

STACKS AND QUEUES

①

void Stack {

int size = 1000

top = -1

STACK
↓

void push(int n) {

top++;

if (top == size - 1) return;

top++;

arr[top] = n;

}

void pop() {

int n = arr[top];

top--;

return n;

}

QUEUE

class Queue {

arr[]

start = -1

end = -1

currSize = 0;

push (element) {

if (currSize == maxSize) return

if (end == -1) {

start = 0

end = 0

} else {

end = (end + 1) % maxSize;

}

arr[end] = element

currSize++;

}

← PUSH

STACK USING QUEUE

4

Approach

→ push(n) → push the element in the queue

use a for loop of size()-1, remove element from queue and again push back to the queue, hence the most recent becomes the most former element.

class Stack {

Queue<Integer> q = new LinkedList<>();

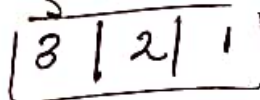
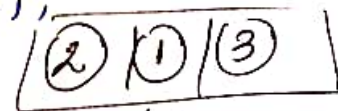
void push(int n) {

q.add(n);

for (int i = 0; i < q.size() - 1; i++) {

q.add(q.remove());

}



now this will get removed first
recent one LIFO

int pop() {

return q.remove();

}

int top {

return q.peek();

}

returns null when empty...

```
public int pop() {
```

```
    if (start == -1) return
```

```
    int popped = arr[start];
```

```
    if (arrSize == 1) {
```

```
        start = -1;
```

```
        end = -1;
```

```
    } else {
```

```
        start = (start + 1) % arrSize;
```

```
    }
```

```
    arrSize--;
```

```
    return popped;
```

```
}
```

```
public int top() {
```

```
    if (start == -1) return -1;
```

```
    return arr[start];
```

```
}
```

```
}
```

... QUEUE USING STACK ...

(5)

class Queue {

Approach 1

```
Stack<Integer> input = new Stack<>();  
Stack<Integer> output = new Stack<>();
```

void push(n) {

```
while(!input.empty()) {  
    output.push(input.pop());  
}
```

```
input.push(n);
```

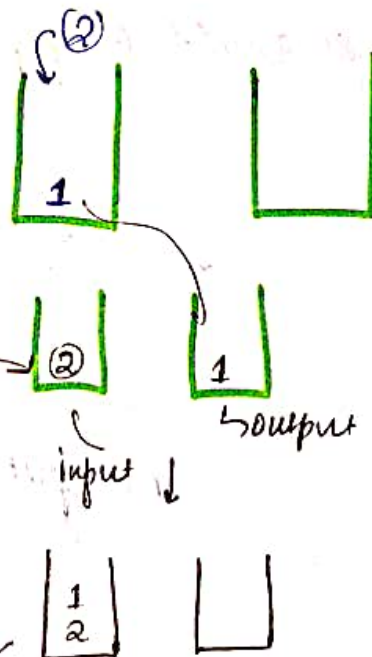
```
while(!output.empty()) {  
    input.push(output.pop());  
}
```

int pop() {

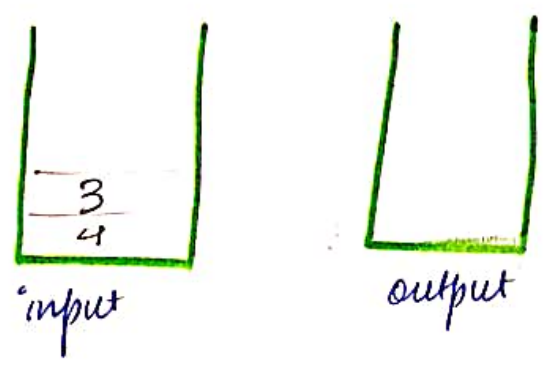
```
if(input.empty()) return -1;
```

```
int val = input.pop();  
return val;
```

