Large Language Model for Computing Midcurve of a Thin Polygon
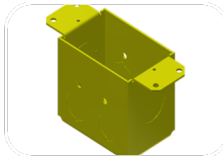
Yogesh Haribhau Kulkarni

Yogesh Haribhau Kulkarni

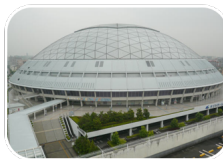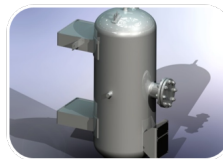Introduction To Midcurve

YHK

Aerospace
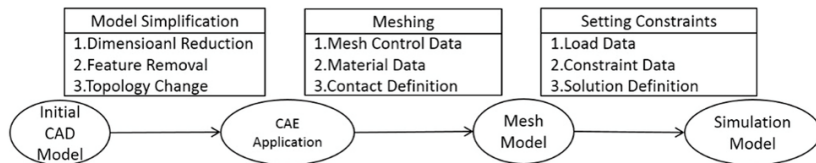

Machinery

Consumer
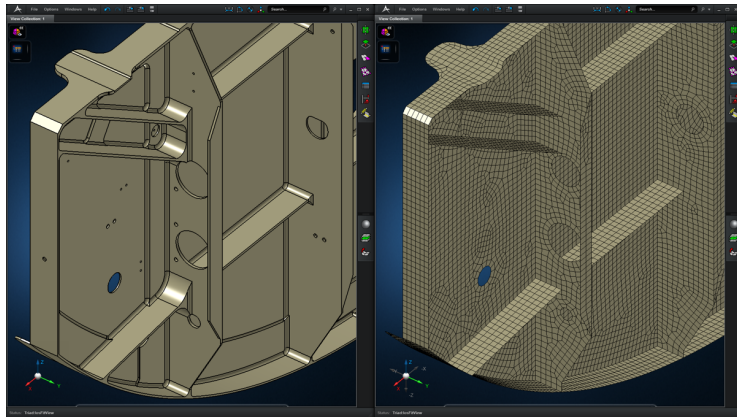Products

Energy

Construction

Industrial
equipment

YHK

Can we use shapes directly?

- ▶ CAD : Designing Shapes
- ▶ CAE : Engineering Analysis
- ▶ CAD→CAE: Simplification for quicker results.

YHK

CAD-CAE

For Shapes like Sheet Metal . . .

	Solid mesh	Shell+Solid mesh	Difference (%)
Element number	344,330	143,063	-58%
Node Number	694,516	75,941	-89%
Total Degrees of freedom	2,083,548	455,646	-78%
Maximum Von. Mises Stress	**418.4 MPa**	**430 MPa**	+3%
Meshing + Solving time	Out of memory	22 mins	N/A (4G RAM)
Meshing + Solving time	**30 mins**	**17 mins**	-43% (12G RAM)

Half the computation time, but similar accuracy

YHK
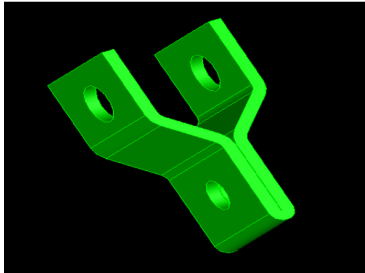
Midsurface is?
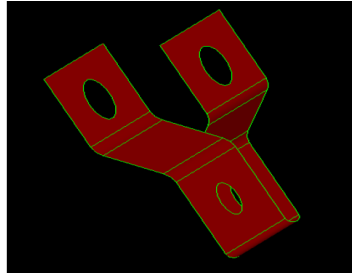
Input: Solid   Output: Midsurface

- ▶ Widely used for CAE of Thin-Walled parts
- ▶ Computation is challenging and still unsolved

YHK

Getting Midsurface

- Going on for decades . . .
- Manually by offsetting and stitching, initially
- Many CAD-CAE packages give automatic option, but . . .

