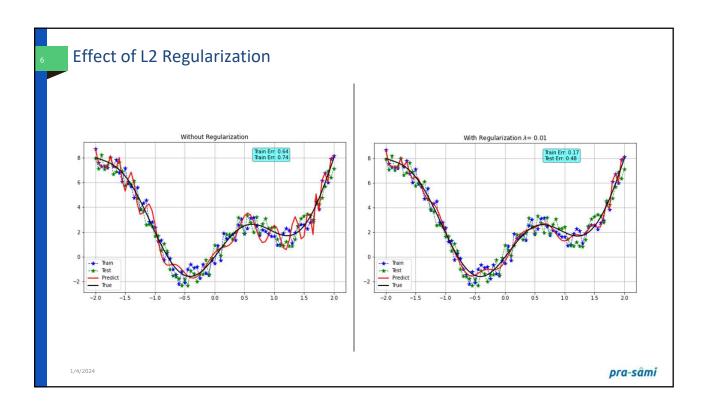


Weights vs. Bias

- \Box For neural networks, we typically choose to use a parameter norm penalty Ω that penalizes only the weights at each layer and leaves the biases un-regularized.
- ☐ The biases typically require less data to fit accurately than the weights.
- ☐ Fitting the weight will requires observing both layer in a variety of conditions.
- □ Each bias controls only a single layer.
- $\ \square$ This means that we do not induce too much variance by leaving the biases un-regularized.
- □ Also, regularizing the bias parameters can introduce a significant amount of under fitting.

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Theory – Logistic Regression – L1 & L2

- ☐ Idea is to minimize Cost Function
 - **❖** J (W, b) = $\frac{1}{m}$ * Σ ℓ (a, y)
 - $= -\frac{1}{m} \{ y * \log(a) + (1-y) * \log(1-a) \}$
- \Box A term is added to Cost function $\frac{\lambda}{2*m}$. $\|W\|_2^2$
- $\Box \qquad J(W, b) = \frac{1}{m} * \Sigma \ell(a, y) + \frac{\lambda}{2*m} . ||W||_2^2$

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Theory – Logistic Regression – L1 & L2

- - This is referred as L2 regularization
 - $\begin{tabular}{ll} \star & \textbf{Regularization hyperparameter λ} : \ \textbf{It is another parameter we tune...} \\ \end{tabular}$
- $||W||_2^2 = \sum_{j=1}^n w_j^2 = W^T$.W
- ☐ Here, we are using Euclidean Norm or L2 Norm
- □ Compared to W, bias b has fewer dimensions, hence, it is generally not considered
- \Box If you add for b, $(\frac{\lambda}{2*m}.b^2)...$ that's ok too
 - * Although its effect will be minimal,
 - * Better to leave it alone.

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Theory – Logistic Regression – L1 & L2

- □ Sometimes L1 too is used
- \Box J (W, b) = $\frac{1}{m}$ * (Σ & (a, y)) + $\frac{\lambda}{2*m}$. $||W||_1$
- \Box Differentation of $\frac{\lambda}{2*m}$. $\|W\|_1 = \frac{\lambda}{2*m} \operatorname{sign}(W)$
 - Will be infinitely small and will have insignificant impact on gradient descent

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Neural Network - Frobenius Norm

- ☐ In neural network, we have different layers with different weights
- ☐ So we look at its cumulative effect over all layers
- □ Hence the Cost function
 - J (W, b) = J (W^[1], b^[1], W^[2], b^[2], W^[3], b^[3]...)

 - * Where $\|\boldsymbol{W}^{[l]}\|^2_{\text{F}} = \sum_{i=1}^{n[l-1]} \sum_{j=1}^{n[l]} (w_{ij}^{\ \ l})^2$
 - > W is (n^[l-1], n^[l]) dimensional matrix
- □ It is called *Frobenius norm* of a matrix
- Also the Euclidean norm defined as the square root of the sum of the absolute squares of its elements

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Frobenius Norm of a Vector

 $\square \|A\|_F = \sqrt{\Sigma(a_{ij})^2}$

i.e.

