

Dr. D. Y. Patil Arts, Commerce & Science College

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Practical - 1

Q.1) Find the data type of the following.

1) >>> A=36

>>> type(A)

O/P:

>>> <class 'int'>

2) >>> A=3+2j

>>> type(A)

O/P:

>>> <class 'complex'>

3) >>> A=3.14

>>> type(A)

O/P:

>>> <class 'float'>

4) >>> A='python'

>>> type(A)

O/P:

>>> <class 'str'>

5) >>> A=[1,2,3,4,5]

>>> type(A)

O/P:

>>> <class 'list'>

Q.2) Print the following string using print statement.

1) >>> A='Hello world !'

>>> print(A)

O/P:

>>> Hello world !

2) >>> B='Mathematics'

>>> Print(B)

O/P:

```
>>> Mathematics
```

Q.3) Evaluate the following expression.

1)

```
>>> A=10%2+7-(3+7)*10/2
```

```
>>> print(A)
```

O/P:

```
>>> -43.0
```

2)

```
>>> B=3*10//3+10%3
```

```
>>> print(B)
```

O/P:

```
>>> 11
```

Q.4) Compare the following expression.

1)

```
>>> A=21
```

```
>>> B=15
```

```
>>> print(A=B)
```

O/P:

```
>>> False
```

2)

```
>>> A=4
```

```
>>> B=5
```

```
>>> print(A!=B)
```

O/P:

```
>>> True
```

3)

```
>>> A=10
```

```
>>> B=15
```

```
>>> print(A<=B)
```

O/P:

```
>>> True
```

4)

```
>>> A=4
```

```
>>> B=8
```

```
>>> print(A<B)
```

O/P:

```
>>> True
```

Q.5) Print the following terms by importing math and c math module.

1) $\log(10)$ with base 10

I/P:

```
>>> import math
>>> print(math.log10(10))
```

O/P:

```
>>> 1.0
```

2) sin(30)

I/P:

```
>>> Import math
>>> print(math.sin(30))
```

O/P:

```
>>> -0.9880316240928618
```

3) Value of pi

I/P:

```
>>> import math
>>> print(math.pi)
```

O/P:

```
>>> 3.141592653589793
```

4) tan(45)

I/P:

```
>>> import math
>>> print(math.tan(45))
```

O/P:

```
>>> 1.6197751905438615
```

5) 3+5j

I/P:

```
>>> a = 3+5j
>>> print(a)
```

O/P:

```
>>> (3+5j)
```

Q.6) Accept the different value by using input() statement and print it from the following code.

1) >>> A=input("A:")

```
>>> A:30
```

```
>>> print(A)
```

```
>>> 30
```

```
2) >>> Name = input ("Enter the Name: ")
>>> Akash
>>> Age = int(input("Age: "))
>>> 20
>>> City = input("City Name: ")
>>> Pune
```

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Practical - 2

Q.1) Define string `x = "Math is Easy"` & `y = "To All"`

- a) Find length of `x` and `y` .
- b) Pick character with index 3 and -1 in `x` and 2 & 4 in `y` .
- c) Using operator `+` & `*` find `2x+y` , `3*x` .

Ans:

```
a) >>> x = "Math is Easy"
>>> y = "To All"
>>> len(x)
>>> 12
>>> len(y)
>>> 6
```

```
b) >>> x = "Math is Easy"
>>> y = "To All"
>>> x[3]
>>> 'h'
>>> x[-1]
>>> 'y'
>>> y[2]
>>> ' '
>>> y[4]
>>> 'l'
```

```
c) >>> 2*x + y
>>> 'Math is EasyMath is EasyTo All'
>>> 3*x
>>> 'Math is EasyMath is EasyMath is Easy'
```

Q.2) Write a python program of concatenation and repetition of string and list.

