

1) a)
(1) Operations in Relational Algebra

* Selection (σ) , selects a subset of rows from relation

* Projection (π) , Deletes unwanted columns from relation

* Cross-product (\times) , Allows us to combine two relation

* Set-difference ($-$) , Tuples in relation 1, but not in relation 2.

* Union (\cup) , Tuples in ^{relation} 1 and in relation 2 combination.

ii) Additional Operations

* Intersection

* Join

* division

⇒ Since each operation returns a relation, operations can be compound (Algebra is closed)

Selection: (student)

sid	sname	rating	age
1	a	4	36
2	b	9	35
3	c	10	35

σ ratings gives (Student)

sid	sname	rating	age
1	a	9	35
2	b	10	35
3	c		

Union, Intersection & Set Difference:-

S_1		S_2	
sid	sname	sid	sname
1	a	2	b
2	b	3	c

$S_1 \cup S_2$ gives \Rightarrow

sid	sname
1	a
2	b
3	c

(Union)

$S_1 \cap S_2$ gives \Rightarrow

sid	sname
2	b

(Intersection)

$S_1 - S_2$ gives \Rightarrow

sid	sname
1	a
2	b

(Set Difference)

Projection:-

sid	sname	age
1	a	35
2	b	25
3	c	35

$\Pi_{age}(S_1)$ gives \Rightarrow age
35
25

Cross product:-

Each row of table 1 is paired with each row of table 2

Join:-

Each row of table 1 is paired with rows of table 2 under some common attribute or Candidate Key

1)

b) ~~Select d.dname from (select d.dname~~

SQL query: Select dname from Dogs where
(select dog dname which never participated)
and select age from Dogs where age > 5 years.

2)

b)

a. $\pi_{\text{(theater name)}} (\sigma_{\text{title} = "3 Idiots" \wedge \text{Time} > 5 \text{pm}})$ (program)

b. $\pi_{\text{(producer name)}} (\sigma_{\text{title (produced)} = \text{title (liked)})}$

a)

$R(A, B, C, D)$

$FD_1 = \{A \rightarrow B, B \rightarrow C, D \rightarrow C\}$

$FD_2 = \{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$

so the subset relation of R ,

$R_1 = \{A, B, C\}$ &

$R_2 = \{A, B, D\}$.

FD_1 and FD_2 combine gives $R(A, B, C, D)$

3). $\text{FD } X \rightarrow Y$ only if X corresponds Y is same in tuple 1 & tuple 2

a) Quantity \rightarrow Name
 * It holds FD (Functional dependency)

b) Quantity \rightarrow Model
 * It doesn't hold FD
 as Quantity 1 has two record Roll's Royce
 Ghost and Ferrari super fast

c) Model \rightarrow Name
 * It doesn't hold
 * It holds Functional dependency

d) Model \rightarrow Quantity
 * It holds functional dependency

e) Name \rightarrow Quantity :-
 * It holds functional dependency