	0
0	0	0	0



Now we iterate through column array first then row array. (11)



is dependant on this value  
therefore if we traverse  
row array first

this one will be converted  
to 0 as this is 0 and  
whenever we will  
set the column array  
every element will become  
zero as this will be 0

∴ we start from column array

int col0 = 1; // mark for column "0"

for (i = 0 → n-1) {

for (j = 0 → m-1) {

if (matrix[i][j] == 0) {

marking for  
row

matrix[i][0] = 0;

matrix[0][j] = 0;

if (i != 0) {

matrix[0][j] = 0;

else col0 = 0;

ensuring that  
your column  
variable  
"col0" is used  
in the 0 column;

$O(m \times n)$

}

}

for ( $i = 1 \rightarrow n$ ) {  
 for ( $j = 1 \rightarrow m$ ) {

if ( $matrix[i][j] != 0$ ) {

if ( $matrix[0][j] || matrix[i][0] == 0$ ) {

$matrix[i][j] = 0;$

}

iterating inner element

}

}

if ( $matrix[0][0] == 0$ ) {

checking if column 0  
needs to be  
set to 0

for ( $j = 0 \rightarrow m$ ) ~~matrix~~  $matrix[0][j] = 0;$   
 {

if (~~row~~  $col0 == 0$ ) {

for ( $i = 0 \rightarrow n$ ) ~~matrix~~  $matrix[i][0] = 0;$

setting column 0 to 0 if  
variable says so.

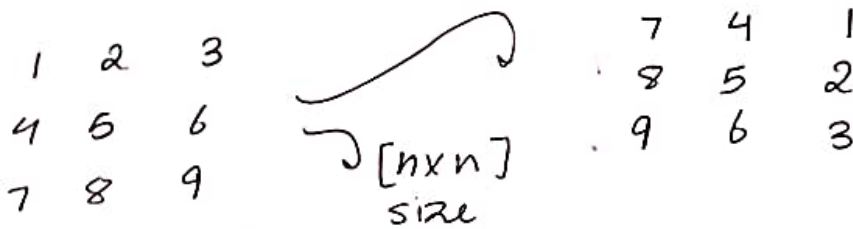
$O(m \times n) \rightarrow$  combined

time  $\rightarrow O(2 \times (m \times n))$

space  $\rightarrow O(1)$

# ROTATE IMAGE BY 90°

13



## BRUTE

→ use an external array

Now  $[0][0] \rightarrow [0][3]$   
 $[0][1] \rightarrow [1][3]$   
 $[0][2] \rightarrow [2][3]$   
 $[0][3] \rightarrow [3][3]$

$0 \rightarrow 3$   
 $(i) \rightarrow (n-1)-i$

Same here as (i) similar for other rows.

$[1][0] \rightarrow [0][2]$   
 $[1][1] \rightarrow [1][2]$   
 $[1][2] \rightarrow [2][2]$   
 $[1][3] \rightarrow [3][2]$

$1 \rightarrow 2$   
 $i \rightarrow (n-1)-i$

o.o

$ans[n][n]$

for ( $i=0 \rightarrow n$ ) {

for ( $j=0 \rightarrow n$ ) {

$ans[j][n-1-i] = matrix[i][j];$

}

return ans;

but !! space also  $O(n^2)$

✓  $O(n^2)$

# OPTIMAL

Now

1 2 3 4  
5 6 7 8  
9 10 11 12  
13 14 15 16

And transpose

1 5 9 13  
2 6 10 14  
3 7 11 15  
4 8 12 16

reverse each row

13	4	5	1
14	10	6	2
8	7	11	15
4	8	12	16

kya baat hai!!  
answer ko  
reverse kr  
gya.

for (i=0 → n) {

for (j=i+1 → n) {

swap(arr[i], arr[j], arr[j], arr[i]);

$O(n/2 \times n/2)$

}

for (i=0 → n) {

int start = 0; end = n-1;

$O(n \times \frac{n}{2})$

while (start < end) {

swap(arr[i][start], arr[j][end]);

start++ ; end-- ;

}

}

}



# SPIRAL MATRIX

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1 2 3 4 5

14 15 16 17 6  
13 20 19 18 7  
12 11 10 9 8

top left right

top	0	1	2	3	4	5
0	1	2	3	4	5	6
1	20	21	22	23	24	7
2	19	32	33	34	25	8
3	18	31	36	35	26	9
4	17	30	29	28	27	10
5	16	15	14	13	12	11

top = 0 bottom = 5

left = 0 right = 5

while (top ≤ bottom && left ≤ right)

inside

for (i = left → right) {  
arr[top][i];  
}

top++;

for (i = top → bottom) {  
print(arr[i][right]);  
}

right--;

for (i = right → left) {  
print(arr[bottom][i]);  
}

bottom++;

for (i = bottom → top) {  
print(arr[i][left]);  
left++;

while (top ≤ bottom || left ≤ right) {

for (i = left → right) print(arr[top][i]);

top++;

for (int i = top → bottom) print(arr[i][right]);

right--;

if (top ≤ bottom) {

for (i = right → left) print(arr[bottom][i]);

bottom--;

if (left ≤ right) {

for (i = bottom → top) print(arr[i][left]);

left++;

}

}

when only  
single  
row given



no top  
here  
would  
to print 13  
again.

13 → 14  
15 → 16

$O(n \times n)$