

## Heap Add and Delete

```
SIZE++;  
arr[SIZE] = ele;  
int pi = SIZE / 2;  
while(pi >= 1) {  
    int ci = pi * 2;  
    if((ci + 1) <= SIZE && arr[ci + 1] > arr[ci])  
        ci = ci + 1;  
    if(arr[pi] > arr[ci])  
        break;  
    int temp = arr[pi];  
    arr[pi] = arr[ci];  
    arr[ci] = temp;  
    pi = pi / 2;  
}
```

SIZE

0

1  $pi=0$

2  $pi=1,0$   $ci=2$

3  $pi=1$   $ci=2$

4  $pi=2,1,0$   $ci=4,2$

6 14 3 26 8 18 21 9 5

26	14	3	6					
1	2	3	4	5	6	7	8	9

$pi=1$

$ci=1*2=2$

$ci+1$

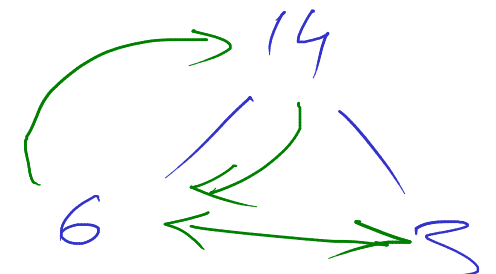
$8 > 14$

X

$arr[pi] > arr[ci]$

