

4.1.22

Network security → measure to protect data during transmission.

Internet Security → " over collection of interconnected networks

Health care, Education, Banking, s/w, Marketing, shopping.

Banking → user credentials → ABC → Database
123 encrypted version

↳ cryptography.

* Gmail information → encrypted information. (Google data center)

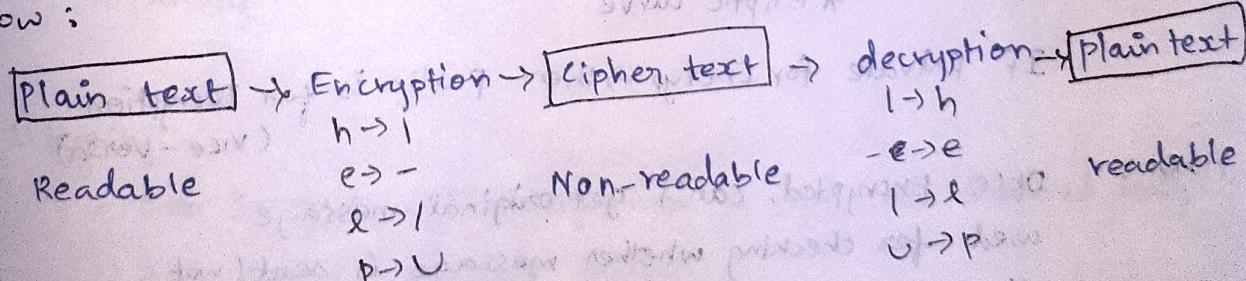
* WhatsApp → encrypted mode of sharing.

Cryptography:

→ method of transmitting secured data by communication in such a way that only the destined person knows about the actual information which is transmitted.

Ex: Person1 → "help" → Person2
X P5 → I-U
X P4 → e → -
P6X → P3X → A9DE → l
only person2 can decrypt the message.

Flow:



(Input space) RAM

06th Jan, 2022 :

- Cipher → algorithm for transforming PT to CT
- Key → Information used in cipher that is only known by sender & receiver
- Encipher → (Encryption) process of converting PT to CT
- Decipher → (Decryption) process of converting CT to PT
- Cryptanalysis → Study of methods of deciphering CT without knowing actual key.
- Cryptology → Domain of cryptography & cryptanalysis.
- Cryptography → Study of encryption principles & methods

Types :

i) Symmetric cryptography

ii) Asymmetric cryptography

iii) Hash functions

Sym: Same key used by both sender & receiver.
also called as private key cryptography.

Algorithms:
* DES
* AES
* IDEA

Asym: different keys. (private & public key)

(PKCryp)
Algorithms:
* RSA
* Elliptic curve

If private for Encrypt → then public is for Decryption
(vice-versa)

Hash: Once Encrypted, can't get original message
used for checking whether message is sent/not.

Algorithms:
* SHA
* MD5 (message digest)

Main Application → (maintain secrecy in the message transformations)
of Cryptographies

Ex : WhatsApp : end-to-end encrypted
(Asymmetric cryptography)

Crypt in: (real life usages)

→ secure communication

* HTTPS (secured hyper text)

* Bluetooth, GSM (Global sys), 802.11iWPA2 (WEP)
for mobile communication

→ user authentication

→ Encrypting files on Disk (EFS, Truecrypt)

→ Content protection (CSS, AACS → Alg for protection Blu-ray movies to get encrypted)

Secure Socket Layers/TLS:

* Handshake protocol: Establishing shared secret key using (Generation) Public-key cryptography

* Record Layer: Transmit data using shared secret key (transmission)

→ Ensuring Confidentiality & Integrity.

Crypt follows CIA triad: confidentiality, Integrity, Availability

11th Jan 2022:

→ confidentiality: Person → personal details → company → need to maintain confidentiality.

→ Data confidentiality: Assuring private/confidential is not made available.

→ privacy:

→ Integrity:

→ Data Integrity: Assuring info in msg are changed only in a specified manner.

→ System Integrity:

→ Availability: system works promptly

OSI Security Architecture:

- used to provide security services.
 - focuses on :
 - i) security attack (action that compromised security)
 - diff attacks takes place on attempt during transmission
 - tackling
 - ii) security service tech to overcome attack
 - iii) security mechanism (implement those service we use)
 - (detect, prevent, recover from a security attack)
- security attack :
- i) passive attack
 - ii) active attack

PA :

PA :
 i) Here, C will modify data
 ii) unauthorised user (attacker) intercepts the data <
 observe the data, how it is transferred & collect the information
(no modification will be done here)

Types of PA:

- i) Release of message contents ② → observed
 - Ex: phone tapping (just listening)
 - Traffic analysis
 - ii) Traffic Analysis
- ii) A → B (will be encrypted message)

Network may be public .

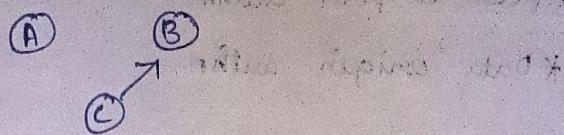
- ③ → observe position of message, length, freq of message , location of the communication channel

Types of AA:

i) masquerade

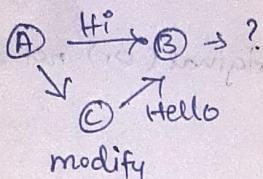
Before A sends, C send to B as if A has sent.

Instead of receiving original, receiver got from attacker



ii) Replay:

① observe & modify and send to receiver.
② receiver will be in confused state.

