

BUBBLE SORT

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23/09/2023

BUBBLE SORT

SORTINGS 01: BUBBLE SORT

- swap the adjacent if needed till we get all the array sorted

ans

5	4	3	2	1
---	---	---	---	---



After sorting array in ascending

1	2	3	4	5
---	---	---	---	---

DRY RUN

5	4	3	2	1
0	1	2	3	4

1st Iteration

1st largest element at it's position

5	4	3	2	1
0	1	2	3	4



swap $a > b \Rightarrow 5 > 4$

4	5	3	2	1



swap $a > b \Rightarrow 5 > 3$

4	3	5	2	1

swap $a > b \Rightarrow 5 > 2$

4	3	2	5	1

swap $a > b \Rightarrow 5 > 1$

a
 b
} Adjacent
value

$a > b \rightarrow \text{swap}$

$a < b \rightarrow \text{NO SWAP}$

1st largest element = 5

2nd Iteration

2nd Largest element at it's positions

4	3	2	1	5
0	1	2	3	4

swap $a > b \Rightarrow 4 > 3$

3	4	2	1
		2	

swap $a > b \Rightarrow 4 > 2$

3	2	4	1
		4	

swap $a > b \Rightarrow 4 > 1$

3	2	1	4
			4

2nd Largest element = 4

3rd Iteration

3rd Largest element at it's positions

3	2	1	4	5
0	1	2	3	4

swap $a > b \Rightarrow 3 > 2$

2	3	1
		1

swap $a > b \Rightarrow 3 > 1$

2	1	3
		3

3rd Largest element = 3

4rt Iteration

4rt Largest element at it's positions

2	1	3	4	5
0	1	2	3	4

swap $a > b \Rightarrow 2 > 1$

1	2
	2

4rt Largest element = 2

1	2	3	4	5
0	1	2	3	4

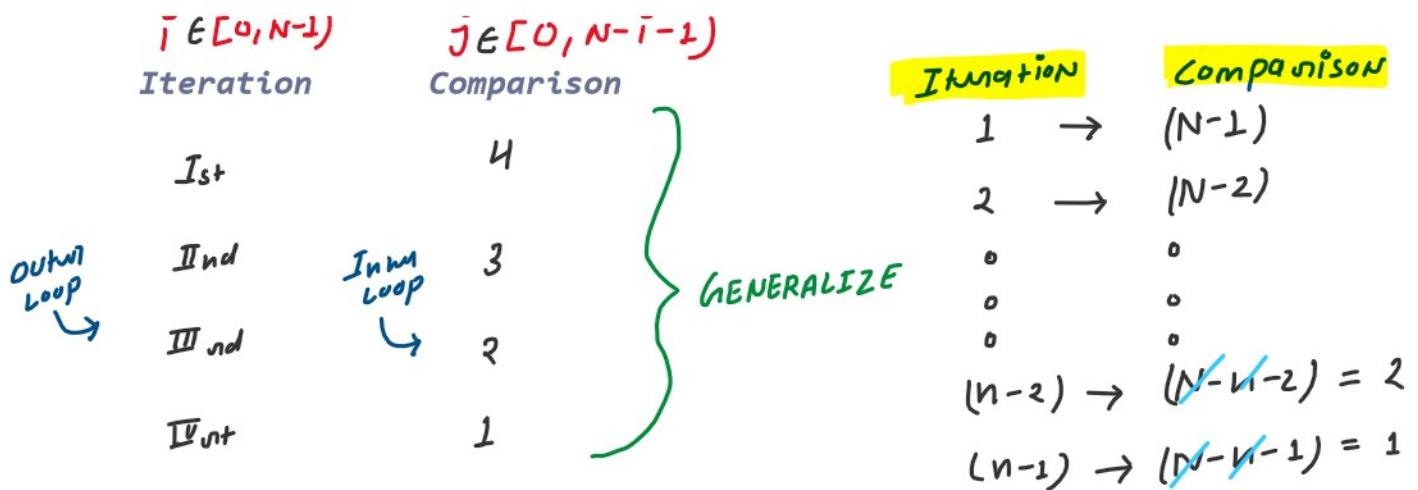
$N = 5$

$i \in [0, N-1]$
Iteration

$j \in [0, N-i-1]$
Comparison

Iteration

Comparison



Ao Po Surius

$$S_n = 1 + 2 + 3 + \dots + (n-2) + (n-1)$$