14	6	3	26					
1	2	3	4	5	6	7	8	9

max = 26



# Merge Sort

## Divide and Conquer

//1. Divide collection (array) into two parts

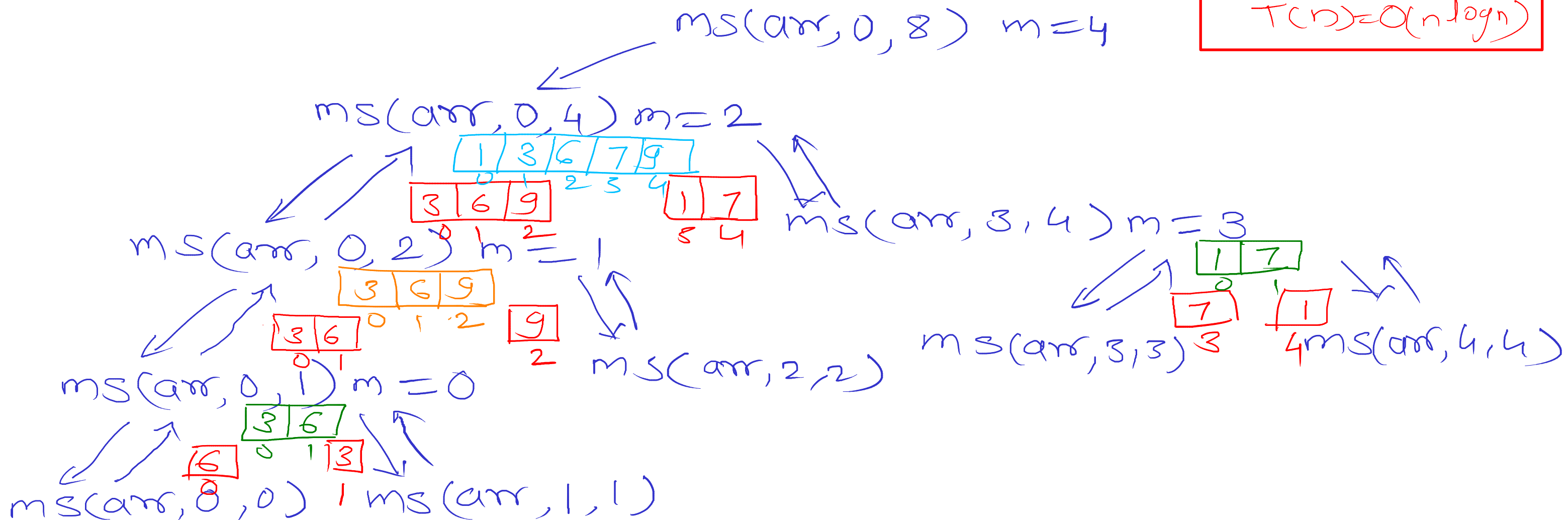
//2. Sort each part individually

//3. merge two sorted partitions in such a way that merged array is sorted

//4. overwrite temp array into original array

<del>6</del>	<del>3</del>	<del>9</del>	<del>7</del>	<del>1</del>	8	2	4	5
0	1	2	3	4	5	6	7	8

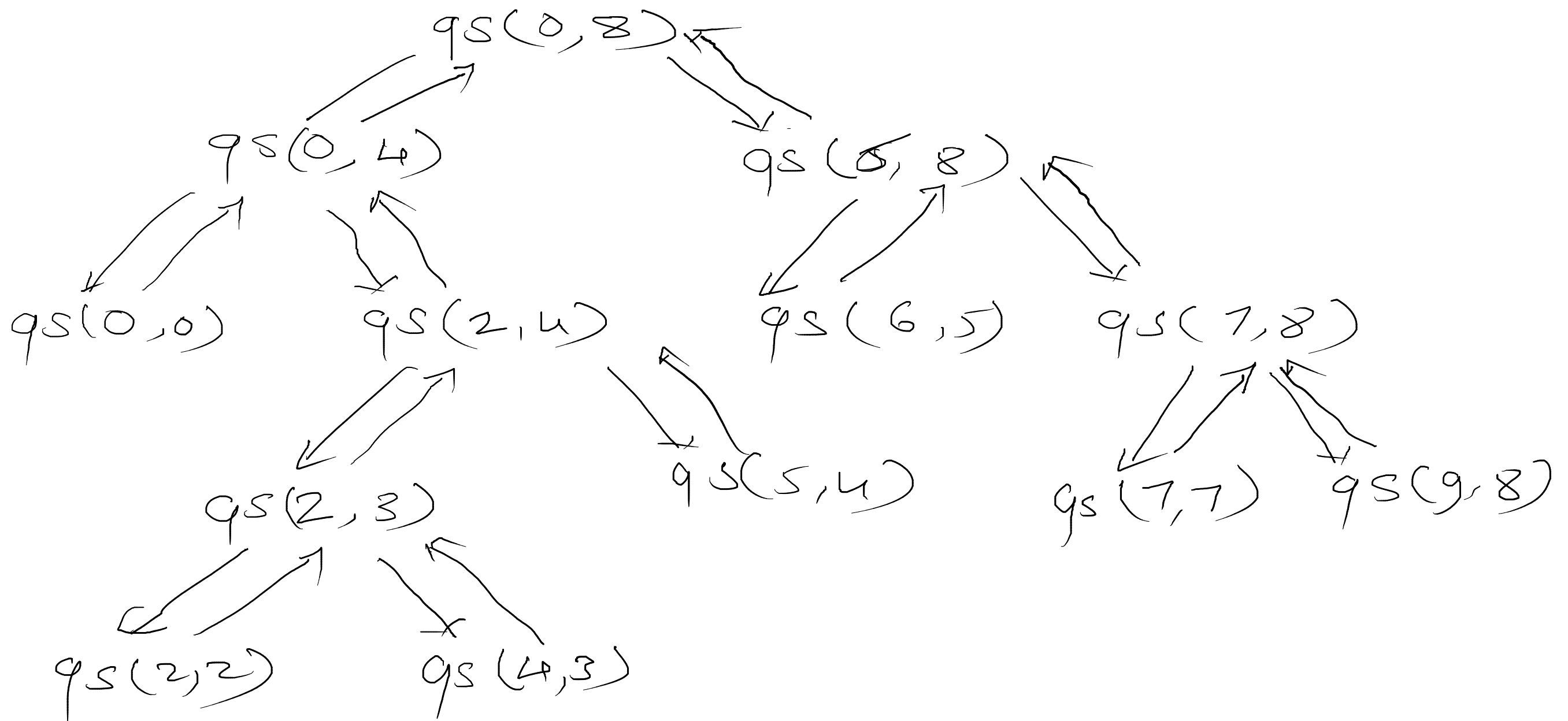
levels of division =  $\log n$   
comparisons =  $n$   
per level  
total comp =  $n \log n$   
 $T(n) = O(n \log n)$



