



# **Sunbeam Institute of Information Technology**

## **Pune and Karad**

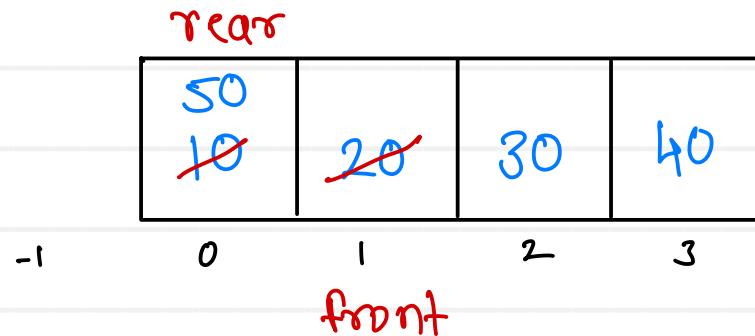
### **Module – Data Structures and Algorithms**

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# Circular queue

size=4



$$\text{front} = (\text{front} + 1) \% \text{ size}$$

$$\text{rear} = (\text{rear} + 1) \% \text{ size}$$

$$\text{front} = \text{rear} = -1$$

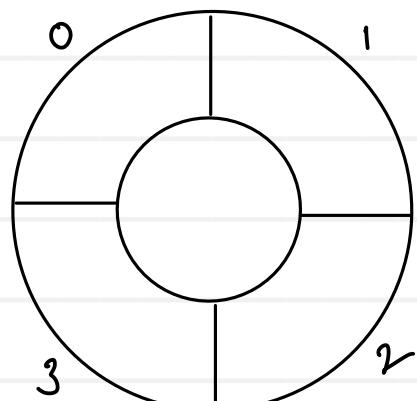
$$= (-1+1)\% 4 = 0$$

$$= (0+1)\% 4 = 1$$

$$= (1+1)\% 4 = 2$$

$$= (2+1)\% 4 = 3$$

$$= (3+1)\% 4 = 0$$



## Operations:

### 1) Push/Enqueue :

- reposition rear (inc)
- add value at rear index

### 2) Pop/Dequeue :

- reposition front (dec)

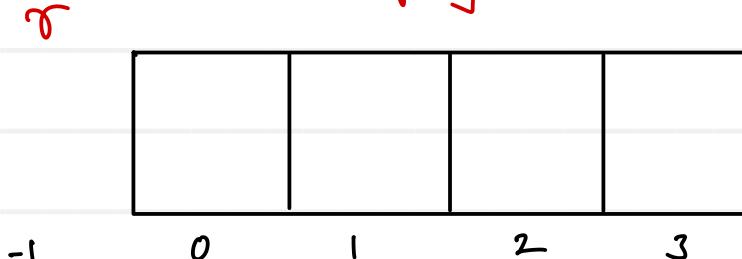
### 3) Peek :

- read value of front+1 index

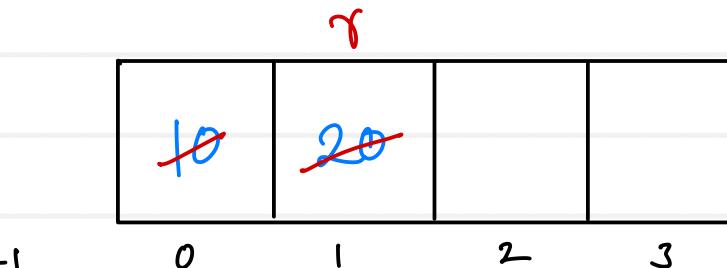
All operations are performed in  $O(1)$  time complexity.

# Circular queue - Conditions

Empty



$\text{front} == \text{rear}$  &  $\text{rear} == -1$



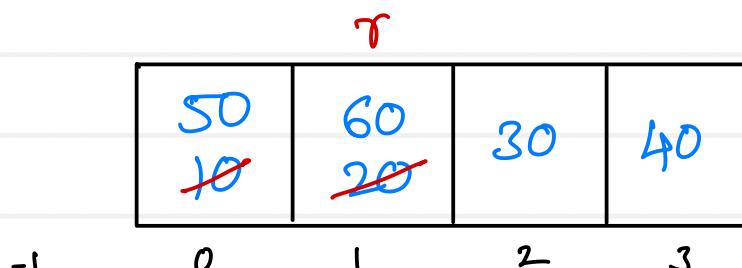
`POP()`  
 $\text{front} = (\text{front} + 1) \% \text{size};$   
if ( $\text{front} == \text{rear}$ )  
     $\text{front} = \text{rear} = -1$

3

Full



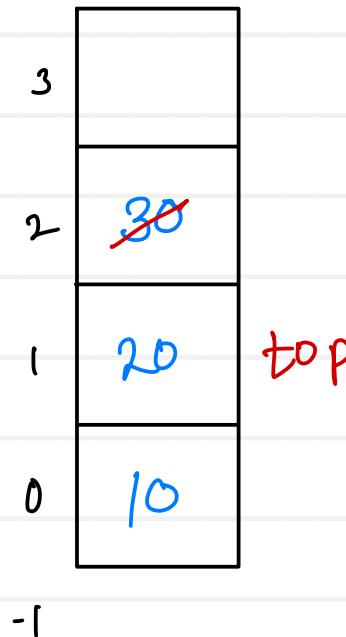
$\text{front} == -1$  &  $\text{rear} == \text{size} - 1$



$\text{front} == \text{rear}$  &  $\text{rear} != -1$

# Stack

- stack is linear data structure which stores similar type of data.
- stack has only one end (top)
- insert & delete both are allowed only from top end



- stack works on principle of "LIFO"  
"Last In First Out".