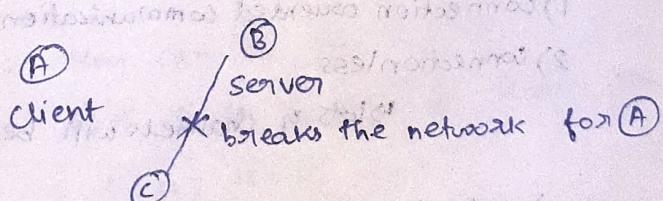


iii) Modification of message:

① A → B → ?
② C → B
Get from sender & modified it to B

iv) Denial of service:

③ break the network of the server providing service



AA:

- Hard to prevent
- physical, SW and network vulnerabilities
- Detect and recover from any disruptions/delays.
- If detection has deterrent effect, it may also contribute to prevent.

PA:

- Neither sender nor receiver can know
- hard to detect
- Encryption can reduce.
- more emphasis on prevention than detection.

Security Service: implements security policies.

i) Authentication

→ to ensure that communication is authentic b/w sender & receiver.

→ two types:

* peer to peer authn.

* Data origin authn.

PP:

Peer → Entity

Authn each entity before transmission. Checking (A), (B)

DO :

check data first, whether it is original (or) not.

Checking source of data

ii) Access control:

→ ability to limit & control the access to the system.

Ex: Bank Manager can access some where employees
can't

iii) Data confidentiality

more useful to prevent passive attack.

Services provided for

1) connection oriented communication

(A) — (B)

2) connectionless

(A) (B)
↳ lots of channels will be there

3) selective field

4) Traffic field/flow (observe source of data to provide security)

iv) Data Integrity: (Assure Receiver gets the sender's message)

v) Non repudiation

(A) → should prove as actual sender.

(B) → should prove as actual receiver.

Characteristics:

→ type of operations used for encrypt, decrypt

i) subst: Each element in plain text is mapped into another element.

ii) transposition: Each element in plain text are rearranged.

→ No. of key used

i) Symmetric 1 key

ii) Asymmetric 2 key → Priv, Pub

→ way in which plain text is processed

i) block cipher

ii) stream

subst: Caesar cipher, Monoalphabetic, Playfair, Hill,

Polyalphabetic, One-Time Pad

Transposition: Rail Fence, Row column Transposition

Caesar Cipher:

→ Each alphabet replaced with alphabet + 3

(letters in Caesar cipher are in groups of 3)

(e.g. $a \Rightarrow d$)

(e.g. $b \Rightarrow e$)

(at random if done deeper, go to break)

Plain text $\rightarrow a$ (P and P are not overlapped) Key $\Rightarrow 3$

Cipher text $\rightarrow d s s o h$

Monoalphabetic: Key can be any number of letters

Both sender & receiver knows the key

($K=3$; $K=4$; $K=7$, ...)

Then $\text{alphabet} + K \Rightarrow \text{cipher text}$

Cryptanalyst will be watching.

Security mechanism: implement security policies by services.

→ process to detect/prevent the messages from unauthorized access.

Protocol → X.800 standard

Specific protocol layers

non-specific protocol layer /
pervasive security mechanism

specific security mechanism:

- Encipherment
- Digital signature (information + signature of sender)
- Access control
- Data Integrity (Assurance for original data)
- Authentication
- Traffic padding (Gaps in the data will be filled, while C doesn't know which is real data, but C does)

→ Routing Control

→ Notarization (selecting a 3rd trusted party to control

communication b/w two entities)

(keeps record of requests made by sender to receiver for later denial)

Pervasive security mechanism:

- Trusted functionality
- Security label
- Event detection (security related issues should be detected)
- Security recovery
- Security audit trail (Periodic review of transmissions in data, about data → personal, security reasons)

Hill cipher : 1929, Lester Hill

$$a \rightarrow 0$$

$$b \rightarrow 1$$

⋮

$$z \rightarrow 25$$

→ select a message to encrypt.

i) welcome

let $n=2$; we | lc | om | ea

→ select a key.

If $n=2$, then key should be 2×2 matrix, $\text{len}(\text{key})=4$

If $n=3$, then key should be 3×3 matrix, $\text{len}(\text{key})=9$

Ex: key = test [4 in length]

$$\text{key} = \begin{bmatrix} t & e \\ s & t \end{bmatrix} \Rightarrow \text{key} = \begin{bmatrix} 19 & 4 \\ 18 & 19 \end{bmatrix}$$

$$a \rightarrow 0 \quad j \rightarrow 9 \quad s \rightarrow 18$$

$$b \rightarrow 1 \quad k \rightarrow 10 \quad t \rightarrow 19$$

$$c \rightarrow 2 \quad l \rightarrow 11 \quad u \rightarrow 20$$

$$d \rightarrow 3 \quad m \rightarrow 12 \quad v \rightarrow 21$$

$$e \rightarrow 4 \quad n \rightarrow 13 \quad w \rightarrow 22$$

$$f \rightarrow 5 \quad o \rightarrow 14 \quad x \rightarrow 23$$

$$g \rightarrow 6 \quad p \rightarrow 15 \quad y \rightarrow 24$$

$$h \rightarrow 7 \quad q \rightarrow 16 \quad z \rightarrow 25$$

$$i \rightarrow 8 \quad r \rightarrow 17$$

→ each pair into component vector, then numerical value

$$\begin{pmatrix} w \\ e \end{pmatrix} \Rightarrow \begin{pmatrix} 22 \\ 4 \end{pmatrix} \quad \begin{pmatrix} l \\ c \end{pmatrix} \quad \begin{pmatrix} 0 \\ m \end{pmatrix} \quad \begin{pmatrix} e \\ a \end{pmatrix}$$
$$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$$
$$\begin{pmatrix} 11 \\ 2 \end{pmatrix} \quad \begin{pmatrix} 14 \\ 12 \end{pmatrix} \quad \begin{pmatrix} 4 \\ 0 \end{pmatrix}$$