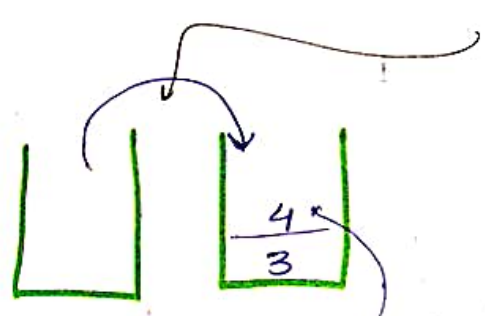
}



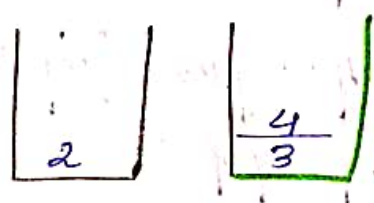
Approach: 2



pop : 4 should be popped first :-
two way



$O(n)$

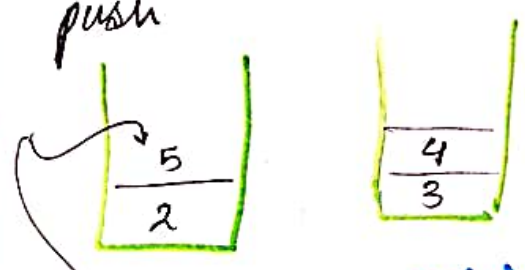


when already there in
output queue just pop

$O(1)$

depends on
if element is
there or not in

push



just push $O(1)$

shifting happens in pop only.
at

MyQueue {
 input } → 2 stacks
 output
 void push(int n) {
 input.push(n);
 }

int pop() {

if (output.empty()) {
 while (input.empty() == false) {
 output.push(input.pop());
 input.pop();
 }

int n = output.peek();
 output.pop();
 return n;
 }

int peek() {
 if (output.empty()) {
 shift input element to
 output
 }

return output.peek();
 }

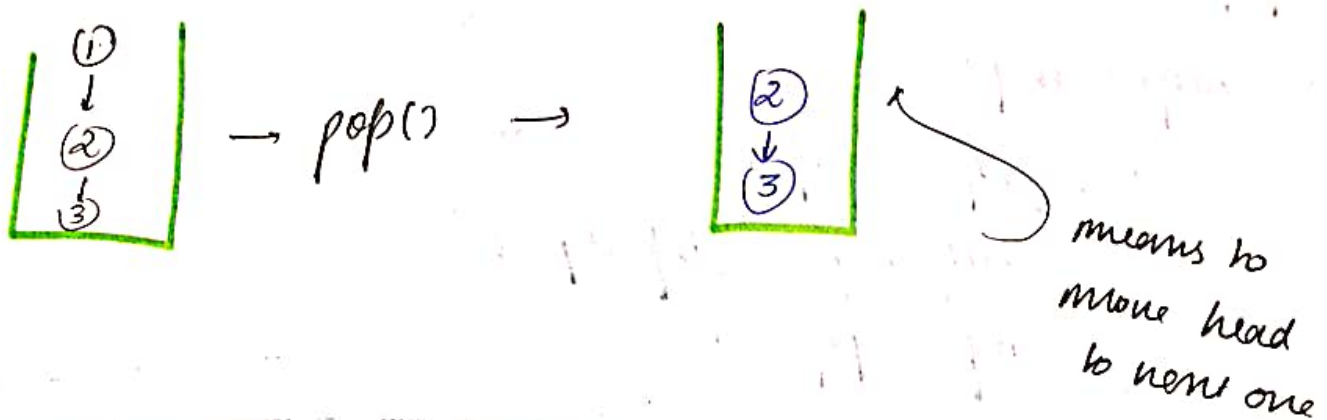
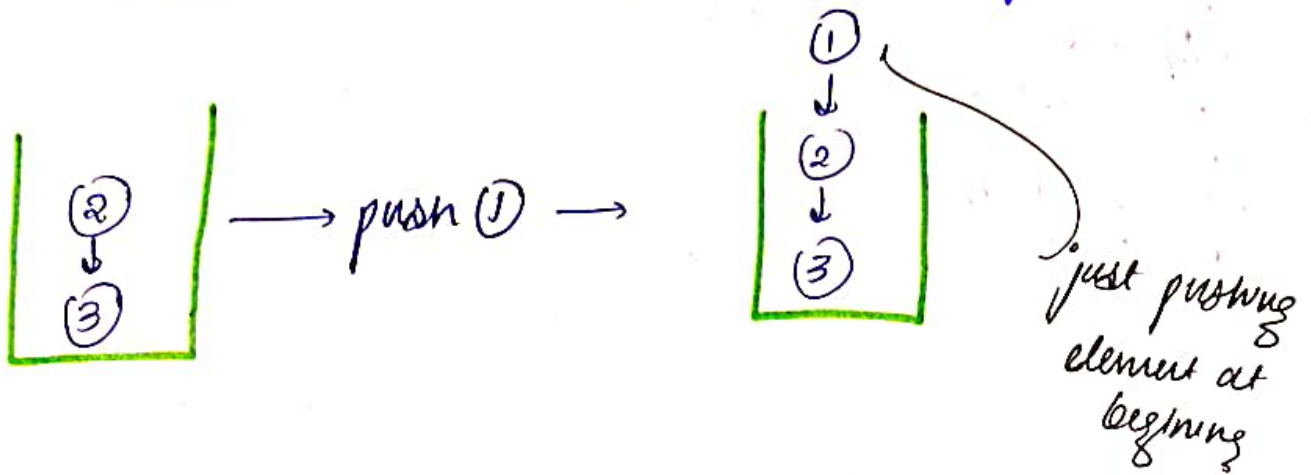
int size() {
 return output.size() + input.size();
 }

$O(n)$ or $O(1)$

$O(n)$ or
 $O(1)$

...STACK USING LINKED LIST...