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} = \sqrt{(1^2 + 2^2 + 3^2 + 4^2 + 5^2 + 6^2 + 7^2 + 8^2 + 9^2)}$$

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Updates to weights

- □ Earlier
 - $\bullet \ \partial W^{[l]} = X . \partial z$
 - And $W^{[l]} = W^{[l]} \alpha \cdot \partial W^{[l]}$
- □ For Regularization we add an extra term at the end

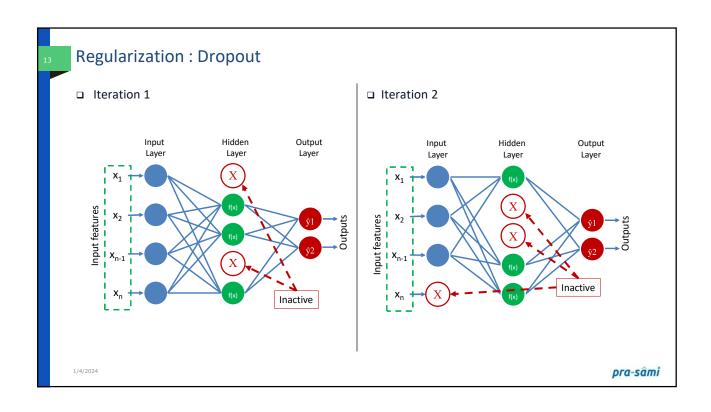
Mathematically, we can show that it is still a valid definition of $\partial W^{[l_l]}$

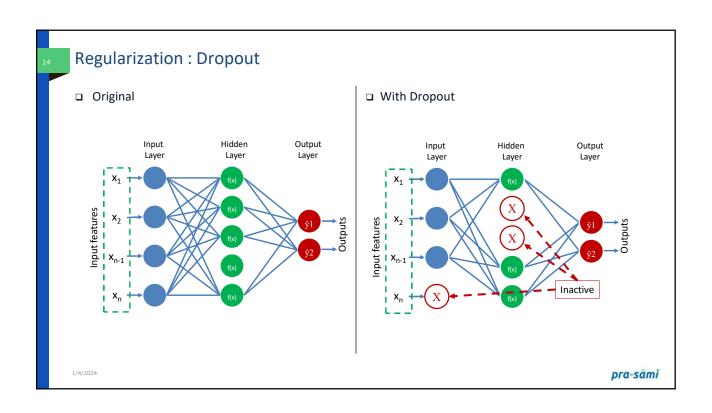
- $W^{[l]} = W^{[l]} \alpha \cdot [X \cdot \partial z + \frac{\lambda}{m} \cdot W^{[l]}]$ $W^{[l]} = (1 \frac{\alpha \cdot \lambda}{m}) \cdot W^{[l]} \alpha \cdot X \cdot \partial z$

Weight Decay

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Regularization: Early Stopping

- □ How long to train the model?
- □ Duration of training → under fit or over fit
- □ Train the model to the point where it performance on test set is best!
- □ Very simple and very effective

How:

- □ Train the model and monitor performance
- □ Save weight every time the performance improves
- □ Stop training if performance has not improved for N epochs
- □ It's the last parameter to tune
 - * Repeated early stopping may lead to over-fitting the validation set
 - * Example: K-fold

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Regularization : Data Augmentation

- Where limited data is available for training the model (when is it not!)
- $\hfill \square$ Very effective in image identification
- Most libraries have Image Generators (parameter driven)
 - Horizontal and Vertical Shift
 - Horizontal and Vertical Flip
 - * Random Rotation
 - Random Brightness / Contrast
 - Random Zoom
 - Random Noise

https://towardsdatascience.com/imageaugmentation-for-deep-learninghistogram-equalization-a71387/609b2

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