



Conceptual Questions

Chapter 2 : Statistical Learning

Q1. For each of parts (a) through (d), indicate whether we would generally expect the performance of a flexible statistical learning method to be better or worse than an inflexible method. Justify your answer.

(a) The sample size n is extremely large, and the number of predictors p is small.

When $n \gg p$, that means we have ample observation and the dimensions are very low meaning we won't be having the curse of dimensionality. A highly flexible model comes with high variance but this limitation is constrained and effectively managed, as the sheer amount of data helps the model to

recognize generalized patterns that will help predict future values and not stray to random noise, stopping the case of overfitting. Hence, a more flexible model is a **better** than inflexible

(b) The number of predictors p is extremely large, and the number of observations n is small.

When $p \gg n$, it generally leads to the case of overfitting in highly flexible models, as with more p the flexible method takes the form of polynomials with high dimensions like x^{100} , or x^{300} . With so many features the data is spread across very sparse or thin (curse of dimensionality), making the requirement of more data exponentially high to cover the space, as it NEEDS to be covered because highly flexible models will learn not only the generalized patterns but also all the random noise patterns making them work exceptionally well on training data but fail on validation and test data, also called as overfitting.

Methods relying on distances like K-nearest neighbors (KNN) also fail because of the thinly spread sparse data

Hence, when $p \gg n$, a highly flexible model leads to overfitting and curse of dimensionality making them a **worse** fit than inflexible statistical learning models.

(c) The relationship between the predictors and response is highly non-linear.

Highly flexible models are generally non-linear. They have more parameters and can therefore learn more complex, non-linear relationships in the data. This would make flexible models generally a **better** fit than inflexible methods.

(d) The variance of the error terms, i.e. $\sigma^2 = \text{Var}(e)$, is extremely high

$$\text{MSE (Mean square error)} = \text{var}(x) + \text{Bias}^2 + \text{Var}(e)$$

Here variance = $E(x - \text{mean})^2$ making this a positive value, Bias = $E(f(\hat{x}) - f(x))$ hence squaring it ensures a non negative value, considering these we can say that the lowest value of MSE will always be $\text{Var}(e)$ which is the irreducible error or noise that is out of our control.

Now according to our question, the variance $\text{var}(e)$ is extremely high, making the lowerbound value of MSE extremely high, which we do not want as we always tend to make MSE value as low as possible. Moreover, flexible models already have high $\text{var}(x)$ and now with high $\text{var}(e)$ the overall MSE would be extremely high for test or validation dataset hence, Flexible statistical learning model will be **worse** than inflexible statistical learning model.

2. Explain whether each scenario is a classification or regression problem, and indicate whether we are most interested in inference or prediction. Finally, provide n and p .

(a) We collect a set of data on the top 500 firms in the US. For each firm we record profit, number of employees, industry and the CEO salary. We are interested in understanding which factors affect CEO salary.

This is a **regression problem** as CEO salary is a quantitative value, where we are more interested in **Inference**, here $n = 500$ and $p = 3$ (profit, number of employees, industry), response variable = 1 (CEO Salary)

(b) We are considering launching a new product and wish to know whether it will be a success or a failure. We collect data on 20 similar products that were previously launched. For each product we have recorded whether it was a success or failure, price charged for the product, marketing budget, competition price, and ten other variables.

$n=20$, $p=13$, response variable = 1 (Success or failure) ; this is also a **classification problem** but we are more interested in **prediction**.

(c) We are interested in predicting the % change in the USD/Euro exchange rate in relation to the weekly changes in the world stock markets. Hence we collect weekly data for all of 2012. For each week we record the % change in the USD/Euro, the % change in the US market, the % change in the British market, and the % change in the German market

$n=52$, $p=3$, response variable = 1(%change in USD/Euro exchange rate); we are interested in **prediction** but this is a **regression problem** as we are predicting a continuous value rather than a class.