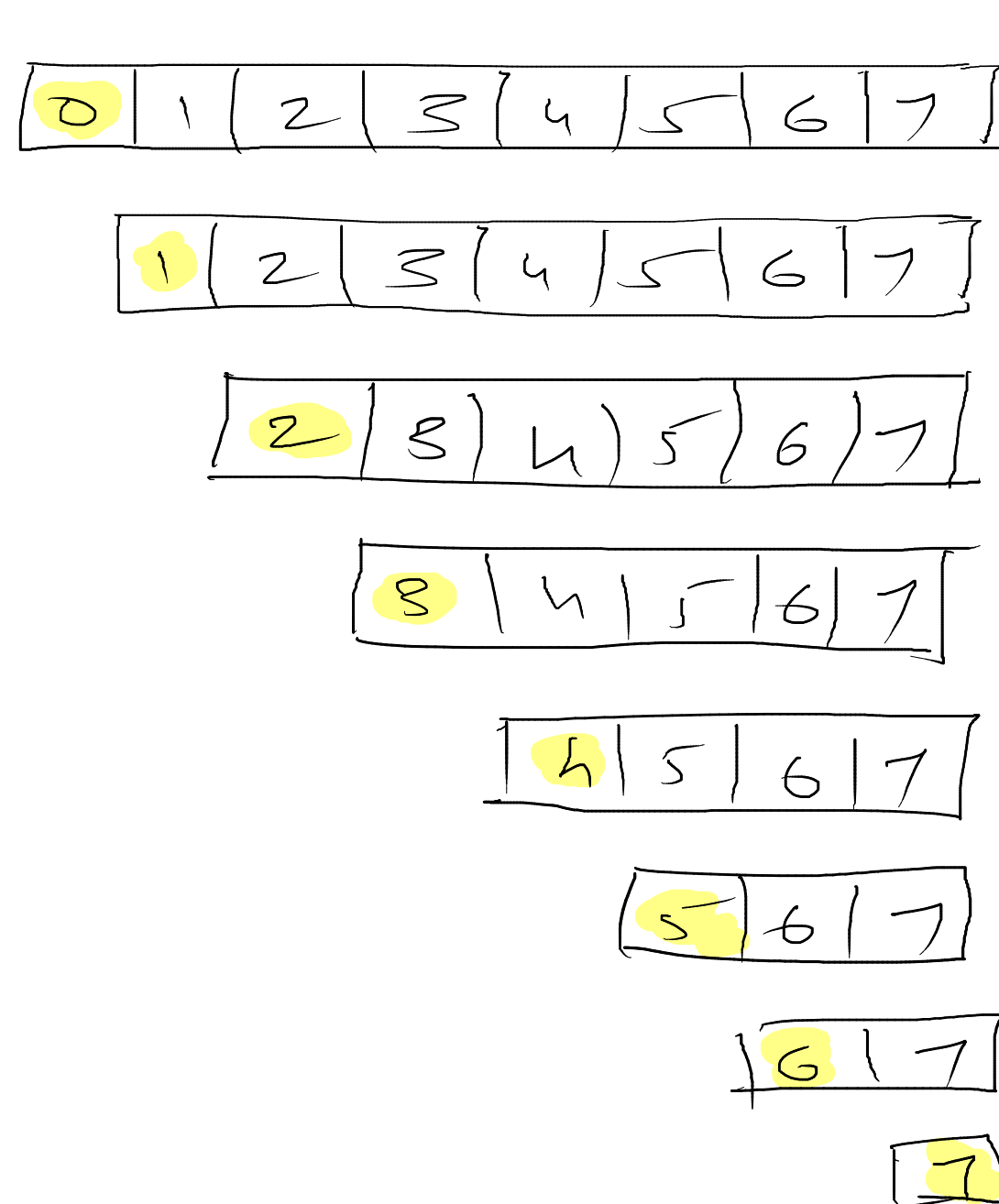