- top always points to last inserted data.

## Operations :

### 1) Add / push :

- 1) reposition top (inc)
- 2) add value at top index

### 2) Delete / pop :

- 1) reposition top (dec)

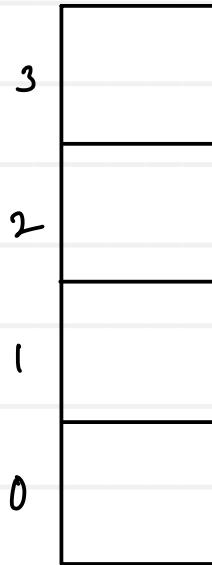
### 3) Peek :

- 1) read / return data of top index

All operations are performed in O(1) time complexity.

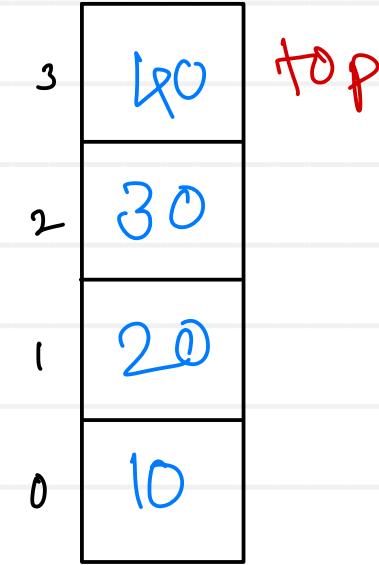
# Stack - Conditions

Empty



$$\text{top} == -1$$

Full



$$\text{top} == \text{size}-1$$



# Applications – Stack and Queue

## Stack

- Parenthesis balancing
- Expression conversion and evaluation
- Function calls
- Used in advanced data structures for traversing

### • Expression conversion and evaluation:

- Infix to postfix
- Infix to prefix
- Postfix evaluation
- Prefix evaluation

Expressions :

1) Infix :  $a+b$  (human)

2) Postfix :  $a\ b\ +$       3) Prefix :  $+ \ a\ b$  (machine)

## Queue

- Jobs submitted to printer
- In Network setups – file access of file server machine is given to First come First serve basis
- Calls are placed on a queue when all operators are busy
- Used in advanced data structures to give efficiency.
- Process waiting queues in OS





# Postfix Evaluation

- Process each element of postfix expression from left to right
- If element is operand
  - Push it on a stack
- If element is operator
  - Pop two elements (Operands) from stack, in such a way that
    - Op2 – first popped element
    - Op1 – second popped element
  - Perform current element (Operator) operation between Op1 and Op2
  - Again push back result onto the stack
- When single value will remain on stack, it is final result
- e.g. 4 5 6 \* 3 / + 9 + 7 -





# Postfix evaluation

Postfix expression : 4 5 6 \* 3 / + 9 + 7 -

$l \longrightarrow r$

$$\textcircled{5} \quad 23 - 7 \\ = 16$$

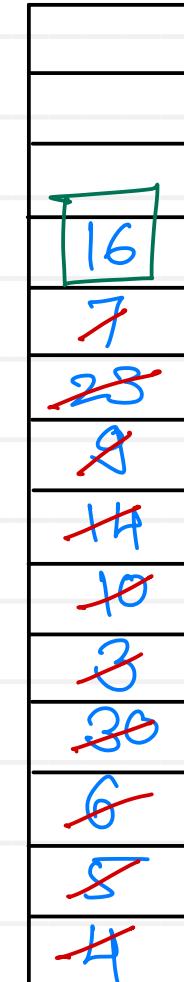
Result : 16

$$\textcircled{4} \quad 14 + 9 \\ = 23$$

$$\textcircled{3} \quad 4 + 10 \\ = 14$$

$$\textcircled{2} \quad 30 / 3 \\ = 10$$

$$\textcircled{1} \quad 5 * 6 \\ = 30$$





# Prefix Evaluation

- Process each element of prefix expression from right to left
- If element is operand
  - Push it on a stack
- If element is operator
  - Pop two elements (Operands) from stack, in such a way that
    - Op1 – first popped element
    - Op2 – second popped element
  - Perform current element (Operator) operation between Op1 and Op2
  - Again push back result onto the stack
- When single value will remain on stack, it is final result
- e.g. - + + 4 / \* 5 6 3 9 7