$$\text{cipher text} \Rightarrow K * P \bmod 26 \Rightarrow K * \begin{pmatrix} w \\ e \end{pmatrix} \bmod 26$$

$$\begin{bmatrix} 19 & 4 \\ 18 & 19 \end{bmatrix} \begin{bmatrix} 22 \\ 34 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 434 \\ 472 \end{bmatrix} \text{ mod } 26 \Leftrightarrow \begin{bmatrix} 18 \\ 4 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 18 \\ 4 \end{bmatrix} \simeq \begin{bmatrix} s \\ e \end{bmatrix}$$

$$\begin{bmatrix} 19 & 4 \\ 18 & 19 \end{bmatrix} \begin{bmatrix} 11 \\ 2 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 217 \\ 236 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 9 \\ 2 \end{bmatrix} \Rightarrow \begin{bmatrix} j \\ c \end{bmatrix}$$

$$\begin{bmatrix} 19 & 4 \\ 18 & 19 \end{bmatrix} \begin{bmatrix} 14 \\ 12 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 314 \\ 480 \end{bmatrix} \Rightarrow \begin{bmatrix} 2 \\ 12 \end{bmatrix} \Rightarrow \begin{bmatrix} c \\ m \end{bmatrix}$$

$$\begin{bmatrix} 19 & 4 \\ 18 & 19 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 46 \\ 72 \end{bmatrix} \Rightarrow \begin{bmatrix} 24 \\ 20 \end{bmatrix} \Rightarrow \begin{bmatrix} y \\ u \end{bmatrix}$$

cipher \Rightarrow Sejeicmyu

Decryption:

$$\text{Plain text} \Rightarrow k^{-1}c \text{ mod } 26$$

$$k^{-1} = \frac{1}{|k|} \text{adj}(k)$$

$$|k| \Rightarrow 289$$

Finding multiplicative inverse:

$$289x \text{ mod } 26 = 1$$

$$\Rightarrow 3x \text{ mod } 26 = 1$$

$$\Rightarrow 3x \equiv 1 \pmod{26} \quad (\text{condition satisfied})$$

$$\therefore x = 9$$

$$\frac{1}{|k|} = 9$$

compute adj(K)

$$K = \begin{bmatrix} 19 & 4 \\ 18 & 19 \end{bmatrix} \Rightarrow \text{adj}(K) = \begin{bmatrix} 19 & -4 \\ -18 & 19 \end{bmatrix}$$

$$K^{-1} = 9 \begin{bmatrix} 19 & -4 \\ -18 & 19 \end{bmatrix} \Rightarrow 9 \begin{bmatrix} 19 & 22 \\ -8 & 19 \end{bmatrix} \Rightarrow \begin{bmatrix} 171 & 198 \\ 72 & 171 \end{bmatrix}$$

$$\begin{bmatrix} 171 & 198 \\ 72 & 171 \end{bmatrix} \begin{bmatrix} 18 \\ 4 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 3896 \\ 1980 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 22 \\ 4 \end{bmatrix}$$

$$\begin{bmatrix} 171 & 198 \\ 72 & 171 \end{bmatrix} \begin{bmatrix} 11 \\ 2 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 2277 \\ 1134 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 15 \\ 16 \end{bmatrix}$$

$$\begin{bmatrix} 171 & 198 \\ 72 & 171 \end{bmatrix} \begin{bmatrix} 14 \\ 12 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 4770 \\ 3060 \end{bmatrix} \text{ mod } 26$$

$$\begin{bmatrix} 171 & 198 \\ 72 & 171 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 684 \\ 72 \end{bmatrix} \text{ mod } 26$$

