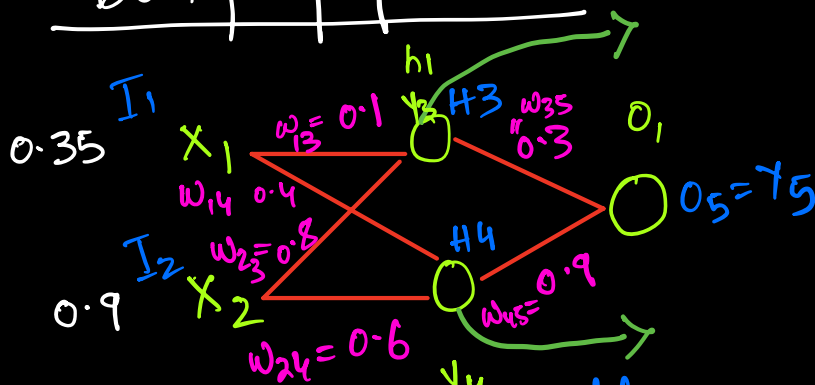


Today's Agenda

- 1) Backpropagation
- 2) Regularization
- 3) Tensorboard (Visualization of Training Acc/Los)

Backpropagation



Assumptions

$$L.R = 1$$

$$0.5 = 0.5$$

5 units = 2 input, 2 hidden neuron & 1 output

Forward Pass

$$\begin{aligned} a_1 &= (w_{13} * x_1) + (w_{23} * x_2) = (0.1 * 0.35) + (0.8 * 0.9) \\ &= 0.0355 + 0.72 \\ &= 0.755 \end{aligned}$$

$$\begin{aligned} a_2 &= (w_{14} * x_1) + (w_{24} * x_2) = (0.4 * 0.35) + (0.6 * 0.9) \\ &= 0.68 \end{aligned}$$

$$y_3 = \text{Sigmoid}(a_1) = 0.68$$

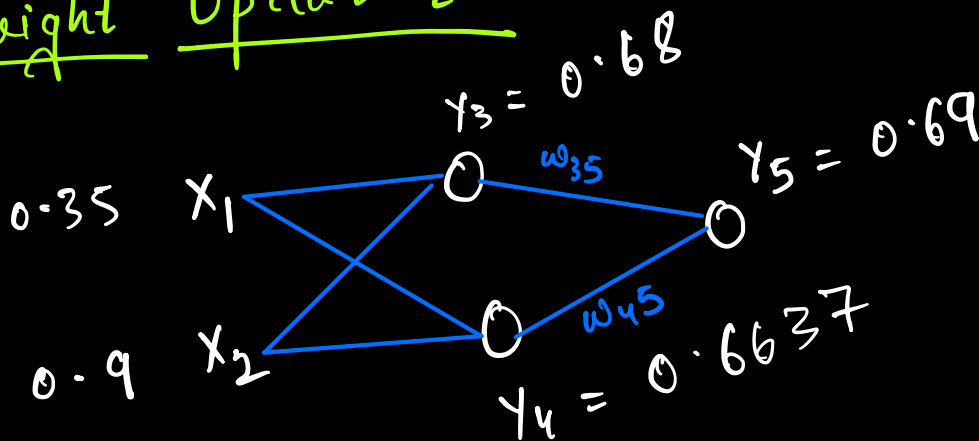
$$y_4 = \text{Sigmoid}(a_2) = 0.6637$$

$$\begin{aligned}
 a_3 &= (w_{35} \times y_3) + (w_{45} \times y_4) \\
 &= (0.3 \times 0.68) + (0.9 \times 0.6637) \\
 &= 0.801
 \end{aligned}$$

$$y_5 = \text{Sigmoid}(a_3) = 0.69$$

$$\text{Loss / Error} = y_{\text{Act}} - y_{\text{pred}} = 0.5 - 0.69 = -0.19$$

Weight Updation



Formula

Weight Change

$$\Delta w_{ij} = \underbrace{n}_{\text{LR}} \underbrace{(\delta_j)}_{\text{output}} \underbrace{O_i}_{\text{Error Term}} \rightarrow \text{LR}$$

$$\delta_j = O_j (1 - O_j) (t_j - O_j) \rightarrow \text{output Neuron}$$

$$\delta_j = O_j (1 - O_j) \sum_k w_{kj} \rightarrow \text{hidden Neuron}$$

$$\begin{aligned}
 &\text{target} = \text{actual} \\
 &= \text{original} = 0.5
 \end{aligned}$$

hidden unit
output unit

$$n = \text{LR} = 1$$

Fore output

$$\begin{aligned}\delta_5 &= y(1-y)(y_{\text{target}} - y) \\ &= 0.69(1-0.69)(0.5 - 0.69) \\ &= -0.0406\end{aligned}$$