$$\begin{aligned} S_n &= \frac{n(n-1)}{2} \\ &= \frac{n^2 - n}{2} \end{aligned} \quad \left. \begin{array}{l} \text{Time complexity} \\ O\left(\frac{n^2}{2} - \frac{n}{2}\right) \end{array} \right\} = O(n^2)$$

```

● ● ●

// SORTINGS 01: BUBBLE SORT
#include<iostream>
#include<vector>
using namespace std;

// BUBBLE SORT Function
void bubbleSort(vector<int> &arr){
    int N=arr.size();

    // Outer Loop
    for(int i=0; i < (N-1); i++){
        // Inner Loop
        for(int j=0; j < (N-i-1); j++){
            // When a>b where a=j and b=j+1 to swap kardo
            if(arr[j] > arr[j+1]){
                swap(arr[j], arr[j+1]);
            }
        }
    }
}

int main(){
    vector<int> arr{5,4,3,1,2};

    bubbleSort(arr);
    for(auto value: arr){
        cout<<value<< " ";
    }
    return 0;
}

/*
INPUT: {5,4,3,1,2}
OUTPUT: {1,2,3,4,5}
TIME COMPLEXITY: O(N^2)
SPACE COMPLEXITY: O(1)
*/

```

$T_{\text{Complexity}} = O(N)$

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SELECTION SORT

SORTINGS 02: SELECTION SORT

- What if, I select the minimum element and put it at right position
- For i th iteration, pick smallest element from i to $(n-1)$ index and swap it with i th element

arr	5	4	3	2	1
-----	---	---	---	---	---

DRY RUN

MinIndex = i^0
Starting me first element ko smallest maan lo

1st Iteration

$i=0$	0	1	2	3	4	$N=5$
		$j=i+1$		swap		

U COM

Step 01: find smallest element's index from $[0, N-1]$

$$i=0 \quad j=4 \quad \text{minIndex} = j = 4$$

Step 02: swap the i th and minIndex position's value

swap(arr[i], arr[minIndex])