$$(11 * 1) + (11 * 2) = 31 * 8$$

$$(11 * 1) + (11 * 3) = 31 * 5$$

$$(11 * 1) + (11 * 2) = 31 * 0$$

$$(11 * 1) + (11 * 2) = 31 * 3$$

$$(11 * 1) + (11 * 2) * 11 = 31 * 8$$

$$(31 * 1) + (31 * 2) = 31 * 3$$

$$(31 * 1) + (31 * 2) = 31 * 0$$

$$(31 * 1) + (31 * 2) = 31 * 1$$

22 Jan :

$$15x + 26y = \gcd(15, 26)$$

$$a = bq + r$$

$$26 = 15 \times 1 + 11 \Rightarrow 26 = 1 \times 15 + 11$$

$$15 = 1 \times 11 + 4$$

$$11 = 2 \times 4 + 3$$

$$4 = 1 \times 3 + 1$$

$$3 = 3 \times 1 + 0$$

$$\boxed{\gcd(15, 26) = 1}$$

Step : 2

$$\begin{aligned} \Rightarrow 1 &= 4 - 1 \times 3 \\ &= 4 - 1 \times (11 - 2 \times 4) \\ &= 4 - (11) + (2 \times 4) \\ &= ((\cancel{*}4)) - ((\cancel{*}11)) + (2 \cancel{*} 4) \\ &= (3 \cancel{*} 4) - (1 \cancel{*} 11) \\ &= (3 \cancel{*} 4) + (-1 \cancel{*} 11) \\ &= (3 \cancel{*} 15 - (1 \cancel{*} 11)) + (-1 \cancel{*} 11) \\ &= 3 \cancel{*} (15 - (1 \cancel{*} 11)) - 11 \\ &= (3 \cancel{*} 15) - (3 \cancel{*} 11) - 11 \\ &= (3 \cancel{*} 15) - (3 \cancel{*} 11) + (-1 \cancel{*} 11) \\ &= (3 \cancel{*} 15) - (4 \cancel{*} 11) \\ &= 3 \cancel{*} 15 - 4 \cancel{*} (26 - 1 \cancel{*} 15) \\ &= (3 \cancel{*} 15) - (4 \cancel{*} 26) + (4 \cancel{*} 15) \\ &= (1 \cancel{*} 15) - (4 \cancel{*} 26) \\ 1 &= (15 \cancel{*} 7) + (26 \cancel{*} -4) \end{aligned}$$

$$15x + 26y$$

$$\therefore x = 7 ; y = -4$$

$$\textcircled{1} 1914x + 899y = \gcd(1914, 899) \rightarrow x = 33; y = -14$$

$$\textcircled{2} 93x + 219y = \gcd(93, 219) \rightarrow x = 8; y = -17$$

①

$$1914 = 899 \times 2 + 116$$

$$= 2 \times \boxed{899 + 116}$$

$$\Rightarrow 899 = 7 \times \boxed{116 + 87}$$

$$116 = 1 \times 87 + 29$$

$$87 = 3 \times 29 + 0$$

$$\gcd(1914, 899) = 29$$

$$\Rightarrow 116 = 1 \times 87 + 29$$

$$\Rightarrow 29 = 116 - 1 \times 87$$

$$= 116 - 1 \times (899 - 7 \times 116)$$

$$= 116 - 1 \times 899 + (7 \times 116)$$

$$= (8 \times 116) - (1 \times 899)$$

$$= 8 \times (1914 - 2 \times 899) - (1 \times 899)$$

$$= 8 \times 1914 - (16 \times 899) - (1 \times 899)$$

$$29 = 8 \times 1914 - (17 \times 899)$$

$$\Rightarrow 1914x + 899y = \gcd(1914, 899)$$

$$\boxed{x = 8; y = -17}$$

$$\begin{array}{r} 899 \sqrt{1914} \\ \hline 1798 \\ \hline 116 \\ \hline 7 \\ \hline 899 \\ \hline 812 \\ \hline 87 \end{array}$$

$$\textcircled{2} \quad 93x + 219y = \gcd(93, 219)$$

$$\Rightarrow 219 = 93 \times 2 + r$$

$$\Rightarrow 219 = 2 \times \boxed{93 + 33}$$

$$93 = 2 \times \boxed{33 + 27}$$

$$33 = 1 \times \boxed{27 + 6}$$

$$27 = 4 \times \boxed{6 + 3}$$

$$6 = 2 \times 3 + 0$$

$$\boxed{\gcd(93, 219) = 3}$$

$$\begin{array}{r} 2 \\ 93 \overline{) 219} \\ 186 \\ \hline 33 \end{array}$$

$$27 = 4 \times 6 + 3$$

$$= 4 \times (33 - 1 \times 27) + 3$$

$$= (4 \times 33) - (4 \times 27) + 3$$

$$= (4 \times 33) - 4 \times (93 - 2 \times 33) + 3$$

$$= (4 \times 33) - (4 \times 93) + (8 \times 33) + 3$$

$$= (12 \times 33) - (4 \times 93) + 3$$

$$= 12 \times (219 - 2 \times 93) + 3 - (4 \times 93)$$

$$= (12 \times 219) - (24 \times 93) + 3 - (4 \times 93)$$

$$\boxed{12 \times 219 - 24 \times 93 + 3}$$

$$27 = 4 * 6 + 3$$

$$\begin{aligned}\Rightarrow 3 &= 27 - 4 * 6 \\&= 4 * 6 - 27 \\&= 4 * 6 - (93 - 2 * 33) \\&= 4 * 6\end{aligned}$$

$$\Rightarrow 27 = 4 * 6 + 3$$

$$\begin{aligned}3 &= 27 - 4 * 6 \\&= 27 - 4 * (33 - 1 * 27) \\&= 27 - (4 * 33) + (4 * 27)\end{aligned}$$

$$\begin{aligned}&= (5 * 27) - (4 * 33) \\&= 5 * (93 - 2 * 33) - (4 * 33)\end{aligned}$$

$$= (5 * 93) - (10 * 33) - (4 * 33)$$

$$= (5 * 93) - (14 * 33)$$

$$= (5 * 93) - 14 * (219 - 2 * 93)$$

$$= (5 * 93) - (14 * 219) + (14 * 93)$$

$$= -(14 * 219) + (33 * 93) \Rightarrow x = 33, y = -14$$

$$\Rightarrow (3 - 2 * 33) - (4 * 33) + (4 * 27)$$

$$\Rightarrow (3 - 2 * 33) - (4 * 33) + 4 * (93 - 2 * 33)$$

25th Jan:

Congruence: If a, b are integers. And $n > 0$.

