

7 days.

Total	⇒ 168	
Sleep	⇒ 49 (7×7)	⇒ 150
Office	⇒ 50 (5×10)	
Normals	⇒ 21 (7×3)	
Fun	⇒ 21 (7×3)	
Scaler class	⇒ 9 (3×3)	

Proc ⇒ $168 - 150$ ⇒ (18)

Q1 Given an array of size N . Find the maximum value of $j-i$ such that $A[i] \leq A[j]$.

Constraints $1 \leq n \leq 10^5 \Rightarrow Tc \text{ possible} \Rightarrow O(n)$
 $-10^9 \leq A[i] \leq 10^9 \Rightarrow O(n \log n)$
 $O(n\sqrt{n})$

Eg : $A = [3, 5, 4, 2]$

$j = 3$: no i available

$j = 2$: $i = 0$, ans $\Rightarrow 2-0 \Rightarrow 2$

$j = 1$: $i = 0$, ans $\Rightarrow 1-0 \Rightarrow 1$

$j = 0$: no j available

Brute force : Check for every pair.

Tc: $O(n^2)$.

Sc: $O(1)$.

Hint 1:

$(\text{first}, \text{second})$
 $\downarrow \quad \downarrow$
 value index
 $A = [3, 5, 4, 2]$

\Rightarrow

$(3, 0)$
$(5, 1)$
$(4, 2)$
$(2, 3)$

Sort on
first term \rightarrow

$(2, 3)$
$(3, 0)$
$(4, 2)$
$(5, 1)$

\updownarrow
 $arr[i]$

0	1	2	3
3	0	0	0

\downarrow
 $arr[j]$

$j=1$
 $i=0 \Rightarrow 1$

$j=2 \Rightarrow 2$
 $i=0$

left min $[n]$

left-min $[i] \Rightarrow$ min element encountered

indices

0	1	2	3
3	0	2	1

$\textcircled{-1}$ in $arr[0 \dots i]$

0	1	2	3
2	3	4	5

\Rightarrow

0	1	2	3
3	0	0	0

$j=1$

\hookrightarrow left min $[n-2]$

arr

$arr[0]$ will never be over i

val	index
(2, 3)	
(3, 0)	
(4, 2)	
(5, 1)	

min_index \Rightarrow arr[0].index $\Rightarrow 3$

$j = 0$ { arr[j].index }

min_index = 0 ans $j-i \Rightarrow -3$

$j = 2$ { arr[2].index }

min_index = 0 ans $\Rightarrow 2-0 \Rightarrow 2$

$j = 1$ { arr[3].index }

ans $\Rightarrow 1-0 \Rightarrow 1$

min_index \Rightarrow min { min_index, arr[j].index }

[0 1 2 3 4
1 2 3 4 5]

(1, 0)
(2, 1)
(3, 2)
(4, 3)
(5, 4)

\Rightarrow 4

-1

$\begin{matrix} & 0 & 1 & 2 & 3 & 4 \\ \lceil & 5 & 4 & 3 & 2 & 1 \rceil \end{matrix}$

j i $A[j] \geq A[i]$
 $j-1$

$\left(\begin{matrix} (1, 4) \\ (2, 3) \\ (3, 2) \\ (4, 1) \\ (5, 0) \end{matrix} \right) \Rightarrow \begin{matrix} \Rightarrow (-1) \\ \Rightarrow (-1) \end{matrix}$

TC: $O(n \log n)$

$\text{vector} \left\langle \text{pair} \langle \text{int}, \text{int} \rangle \right\rangle \text{vec};$

$\text{vec.push-back}(\text{make_pair}(\text{arr}[i], i));$

Q2 Given a matrix of size $N \times M$, find the sum of all submatrix sum. 1.