YHK
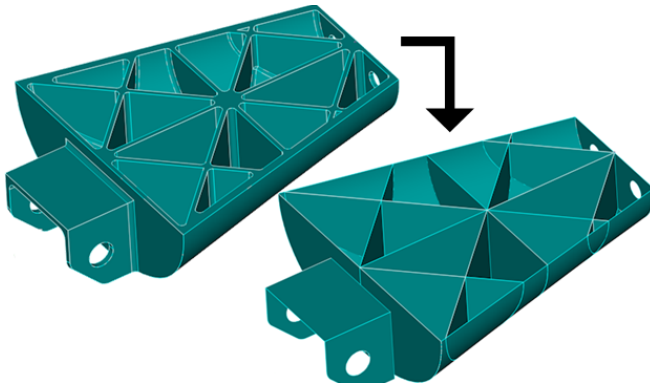
Look at the output
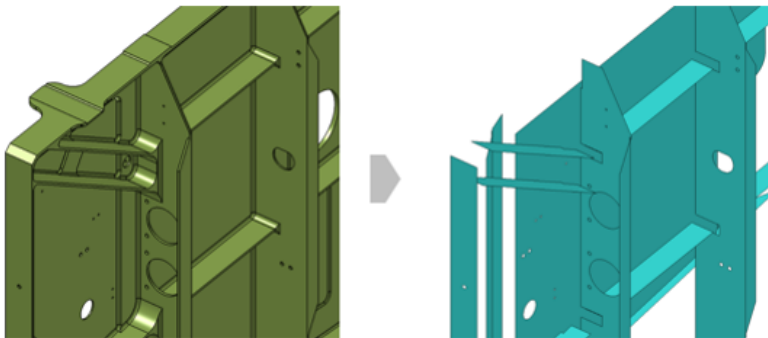
Can't tolerate gaps

- ▶ We have thickness sampling,
- ▶ To recreate-represent the original shape
- ▶ Input and output difference not desirable

YHK

For a simple model like

YHK
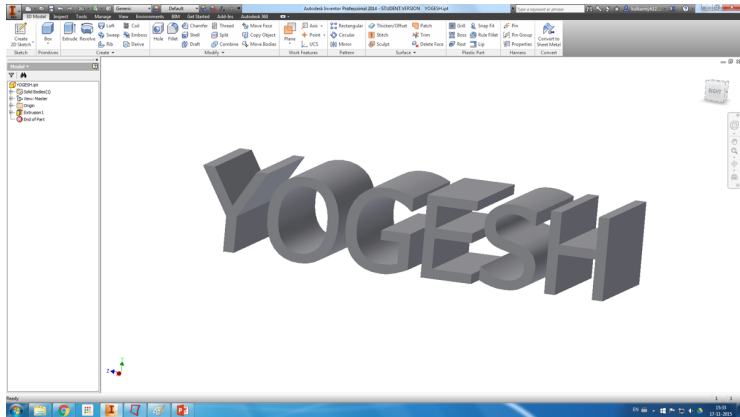
You get
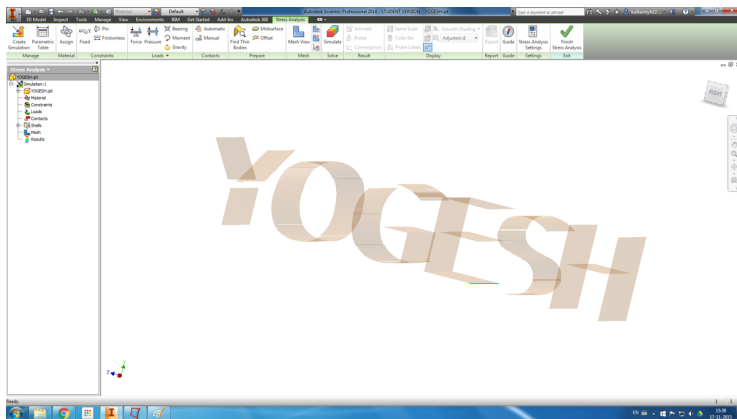
For a far simpler shape
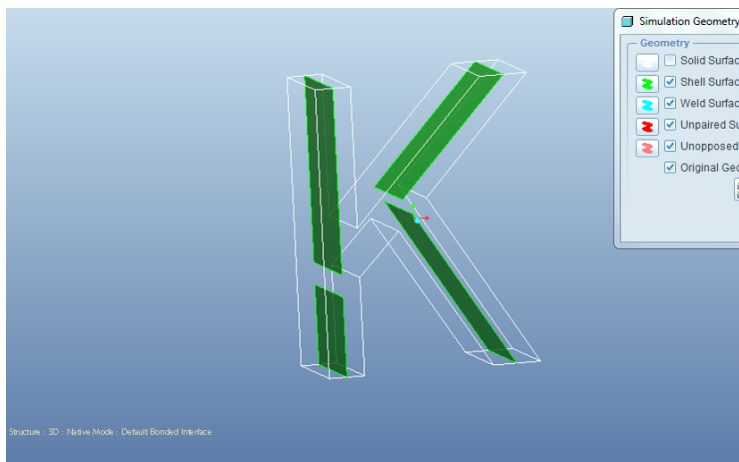
Current Quality
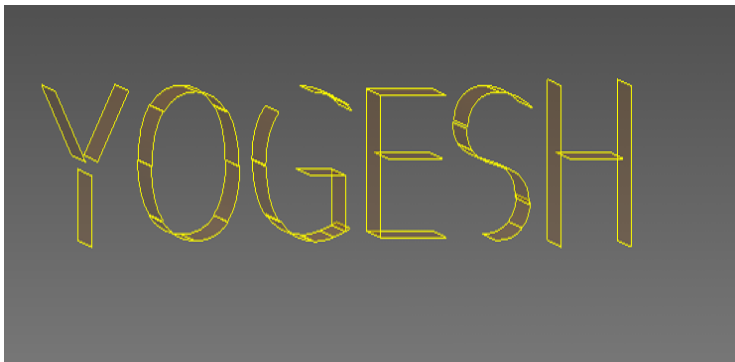
- Errors take weeks to correct for complex parts.
- But still preferred, due to vast savings time
- From Days to hours . . .