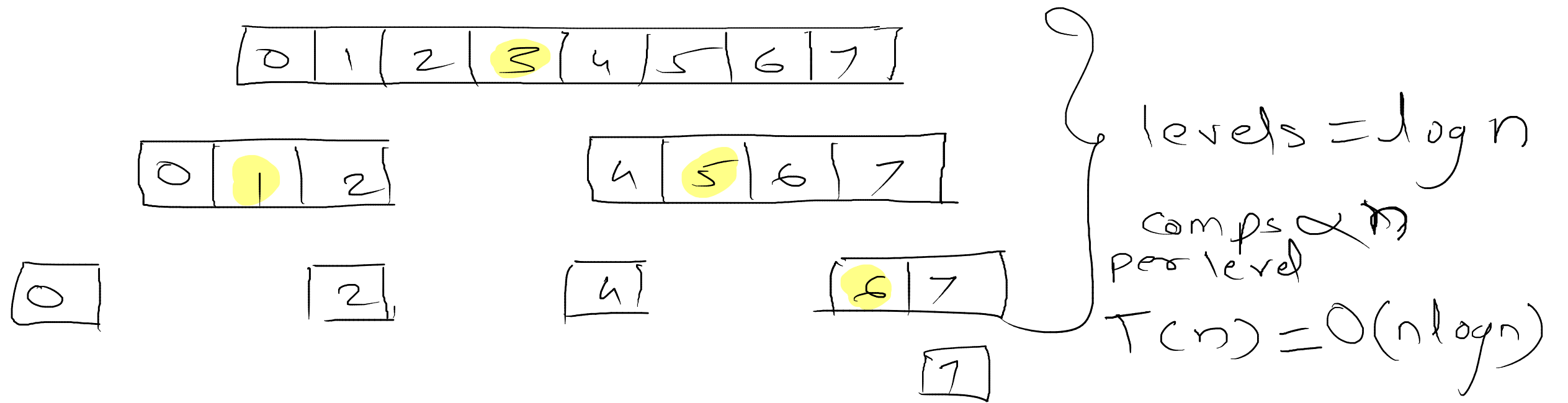
# Quick Sort