Ans

$$\begin{matrix} & 0 & 1 \\ 0 & \begin{bmatrix} 3 & 1 \end{bmatrix} \\ 1 & \begin{bmatrix} -1 & -2 \end{bmatrix} \\ 2 & \begin{bmatrix} 2 & 4 \end{bmatrix} \end{matrix} \Rightarrow$$

$$\left\{ \begin{array}{l} \begin{bmatrix} 3 \end{bmatrix}, \begin{bmatrix} 3, 1 \end{bmatrix}, \begin{bmatrix} 3 \end{bmatrix}, \begin{bmatrix} 3, 1 \end{bmatrix} \\ \begin{bmatrix} 3 \end{bmatrix}, \begin{bmatrix} 3, 1 \end{bmatrix}, \begin{bmatrix} 1 \end{bmatrix}, \begin{bmatrix} 1, -2 \end{bmatrix} \\ \begin{bmatrix} 1 \end{bmatrix}, \begin{bmatrix} -2 \end{bmatrix}, \begin{bmatrix} -1 \end{bmatrix}, \begin{bmatrix} -1, -2 \end{bmatrix}, \begin{bmatrix} -1 \end{bmatrix} \\ \begin{bmatrix} -1, -2 \end{bmatrix}, \begin{bmatrix} -2 \end{bmatrix}, \begin{bmatrix} -2 \end{bmatrix}, \begin{bmatrix} 2 \end{bmatrix}, \begin{bmatrix} 2, 4 \end{bmatrix} \\ \begin{bmatrix} 2 \end{bmatrix}, \begin{bmatrix} 4 \end{bmatrix} \end{array} \right\}$$

$$\begin{aligned} \text{Sum} \Rightarrow & (3 \times 6) + (1 \times 6) + (-1 \times 8) + (-2 \times 8) \\ & + (2 \times 6) + (4 \times 6) \Rightarrow \boxed{36} \end{aligned}$$

$$[a, b] \Rightarrow b - a + 1$$

$$[j, n-1] \Rightarrow n - j + 1 = (n - j)$$

	0	1	2	3	4	5	6
0	TL	TL	TL	TL			
1	TL	TL	TL	TL			
2	TL	TL	TL	TL			
3	TL	TL	TL	TL BR	BR	BR	BR
4				BR	BR	BR	BR
5				BR	BR	BR	BR
6				BR	BR	BR	BR
7				BR	BR	BR	BR

$(i,j) \Rightarrow (3,2)$

no of TL $\Rightarrow (i+1) \times (j+1)$

no of BR $\Rightarrow (n-i) \times (m-j)$

$$20 + 20 + 20 + 20 + 20$$

----- \Rightarrow 16 times

$$16 \times 20 \Rightarrow \boxed{320}$$

Break: 10:45

Q3 Given a 2D Matrix, every row sorted, every column sorted. Find an element K.

$\left(\begin{array}{l} n = \text{rows} \\ m = \text{columns} \end{array} \right)$

K=15

	0	1	2	3	4	5
0	-1	2	4	5	9	11
1	1	4	7	8	10	14
2	3	7	9	10	12	18
3	6	10	12	14	16	20
4	9	13	16	19	22	24
5	11	15	19	21	24	27
6	14	20	25	29	31	39
7	18	24	29	32	34	42

Brute Force 1: Iterate on every element: $Tc: O(mn)$

Brute Force 2: Iterate on each row and do binary search $Tc: O(n \log m)$

Brute Force 3: Iterate on each column and do binary search $Tc: O(m \log n)$

K=15

	0	1	2	3	4	5
0	-1	2	4	5	9	11
1	1	4	7	8	10	14
2	3	7	9	10	12	18
3	6	10	12	14	16	20
4	9	13	16	19	22	24
5	11	15	19	21	24	27
6	14	20	25	29	31	39
7	18	24	29	32	34	42

$i = 0, j = m-1$

while ($j \geq 0$ & $i < n$) {

if ($arr[i][j] > k$) {
// ignore below

$j--$;

} else if ($arr[i][j] < k$)
// ignore left

$i++$;

} else

return true;

}

}

return false;

TC : $O(m+n)$
SC : $O(1)$

$i++ = A, j-- = 13$

A, A, B, B, A, B, A, B, ...

$(n+m) \Rightarrow$

#

6x4

	0	1	2	3
0	TL	TL	TL	
1	TL	TL	TL	
2	TL	TL	TL	
3	TL	TL	TL BR	BR
4			BR	BR
5			BR	BR

$$TL = 12$$

$$BR \Rightarrow 6$$

$$6 + 6 + 6 + 6 + 6$$

$$12 \times 6 \Rightarrow 72$$

$$72 \times add(i)[j]$$