YHK

Midsurface Computation

- ▶ Midsurface of a Patch is Midcurve of its profile extruded.
- ▶ So, it boils down to computing 1D midcurve of a 2D profile

YHK
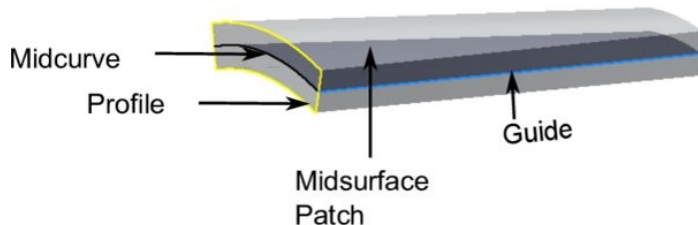
What is a Midcurve?

- Midsurface : From 3D thin Solid to 2D Surface
- Midcurve : From 2D Profile to 1D Curve
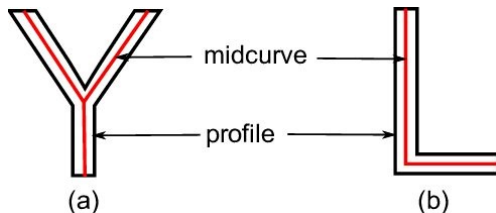
Many Approaches

- More than 6 decades of research...
- Most CAD-CAE packages...
- Rule-based!! Heuristic!! Case-by-case basis!!
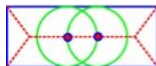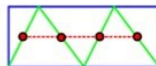
MAT   CAT   Thinning   Pairs

