

BOOLEAN ALGEBRA

1. Absorption Laws:

$$A + A \cdot B = A$$

$$A (A + B) = A$$

2. $A + A'B = A + B$

$$A \cdot (A' + B) = A \cdot B$$

3. Transposition Theorem:

$$AB + A'C = (A + C) \cdot (A' + B)$$

4. Consensus Theorem:

$$AB + A'C + BC = AB + A'C$$

$$(A + B) \cdot (A' + C) \cdot (B + C) = (A + B) \cdot (A' + C)$$

Duals

Given Expression	Dual
1. $\bar{0} = 1$	$\bar{1} = 0$
2. $0 \cdot 1 = 0$	$1 + 0 = 1$
3. $0 \cdot 0 = 0$	$1 + 1 = 1$
4. $1 \cdot 1 = 1$	$0 + 0 = 0$
5. $A \cdot 0 = 0$	$A + 1 = 1$
6. $A \cdot 1 = A$	$A + 0 = A$
7. $A \cdot A = A$	$A + A = A$
8. $A \cdot \bar{A} = 0$	$A + \bar{A} = 1$
9. $A \cdot B = B \cdot A$	$A + B = B + A$
10. $A \cdot (B \cdot C) = (A \cdot B) \cdot C$	$A + (B + C) = (A + B) + C$
11. $A \cdot (B + C) = AB + AC$	$A + BC = (A + B)(A + C)$
12. $A(A + B) = A$	$A + AB = A$
13. $A \cdot (A \cdot B) = A \cdot B$	$A + A + B = A + B$
14. $\overline{AB} = \bar{A} + \bar{B}$	$\overline{A + B} = \bar{A} \bar{B}$
15. $(A + B)(\bar{A} + C)(B + C)$ $= A + B(\bar{A} + C)$	$AB + \bar{A}C + BC = AB + \bar{A}C$
16. $(A + C)(\bar{A} + B) = AB + \bar{A}C$	$AC + \bar{A}B = (A + B)(\bar{A} + C)$
17. $A + \bar{B}C = (A + \bar{B})(A + C)$	$A(\bar{B} + C) = (A\bar{B} + AC)$
18. $(A + B)(C + D) = AC + AD + BC + BD$	$(AB + CD) = (A + C)(A + D)$ $(B + C)(B + D)$
19. $A + B = AB + \bar{A}B + A\bar{B}$	$AB = (A + B)(\bar{A} + B)(A + \bar{B})$
20. $A + B(\overline{C + DE}) = A + B\bar{C}\bar{D}\bar{E}$	$A[B + \overline{(C \cdot D + E)}]$ $= A \cdot (B + \bar{C} + \bar{D} + \bar{E})$
21. $\overline{\bar{A}B + \bar{A} + AB} = 0$	$\overline{A + B \cdot \bar{A} \cdot (A + B)} = 1$
22. $AB + \bar{A}\bar{C} + A\bar{B}C (AB + C) = 1$	$(A + B)(\bar{A} + \bar{C}) \cdot [(A + \bar{B} + C) + (A + B)C] = 0$

Duality principle:

Every theorem has an equivalent theorem by performing the following operation:

1. Change every AND operation to OR operation (Change every dot sign to plus sign) and vice-versa.
2. Change every '0' to '1' and vice-versa.