$$a \equiv b \pmod{n} \Rightarrow n \mid (a-b)$$

Example: $(5, 3) \Rightarrow 15 \equiv 3 \pmod{12}$ If $\frac{12}{12} = 1$

$$\Rightarrow \frac{12}{15-3} \Rightarrow \frac{12}{12} = 1$$

Modular arithmetic property:

i) $(a+b) \pmod{n} = [(a \pmod{n}) + (b \pmod{n})] \pmod{n}$

(expand mod n until Left value is less than n)

ii) $(a-b) \pmod{n} = [(a \pmod{n}) - (b \pmod{n})] \pmod{n}$

iii) $(a \times b) \pmod{n} = [(a \pmod{n}) * (b \pmod{n})] \pmod{n}$

Modular Exponentiation:

① Compute $3^{10} \pmod{5}$

$$3^2 \pmod{5} \Rightarrow 9 \pmod{5} \equiv 4$$

$$\begin{cases} x^{a+b} = x^a \cdot x^b \\ (x^a)^b = x^{ab} \end{cases}$$

$$3^4 \pmod{5} \Rightarrow 3^{2+2} \pmod{5}$$

$$\Rightarrow 3^2 \cdot 3^2 \pmod{5} \Leftrightarrow [(3^2 \pmod{5}) * (3^2 \pmod{5})]$$

$$\Rightarrow [4 * 4] \Rightarrow 16 \pmod{5}$$

Perform mod 5

$$16 \pmod{5} \Rightarrow 1 \pmod{5}$$

$$3^8 \pmod{5} \Rightarrow 3^4 \cdot 3^4 \pmod{5}$$

$$\Rightarrow [(3^4 \pmod{5}) * (3^4 \pmod{5})]$$

$$\Rightarrow [1 * 1] \Rightarrow 1 \pmod{5}$$

$$\Rightarrow 3^{10} \pmod{5} \Rightarrow 3^8 \cdot 3^2 \pmod{5}$$

$$\Rightarrow [(3^8 \pmod{5}) * (3^2 \pmod{5})]$$

$$\Rightarrow [1 * 4] \Rightarrow 4 \pmod{5}$$

$$\textcircled{2} \quad 3^{20} \bmod 5$$

$$\textcircled{3} \quad 2^{34} \bmod 5$$

Fermat's Theorem: (Fermat's little theorem)

→ used in public key cryptography.

→ Let p be prime number, ' a ' is a tve integer not divisible by p . and $\gcd(a, p) = 1$
then $a^{p-1} \equiv 1 \pmod{p}$

$(a, p) \rightarrow$ relatively prime (no common factors other than 1)
[coprime]

$$\Rightarrow \frac{a^p}{a} \equiv 1 \pmod{p} \Rightarrow a^p \equiv a \pmod{p}$$

→ Acc. to. congruence rule, $a \equiv r \pmod{b}$ [$b/a, \text{rem}=r$]

$$a^{p-1} \equiv 1 \pmod{p} \Rightarrow 1$$

$$a^p \equiv a \pmod{p} \Rightarrow a$$

$$\textcircled{1} \quad 3^{20} \bmod 5$$

$$\Rightarrow 3^2 \bmod 5 \Rightarrow 9 \bmod 5 = 4$$

$$3^4 \bmod 5 \Rightarrow 3^2 \cdot 3^2 \bmod 5 \Rightarrow [(3^2 \bmod 5) * (3^2 \bmod 5)]$$

$$\Rightarrow [4 * 4] \Rightarrow 16 \bmod 5$$

$$\Rightarrow 16 \bmod 5 \Rightarrow 1$$

$$3^8 \bmod 5 \Rightarrow 3^4 \cdot 3^4 \bmod 5 \Rightarrow [(3^4 \bmod 5) * (3^4 \bmod 5)]$$

$$\Rightarrow [1 * 1] \Rightarrow 1$$

$$3^{10} \bmod 5 \Rightarrow (3^8 \cdot 3^2 \bmod 5) \Rightarrow [(3^8 \bmod 5) * (3^2 \bmod 5)]$$

$$\Rightarrow [1 * 4] \Rightarrow 4$$

$$3^{20} \bmod 5 \Rightarrow 3^{10} \cdot 3^{10} \bmod 5 \Rightarrow [(3^{10} \bmod 5) * (3^{10} \bmod 5)]$$

$$\Rightarrow [4 * 4] \Rightarrow 16 \bmod 5$$

$$\Rightarrow 1$$

$$\textcircled{2} \quad 2^{34} \bmod 5$$

$$\Rightarrow 2^4 \bmod 5 \Rightarrow 16 \bmod 5 \Rightarrow 1$$

$$\Rightarrow 2^8 \bmod 5 \Rightarrow 2^4 \cdot 2^4 \bmod 5 \Rightarrow [(2^4 \bmod 5) * (2^4 \bmod 5)] \Rightarrow [1 * 1] \Rightarrow 1$$

$$\Rightarrow 2^{16} \bmod 5 \Rightarrow [(2^8 \bmod 5) * (2^8 \bmod 5)] \Rightarrow [1 * 1] \Rightarrow 1$$

$$\Rightarrow 2^{32} \bmod 5 \Rightarrow 2^{16} \cdot 2^{16} \bmod 5 \Rightarrow [(2^{16} \bmod 5) * (2^{16} \bmod 5)] \Rightarrow [1 * 1] \Rightarrow 1$$

$$\Rightarrow 2^{34} \bmod 5 \Rightarrow 2^{32} \cdot 2^2 \bmod 5 \Rightarrow [(2^{32} \bmod 5) * (2^2 \bmod 5)]$$

$$2^2 \bmod 5 \Rightarrow 4 \bmod 5 \Rightarrow 4 \Rightarrow [1 * 4] \Rightarrow 4$$