# Prefix evaluation

Prefix expression : - + + 4 / \* 5 6 3 9 7

$\leftarrow l \qquad \sigma \rightarrow$

Result : 16

⑤  $23 - 7$   
 $= 16$

④  $14 + 9$   
 $= 23$

③  $4 + 10$   
 $= 14$

②  $30 / 3$   
 $= 10$

①  $5 * 6$   
 $= 30$





# Infix to Postfix Conversion

- Process each element of infix expression from left to right
- If element is Operand
  - Append it to the postfix expression
- If element is Operator
  - If priority of topmost element (Operator) of stack is greater or equal to current element (Operator), pop topmost element from stack and append it to postfix expression
  - Repeat above step if required
  - Push element on stack
- Pop all remaining elements (Operators) from stack one by one and append them into the postfix expression
- e.g. a \* b / c \* d + e - f \* h + i



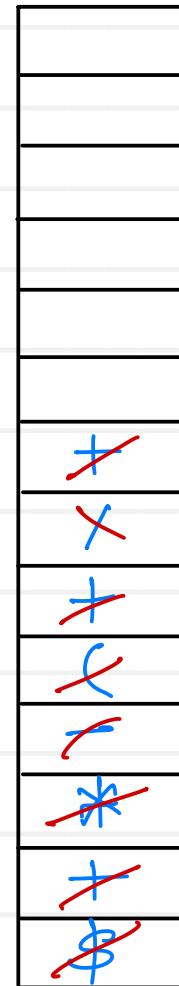


# Infix to Postfix conversion

Infix expression :  $1 \$ 9 + 3 * 4 - ( 6 + 8 / 2 ) + 7$

$\leftarrow$   $\longrightarrow$

Postfix expression :  $19\$34*+682/+7+$



)

+  
x  
+  
x  
/  
\*

-  
+  
x  
/  
\*

+  
\$

Priority :  
( )  
\$  
\* / %  
+ -





# Infix to Prefix Conversion

- Process each element of infix expression from right to left
- If element is Operand
  - Append it to the prefix expression
- If element is Operator
  - If priority of topmost element of stack is greater than current element (Operator), pop topmost element from stack and append it to prefix expression
  - Repeat above step if required
  - Push element on stack
- Pop all remaining elements (Operators) from stack one by one and append them into the prefix expression
- Reverse prefix expression
- e.g. a \* b / c \* d + e - f \* h + i





# Infix to Prefix conversion

Infix expression :  $1 \$ 9 + 3 * 4 - ( 6 + 8 / 2 ) + 7$

$\swarrow \qquad \searrow$

Expression :  $728/6+43*91\$+-+$

Prefix expression :  $+ - + \$ 1 9 * 3 4 + 6 / 8 2 7$





# Prefix to Postfix

- Process each element of prefix expression from right to left
- If element is an Operand
  - Push it on to the stack
- If element is an Operator
  - Pop two elements (Operands) from stack, in such a way that
    - Op1 – first popped element
    - Op2 – second popped element
  - Form a string by concatenating Op1, Op2 and Opr (element)
  - String = “Op1+Op2+Opr”, push back on to the stack
- Repeat above two steps until end of prefix expression.
- Last remaining on the stack is postfix expression
- e.g. \* + a b – c d





# Postfix to Infix

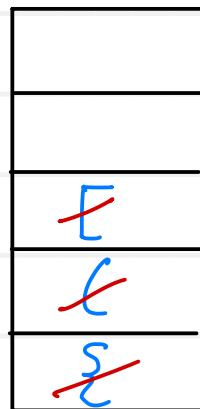
- Process each element of postfix expression from left to right
- If element is an Operand
  - Push it on to the stack
- If element is an Operator
  - Pop two elements (Operands) from stack, in such a way that
    - Op2 – first popped element
    - Op1 – second popped element
  - Form a string by concatenating Op1, Opr (element) and Op2
  - String = “Op1+Opr+Op2”, push back on to the stack
- Repeat above two steps until end of postfix expression.
- Last remaining on the stack is infix expression
- E.g. a b c - + d e - f g - h + / \*



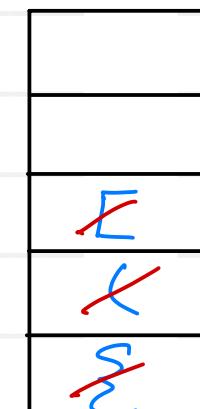


# Parenthesis balancing using stack

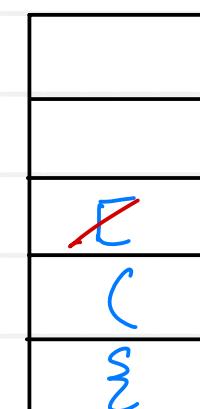
{ ( [ ] ) }



{ ( [ ] ) } )



{ ( [ ) ] }



] == [  
) == (  
} == {

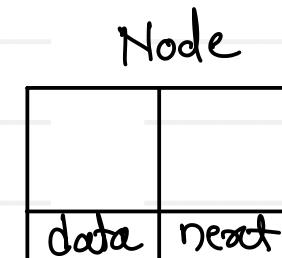
] == [  
) == (  
} == {  
) ?