Ans:

```
# concatenation of string :-
>>> x = "hello "
>>> y = "I am in sybsc(cs)"
>>> x + y
```

```

>>> 'hello I am in sybsc(cs)'

# repetition of string :-
>>> x = "hello "
>>> y = "I am in sybsc(cs)"
>>> x*2
>>> 'hellohello'
>>> y*2
>>> 'I am in sybsc(cs)I am in sybsc(cs)'

# concatenation of list :-
>>> L1 = ['mango','apple','banana',45,78,'kiwi']
>>> L2 = ['bottle','book',66,90,'pen']
>>> L1 + L2
>>> ['mango', 'apple', 'banana', 45, 78, 'kiwi', 'bottle', 'book',
    66, 90, 'pen']

# repetition of list :-
>>> L1 = ['mango','apple','banana',45,78,'kiwi']
>>> L2 = ['bottle','book',66,90,'pen']
>>> L1 * 2
>>> ['mango', 'apple', 'banana', 45, 78, 'kiwi', 'mango', 'apple',
    'banana', 45, 78, 'kiwi']
>>> L2 * 2
>>> ['bottle', 'book', 66, 90, 'pen', 'bottle', 'book', 66, 90,
    'pen']

```

Q.3) write a python program to create a nested list & diaplay its element.

Ans:

```

>>> L = ['a', 'b', ['cc', 'dd', ['eee', 'fff']], 'g', 'h']
>>> print(L)
>>> ['a', 'b', ['cc', 'dd', ['eee', 'fff']], 'g', 'h']
>>> Print(L[2])
>>> ['cc','dd',['eee','fff']]

```

Q.4) Write a python program to create list using range function.

Ans:

```

>>> My_list = [*range(10, 20, 1)]
>>> print(My_list)
>>> [10, 11, 12, 13, 14, 15, 16, 17, 18, 19]

```

Q.5) Write a python program using membership operator ('not in' and 'is' operator) for list.

Use: x=[1,2,3,'Rose','Pink','math','easy']

Ans:

```
# 'in' operator:
```

```
L1=[1,2,3,'Rose','Pink','math','easy']
```

```
L2=[2,3,4,'red']
```

```
if L1 in L2:
```

```
    print("True")
```

```
else:
```

```
    print("False")
```

OUTPUT-

```
>>> False
```

```
# 'not in' operator:
```

```
L1=[1,2,3,'Rose','Pink','math','easy']
```

```
L2=[2,3,4,'red']
```

```
if L1 not in L2:
```

```
    print("True")
```

```
else:
```

```
    print("False")
```

OUTPUT-

```
>>> True
```

Q.6) Define tuple with single element & verify its type.

Ans:

```
>>> tuple1 = (5) type(tuple1)
```

```
>>> <class 'int'>
```

Q.7) Write a python program to write a function that return area and circumference of Circle.

Ans:

```
from math import *
```

```
def f(r):
```

```
    c = 2 * pi * r
```

```
    a = pi * r * r
```

```
    return c, a,
```

```
print(f(5))
```


OUTPUT-

(31.41592653589793, 78.53981633974483)

Q.8) Construct a valid list in python to convert it into a string.

Ans:

```
>>> mylist = ['I', 'me', 'you', 'they']
>>> mystr = ','.join(mylist)
>>> print(mystr)
O/P
>>> I,me,you,they
>>> type(mystr)
O/P
>>> <class 'str'>
>>> type(mylist)
O/P
>>> <class 'list'>
```

Q.9) Write a python program using range() function to display all prime Numbers between 1 to 100.

Program:

```
Lower = 2
Upper = 100
print("Prime numbers between", Lower, "to", Upper, "are :")
for n in range(Lower, Upper + 1):
    for i in range(2, n):
        if n % i == 0:
            break
    else:
        print(n)
```

OUTPUT:

Prime numbers between 2 to 100 are :

2
3
5
7
11
13
17
19
23

29
31
37
41
43
47
53
59
61
67
71
73
79
83
89
97

Q.10) Write a string traversal program with while loop.

Program:

```
Z = "Black Bear"
Index = 0
while index < len(Z):
    Letter = Z[index]
    print(Letter)
    Index = Index + 1
```

OUTPUT:

B
l
a
c
k

B
e
a
r

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Practical - 3

Q.1) Find the range of the following function

- a) range(10)
- b) range(1,5)
- c) range(1, 10, 2)
- d) range(5,2)
- e) range(10, -10, -2)

Ans:

a)

```
L1 = range(10)
for i in L1:
    print(i, end=' ')
print()
```

OUTPUT-

0 1 2 3 4 5 6 7 8 9

b)

```
L1 = range(1, 5)
for i in L1:
    print(i, end=' ')
print()
```

OUTPUT-

1 2 3 4

c)

```
L1 = range(1, 10, 2)
for i in L1:
    print(i, end=' ')
print()
```

OUTPUT-

1 3 5 7 9

d)

```
L1 = range(2, 20)
for i in L1:
    print(i, end=' ')
print()
```

OUTPUT-

2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19

e)

```
L1 = range(-10, 10, 2)
for i in L1:
    print(i, end=' ')
print()
```

OUTPUT-

-10 -8 -6 -4 -2 0 2 4 6 8

Q.2) Write a python program to find gcd of two numbers using for loop.