29th Jan

$$\text{compute } 5^{18} \bmod 19$$

19 \rightarrow Prime number

$g(5, 19)$ should be equal to 1

Finding whether 5 divides 19 $\Rightarrow 19 \mid 5$

$$\Rightarrow a^{p-1} \bmod p$$

$$a^{p-1} = 1 \bmod p \Rightarrow \boxed{a^{-1} \bmod p = 1} \rightarrow \text{fermet's theorem}$$

$$\Rightarrow 5^{19-1} \bmod 19$$

$$\Rightarrow 5^{18} \bmod 19 = 1$$

$$a^p = a \bmod p \Rightarrow \boxed{a^p \bmod p = a} \rightarrow \text{fermet's theorem}$$

$$5^{19} \bmod 19 \Rightarrow 5$$

$$5 = 5$$

$$5^{20} \bmod 19$$

write power in multiples of p.

$$-0 \Rightarrow 19 \times 1 + 1 \rightarrow a = bq + r$$

$$5^{20} \bmod 19 \Rightarrow 5^{19 \times 1 + 1} \bmod 19$$

$$\Rightarrow ((5^{19})^1 * 5^1) \bmod 19$$

$$\Rightarrow (5^{19} \bmod 19) * 5 \bmod 19$$

$$\Rightarrow [5 * 5] \bmod 19$$

$$\Rightarrow 25 \bmod 19 \Rightarrow 6$$

compute $9^{194} \bmod 73$

3 → prime number

(d(9, 73)) should be 1

$$194 > 73$$

$$194 \bmod 73 \Rightarrow 9^{73 \times 10 + 64} \bmod 73$$

$$\Rightarrow (9^{73})^{10} * 9^{64} \bmod 73$$

$$\Rightarrow (9^{73} \bmod 73)^{10} * (9^{64} \bmod 73)$$

$$\Rightarrow \cancel{(9^{73})^{10}} * 64 \Rightarrow 9^{10} * (9^{64} \bmod 73)$$

$$\Rightarrow 9^{74} \bmod 73$$

$$\Rightarrow 9^{73 \times 1 + 1} \bmod 73$$

$$\Rightarrow (9^{73})^1 * 9^1 \bmod 73$$

$$\Rightarrow (9^{73} \bmod 73) * (9 \bmod 73)$$

$$\Rightarrow 9 * 9 \Rightarrow 81 \bmod 73 \Rightarrow 8 \mid 1$$

1st Feb

use of symmetric : older method.

→ faster & more efficient, takes toll on network due to perf.

→ Examples:

* DES (Data Encryption Standard)

* AES (Adv. Enc. std)

* RC4, RC5, RC6

RC4 → Stream cipher

* IDEA (Internation Data Enc. A)

* Blowfish

IDEA → Block cipher

Public key → Known to everyone.

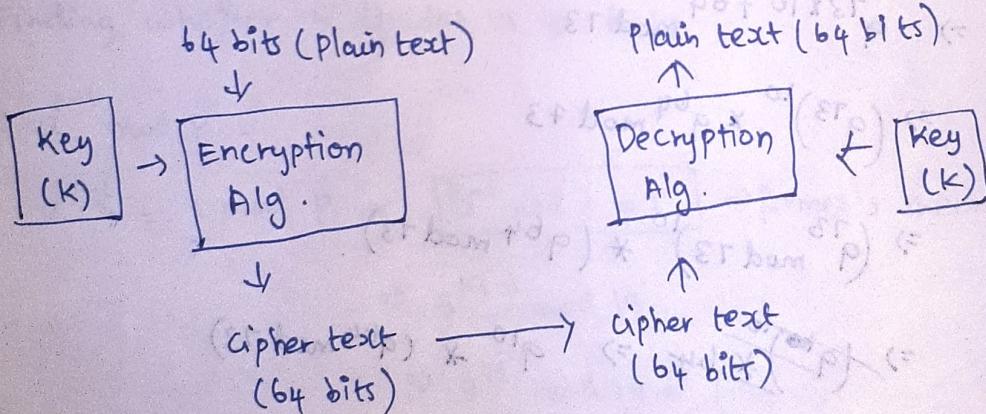
Private key → only to the receiver.

BLOCK CIPHER:

→ data blocks from plain text.

↳ same size (fixed)

↳ 64 bits / 128 bits



Ex:

HelloVIT Welcome!

1st 8 bit \rightarrow HelloVIT

2nd 8 bit \rightarrow Welcome!

Step 2: convert to hexadecimal character of 16. $(8 \times 2) \rightarrow (4A1F3F\ldots)$

Step 3: Each hexadecimal value to binary (in 4 bits)

Ex: A \rightarrow 1010

1 \rightarrow 0001

4 \rightarrow 0100

F \rightarrow 1111

so totally, 64 bits will be generated (16×4)

\hookrightarrow single ~~bits~~ block.

\hookrightarrow input to encryption algorithm.

Ex: Welcome \rightarrow VIT

\downarrow
8 bits

4 bits

\downarrow
16 bit Hexad

\downarrow
8 bits Hexad

\downarrow
64 bit binary

\downarrow
32 bit binary + 32 bit binary zeros

\downarrow
64 bit binary.

