

Example 1 - Kirchhoff's Laws

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- Find the steady-state current for the circuit shown in Figure.
- Also, find the phasor voltage across each element and construct a phasor diagram.

Step 1: To convert circuit elements of AC circuit using complex impedances

$$\omega = 500$$

$$Z_L = j\omega L = j \cdot 500 \cdot 0.3 = 150j$$

$$Z_C = 1/j\omega C = 1/(j \cdot 500 \cdot 40 \cdot 10^{-6}) = -50j$$

Step 2: To convert the voltage or currents in phasor form

$$v_s(t) = 100 \cos(500t + 30^\circ)$$

$$V_s = 100 \angle 30^\circ$$

Step 3: KVL

$$-100 \angle 30^\circ + 100(I) + (150j)I + (-50j)I = 0$$

$$(100 + 150j - 50j)I = 100 \angle 30^\circ$$

$$I = 100 \angle 30^\circ / (100 + 100j)$$

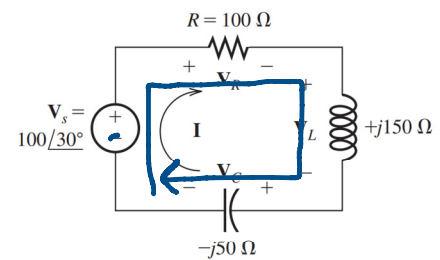
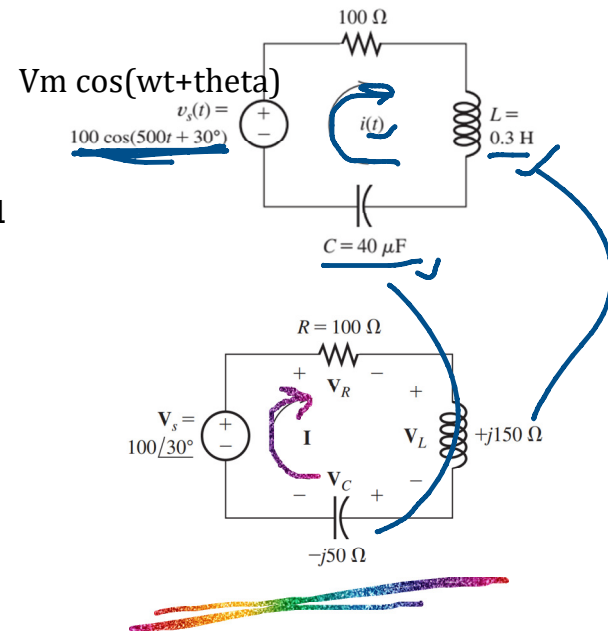
$$I = (100(\cos(30^\circ) + j\sin(30^\circ))) / (100 + 100j)$$

=

$$V_R = 100 * I$$

$$V_L = 150j * I$$

$$V_C = -50j * I$$



Example 2 - Node-Voltage Analysis

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- Use the node-voltage technique to find $v_1(t)$ and $v_2(t)$ in steady state for the circuit shown in Figure

Step 1: Convert the Circuit elements in to complex impedances

$$\omega = 100$$

$$Z_L = j\omega L = j \cdot 100 \cdot 0.1 = 10j$$

$$Z_C = 1/(j\omega C) = -5j$$

Step 2: Convert the voltage or currents sources into phasor form

$$2\sin(100t) \rightarrow 2\angle -90^\circ$$

$$1.5\cos(100t) \rightarrow 1.5\angle 0^\circ$$

Step 3:

Node 1:

$$(V_1 - 0)/10 + (V_1 - V_2)/(-5j) - 2\angle -90^\circ = 0$$

Node 2:

$$(V_2 - V_1)/(-5j) + (V_2 - 0)/10j - 1.5\angle 0^\circ = 0$$

$$(1/10 - 1/5j) v_1 + (1/5j) v_2 = 2\angle -90^\circ = 2(\cos(-90^\circ) + j\sin(-90^\circ)) = 2(0 + j(-1)) = -2j$$

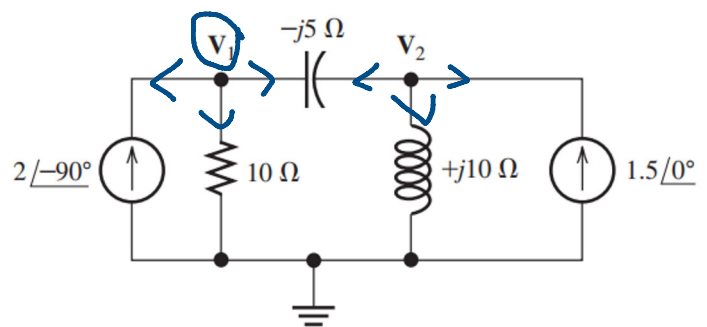
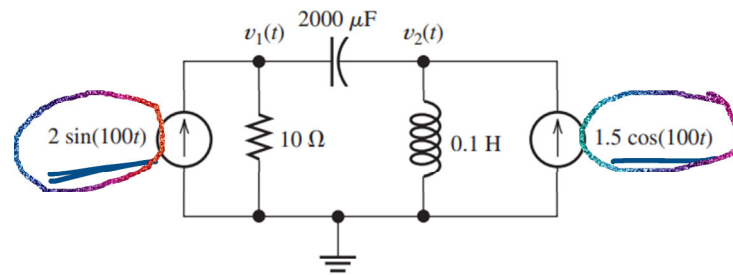
$$(1/5j) v_1 + (-1/5j + 1/10j) v_2 = 1.5\angle 0^\circ = 1.5(\cos(0^\circ) + j\sin(0^\circ)) = 1.5(1 + 0) = 1.5$$

$$\mathbf{A} = \begin{bmatrix} 1/10 - 1/5j & 1/5j \\ 1/5j & -1/5j + 1/10j \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} -2j \\ 1.5 \end{bmatrix}$$

$$V_1 = 14.0000 + 8.0000i$$

$$V_2 = 28.0000 + 1.0000i$$



Example 3 - Mesh Current Analysis

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- Solve for the mesh currents I_1 and I_2

Step 1 & Step 2: ✕

Step 3:

Loop 1:

$$5(I_1) + 15j(I_1 - I_2) - 20\angle 0^\circ = 0$$

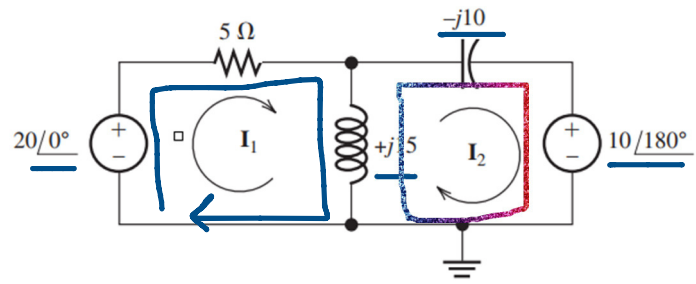
Loop 2:

$$-10j(I_2) + 15j(I_2 - I_1) + 10\angle 180^\circ = 0$$

$$() I_1 + () I_2 =$$

$$() I_1 + () I_2 =$$

I_1 and I_2



Example 4 - AC Power Calculations

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