Fore hidden

$$\begin{aligned}\delta_3 &= y(1-y) w_{35} * \delta_5 \\ &= 0.68(1-0.68) * (0.3 * -0.0406) \\ &= -0.00265\end{aligned}$$

$$\begin{aligned}\delta_4 &= y(1-y) w_{45} * \delta_5 \\ &= 0.6637(1-0.6637) 0.9 * -0.0406 \\ &= -0.0082\end{aligned}$$

$$\delta_5 = -0.0406$$

$$\delta_3 = -0.00265$$

$$\delta_4 = -0.0082$$

Weight change

$$\Delta w_{ij} = n \delta_j O_i$$

Annotations: δ_j is labeled "Error Term", O_i is labeled "Output y ", and n is labeled "L.R".

Output Neuron (w.c)

$$\begin{aligned}\Delta w_{45} &= 1 * \delta_5 * \textcircled{y_4} \\ &= 1 * -0.0406 * 0.6637 = \underline{-0.0269}\end{aligned}$$

Diagram: An arrow points from the circled y_4 to the text "Feed forward".

$$\underline{w_{45}(\text{new}) = \Delta w_{45} + w_{\text{old}}$$

$$= -0.0269 + 0.9$$

$$= 0.8731$$

$$\left\{ \begin{array}{l} \checkmark \\ w_{\text{new}} = \frac{w_{\text{old}} - \frac{\partial L}{\partial w_{\text{old}}}}{w_{\text{old}} + \frac{\partial L}{\partial w_{\text{old}}}} \end{array} \right.$$

$$w_{\text{old}} + \frac{\partial L}{\partial w_{\text{old}}}$$

$$\Delta_{35} = 1 \times \delta_5 \times 0.3$$

$$= 1 \times -0.0406 \times 0.68$$

$$= -0.0276$$

$$y_3 = 0.3$$

$$y_4 = 0.4$$

$$y_5 = 0.5$$

$$w_{35}(\text{new}) = \Delta w_{35} + w_{35} \text{ old}$$

$$= -0.0276 + 0.3$$

$$= 0.2724$$

$$w_{14} = \eta \delta_4 \odot_i$$

$$= \eta \delta_4 \times 1$$

$$= 1 \times -0.0082 \times 0.35$$

$$= -0.0028$$

$$w_{24} = \eta \delta_4 \odot_2$$

$$= 1 \times -0.0082 \times 0.9 = -0.00738$$

$$w_{14} \text{ new} = \Delta + w_{\text{old}} = -0.0028 + 0.4 = 0.397$$

$$w_{24} \text{ new} = -0.00738 + 0.6 = 0.5962$$

$$\Delta w_{13} = n \delta_3 o_1 = -0.00265 \times 0.35 = -0.0009$$

$$\Delta w_{23} = n \delta_3 o_2 = -0.00265 \times 0.9 = -0.0023$$

$$w_{13} \text{ new} = \Delta w_{13} + w_{\text{old}} = -0.0009 + 0.1 = 0.0991$$

$$w_{23} \text{ new} = \Delta w_{23} + w_{\text{old}} = 0.0023 + 0.8 = 0.797$$

$$w_1 =$$

$$w_2 =$$

$$w_3 =$$

$$w_4 =$$

$$w_5 =$$

$$w_6 =$$

→ 2nd Epoch *

1) Forward Propagation

1 Epoch = 10 iterations

Regularization

L1 Regularization (Lasso)

$$\text{Loss with L1} = \text{Loss} + \lambda \sum |w_i|$$

→ sum of absolute values of weights

→ Regularization Term

λ Penalize the large weights

ML → 1) Feature Selection avoid overfitting
2) Sparse weights vectors

Ridge (L2 Regularization)

$$L_2 \text{ with Loss} = \text{Loss} + \lambda \sum (w_i^2)$$

L1 → weights zero

L2 → towards smaller value close to 0, but not zero

L2 → widely used in deep learning

python

Copy code

```

from tensorflow.keras import layers, models, regularizers

model = models.Sequential()
model.add(layers.Dense(64, kernel_regularizer=regularizers.l1(0.01), activation='relu'))
model.add(layers.Dense(64, kernel_regularizer=regularizers.l1(0.01), activation='relu'))
model.add(layers.Dense(num_classes, activation='softmax'))

model.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
model.fit(x_train, y_train, epochs=10, batch_size=32)

```

python

Copy code

```

from tensorflow.keras import layers, models, regularizers

model = models.Sequential()
model.add(layers.Dense(64, kernel_regularizer=regularizers.l2(0.01), activation='relu'))
model.add(layers.Dense(64, kernel_regularizer=regularizers.l2(0.01), activation='relu'))
model.add(layers.Dense(num_classes, activation='softmax'))

model.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
model.fit(x_train, y_train, epochs=10, batch_size=32)