Principles:

\rightarrow # of rounds

\rightarrow Design of Function F

\rightarrow Key schedule Algorithm

Modes of operation:

ECB (Electronic codebook)

CBC (cipher block

CFB

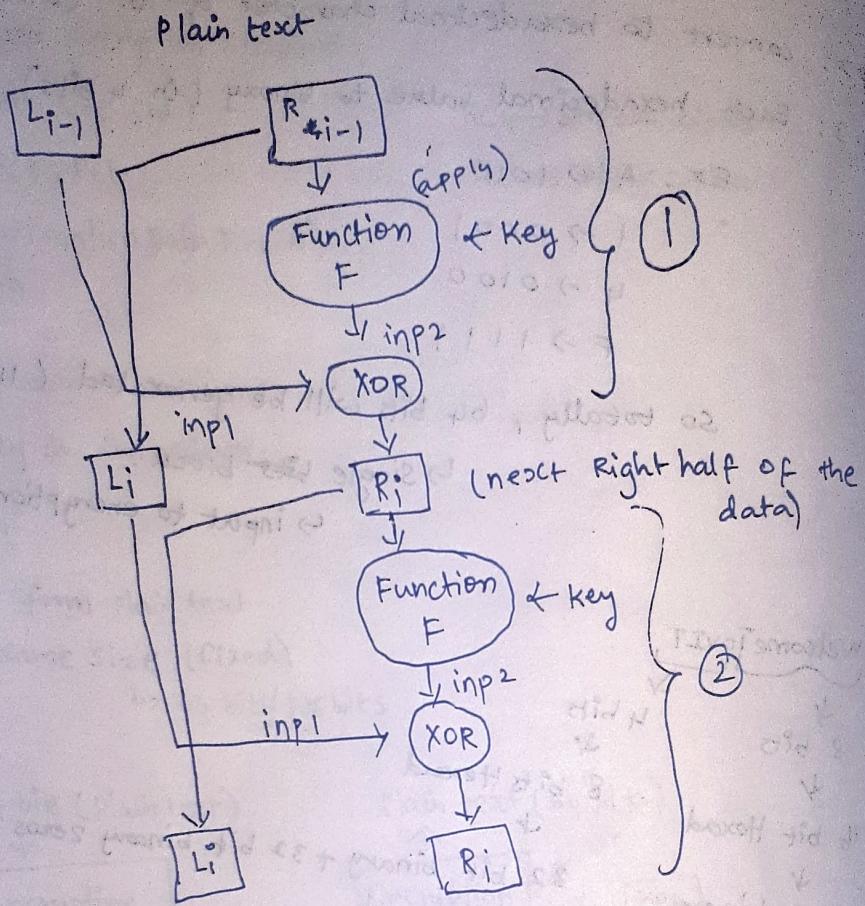
OFB

CTR

Feistel Block Cipher:

→ Structure that implements substitution by permutation.

↓
implements alternatively.



$$L_i \Rightarrow R_{i-1}$$

$$R_i \Rightarrow L_{i-1} \text{ XOR } (\text{function}(R_{i-1}, \text{key}))$$

Parameters:

No. of rounds ↑ then complexity ↑ security also ↑
 ↳ Normally 16 rounds.

Block size ↑ then security ↑ but encryp & decryp ↓

Key size ↑ security ↑ complexity ↑
 Subkey → differs round to round

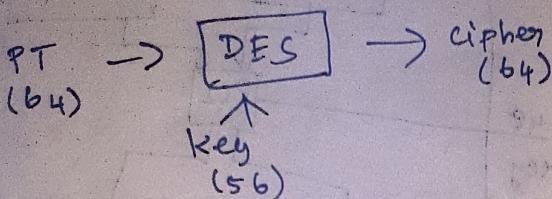
DES:

Block size \rightarrow 64 bits

Key size \rightarrow 64 bits should be but 56 bits

rounds \rightarrow 16

16 Intermediate keys each 48 bits

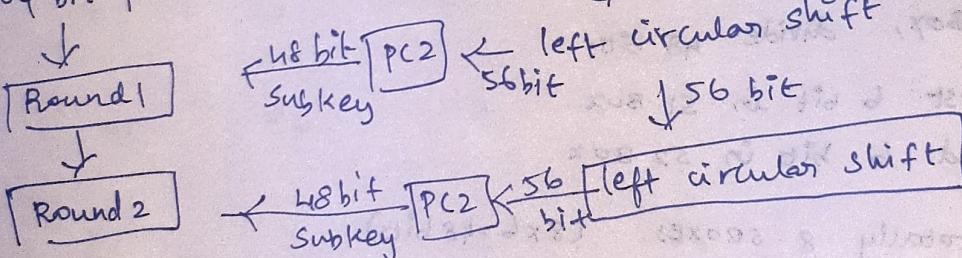


64 bit plain text
 \hookrightarrow gives to initial permutation. \rightarrow 64 bit to round 1

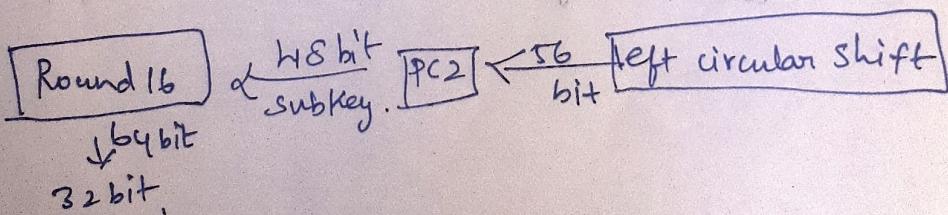
First bit of output \rightarrow 58th of inp
50th of inp
7th of inp

