

Que 1) Plot a histogram,

10, 13, 18, 22, 27, 32, 38, 40, 45, 51, 56, 57, 88, 90, 92, 94, 99

Que 2) In a quant test of the CAT Exam, the population standard deviation is known to be 100. A sample of 25 tests taken has a mean of 520. Construct an 80% CI about the mean.

Que 3) A car believes that the percentage of citizens in city ABC that owns a vehicle is 60% or less. A sales manager disagrees with this. He conducted a hypothesis testing surveying 250 residents & found that 170 residents responded yes to owning a vehicle.

- State the null & alternate hypothesis.
- At a 10% significance level, is there enough evidence to support the idea that vehicle owner in ABC city is 60% or less.

Que 4) What is the value of the 99 percentile?

2,2,3,4,5,5,5,6,7,8,8,8,8,9,9,10,11,11,12

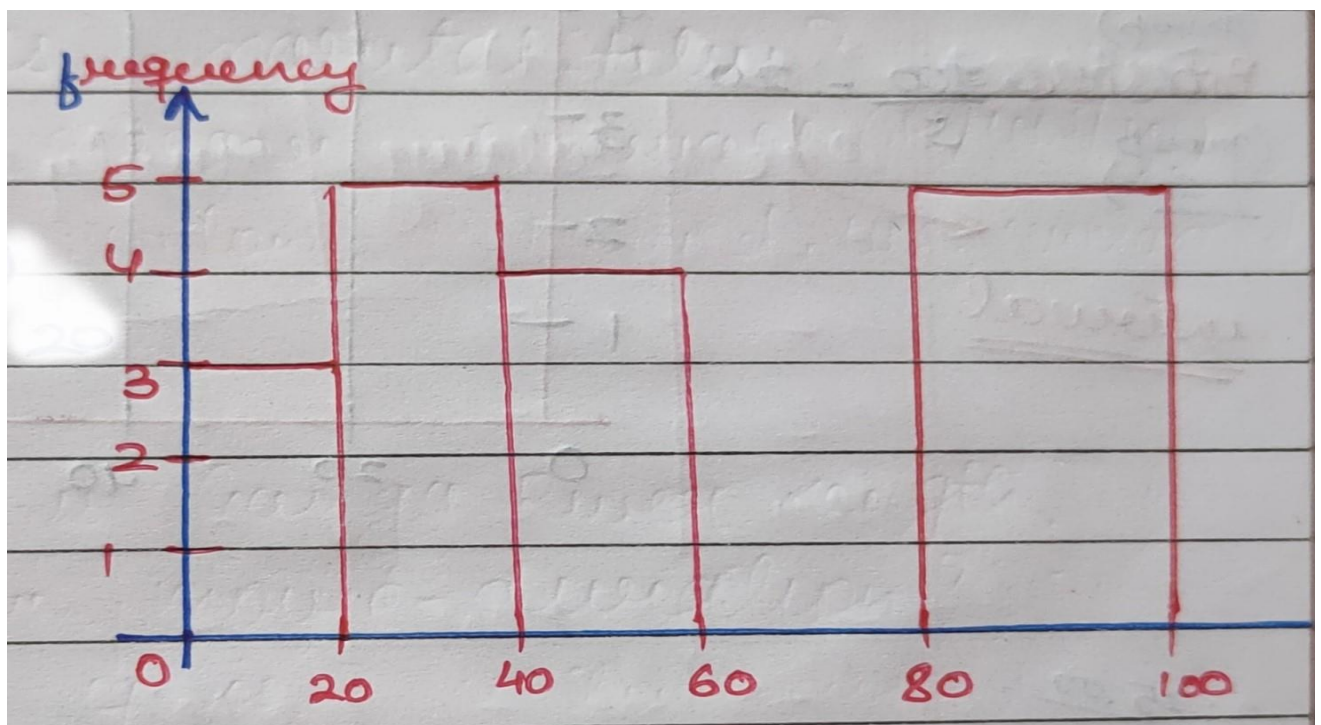
Que 5) In left & right-skewed data, what is the relationship between mean, median & mode?

Draw the graph to represent the same.

Solution 1 : Bins =5

$$\text{Bin size} = 100/5 = 20$$

Figure :



Solution 2

$$\sigma = 100, \quad n = 25$$

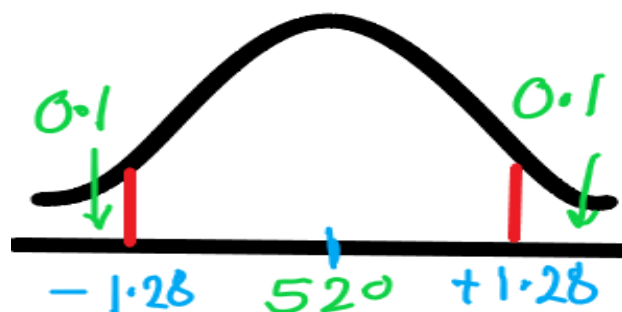
$$\bar{x} = 520, \quad CI = 80\%$$

$$\alpha = 1 - CI = 1 - 0.8 = 0.2$$

$$CI = \text{point Estimate} \pm \text{Margin of Error}$$
$$= \bar{x} \pm \left[ Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}} \right]$$