) != [

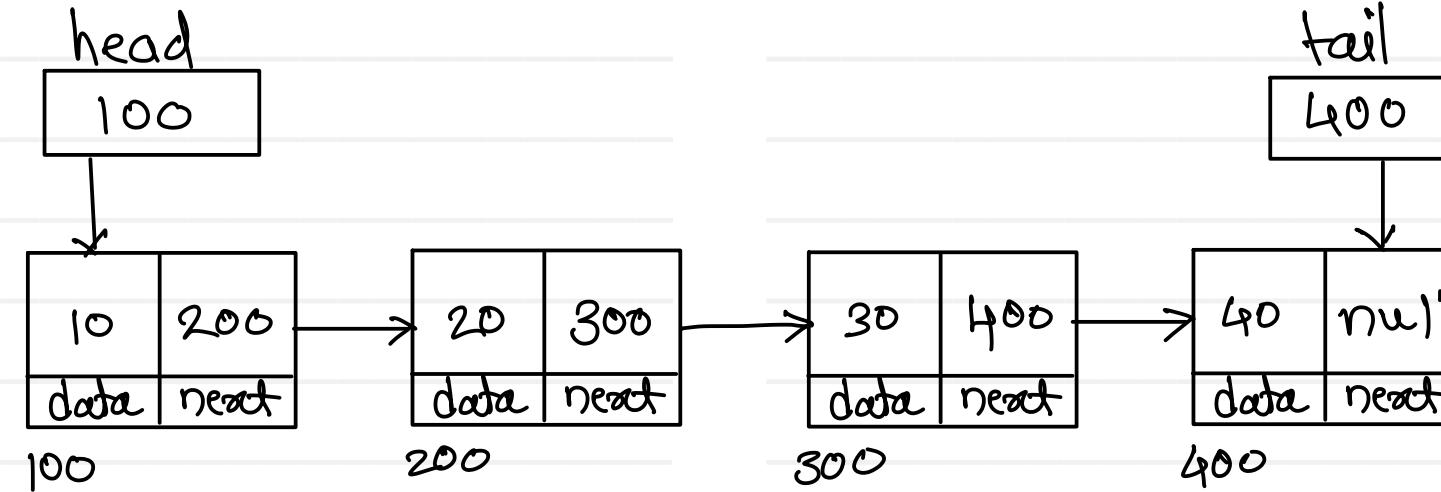


# Linked List

- linear data structure
- Address/link of next data is kept with current data
- every element is known as "Node"
- every node has two parts:
  - 1> data : actual value
  - 2> link/next : address/reference of next data



- address/reference of first node is kept into head reference
- address/reference of last node is kept into tail reference (optional)





# Linked List

## Operations

- 1. Add first
- 2. Add last
- 3. Add position ( insert )

- 1. Delete first
- 2. Delete last
- 3. Delete position

- 1. Display ( traverse ) ( forward/ backward)

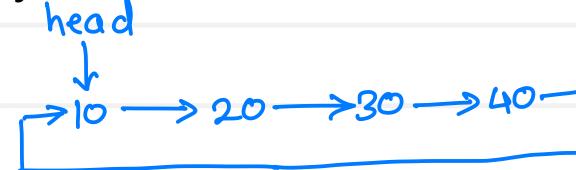
- 1. Search
- 2. Sort
- 3. Reverse

## Types

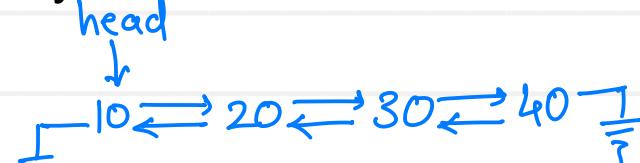
- 1. Singly linear linked list



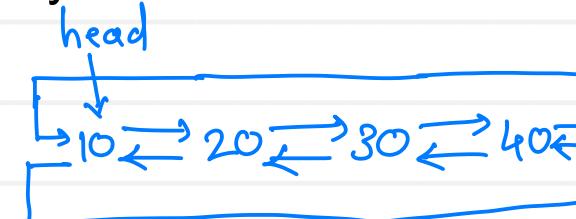
- 2. Singly circular linked list



- 3. Doubly linear linked list



- 4. Doubly circular linked list





# Linked List

Node has two parts

data : int , char, float, double, enum, class, String

next : reference

class Node {

    int data;

    Node next;

}

Why static?