5 1

YE Apni \rightarrow ① 4 3 2 5
Right position
pan hai

swap

2nd Iteration

<u>1</u>	4	3	2	5
0	1	2	3	4

3 COM

Step 01: find smallest element's index from $[0, N-1]$

$$i = 1 \quad j = 3 \quad \minIndex = j \\ = 3$$

Step 02: swap the i th and \minIndex position's value

swap(arr[¹i], arr[minIndex])
⁴ ₂

*YE DONO APNI
Right position
pan hai*

1	2	3	4	5
---	---	---	---	---

3rd Iteration

<u>1</u>	2	<u>3</u>	4	5
0	1	2	3	4

2 COM

Step 01: find smallest element's index from $[0, N-1]$

$$i = 2 \quad j = 2 \quad \minIndex = j \\ = 2$$

Step 02: swap the i th and \minIndex position's value

swap(arr[³i], arr[minIndex])
³ ₃

1 2 3 4 5

4rt Iteration

<u>1</u>	2	<u>3</u>	<u>4</u>	5
0	1	2	3	4

1 COM

Step 01: find smallest element's index from $[0, N-1]$

$$i = 3 \quad j = 3 \quad \minIndex = j \\ = 3$$

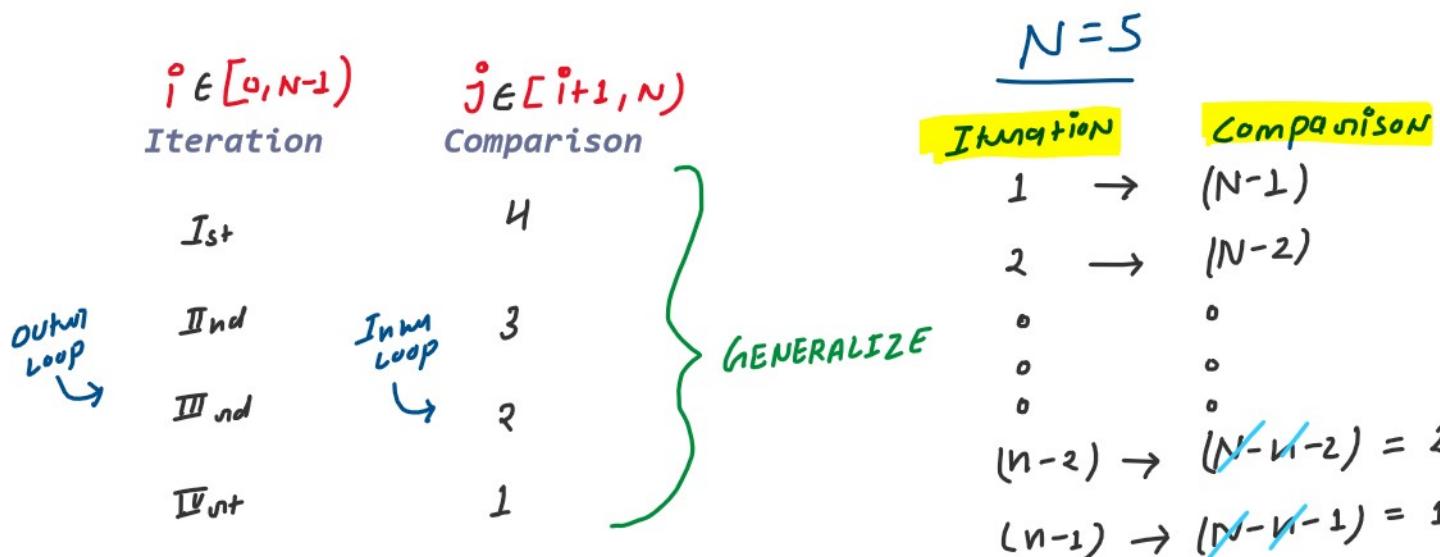
Step 02: swap the i th and \minIndex position's value

$\text{swap}(\text{arr}[i], \text{arr}[\minIndex])$

1 2 3 4 5

Sorted Array

	1	2	3	4	5
0	1	2	2	3	4



$$T.C.O \Rightarrow O\left(\frac{n^2}{2} - \frac{n}{2}\right) \Rightarrow O(n^2)$$

$$S.C.O \Rightarrow O(1)$$

```

// ✓ SORTING 02: SELECTION SORT
#include<iostream>
#include<vector>
using namespace std;

// SELECTION SORT Function
void selectionSort(vector<int> &arr){
    int N = arr.size();

    for(int i=0; i < N-1; i++){
        // Lets assume ki 1st index par jo value hai wo hi smallest hai
        int minIndex = i;

        // ►Step 01: find smallest element's index from [0,N-1]
        for(int j = i+1; j < N; j++){ → O(N)
            if(arr[j] < arr[minIndex]){
                minIndex = j;
            }
        }
        // ►Step 02: swap the ith and minIndex position's value
        swap(arr[i], arr[minIndex]);
    }
}

```

```

        minIndex = j;
    }
}
// ►Step 02: swap the ith and minIndex position's value
swap(arr[i], arr[minIndex]);
}

int main(){
    vector<int> arr{5,4,3,1,2};
    selectionSort(arr);
    for(auto value: arr){
        cout<<value<<" ";
    }
    return 0;
}

/*
INPUT: {5,4,3,1,2}
OUTPUT: {1,2,3,4,5}
TIME COMPLEXITY: O(N^2)
SPACE COMPLEXITY: O(1)
*/

```

$$T.C. = O(N) * O(N)$$

$$= O(N \times N)$$

$$= O(N^2)$$

$$S.C. = O(1)$$

INSERTION SORT

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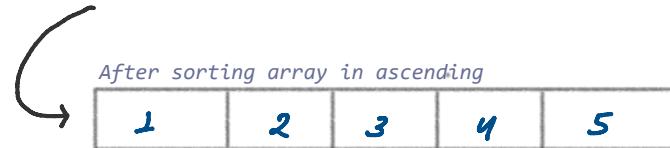
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INSERTION SORT