(5)



Stack push (n) {

StackNode element = new StackNode(n);

element->next = top;

top = element;

Size++;

}

StackPop() {

if (top == null) return -1;

int topData = top.data;

~~StackNode temp = top;~~

top = top.next;

return topData;

}

(16)



word enqueue (value) &

```
temp = new QueueNode(value);
```

else {

front = mean = center;

else Σ

мат = еср

3 size + 1 }

void dequeue() {

if (front == null) {
empty

}

else {

QueueNode temp = front;

front = front.next;

size--;

}

}

(11)

INFIX TO POSTFIX

13

Algorithm steps

- initialize an empty stack (for operators)
- initialize an empty result (postfix expression)
- scan expression from left to right
- for each token:
 - operand → add directly to postfix expression
 - left ' (' → push onto stack
 - right ')' → pop until '(' is encountered and add to postfix and discard both parentheses.
 - operator (+, -, *, /, ^):
 - if precedence of current operator \leq precedence of top of stack
pop and top should not be '('
push operator onto stack

- after expression pop all remaining operation from stack to prefix postfix

(15)

Associativity
 $\wedge \rightarrow 3 \rightarrow$ right to left
 $\times / \% \rightarrow 2 \rightarrow$ left to right
 $+ - \rightarrow 1 \rightarrow$ left to right

Associativity

$A - B - C$
 first two then
 $A - B$
 then $(A - B) - C$
 (left to right evaluation when precedence equal)

$2^3 3^4$
 first two
 $2^3 3^4$ or not $2^3 3^4$
 $2^3 3^4$ X

$2^8 1$
 then two (right to left evaluation when precedence is equal)

* otherwise wrong output

INFIX TO PREFIX

19

$$(A+B) * C - D + F$$

- # Reverse the given infix
- # Do infix to postfix conversion
 - do not pop when precedence is equal
 - we only pop when right associative operator
- # Reverse the answer

$$\begin{aligned} & (A+B) * C - D + F \\ & \left(\begin{array}{l} f + d - c *) B + A C \end{array} \right) \text{opening} \rightleftharpoons \text{closing} \\ & \left(\begin{array}{l} f + d - c * (B + A) \end{array} \right) \\ & \quad \downarrow \\ & \quad \text{postfix} \end{aligned}$$

$$\rightarrow FDCBA+*-+$$

↓
reverse

$$+-*+ABCDF$$

★ Associativity check

15

```
while (!stack.isEmpty() && precedence(curr) ≤  
      precedence(stack.peek()) &&  
      isLeftAssociative(curr)) {
```

```
    postfix.append(stack.pop());
```

```
}
```

```
isLeftAssociative(char ch) {
```

```
    return ch != '^';
```

```
}
```

element pop only
when left to
right associativity

$O(n)$ — time

$O(n)$ — SPACE



```

while (!stack.isEmpty() &&
    precedence(stack.peek()) > precedence(curr) ||
    (precedence(stack.peek()) == precedence(curr) &&
     isRightAssociative(curr.op))) {
    result.append(stack.pop());
}

```

when == then
associativity
should be right

why?

we scan reverse the expression
 \therefore associativity gets flipped

left (+, -, *, /) becomes right
 right (^) becomes left

$2^3^4 \rightarrow$ we do not pop as exp evaluates to
 right to left
 \downarrow

$4^3^2 \rightarrow$ we need to pop as ~~right to~~
 associativity changes and needs
 to evaluate 4^3 first.