YHK
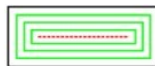
When-What?
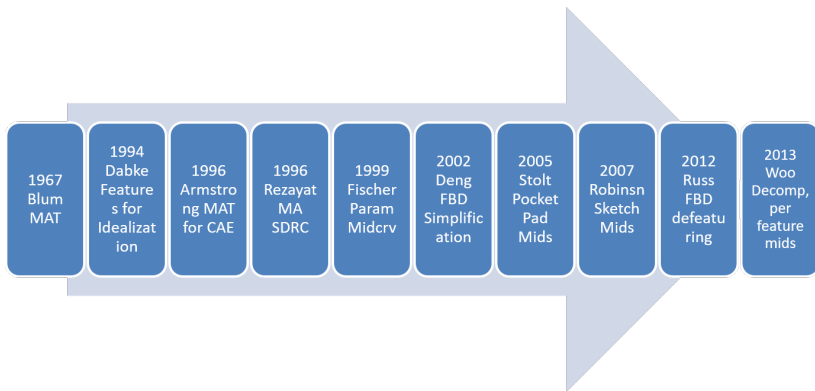
2017: My PhD Work: Rule-based

YHK
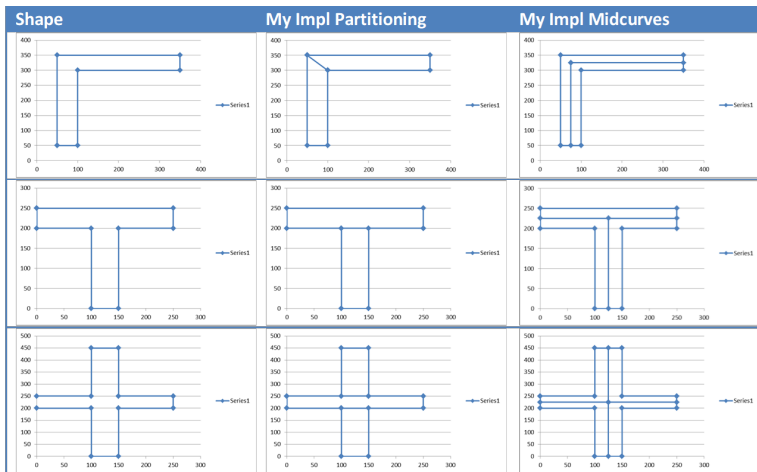
Limitations

- ▶ Fully rule-based
- ▶ Need to adjust for new shapes
- ▶ So, not scalable

Idea

Can Large Language Models "learn" the dimension reduction transformation?

YHK

LLMs for Midcurve Implementation

YHK

Proposed Approach

Text to Text Transformation Learning:

- ▶ Geometric Representation: A text-based representation of the geometry/graph/network will be explored to leverage Natural Language Processing (NLP) techniques.

- ▶ Existing Methods: The paper (Fatemi, Halcrow, and Bryan 2023) surveys several text-based representations for graph data, but none appear specifically suited for geometric shapes.

- ▶ Proposed Approach: A geometry representation similar to 2D Boundary Representation (B-rep) will be utilized, adapting the concept from 3D to 2D.

YHK

Representation of Geometry

▶ One limitation of 2D geometry-shape, represented as a sequential list of points, is that we can not represent line intersections or concentric loops.

▶ To address this a more comprehensive structure has been proposed which is based on the corresponding 3D structure popular in Solid Modeling, called Brep (Boundary Representation).

YHK

2D Brep Representation

Leverage a geometry representation similar to that found in 3D B-rep
(Boundary representation), but in 2D. It can be shown as:

```
1  {
     'ShapeName': 'I',
3    'Profile': [(5.0, 5.0), (10.0, 5.0), (10.0, 20.0), (5.0, 20.0)],
     'Midcurve': [(7.5, 5.0), (7.5, 20.0)],
5    'Profile_brep': {
         'Points': [(5.0, 5.0), (10.0, 5.0), (10.0, 20.0),(5.0, 20.0)], # list of
           (x,y) coordinates
7        'Lines': [[0, 1], [1, 2], [2, 3], [3, 0]], # list of point ids (ie index
           in the Points list)
                     'Segments': [[0, 1, 2, 3]] # list of line ids (ie index in
           Lines list)
9        },
     'Midcurve_brep': {
11       'Points': [(7.5, 5.0), (7.5, 20.0)],
         'Lines': [[0, 1]],
13                   'Segments': [[0]]
         },
15 }
```

