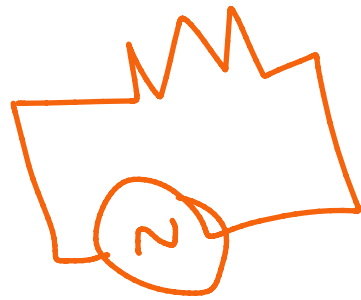


Power Delivered to a Resistance by a Sinusoidal Source

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- Suppose that a voltage given by $v(t)=100\cos(100\omega t)\text{V}$ is applied to a 50Ω resistance.
- Sketch $v(t)$ to scale versus time.
- Find the rms value of the voltage and the average power delivered to the resistance.
- Find the power as a function of time and sketch to scale

$$v(t)=100\cos(100\omega t)\text{V}$$

$$R=50\text{ Ohm}$$

1. RMS value of Voltage (V_{rms})

$$V_{\text{rms}} = V_m/\sqrt{2}$$

$$= 100/\sqrt{2} = 100/1.414 = 70.7\text{ V}$$

$$2. P_{\text{avg}} = V_{\text{rms}}^2/R = 70.7^2/50 = 100\text{ W}$$

$$p(t) = v(t)^2/R$$

$$= (100\cos(100\omega t))^2/50$$

$$= 200 \cos^2(100\omega t)$$

ω = radians per sec

f = Hz

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- Suppose that a sinusoidal voltage is given by

$$v(t) = 150 \cos(200\pi t - 30^\circ) \text{ V}$$

- Find the angular frequency, the frequency in hertz, the period, the peak value, and the rms value.
- If this voltage is applied to a 50Ω resistance, compute the average power delivered.
- Sketch $v(t)$ to scale versus time

1. Angular Frequency (ω) = 200π

2. Frequency in Hz =

$$\omega = 2\pi f$$

$$v(t) = 150 \cos(200\pi t - 30^\circ) \text{ V}$$

$$F = \omega / 2\pi = 100 \text{ Hz}$$

3. Period (T) = $1/f = 0.01 \text{ sec}$

4. Peak value (V_m) = 150

5. Rms Value (V_{rms}) = $v_m / \sqrt{2} = 150 / \sqrt{2} = 106.0 \text{ V}$

6.

7. $P_{avg} = V_{rms}^2 / R = 106^2 / 50 = 224.72 \text{ W}$

$$T=4$$

$$F=1/4 = 0.25$$

$$W=2 * \pi * F = 2*\pi*0.25 \text{ rad/sec} = 0.5\pi$$

$$V(t) = \sin(0.5\pi t)$$