① no dependency of  
List class to create  
object of Node class

② private non static  
fields of List class  
should not be accessed  
into Node class

class List {

    static class Node {

        int data;

        Node next;

    }

    Node head, tail;

    int size;

    List() { --- }

    add() { --- }

    delete() { --- }

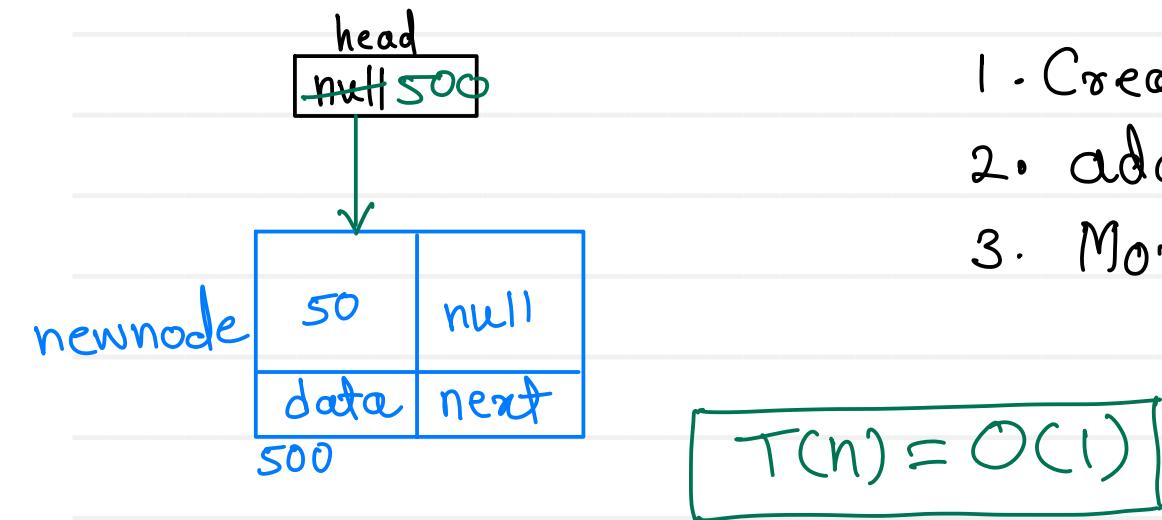
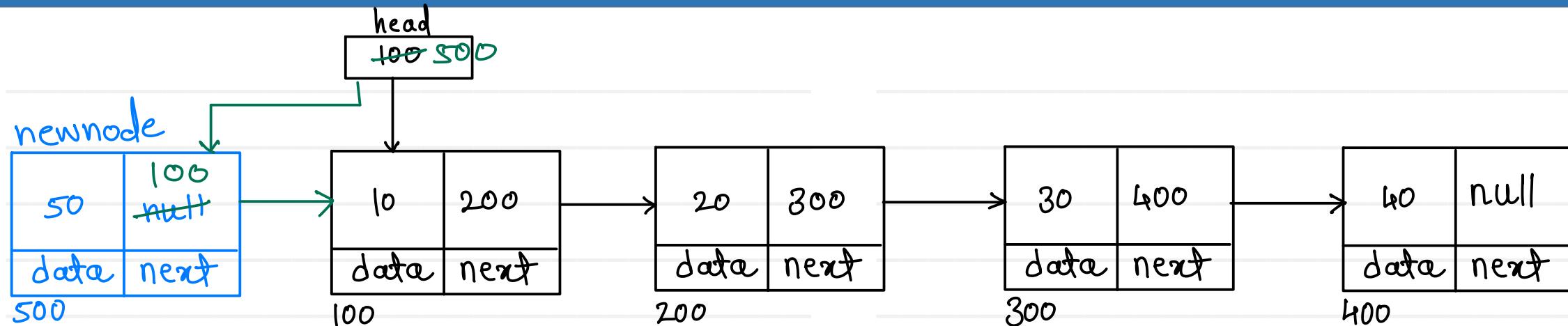
    display() { --- }