Ans:

```
import math
def phi(n):
    for x in range(1, n):
        if math.gcd(n,x)==1:
            print(x, end=' ')
phi(10)
```

OUTPUT-

1 3 7 9

Q.3) Write a python program to find table of 22 using for loop.

Ans:

```
def table(n):
    for i in range(1,11):
        print (n*i, end= ' ')
table(22)
```

OUTPUT-

22 44 66 88 110 132 154 176 198 220

Q.4) Write a python program to find table of 19 using while loop.

Ans:

```
i=1
n=int(input("Table of "))
while i<=10:
    print(n*i)
    i=i+1
Table of 19
```

OUTPUT-

```
19
38
57
76
95
114
133
152
171
190
```

Q.5) Write a python program to find first 10 terms of Fibonacci sequence using for loop.

Ans:

```
a = 0
b = 1
for i in range(10):
    a, b=b, a+b
    print(a, end= ' ')
```

OUTPUT-

```
1 1 2 3 5 8 13 21 34 55
```

Q.6) Write a python program to check the student is pass, fail or distinction.

Ans:

```
ame = input("Name of the student : ")
Marks = int(input('Marks = '))
if Marks > 39:
```

```
if Marks > 75:
    print("first class with distinction")
elif Marks < 76 and Marks > 59:
    print("first class")
else:
    print("Second class")
else:
    print("fail")
```

OUTPUT-

Name of the student : Nisha

Marks = 71

first class

Name of Student:

Roll No.:

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Practical - 4

Q.1) Write a program to find divisors of any number using input function.

1) Write a python programme to find divisors of any number using input function.

Ans-

```
n = int(input("Divisor of : "))
for i in range(1,n+1):
    if n%i == 0:
        print(i)
```

OUTPUT-

```
>>> Divisor of :10
1
2
5
10
```

Q.2) Write a python program to print the absolute value of given number.

Ans-

```
n = float(input("Enter the value:"))
absolute = abs(int(n))
print("\n The absolute value of the number is:->",absolute)
```

OUTPUT-

```
>>> Enter the value: 5.23
The absolute value of the number is:-> 5
```

Q.3) Write a python program to print the table of given number.

Ans-

```
i = 1
n = int(input("Table of :"))
while i<=10:
    print(n*i) i=i+1
```

OUTPUT-

Table of : 5

5
10
15
20
25
30
35
40
45
50

Q.4) Define a function that print all integers between 1 to n that are relatively prime.

Ans-

```
import math
def phi(n):
    for x in range (1,n):
        if math.gcd(n,x)==1:
            print(x)
```

OUTPUT-

```
phi(10)
1
3
7
9
```

Q.5) Define Euler's phi function in python.

Ans-

```
Import math
def phi(n):
    i =0:
    for i in range(1,n):
        if math.gcd(n,i) == 1:
            i = i+1
            print(I, end=' ')
```

OUTPUT-

```
phi(10)
2 4 8 10
```


Q.6) Write a program to check the person is eligible for voting or not and senior citizen or not.

Ans-

```
a = int(input("Enter your age :"))
if a>=60:
    print("You are eligible for voting and you are senior
          citizen ")
elif 18<=a<60:
    print("You are eligible for voting and you are not senior
          citizen")
else:
    print("You are not eligible for voting")
```

OUTPUT-

```
Enter your age :5
You are not eligible for voting
```

```
Enter your age : 55
You are eligible for voting and you are not senior citizen
```

```
Enter your age : 70
You are eligible for Voting and you are senior citizen
```

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Practical – 5

Q.1) For vectors $U = \begin{bmatrix} 5 \\ 6 \\ 0 \end{bmatrix}$ & $V = \begin{bmatrix} 1 \\ 0 \\ -2 \end{bmatrix}$

Find a) $U+V$ b) $3V$ c) $2U + 3V$ Ans:

```
from sympy import *
U = Matrix([[2],[5],[-3]])
V = Matrix([[1],[0],[-2]])
```

```
a) >>> U + V
      Matrix([
[ 3],
[ 5],
[-5]])
```

```
b) >>> 3 * V
      Matrix([
[ 3],
[ 0],
[-6]])
```

```
c) >>> 2*U+3*V
      Matrix([
[ 7],
[ 10],
[-12]])
```

Q.2) Construct the following matrices using python

- Identity matrix of order 6
- Zero matrix with order 5x6
- ones matrix of order 5x4
- Diagonal matrix with (4,-5,1) as a diagonal element.