YHK

Data

ShapeName	Profile	Midcurve	Profile_brep	Midcurve_brep
I	[[5.0, 5.0], [10.0, 5.0], [10.0, 20.0], [5.0, 20.0]]	[[7.5, 5.0], [7.5, 20.0]]	{"Points": [[5.0, 5.0], [10.0, 5.0], [10.0, 20.0], [5.0, 20.0]], "Lines": [[0, 1], [1, 2], [2, 3], [3, 0]], "Segments": [[0, 1, 2, 3]]}	{"Points": [[7.5, 5.0], [7.5, 20.0]], "Lines": [[0, 1]], "Segments": [[0]]}
L	[[5.0, 5.0], [10.0, 5.0], [10.0, 30.0], [35.0, 30.0], [35.0, 35.0], [5.0, 35.0]]	[[7.5, 5.0], [7.5, 32.5], [35.0, 32.5]]	{"Points": [[5.0, 5.0], [10.0, 5.0], [10.0, 30.0], [35.0, 30.0], [35.0, 35.0], [5.0, 35.0]], "Lines": [[0, 1], [1, 2], [2, 3], [3, 4], [4, 5], [5, 0]], "Segments": [[0, 1, 2, 3, 4, 5]]}	{"Points": [[7.5, 5.0], [7.5, 32.5], [35.0, 32.5]], "Lines": [[0, 1], [1, 2]], "Segments": [[0, 1]]}
Plus	[[0.0, 25.0], [10.0, 25.0], [10.0, 45.0], [15.0, 45.0], [15.0, 25.0], [25.0, 25.0], [25.0, 20.0], [15.0, 20.0], [15.0, 0.0], [10.0, 0.0], [10.0, 20.0], [0.0, 20.0]]	[[12.5, 0.0], [12.5, 22.5], [12.5, 45.0], [0.0, 22.5], [25.0, 22.5]]	{"Points": [[0.0, 25.0], [10.0, 25.0], [10.0, 45.0], [15.0, 45.0], [15.0, 25.0], [25.0, 25.0], [25.0, 20.0], [15.0, 20.0], [15.0, 0.0], [10.0, 0.0], [10.0, 20.0], [0.0, 20.0]], "Lines": [[0, 1], [1, 2], [2, 3], [3, 4], [4, 5], [5, 6], [6, 7], [7, 8], [8, 9], [9, 10], [10, 11], [11, 0]], "Segments": [[0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]]}	{"Points": [[12.5, 0.0], [12.5, 22.5], [12.5, 45.0], [0.0, 22.5], [25.0, 22.5]], "Lines": [[0, 1], [4, 1], [2, 1], [3, 1]], "Segments": [[0], [1], [2], [3]]}
T	[[0.0, 25.0], [25.0, 25.0], [25.0, 20.0], [15.0, 20.0], [15.0, 0.0], [10.0, 0.0], [10.0, 20.0], [0.0, 20.0]]	[[12.5, 0.0], [12.5, 22.5], [25.0, 22.5], [0.0, 22.5]]	{"Points": [[0.0, 25.0], [25.0, 25.0], [25.0, 20.0], [15.0, 20.0], [15.0, 0.0], [10.0, 0.0], [10.0, 20.0], [0.0, 20.0]], "Lines": [[0, 1], [1, 2], [2, 3], [3, 4], [4, 5], [5, 6], [6, 7], [7, 0]], "Segments": [[0, 1, 2, 3, 4, 5, 6, 7]]}	{"Points": [[12.5, 0.0], [12.5, 22.5], [25.0, 22.5], [0.0, 22.5]], "Lines": [[0, 1], [1, 2], [3, 1]], "Segments": [[0], [1], [2]]}
I_scaled_2	[[10.0, 10.0], [20.0, 10.0], [20.0, 40.0], [10.0, 40.0]]	[[15.0, 10.0], [15.0, 40.0]]	{"Points": [[10.0, 10.0], [20.0, 10.0], [20.0, 40.0], [10.0, 40.0]], "Lines": [[0, 1], [1, 2], [2, 3], [3, 0]], "Segments": [[0, 1, 2, 3]]}	{"Points": [[15.0, 10.0], [15.0, 40.0]], "Lines": [[0, 1]], "Segments": [[0]]}
L_scaled_2	[[10.0, 10.0], [20.0, 10.0], [20.0, 60.0], [70.0, 60.0], [70.0, 70.0], [10.0, 70.0]]	[[15.0, 10.0], [15.0, 65.0], [70.0, 65.0]]	{"Points": [[10.0, 10.0], [20.0, 10.0], [20.0, 60.0], [70.0, 60.0], [70.0, 70.0], [10.0, 70.0]], "Lines": [[0, 1], [1, 2], [2, 3], [3, 4], [4, 5], [5, 0]], "Segments": [[0, 1, 2, 3, 4, 5]]}	{"Points": [[15.0, 10.0], [15.0, 65.0], [70.0, 65.0]], "Lines": [[0, 1], [1, 2]], "Segments": [[0, 1]]}