    deleteAll() { --- }

}



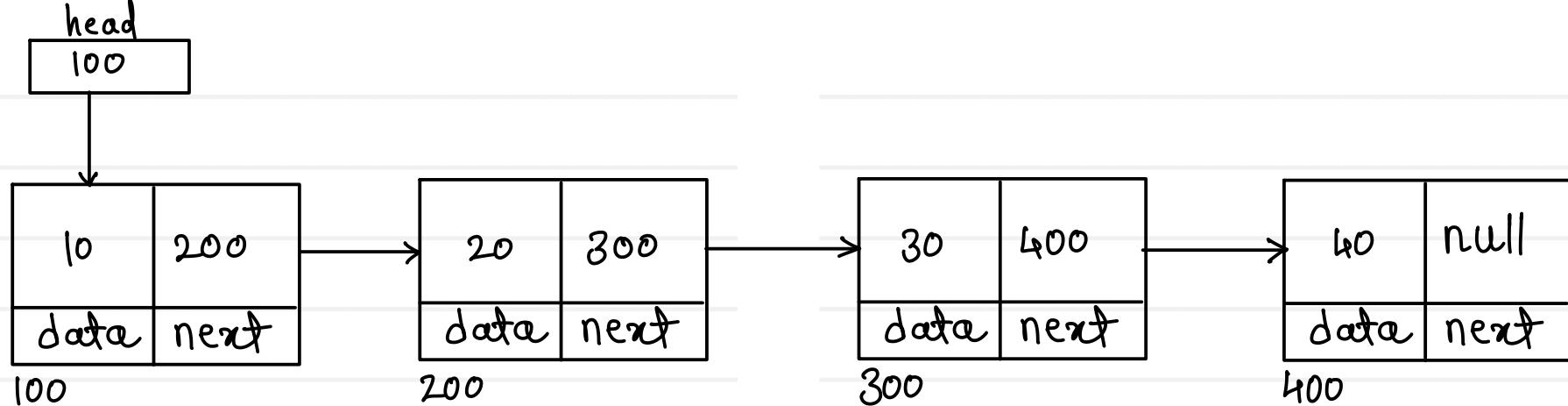
# Singly linear Linked List - Add first



1. Create Node with given data/value.
2. add first node into next of newnode
3. Move head on newnode

$\text{newnode}.\text{next} = \text{head}$   
 $\text{head} = \text{newnode}$

# Singly linear Linked List - Display

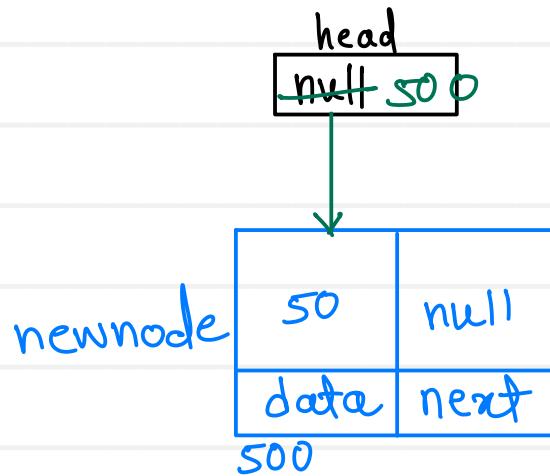
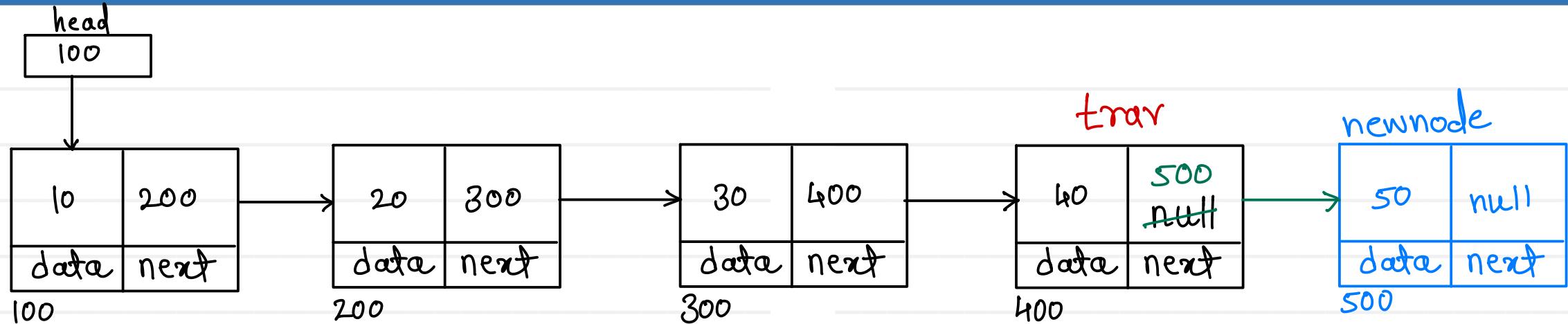


trav	trav.data	trav.next
100	10	200
200	20	300
300	30	400
400	40	null
null		

1. Create trav & start at head.
2. print/visit current node (trav.data)
3. go on next node (trav.next)
4. repeat above two steps for each node