## Divide and Conquer

- //1. select pivot (axis/reference) element from array
- //2. arrange all smaller elements than pivot to the left side of pivot
- //3. arrange all greater elements than pivot to the right side of pivot
- //4. sort individual partitions(left and right of pivot) by applying same method



# Quick Sort



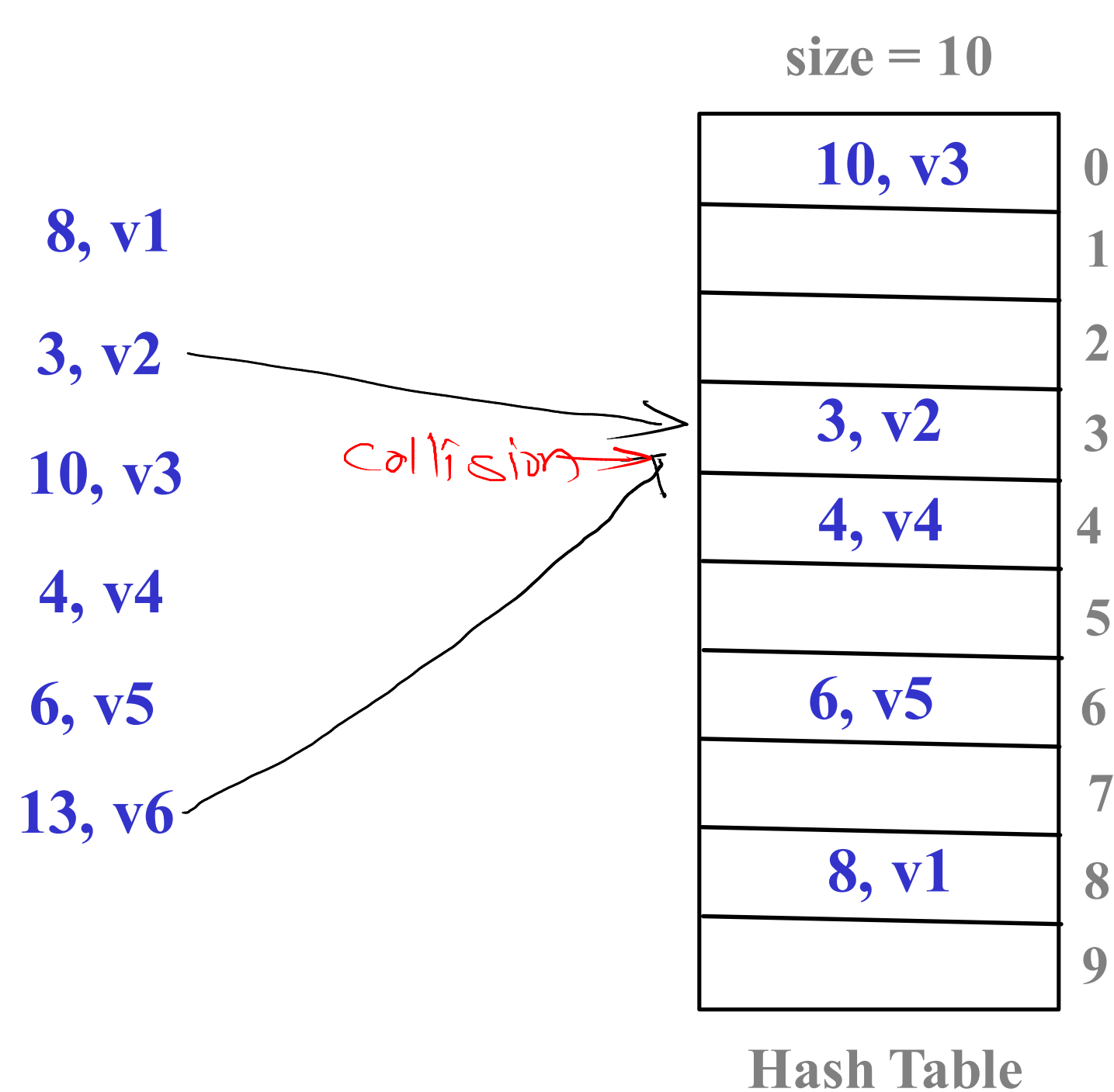
Time complexity of quick sort also depends on selection of pivot.

levels =  $n$   
 comp  $\propto n$   
 per level

$$T(n) = O(n^2)$$

Pivot selection —  
 to improve performance  
 — dual pivot quick sort  
 — median of 3