64 bit key \rightarrow input to \rightarrow permuted choice - 1
PC 1
 \star
56 bit key

64 bit plain text after PC



(input to 32 bit swapping \downarrow 56 bit)

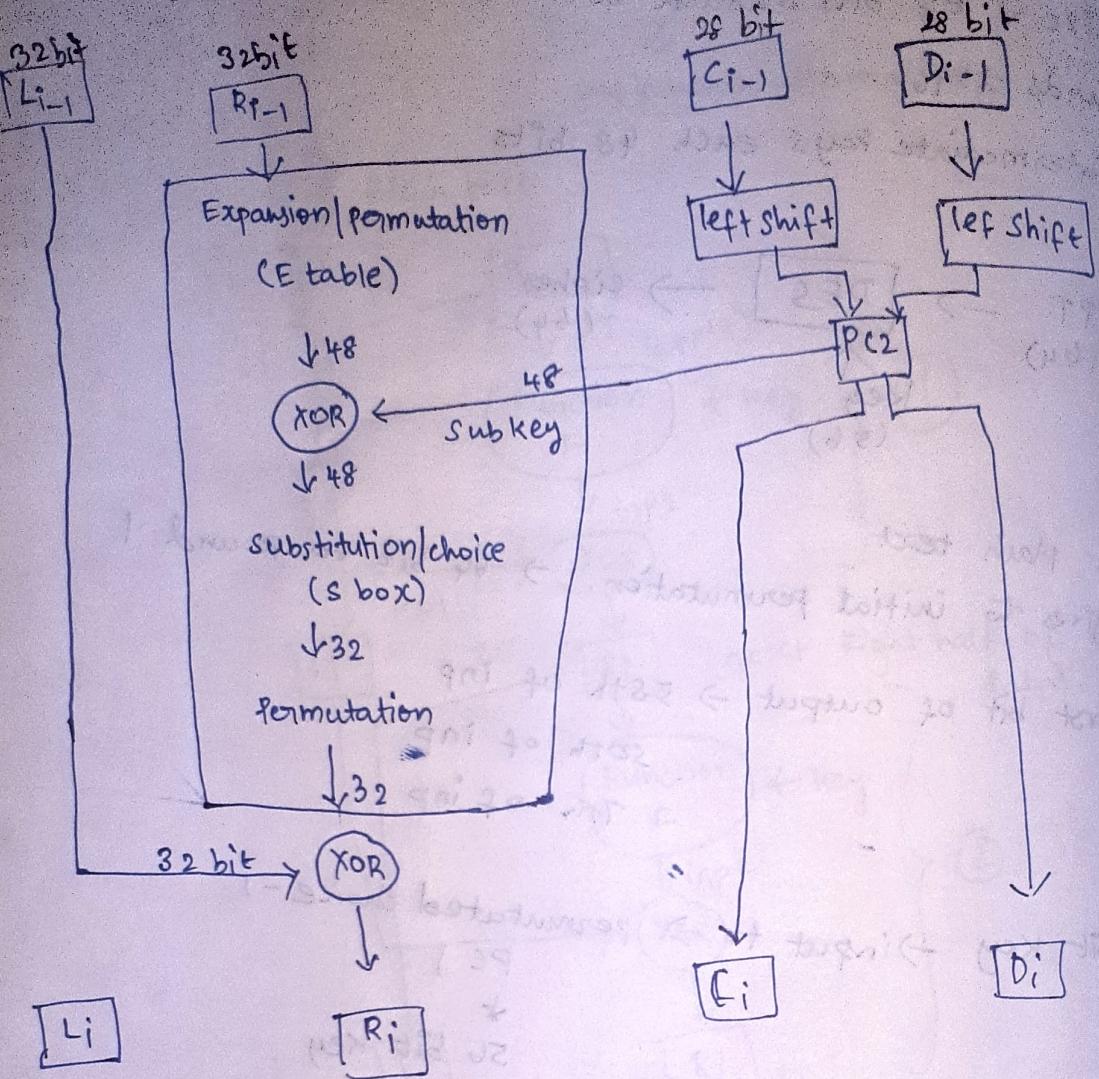


Input to ↓

Inverse initial permutation \rightarrow 64 bit cipher text.

3rd Feb:

Round 1 DES:



In Sbox, divide 48 bits.

→ First 6 bit in S1 Box

→ 2nd 6 bits in S2 Box

⇒ So totally 8 Sboxes ($8 \times 6 = 48$ bits)

6 bits → Box → 4 bits output

(So totally 32 bits as output)

6 bit \rightarrow $b_1 b_2 b_3 b_4 b_5 b_6$

$b_1 b_6 \rightarrow$ row of matrix (2 bits \rightarrow 00, 01, 10, 11) \rightarrow so 4 rows

$b_2 b_3 b_4 b_5 \rightarrow$ column of matrix (4 bits \rightarrow 0, ..., 15) \rightarrow so 16 col.

matrix $\rightarrow 4 \times 16$

Example:

B = 101111

$b_1 b_6 = 11 \Rightarrow$ row = 3

$b_2 b_3 b_4 b_5 \Rightarrow 0111 \Rightarrow$ column = 7

7 + 3 \Rightarrow 10 \Rightarrow 1010 is output (4 bit value)