$$T(n) = O(n)$$

# Singly linear Linked List - Add last

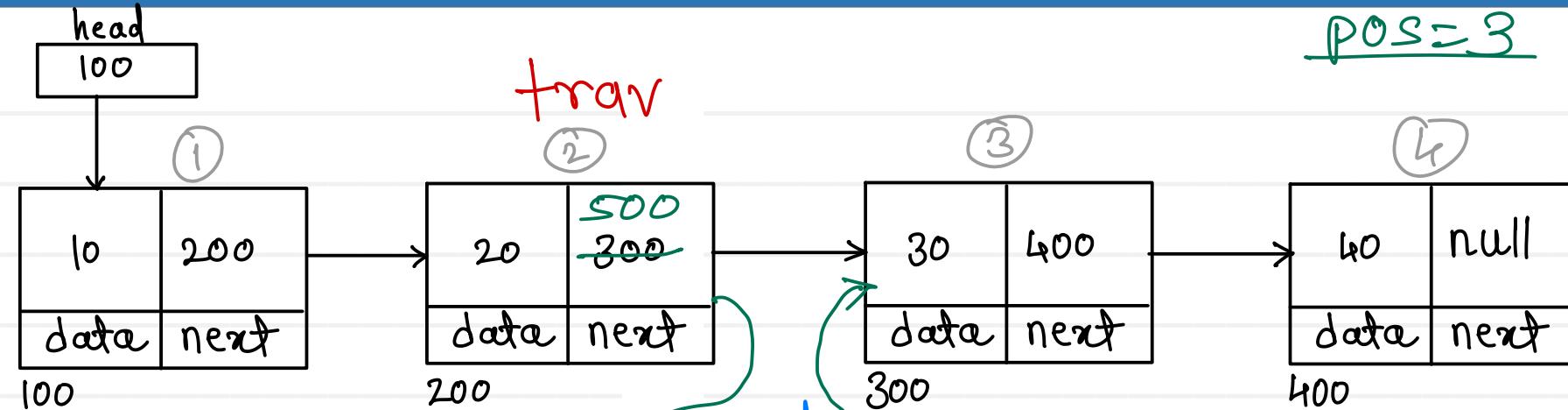


1. Create Node with value
2. if list is empty
  - a. add newnode into head
3. if list is not empty
  - a. traverse till last node
  - b. add newnode into next of lastnode

while (trav.next != null)  
 trav = trav.next;

$$T(n) = O(n)$$

# Singly linear Linked List - Add position



1. Create node with data
2. if list is empty  
head = newnode;
3. if list is not empty

a. traverse till pos-1 node

b. add pos node into next of newnode

c. add newnode into next of pos-1 node

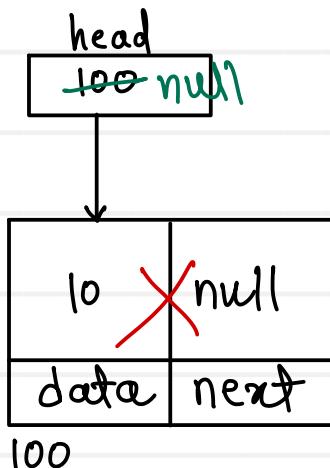
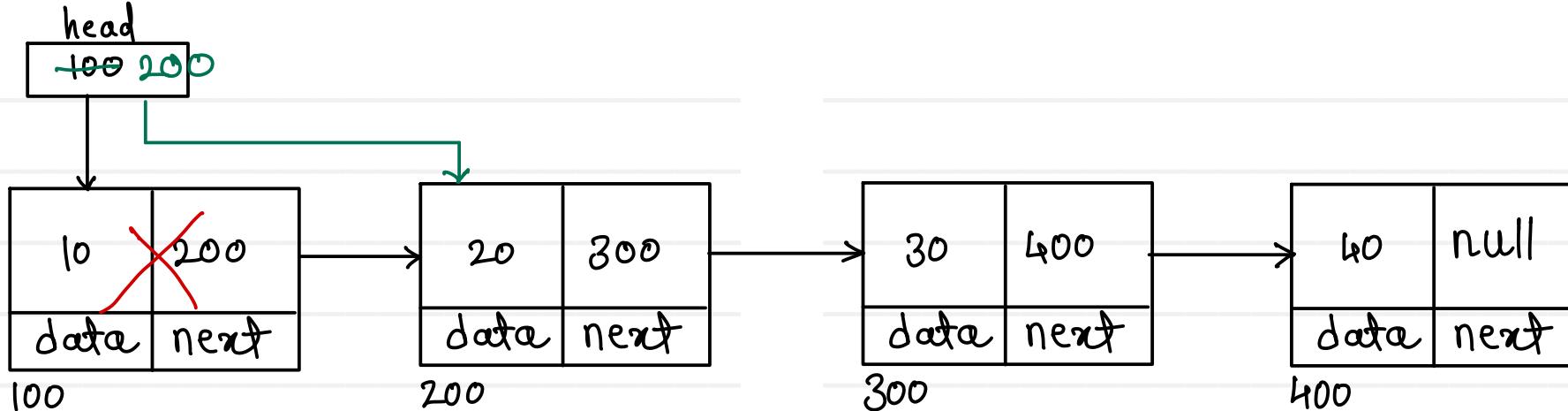
$$T(n) = O(n)$$

