

- 1) The wavefunction of which orbital is spherically symmetric: [Gate 2017]
 - a) p_x
 - b) p_y
 - c) s
 - d) d_{xy}
- 2) The contour integral $\oint \frac{dz}{1+z^2}$ evaluated along a contour going from $-\infty$ to ∞ along the real axis and closed in the lower-half plane by a half circle is equal to _____.(up to two decimal places). [Gate 2017]
- 3) The compton wavelength of a proton is _____ fm .(up to two decimal places).
 $(m_p = 1.67 \times 10^{-27} kg, h = 6.626 \times 10^{-34} Js, e = 1.602 \times 10^{-19} C, c = 3 \times 10^8 ms^{-1})$
 [Gate 2017]
- 4) Which one of the following conservation laws is violated in the decay $\tau^+ \rightarrow \mu^+ \mu^+ \mu^-$
 - a) Angular momentum
 - b) Total Lepton number
 - c) Electric charge
 - d) Tau number
- 5) Electromagnetic interactions are: [Gate 2017]
 - a) C non-conserving but CP conserving
 - b) C conserving
 - c) CP non-conserving but CPT conserving
 - d) CPT non-conserving
- 6) A one dimensional simple harmonic oscillator with Hamiltonian $H_0 = \frac{p^2}{2m} + \frac{1}{2}kx^2$ is unjeected to a small perturbation. $H_1 = \alpha x + \beta x^2 + \gamma x^4$. The first order correction to the ground state energy is dependent on [Gate 2017]
 - a) only β
 - b) α and γ
 - c) α and β
 - d) only γ
- 7) For the Hamiltonian $H = a_0 I + \vec{b} \cdot \vec{\sigma}$ where $a_0 \in \mathbb{R}$, \vec{b} is a real vector, I is the 2×2 identity matrix, and $\vec{\sigma}$ are the Pauli matrices, the ground state energy is [Gate 2017]
 - a) $|b|$
 - b) $2a_0 - |b|$
 - c) $a_0 - |b|$
 - d) a_0
- 8) The cofficient of e^{ikx} in the Fourier expansion of $u(x) = A \sin^2(\alpha x)$ for $k = -2\alpha$ is [Gate 2017]
 - a) $A/4$
 - b) $-A/4$
 - c) $A/2$
 - d) $-A/2$
- 9) The degeneracy of the third energy level of a 3-dimensional isotropic quantum harmonic oscillator is [Gate 2017]

a) 6

b) 12

c) 8

d) 10

10) The electronic ground state energy of the Hydrogen atom is -13.6eV . The highest possible electronic energy eigenstate has an energy equal to [Gate 2017]

a) 0

b) 1eV c) $+13.6\text{eV}$

d) inf

11) A reversible Carnot engine is operated between temperatures T_1 and T_2 ($T_2 > T_1$) with a photon gas as the working substance. The efficiency of the engine is [Gate 2017]

a) $1 - \frac{3T_1}{4T_2}$ b) $1 - \frac{T_1}{T_2}$ c) $1 - \left(\frac{T_1}{T_2}\right)^{\frac{3}{4}}$ d) $1 - \left(\frac{T_1}{T_2}\right)^{\frac{4}{3}}$

12) In the nuclear reaction $^{13}\text{C}_6 + \nu_e \rightarrow ^{13}\text{N}_7 + X$, the particle X is [Gate 2017]

a) an electron

b) an anti-electron

c) a muon

d) a pion

13) Three charges ($2C, -1C, -1C$) are placed at the vertices of an equilateral triangle of side 1m as shown in the figure. The component of the electric dipole moment about the marked origin along the \hat{y} direction is _____ Cm . [Gate 2017]

