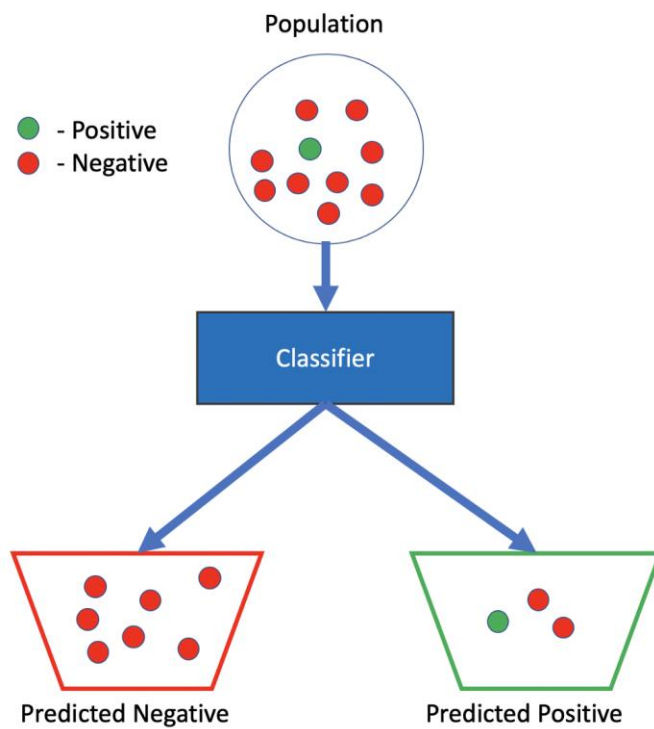


PRECISION RECALL



		Real	
		Positive	Negative
Predicted	Positive	1	2
	Negative	0	7

$$\text{precision} = \frac{tp}{tp + fp} = \frac{1}{3} = 33\%$$

$$\text{recall} = \frac{tp}{tp + fn} = \frac{1}{1} = 100\%$$

$$\text{specificity} = \frac{tn}{tn + fp} = \frac{7}{9} = 78\%$$

$$\text{sensitivity} = \text{recall} = 100\%$$

		Real	
		Positive	Negative
Predicted	Positive	True Positive (tp)	False Positive (fp)
	Negative	False Negative (fn)	True Negative (tn)

$$\textit{precision} = \frac{tp}{tp + fp}$$

Precision — Out of all the examples that predicted as positive, how many are really positive?

$$\textit{recall} = \frac{tp}{tp + fn}$$

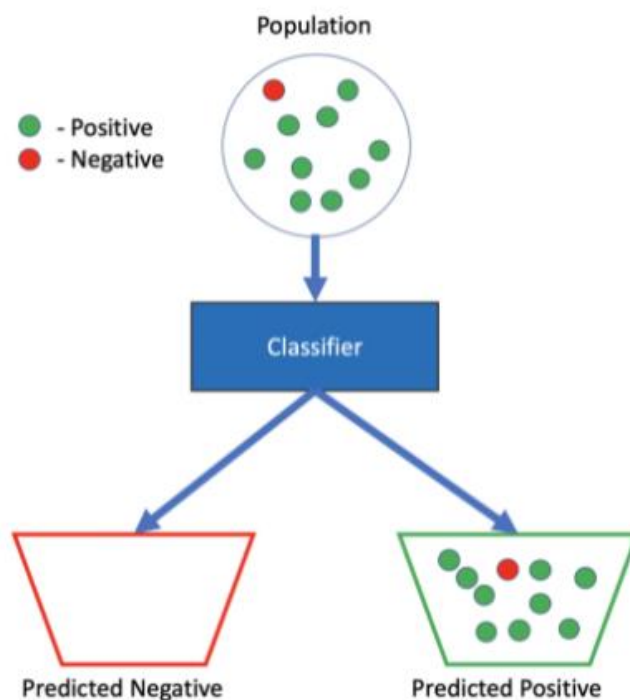
Recall — Out of all the positive examples, how many are predicted as positive?

$$\textit{specificity} = \frac{tn}{tn + fp}$$

Specificity — Out of all the people that do not have the disease, how many got negative results?