Node trav = head;  
for(int i=1; i < pos-1; i++)  
trav = trav.next;

pos=3.  
trav i i < 2  
100 1 T  
200 2 F

pos=5  
trav i i < 4  
100 1 T  
200 2 T  
300 3 T  
400 4 F

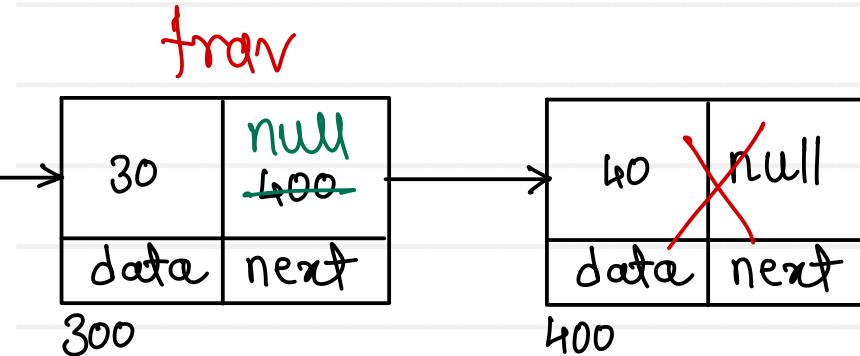
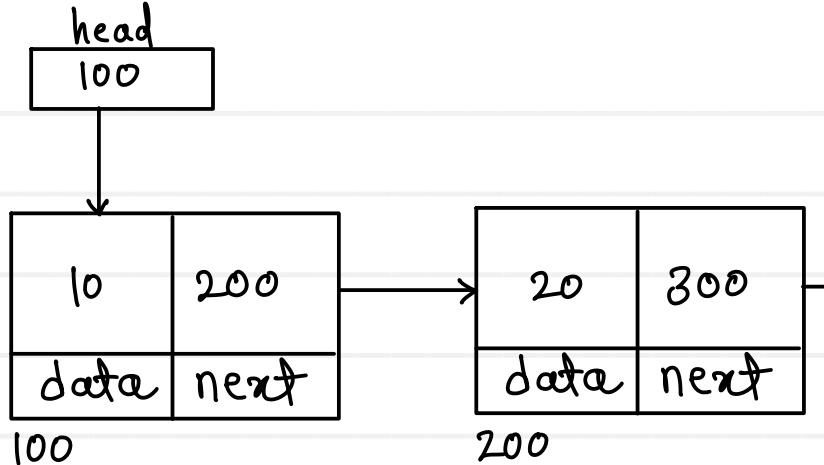
# Singly linear Linked List - Delete first



1. if list is empty  
return :
2. if list is not empty  
move head on second node

$$T(n) = O(1)$$

# Singly linear Linked List - Delete last

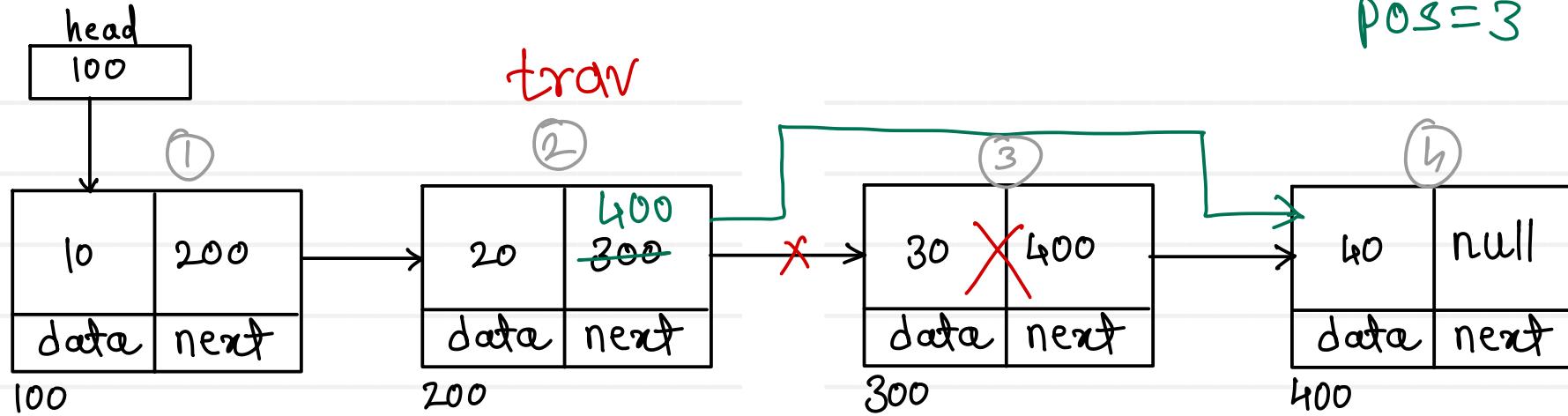


1. if list is empty  
return;
- 2 if list has single node  
 $\text{head} = \text{null};$
3. if list has multiple nodes
  - a. traverse till second last node
  - b. add null into next of second last node

`while (trav.next != null)  
trav = trav.next;`

$$T(n) = O(n)$$

# Singly linear Linked List - Delete position



1. if list is empty  
return;
2. if list has single node  
 $\text{head} = \text{null};$
3. if list has multiple nodes
  - a. traverse till  $\text{pos}-1$  node
  - b. add  $\text{pos}+1$  node into next of  $\text{pos}-1$  node

$$T(n) = O(n)$$



Thank you!!!

Devendra Dhande

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