YHK

Data Explanation

Column information is as below:

- ▶ ShapeName (text): name of the shape. Just for visualization/reports.
- ▶ Profile (text): List of Points coordinates (x,y) representing outer profile shape, typically closed.
- ▶ Midcurve (text): List of Points coordinates (x,y) representing inner midcurve shape, typically open.
- ▶ Profile_brep (text): Dictionary in Brep format representing outer profile shape, typically closed.
- ▶ Midcurve_brep (text): Dictionary in Brep format representing inner midcurve shape, typically open.

Each Segment is a continuous list of lines. In case of, say 'Midcurve-T', as there is an intersection, we can treat each line in a separate segment. In the case of 'Profile O', there will be two segments, one for outer lines and another for inner lines. Each line is a list of points, for now, linear. Points is a list of coordinates (x,y), later can be (x,y,z).

YHK

Data Resolution

▶ Once we have this Brep representations of both, profile and the
  corresponding midcurve, in the text form, then we can try various machine
  translation approaches or LLM based fine tuning or few-shots prompt
  engineering.

▶ One major advantage of text based method over image based method is
  that image output still has stray pixels, cleaning which will be a complex
  task. But the text method has exact points. It may just give odd lines,
  which can be removed easily.

YHK

Prompt based techniques

YHK

Few Shots Prompt

```
1  You are a geometric transformation program that transforms input 2D polygonal
        profile to output 1D polyline profile. Input 2D polygonal profile is
        defined by set of connected lines with the format as: ...

3  Below are some example transformations, specified as pairs of 'input' and the
        corresponding 'output'. After learning from these examples, predict the
        'output' of the last 'input' specified.
   Do not write code or explain the logic but just give the list of lines with
        point coordinates as specified for the 'output' format.

5  input:[((5.0,5.0), (10.0,5.0)), ... ((5.0,35.0), (5.0,5.0))]
7  output: [((7.5,5.0), (7.5, 32.5)), ... ((35.0, 32.5) (7.5, 32.5))]

9  input: [((5,5), (10, 5)), ...  (5, 20)), ((5, 20),(5,5))]
   output: [((7.5, 5), (7.5, 20))]

11  :
13  input:[((0, 25.0), (25.0,25.0)),...  ((0,20.0),(0, 25.0))]
   output:
```
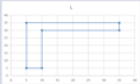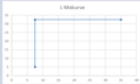
YHK

Few Shot Examples Shapes

The first input example above represents 'L' shape (shown below) and the
second is an 'I', whereas the 3rd is a 'Plus' sign shape.

Profile Data		Profile Picture	Midcurve Data		Midcurve Picture
5.0	5.0		7.5	5.0	
10.0	5.0		7.5	32.5	
10.0	30.0		35.0	32.5	
35.0	30.0		7.5	32.5	
35.0	35.0				
5.0	35.0				

YHK

Few Shot Examples Shapes

The last shape for which LLM has been asked for the answer is actually a 'T' shape. The picture below shows the correct/actual answer as well.