Ans:

```
a) from sympy import *
    eye(6)
```

```
Matrix([
[1, 0, 0, 0, 0, 0],
[0, 1, 0, 0, 0, 0],
[0, 0, 1, 0, 0, 0],
[0, 0, 0, 1, 0, 0],
[0, 0, 0, 0, 1, 0],
[0, 0, 0, 0, 0, 1]])
```

b) >>> zeros(5,6)

```
Matrix([
[0, 0, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 0]])
```

c) >>> ones(5,4)

```
Matrix([
[1, 1, 1, 1],
[1, 1, 1, 1],
[1, 1, 1, 1],
[1, 1, 1, 1],
[1, 1, 1, 1]])
```

d) >>> diag(4,-5,1)

```
Matrix([
[4, 0, 0],
[0, -5, 0],
[0, 0, 1]])
```

Q.3) For the following matrices

$$A = \begin{bmatrix} 4 & 2 & 4 \\ 4 & -1 & 1 \\ 2 & 4 & 2 \end{bmatrix} \quad \& \quad B = \begin{bmatrix} 5 & 2 & 3 \\ 3 & -7 & 5 \\ 3 & 1 & -1 \end{bmatrix}$$

Find a) A+B b) A-B c) A⁻¹ d) B*A e) B⁻¹AB
f) A⁴

Ans:

```
from sympy import *
A = Matrix([[4,2,4],[4,-1,1],[2,4,2]])
```

```
B = Matrix([[5,2,3],[3,-7,5],[3,1,-1]])
```

a) >>> A + B

```
Matrix([
  [9, 4, 7],
  [7, -8, 6],
  [5, 5, 1]])
```

b) >>> A - B

```
Matrix([
  [-1, 0, 1],
  [ 1, 6, -4],
  [-1, 3, 3]])
```

c) >>> A.inv()

```
Matrix([
  [-1/6, 1/3, 1/6],
  [-1/6, 0, 1/3],
  [ 1/2, -1/3, -1/3]])
```

d) >>> B * A

```
Matrix([
  [34, 20, 28],
  [-6, 33, 15],
  [14, 1, 11]])
```

e) >>> B.inv()*A*B

```
Matrix([
  [ 522/59, -303/59, 405/59],
  [-22/59, 46/59, -72/59],
  [-108/59, 435/59, -273/59]])
```

f) >>> A**4

```
Matrix([
  [2060, 1198, 1622],
  [1106, 613, 857],
  [1456, 848, 1120]])
```

Q.4) For matrix $A = \begin{bmatrix} -5 & 2 & 3 \\ 3 & -7 & 5 \\ -3 & 10 & -11 \end{bmatrix}$. Do the following with sequence,

- a) Delete 2nd column
- b) Add row [2,3,0] in first row
- c) Delete last row

Ans:

```
from sympy import*
A = Matrix([[ -5,2,3],[3,-7,5],[-3,10,-11]])
>>> A
Matrix([
  [-5,  2,  3],
  [ 3, -7,  5],
  [-3, 10, -11]])
```

- a) >>> A.col_del(1) A

```
Matrix([
  [-5,  3],
  [ 3,  5],
  [-3, -11]])
```

- b) >>> A.row_insert(0, Matrix([[2, 3, 0]]))

```
Matrix([
  [ 2,  3,  0],
  [-5,  2,  3],
  [ 3, -7,  5],
  [-3, 10, 11]])
```

- c) >>> A.row_del(2) A

```
Matrix([
  [-5,  2,  3],
  [ 3, -7,  5]])
```

Q.5) Using Python apply the following operations on

$$A = \begin{bmatrix} 1 & 7 & 1 \\ 4 & -2 & 1 \\ 3 & 1 & 2 \end{bmatrix}$$

- a) Delete 3rd row
- b) Delete 1st column
- c) Delete the last column

Ans:

```
from sympy import*
A = Matrix([[1,7,1],[4,-2,1],[3,1,2]])
>>> A
```

```
Matrix([
  [1, 7, 1],
  [4, -2, 1],
  [3, 1, 2]])
```

a) >>> A.row_del(2) A

```
Matrix([
  [1, 7, 1],
  [4, -2, 1]])
```

b) >>> A.col_del(0) A

```
Matrix([
  [ 7, 1],
  [-2, 1]])
```

c) >>> A.col_del(1) A

```
Matrix([
  [ 7],
  [-2]])
```

Q. 6) For matrix $A = \begin{bmatrix} 1 & 0 & 4 \\ 2 & 1 & -1 \\ 3 & 4 & 2 \end{bmatrix}$ insert $A = \begin{bmatrix} 5 \\ 3 \\ 0 \end{bmatrix}$ as a 3rd column.