# Hashing



$$h(k) = k \% \text{size}$$

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(10) = 10 \% 10 = 0$$

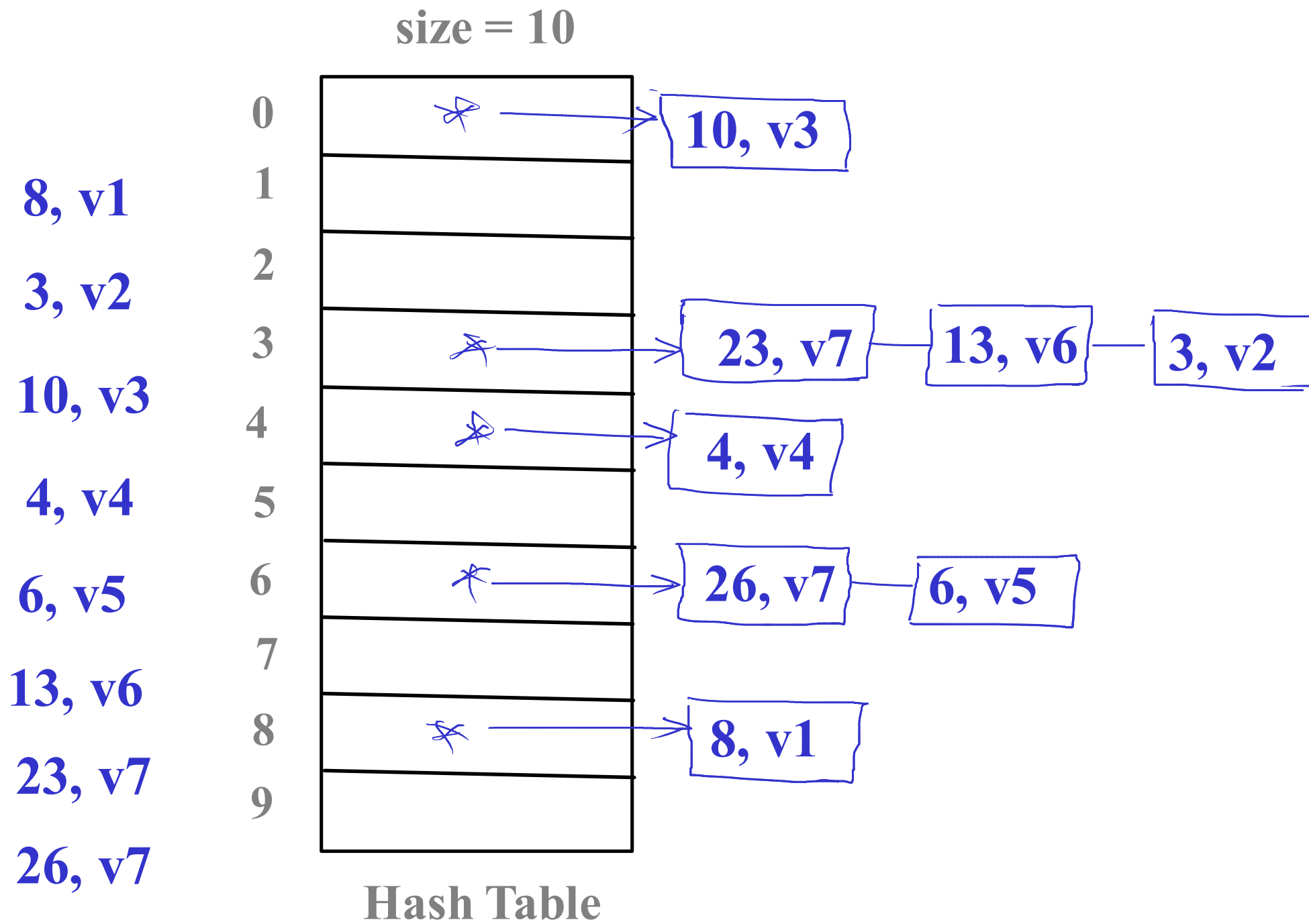
$$h(4) = 4 \% 10 = 4$$

$$h(6) = 6 \% 10 = 6$$

$$h(13) = 13 \% 10 = 3 \text{ (collision)}$$

# Closed Addressing/ Seperate Chaining / Chaining

$$h(k) = k \% \text{size}$$



$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(10) = 10 \% 10 = 0$$

$$h(4) = 4 \% 10 = 4$$

$$h(6) = 6 \% 10 = 6$$

$$h(13) = 13 \% 10 = 3$$

$$h(23) = 23 \% 10 = 3$$

$$h(26) = 26 \% 10 = 6$$