Profile Data		Profile Picture	Midcurve Data		Midcurve Picture
0	25.0		12.5	0	
25.0	25.0		12.5	22.5	
25.0	20.0		25.0	22.5	
15.0	20.0		0	22.5	
15.0	0				
10.0	0				
10.0	20.0				
0	20.0				

YHK

Output

And the outputs computed by various LLMs (ChatGPT, Perplexity AI, Bard) ,
along with the real/actual answer:

```
Actual: [((12.5,0), (12.5,22.5)), ((12.5,22.5),(25.0,22.5)),
     ((12.5,22.5),(0,22.5))]
ChatGPT: [((2.5, 0), (2.5, 22.5)), ((2.5, 22.5), (2.5, 45.0)), ((2.5, 22.5),
     (25.0, 22.5)), ((2.5, 22.5), (12.5, 22.5)), ((2.5, 22.5), (0, 22.5)),
     ((2.5, 22.5), (25.0, 22.5))]
Perplexity: [((12.5,0), (12.5, 22.5)), ((12.5, 22.5),(12.5,45.0)), ((12.5,
     22.5), (0,22.5)), ((12.5, 22.5), (25.0,22.5))]
Bard: [((12.5, 0), (12.5, 25.0)), ((12.5, 25.0), (25.0, 25.0)), ((25.0, 25.0),
     (25.0, 0))]
```

YHK

Output

Visually here is how results from different LLMs look:
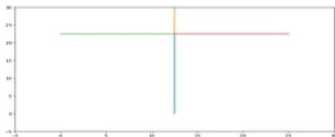
Interpretation

All of the above have failed. Even latest, the results are:

- ▸ `llama 7B g4_0 ggml`: `(8, 17)` & `(64, 32)`: Wrong.
- ▸ `Bard`: `[((8.33,5),(8.33, 22.5)), ((8.33, 22.5), (25,22.5)), ((8.33, 22.5), (0,25))]`: Wrong.
- ▸ `Hugging Chat`: `[((12.5, 0), (12.5, 22.5)), ((12.5, 22.5), (25.0, 22.5)), ((25.0, 22.5), (25.0, 25.0))]`: a bit wrong on the last line
- ▸ `GPT-4`: `[((12.5,0), (12.5,22.5)), ((12.5,22.5),(0,22.5)), ((12.5,22.5),(25.0,22.5))]` just change in sequence of lines, and that's inconsequential, so the answer is correct.

YHK

Interpretation

LLMs by an large seem to have failed for such simple shapes.
There could be two prominent reasons:

- ▶ The prompt design was not effective and could be improved upon.
- ▶ The LLM model itself is not able to learn the pattern and predict well.

The current geometry representation as a sequence of lines, has limitations.
Trying to look for a good representation to store geometry/graph/network as text so that NLP (Natural Language Techniques) can be applied.

YHK

Fine-tuning based techniques

YHK

Training Data

```
from datasets import load_dataset, Dataset, DatasetDict

base_url = "/content/drive/MyDrive/ImpDocs/Work/AICoach/Notebooks/data/"
dataset = load_dataset("csv", data_files={"train": base_url + "midcurve_llm_train.csv",
                                          "test": base_url + "midcurve_llm_test.csv",
                                          "validation": base_url + "midcurve_llm_val.csv"})
DatasetDict({
    train: Dataset({
        features: ['ShapeName', 'Profile', 'Midcurve', 'Profile_brep', 'Midcurve_brep'],
        num_rows: 793
    })
    test: Dataset({
        features: ['ShapeName', 'Profile', 'Midcurve', 'Profile_brep', 'Midcurve_brep'],
        num_rows: 99
    })
    validation: Dataset({
        features: ['ShapeName', 'Profile', 'Midcurve', 'Profile_brep', 'Midcurve_brep'],
        num_rows: 100
    })
})
```