$$2^3^4$$

↓

$$4^3^2 \rightarrow$$

$$\boxed{43^2^}$$

↪

$$^2^34$$



but when not popped

$$2^3^4$$

↓

$$4^3^2 \rightarrow$$

$$\boxed{432^{}^}$$

$$^{}^234$$



wrong evaluation

this will be evaluated first wrong



$$\text{time} - \underbrace{O(\frac{n}{2}) + O(\frac{n}{2})}_{\text{reverse}} + O(2N)$$

$$\text{space} - O(N)$$

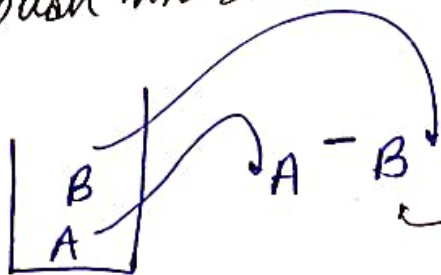
POSTFIX TO INFIX

(17)

$AB - DE + F * /$

Scan left to right

- operand are pushed onto stack
- when operator can pop two operand combine and push into stack



first popped should be on right

$A B - D E + F * /$

	st
A	A
B	A B
-	(A - B)
D	(A - B), D
E	(A - B), D, E
+	(A - B), (D + E)
F	(A - B), (D + E), F
*	(A - B), ((D + E) * F)
/	((A - B) / ((D + E) * F))

empty stack

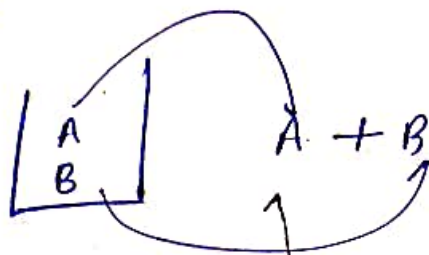
PREFIX TO INFIX

(18)

- # Scan from right to left
- # Same as before

but

A



first popped will come in front.

POSTFIX TO PREFIX

$AB - DE + f \times /$

pattern = (operator) (top 2) (top 1)

or

A	_____	A
B	_____	AB
-	_____	-AB
D	_____	-AB, D
E	_____	-AB, D, E
+	_____	-AB, +DE
f	_____	-AB, +DE, f
*	_____	-AB, *DEF
/	_____	/-AB*DEF

PREFIX TO POSTFIX

(19)

1-AB * + DEF

scan from right to left

pattern = (top 1) (top 2) (operator)



	st
A	A
F	F
E	F, E
D	F, E, D
+	F, DE+
*	DE+ F*
B	DE+ F* , B
A	DE+ F* , B, A
-	DE+ F* , AB -
/	AB - DE+ F* /

NEXT GREATER ELEMENT

20

MONOTONIC STACK → when elements are stored in specific order.

ans = [6, 0, 8, 1, 3] -1
tell the next greater
[8, 8, -1, 3, -1]

BRUTE

iterate and find next greater $O(n^2)$
for ($i=0 \rightarrow n-1$) {
 for ($j=i+1 \rightarrow \dots$) {
 if ($arr[i] > arr[j]$)

OPTIMAL

traverse from back

4	12	5	3	1	2	5	3	1	2	4	6
---	----	---	---	---	---	---	---	---	---	---	---

(-1)

4 | 6

↑ in stack there is 6

∴ next greater = 6

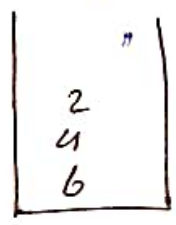
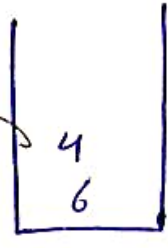
push 4 in stack



2 |

in stack (4) nge

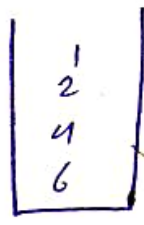
and push 2 in stack



1 |

Stack (2) nge

and push (2) (1)



3 |

★ true find next greater

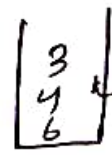
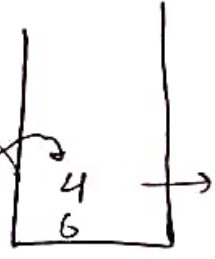
if we insert 3 directly then



3 to find nge
2 and 1 do not matter
is pop and maintain order

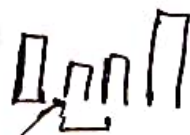
3

3 nge → 4
and push 3



we do not need 1 and 2

mono specific order
we do not need middle



smaller one

to find nge

findNGE () {

for (i = n-1) → 0 {

while (!st.empty() && st.top() <= arr[i]) st.pop();

if (st.empty()) nge[i] = -1
else nge[i] = st.top()

st.push(arr[i])

}

return nge

}

Time - $O(2N)$

when last element
is biggest one
and at max
only n element
can be removed
overall
 $\therefore N + N = 2N$

SPACE $\rightarrow O(N)$