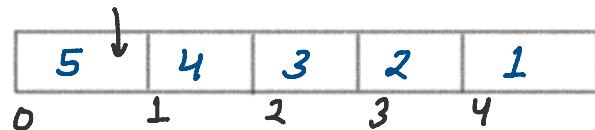
SORTINGS 03: INSERTION SORT

- Move element of $\text{arr}[0, i-1]$ that are greater than key to one position ahead of there current position

arr  $N=5$

DRY RUNExample: 01

Always ignore the first element



$$i^{\circ}=1 \quad j^{\circ}=i^{\circ}-1$$

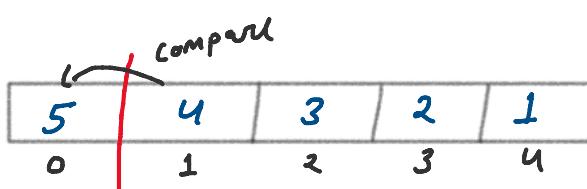
initially store the second element as a key value to Move element of $\text{arr}[0, i-1]$ that are greater than key to one position ahead of there current position

$$\text{key} = \text{arr}[i] \boxed{4}$$

1st Iteration

$$\text{key} = 4$$

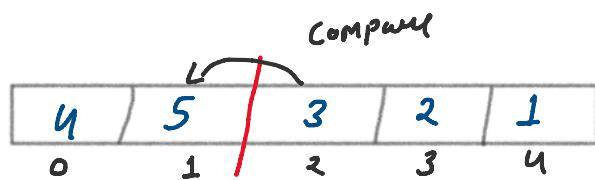
$$i^{\circ}=1, j^{\circ}=0$$



$$5 > 4 \checkmark \rightarrow 4 \ 5 \ 3 \ 2 \ 1$$

2nd Iteration

$$\text{key} = 3$$



2nd Iteration



$$key = 3$$

$$i=2, j=1$$

$$i=2, j=0$$

$573 \rightarrow 5\cancel{3} 521$
 $473 \rightarrow 34521$

3rd Iteration

$$key = 2$$

$$i=3, j=2$$

$$i=3, j=1$$

$$i=3, j=0$$

3	4	5	2	1
0	1	2	3	4

$572 \rightarrow 3\cancel{4}251$
 $472 \rightarrow 3\cancel{2}451$
 $372 \rightarrow 23451$

4rt Iteration

$$key = 1$$

$$i=4, j=3$$

$$i=4, j=2$$

$$i=4, j=1$$

$$i=4, j=0$$

2	3	4	5	1
0	1	2	3	4

$571 \rightarrow 2\cancel{3}415$
 $471 \rightarrow 2\cancel{3}145$
 $371 \rightarrow 2\cancel{1}345$
 $271 \rightarrow 12345$

$i=5 \{ \text{Right part } \dots \dots \text{ } (i < 5) \text{ END}$

Final Output

1	2	3	4	5
-----	-----	-----	-----	-----

DRY RUN

Example: 02

ans	44	33	55	22	11
	0	1	2	3	4

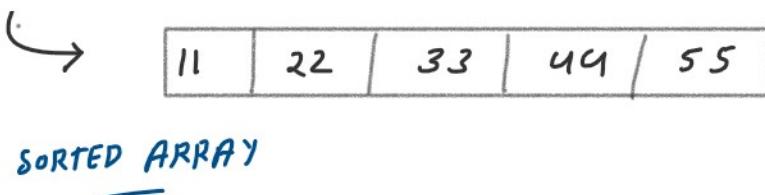
$$N=5$$

$i=1, j=i-1$

11	22	33	44	55
------	------	------	------	------

$$i=1, j=i-1$$

$$key = arr[i]$$



Iteration: 01

44	33	55	22	11
0	1	2	3	4

$$key = 33$$

$$i=1, j=0$$

$$44 > 33 \checkmark \rightarrow 33 \ 44 \ 55 \ 22 \ 11$$

Iteration: 02

33	44	55	22	11
0	1	2	3	4

$$key = 55$$

$$i=2, j=1$$

$$44 > 55 \times \rightarrow \text{SAME} \Rightarrow 33 \ 44 \ 55 \ 22 \ 11$$

Break inner loop

Iteration: 03

33	44	55	22	11
0	1	2	3	4

$$key = 22$$

$$i=3, j=2$$

$$i=3, j=1$$

$$i=3, j=0$$

$$55 > 22 \checkmark \rightarrow \begin{matrix} 33 & 44 & 22 & 55 & 11 \\ 33 & 22 & 44 & 55 & 11 \end{matrix}$$