YHK

Data Preprocessing

The dataset is used to fine-tune the base model called "Salesforce/codet5-small". Trained model is saved and used for inference on test samples.

```python
from transformers import T5ForConditionalGeneration, AdamW, get_linear_schedule_with_warmup
import pytorch_lightning as pl

class CodeT5(pl.LightningModule):
    def __init__(self, lr=5e-5, num_train_epochs=15, warmup_steps=1000):
        super().__init__()
        self.model_name = "Salesforce/codet5-small"
        self.model = T5ForConditionalGeneration.from_pretrained(self.model_name)
        self.save_hyperparameters()

    def forward(self, input_ids, attention_mask, labels=None):
        outputs = self.model(input_ids=input_ids, attention_mask=attention_mask, labels=labels)
        return outputs
        :
        :

model = CodeT5()

trainer = Trainer(max_epochs=5,accelerator="auto",# gpus=1,
                default_root_dir="/content/drive/MyDrive/CodeT5/Notebooks/Checkpoints",
                logger=wandb_logger,
                callbacks=[early_stop_callback, lr_monitor])
trainer.fit(model)
```

YHK

Inferencing

The output predicted far away from the corresponding ground truth.
There could be many reasons for the mismatch such the quality of LLM,
training parameters, and above all, need for a far bigger dataset for fine-tuning.
But overall, the approach and preliminary results look promising to warrant
further investigations.

```
1  input_ids = tokenizer(test_example['Profile_brep'], return_tensors='pt').input_ids
   outputs = model.generate(input_ids)
3
   print("Ground truth:", test_example['Midcurve_brep'])
5  print("Generated Midcurve:", tokenizer.decode(outputs[0], skip_special_tokens=True))

7  Ground truth: "{\"Points\": [[−8.4, 3.28], [−20.68, −5.33]], \"Lines\": [[0, 1]], \"Segments\": [[0]]}"
   Generated Midcurve: "{\"Points\": [[−8.83, 4.32], [−21.23
```

YHK

Summary

- Traditional methods of computing midcurves are predominantly rules-based and thus, have limitation of not developing a generic model which will accept any input shape.
- A novel Large Language Model based approach attempts to build such a generic model.
- One such model, GPT-4, seems to be very effective. Although other proprietary and open-source models need to catch-up with GPT-4, even GPT-4 needs to be developed further to understand not just sequential lines but graphs/networks with different shapes, essentially, the geometry.

YHK

Summary

- This research significantly advances midcurve computation by exploring the interplay between established methodologies and cutting-edge approaches, particularly integrating Large Language Models (LLMs).
- Emphasizing the nuanced nature of geometric dimension reduction, it identifies challenges in handling variable-length input data, representing intricate shapes, and addressing limitations in existing models.

YHK

MidcurveLLM Architecture

- ▶ Utilizes an Encoder-Decoder architecture and B-rep structures.
- ▶ Showcases promise, despite discrepancies with ground truths.

YHK

Implications and Future Directions

- ▶ Points to the need for more extensive datasets and refined training parameters.
- ▶ Serves as a crucial catalyst for advancing midcurve computation methodologies.
- ▶ Invites further scrutiny and advancements in the transformative intersection of geometry and advanced machine learning.

YHK

References

▶ Kulkarni, Y. H.; Deshpande, S. Medial Object Extraction - A State of the Art In International Conference on Advances in Mechanical Engineering, SVNIT, Surat, 2010.

▶ Kulkarni, Y. H.; Sahasrabudhe, A.D.; Kale, M.S Dimension-reduction technique for polygons In International Journal of Computer Aided Engineering and Technology, Vol. 9, No. 1, 2017.

▶ Chollet, F. Building Autoencoders in Keras In https://blog.keras.io/building-autoencoders-in-keras.html , 2019.

▶ Video: https://www.youtube.com/embed/ZY0nuykqgoE?featureōembed

▶ Presentation: https://drive.google.com/file/d/1Tx5JJK1˷LUfIMTW-B43HNN2GDMKJMOxR/preview

▶ Short paper: https://vixra.org/abs/1904.0429

▶ Github repo, source code: https://github.com/yogeshhk/MidcurveNN

YHK

Thanks ... yogeshkulkarni@yahoo.com

YHK