$$Z_{\alpha/2} = Z_{\frac{0.2}{2}} = Z_{0.1}$$

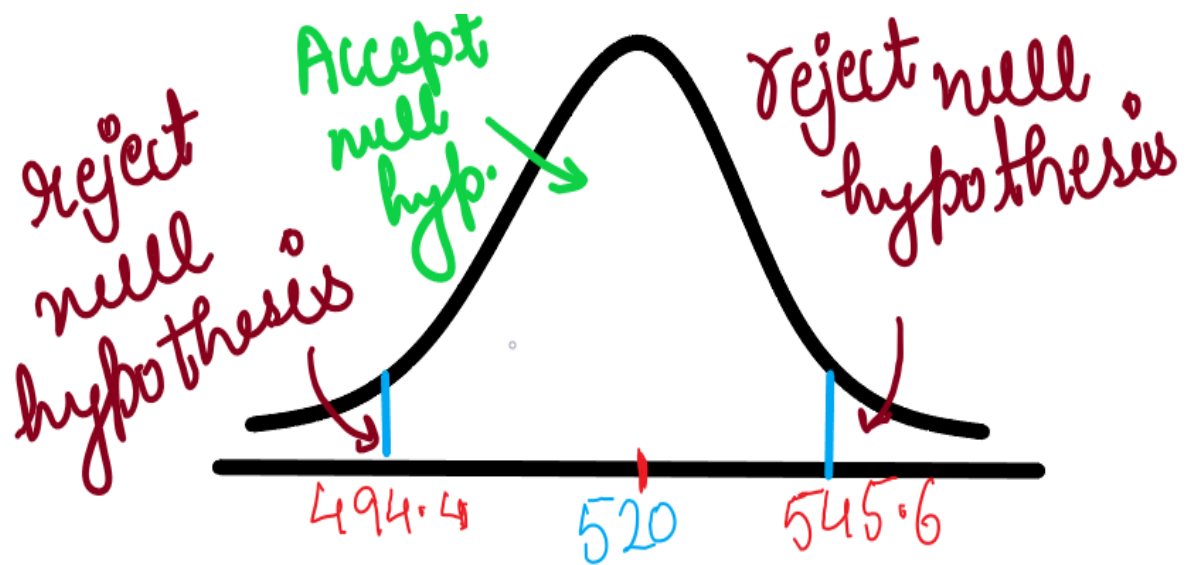
$$\text{Remaining Area} = 1 - 0.1 = 0.9$$
$$\pm 1.28 \text{ (Z-table)}$$



$$\text{Lower fence} = \bar{x} - Z_{\alpha/2} \left( \frac{\sigma}{\sqrt{n}} \right)$$
$$= 520 - 1.28 \times \left( \frac{100}{\sqrt{25}} \right)$$

$$= 494.4$$

$$\begin{aligned} \text{higher fence} &= 520 + 1.28 \times (100 \sqrt{25}) \\ &= 545.6 \end{aligned}$$



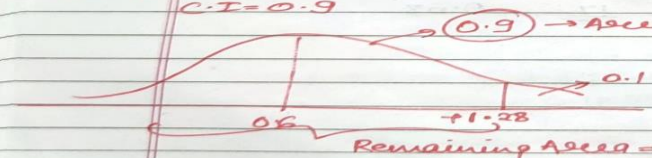
### Solution 3

02:51:00  $x = 170, n = 250$

Step 1:  $H_0: P_0 = 60\%$   
 $H_1: P_0 > 60\%$

Step 2:  $\hat{p} = \frac{x}{n} = \frac{170}{250} = 0.68$   
 $q_0 = 1 - P_0 = 1 - 0.6 = 0.4$

Step 3:  $\alpha = 0.1$   
 $C.I. = 0.9$



Remaining Area =  $1 - 0.1 = 0.9$

Step 4: Z Test (with prop)  $= \frac{\hat{p} - P_0}{\sqrt{\frac{P_0 q_0}{n}}} = \frac{0.68 - 0.6}{\sqrt{\frac{0.6 \times 0.4}{250}}} = +2.58$

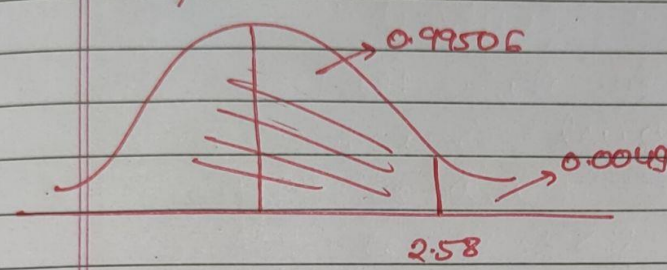
Step 4(i) Conclusion:

P-value method:

$+1.28 < +2.58$

Null hypothesis is rejected.

Ownership is  $> 60\%$ .



Remaining Area =  $1 - 0.99506 = 0.0049$

$p\text{-value} < \alpha$

$\rightarrow$  Null hypothesis is rejected

#### Solution 4

2,2,3,4,5,5,5,6,7,8,8,8,8,8,9,9,10,11,11,12

$n = 20$

$$\text{Value} = (\text{Percentile}/100) * (n+1)$$

$$= (99/100) * (20+1)$$

$$0.99 * 21 = 20.79\text{th index}$$

20.79<sup>th</sup> Index is 12 .....Ans.

#### Solution 5