$$44 > 22 \checkmark \rightarrow \begin{matrix} 33 & 22 & 44 & 55 & 11 \\ 22 & 33 & 44 & 55 & 11 \end{matrix}$$

$$33 > 22 \checkmark \rightarrow \begin{matrix} 22 & 33 & 44 & 55 & 11 \\ 22 & 33 & 44 & 55 & 11 \end{matrix}$$

Iteration: 04

22	33	44	55	11
0	1	2	3	4

$$key = 11$$

$$i=4, j=3$$

$$i=4, j=2$$

$$i=4, j=1$$

$$i=4, j=0$$

$$55 > 11 \checkmark \rightarrow \begin{matrix} 22 & 33 & 44 & 11 & 55 \\ 22 & 33 & 11 & 44 & 55 \end{matrix}$$

$$44 > 11 \checkmark \rightarrow \begin{matrix} 22 & 11 & 33 & 44 & 55 \\ 22 & 11 & 33 & 44 & 55 \end{matrix}$$

$$33 > 11 \checkmark \rightarrow \begin{matrix} 22 & 11 & 33 & 44 & 55 \\ 11 & 22 & 33 & 44 & 55 \end{matrix}$$

$$22 > 11 \checkmark \rightarrow \begin{matrix} 11 & 22 & 33 & 44 & 55 \\ 11 & 22 & 33 & 44 & 55 \end{matrix}$$

$i = -1 \dots \text{END Inner loop}$

$i=4, j=0$

22 > 11 ✓

$j = -1 \times END \text{ Inner loop}$

$i=5 \{ \text{Right just 0000... } (i < 5)$

↳ Final output

11	22	33	44	55
----	----	----	----	----

$i \in [1, N]$ Iteration	$j \in [i-1, 0]$ Comparison		$N=5$	
Ist	1	GENERALIZE	1 → 1	Comparison
IInd	2		2 → 2	
IIIrd	3		0 0 0	
IVth	4		n-1 → n-1 n → n	

$$\begin{aligned}
 S_n &= 1 + 2 + 3 + \dots + n \\
 &= O\left(\frac{n^2 - n}{2}\right) \Rightarrow O(n^2)
 \end{aligned}$$

$$\begin{aligned}
 T.C. &= O(n^2) \\
 S.C. &= O(1)
 \end{aligned}$$

```
// ✓ SORTINGS 03: INSERTION SORT

#include<iostream>
#include<vector>
using namespace std;

// INSERTION SORT Function
void insertionSort(vector<int> &arr){
    int N=arr.size();
    for(int i=1; i<N; i++){
        // Key value = key value se pahle ki all values ko hum compare karte hai key value se hi
        // taki key value ko hum uske right position par rakh paye
        int key = arr[i];
        int j = i-1;

        // Move element of arr[0,i-1] that are greater than key to one position ahead of there current position
        while(j>=0 && arr[j]>key){
            arr[j+1]=arr[j];
            j--;
        }
        // Insert key at right index/position (Insertion)
        arr[j+1]=key;
    }
}

int main(){
    vector<int> arr{5,4,3,1,2};

    insertionSort(arr);
    for(auto value: arr){
        cout<<value<<" ";
    }
    return 0;
}

/*
INPUT: {5,4,3,1,2}
OUTPUT: {1,2,3,4,5}
TIME COMPLEXITY: O(N^2)
SPACE COMPLEXITY: O(1)
*/
```