```

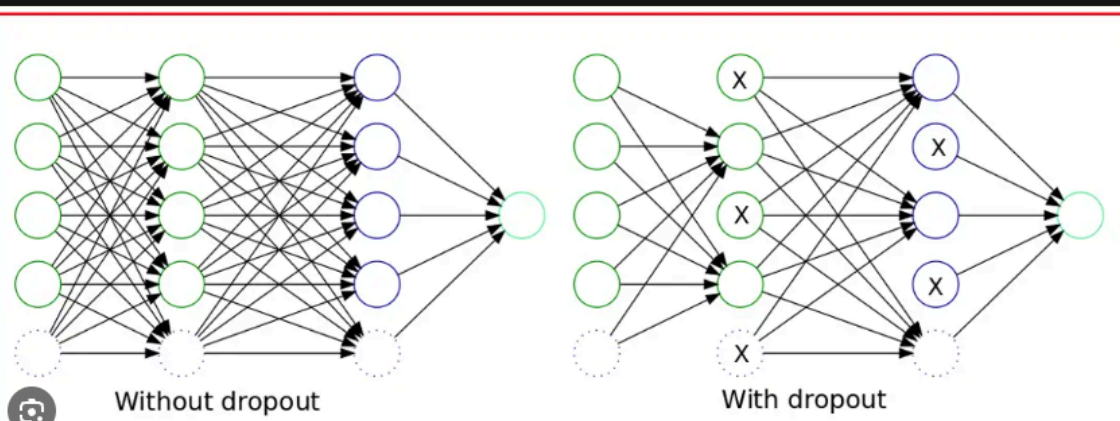
Dropout

Inactive / Deactive

No Activation

neurons in a layer

Hide something from the network



$$0 \cdot (wx + b) = 0$$

$h_1 \rightarrow$ hidden layer

Dropout (·)

Hide & Show
↳ generalized

random selection
of neurons
in every iteration
of epochs.

64 neurons

= 6 neurons

12 neurons = 20%

15 neurons

18 neurons

25% =

30% =

Not more than 30%

Information loss for the network

```
# Define the model architecture with dropout regularization
```

```
model = Sequential([
```

```
    Dense(512, activation='relu', input_shape=(784,)),
```

```
    Dropout(0.2), # Dropout with probability 0.2
```

```
    Dense(512, activation='relu'),
```

```
    Dropout(0.2), # Dropout with probability 0.2
```

```
    Dense(10, activation='softmax')
```

```
])
```

512

General Thumb Rule

- 1) Don't use it in the start
- 2) Not more than 30%.
- 3) Use it when you are closing the network

(0.05) Penultimate layer
(0.1) Ultimate layer (last layer)
(0.15) Output X
(0.25) * input

Dense penultimate
Dense ultimate
Dense, softmax Output layer
only on Training

L
L-1
L-2
L-3

1) Early Stopping

Stop the training at a certain point
when there is no improvement.

Metrics

→ Acc / Loss

Epoch 1

0.21

Better

0.04 ✓

Epoch 15

0.0401

Epoch 25

0.04001

Epoch 35

0.03998

Epoch 99

Overfitting

0.3

35 - 99 epochs
overfitting)

Callbacks noise

No Network change

Model Strategy

Training Strategy

```
python Copy code

import numpy as np
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense
from tensorflow.keras.callbacks import EarlyStopping
from sklearn.model_selection import train_test_split

# Generate some dummy data
X = np.random.rand(1000, 10)
y = np.random.randint(2, size=(1000,))

# Split data into training and validation sets
X_train, X_val, y_train, y_val = train_test_split(X, y, test_size=0.2, random_state=0)

# Define a simple neural network model
model = Sequential()
model.add(Dense(64, activation='relu', input_dim=10))
model.add(Dense(1, activation='sigmoid'))

# Compile the model
model.compile(optimizer='adam', loss='binary_crossentropy', metrics=['accuracy'])

# Define early stopping criteria
early_stopping = EarlyStopping(monitor='val_loss', patience=5, verbose=1, restore_best_weights=True)

# Train the model with early stopping
history = model.fit(X_train, y_train, epochs=100, batch_size=32, validation_data=(X_val, y_val),
                    callbacks=[early_stopping])

# Evaluate the model
loss, accuracy = model.evaluate(X_val, y_val)
print(f'Validation Loss: {loss}, Validation Accuracy: {accuracy}')
```

```
ng criteria
yStopping(monitor='val_loss', patience=5, verbose=1, restore_best_weights=True)
```