$$\textit{sensitivity} = \frac{tp}{tp + fn}$$

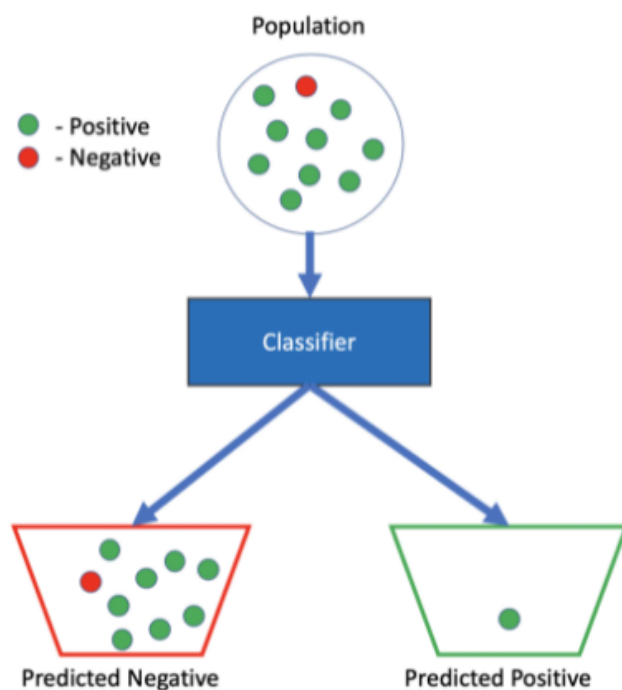
Sensitivity — Out of all the people that have the disease, how many got positive test results?



		Real	
		Positive	Negative
Predicted	Positive	9	1
	Negative	0	0

$$\begin{aligned} \textit{precision} &= \frac{tp}{tp + fp} = \frac{9}{10} = \mathbf{90\%} \\ \textit{recall} &= \frac{tp}{tp + fn} = \frac{9}{9} = \mathbf{100\%} \\ \textit{specificity} &= \frac{tn}{tn + fp} = \frac{0}{1} = \mathbf{0\%} \\ \textit{sensitivity} &= \textit{recall} = \mathbf{100\%} \end{aligned}$$

Example 3 — High Precision, Low Recall, and High Specificity



		Real	
		Positive	Negative
Predicted	Positive	1	0
	Negative	8	1

$$\begin{aligned} \text{precision} &= \frac{tp}{tp + fp} = \frac{1}{1} = 100\% \\ \text{recall} &= \frac{tp}{tp + fn} = \frac{1}{9} = 11\% \\ \text{specificity} &= \frac{tn}{tn + fp} = \frac{1}{1} = 100\% \\ \text{sensitivity} &= \text{recall} = 11\% \end{aligned}$$

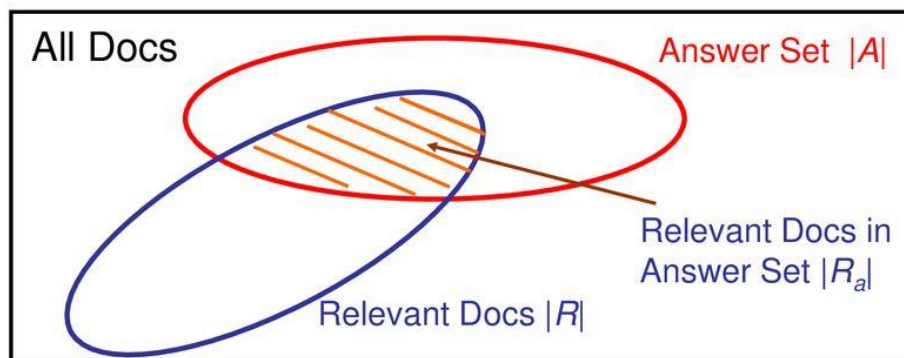
Precision (also called [positive predictive value](#)) is the fraction of relevant instances among the retrieved instances, while **recall** (also known as [sensitivity](#)) is the fraction of relevant instances that were retrieved. Both precision and recall are therefore based on [relevance](#).

PRECISION: FRACTION OF RELAVANT AMONG RETRIEVED

RECALL: FRACTION OF RETRIEVED WERE RELEVANT

Recall and Precision

- Recall ($\frac{|R_a|}{|R|}$)
 - The fraction of the relevant documents which has been retrieved
- Precision ($\frac{|R_a|}{|A|}$)
 - The fraction of the retrieved documents which is relevant



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Unranked retrieval evaluation: Precision and Recall

- **Precision:** fraction of retrieved docs that are relevant
= $P(\text{relevant}|\text{retrieved})$
- **Recall:** fraction of relevant docs that are retrieved =
 $P(\text{retrieved}|\text{relevant})$

	Relevant	Nonrelevant
Retrieved	tp	fp
Not Retrieved	fn	tn

- Precision $P = tp/(tp + fp)$
- Recall $R = tp/(tp + fn)$

True state of patient's health

		Disease	No disease
Test result	Alert	5	3
	No alert	4	8