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CUSTOM COMPARATOR

CUSTOM COMPARATOR

C++ STL Concept



1. SORT A VECTOR: When you want to sort a vector using C++ STL sort data structure then syntax is

```
● ● ●  
// SORT A VECTOR  
vector<int> v;  
  
// Syntax of sorting  
sort(v.begin(), v.end());
```

increasing order sorting by *default*

2. SORT A ARRAY: When you want to sort a vector using C++ STL sort data structure then syntax is

```
● ● ●  
// SORT A ARRAY:  
int arr[];  
  
// Syntax of sorting  
sort(arr, arr+n);
```

increasing order sorting by *default*

/*
Where
- arr is a base address of array
- n is length of array
*/

1. SORT A VECTOR:

```
// ✓ CUSTOM COMPARATOR 01: SORT A VECTOR  
#include <algorithm>
```

2. SORT A VECTOR

```
// ✓ CUSTON COMPARATOR 01: SORT A VECTOR
#include <algorithm>
#include <iostream>
#include <vector>

using namespace std;

// Printing Method
void print(vector<int> &v) {
    for (int i = 0; i < v.size(); ++i) {
        cout << v[i] << " ";
    }
    cout << endl;
}

// Custom Comparator ki return value always true ya false hoti hai
bool myComparator1(int &a, int &b) {
    return a > b; // decreasing order sorting
}

bool myComparator2(int &a, int &b) {
    return a < b; // increasing order sorting
}

int main() {
    vector<int> v = {44, 55, 22, 11, 33};

    cout << "Vector" << endl;
    print(v);

    cout << "Increasing order sorting by default" << endl;
    sort(v.begin(), v.end());
    print(v);

    cout << "Decreasing order sorting by my comparator 1" << endl;
    sort(v.begin(), v.end(), myComparator1);
    print(v);

    cout << "Increasing order sorting by my comparator 2" << endl;
    sort(v.begin(), v.end(), myComparator2);
    print(v);

    return 0;
}

/*
Vector
44 55 22 11 33
Increasing order sorting by default
11 22 33 44 55
Decreasing order sorting by my comparator 1
55 44 33 22 11
Increasing order sorting by my comparator 2
11 22 33 44 55
*/
```

```
// Custom comparator for decreasing order sorting
bool myComparator1(int &a, int &b) {
    return a > b;
}

// Custom comparator for increasing order sorting
bool myComparator2(int &a, int &b) {
    return a < b;
}
```

2. SORT VECTOR OF VECTOR:

Declaration Syntax of 2D vector

$\text{vector} \langle \text{vector} \langle \text{int} \rangle \rangle \text{ v} \overset{n=5}{i}$



Index 0 → v_0 

Index 1 → v_1 

Index 2 → v_2 

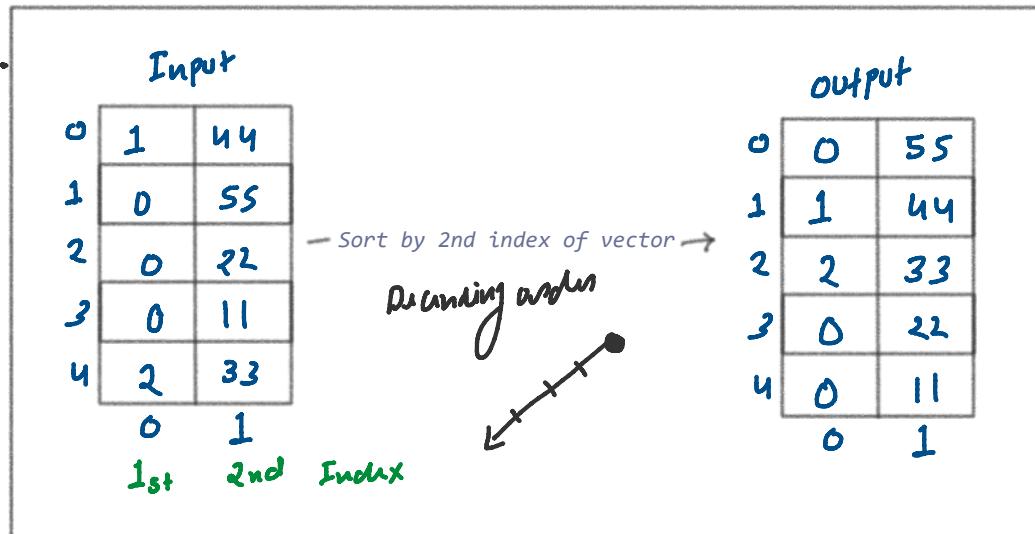
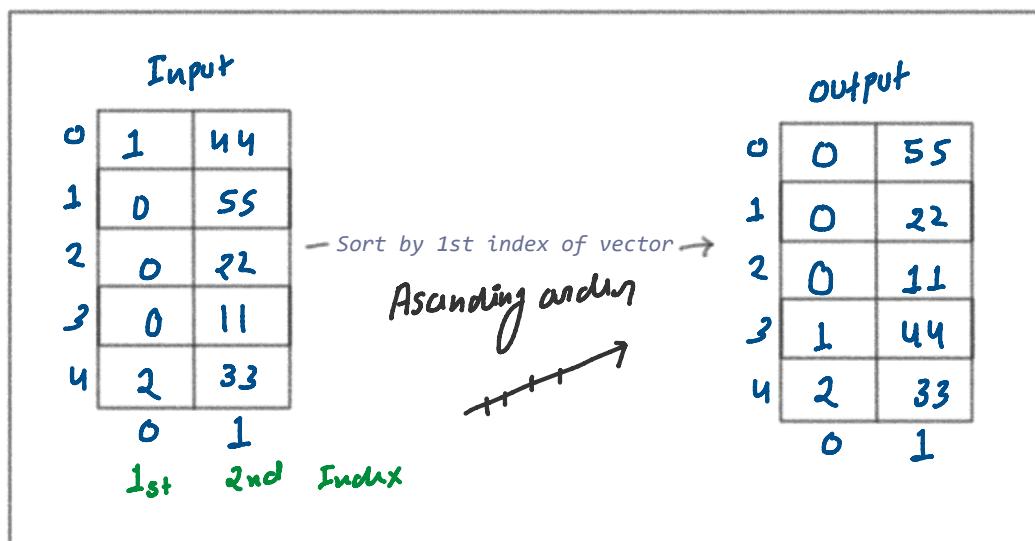
Index 3 → v_3 

Index 4 → v_4 



0	1	44
1	0	55
2	0	22
3	0	11
4	2	33
0	1	

Row Col



```

// ✓CUTOM COMPARATOR 02: SORT VECTOR OF VECTOR
#include <algorithm>
#include <iostream>
#include <vector>
using namespace std;

// Printing Method

void print(vector<vector<int>> &v) {
    for (int i = 0; i < v.size(); ++i) {
        vector<int> &temp = v[i];
        int a = temp[0];
        int b = temp[1];
        cout << a << " " << b << endl;
    }
    cout << endl;
}

// Custom Comparator ki return value always true ya false hoti hai

bool myComparator1(vector<int> &a, vector<int> &b) {
    return a[0] < b[0]; // increasing order sorting by 1st index
}

bool myComparator2(vector<int> &a, vector<int> &b) {
    return a[1] < b[1]; // increasing order sorting by 2nd index
}

int main() {
    // vector of vector sorting
    vector<vector<int>> v;

    int n;
    cout << "Enter size:\n";
    cin >> n;

    // Taking input from user in 2D vector
    for (int i = 0; i < n; ++i) {

        int a, b;
        cout << "Enter a, b" << endl;
        cin >> a >> b;

        // Creation of 1D vector temp
        vector<int> temp;

        // Inserting element a at 0th and b at 1st index in 1D vector
        temp.push_back(a);
        temp.push_back(b);

        // Inserting 1D vector temp in 2D vector v
        v.push_back(temp);
    }

    cout << "Here are the Values" << endl;
    print(v);

    cout << "Sorted by 1st index" << endl;
    sort(v.begin(), v.end(), myComparator1);
    print(v);

    cout << "Sorted by 2st index" << endl;
    sort(v.begin(), v.end(), myComparator2);
    print(v);

    return 0;
}

```