Ans:

```
from sympy import*
A = Matrix([[1,0,4],[2,1,-1],[3,4,2]])
>>> A
Matrix([
  [1, 0, 4],
  [2, 1, -1],
  [3, 4, 2]])

>>> A.col_insert(2,Matrix([[5],[6],[0]]))
Matrix([
  [1, 0, 5, 4],
  [2, 1, 6, -1],
  [3, 4, 0, 2]])
```

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Practical – 6

Q.1) For matrix

```
D = [10, 2, 3]
     [12, -7, 15]
     [-15, 10, -11]
```

- a) Find its transpose
- b) Find its determinant
- c) Find inverse if it exist.

Ans-

```
from sympy import *
D = Matrix([[10, 2, 3], [12, -7, 15], [-15, 10, -11]])
>>> D
Matrix([
  [ 10, 2, 3],
  [ 12, -7, 15],
  [-15, 10, -11]])
a) >>> D.T                      # Transpose of matrix D
Matrix([
  [10, 12, -15],
  [ 2, -7, 10],
  [ 3, 15, -11]])
b) >>> D.det()                  # determinant of matrix D
-871
c) >>> D.inv()                  # inverse of matrix D
Matrix([
  [ 73/871, -4/67, -51/871],
  [93/871, 5/67, 114/871],
  [-15/871, 10/67, 94/871]])
```

Q.2) For matrix

```
B=[1 -1 -2 4]
   [2 -1 -1 2]
   [2 1 4 16]
```

- a) Find reduce row echelon form
- b) Find column space
- c) Find null space

Ans-

```
from sympy import *
B = Matrix([[1,-1,-2,4],[2,-1,-1,2],[2,1,4,16]])
>>> B
Matrix([
[1, -1, -2, 4],
[2, -1, -1, 2],
[2, 1, 4, 16]])
```

a) >>> B.rref() # reduced row echelon form of matrix B
(Matrix([
[1, 0, 0, 24],
[0, 1, 0, 72],
[0, 0, 1, -26]]), (0, 1, 2))

b) >>> B.columnspace() # column space of matrix B
[Matrix([
[1],
[2],
[2]])], Matrix([
[-1],
[-1],
[1]])], Matrix([
[-2],
[-1],
[4]])]

c) >>> B.nullspace() # nullspace of matrix B
[Matrix([
[-24],
[-72],
[26],
[1]])]

Q.3) For matrix
A = [-5, 2, 3]
[-3, 10, -11]
[3, -7, 5]
find rank of A.

Ans-

```
from sympy import *
```



```

A = Matrix([[ -5, 2, 3], [ 3, -7, 5], [-3, 10, -11]])
>>> A
Matrix([
  [-5, 2, 3],
  [ 3, -7, 5],
  [-3, 10, -11]])
>>> A.rank()           # rank of matrix A
3

```

Q.4) Find rank of matrix

```

M = [2 0 3]
    [0 1 2]
    [3 0 4]

```

Ans-

```

from sympy import *
M = Matrix([[2,0,3],[0,1,2],[3,0,4]])
>>> M
Matrix([
  [2, 0, 3],
  [0, 1, 2],
  [3, 0, 4]])
>>> M.rank()           # rank of matrix M
3

```

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Practical – 7

Q.1) Find the solution of $AX = b$ by Gauss elimination method where

$$A = \begin{pmatrix} 3 & 2 & -1 \\ 2 & -2 & 4 \\ 2 & -1 & 2 \end{pmatrix} \quad \text{and} \quad b = \begin{pmatrix} 3 \\ 6 \\ 9 \end{pmatrix}$$

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[3, 2, -1], [2, -2, 4], [2, -1, 2]])
B = Matrix([[3], [6], [9]])
print(linsolve((A, b), [x, y, z]))
```

OUTPUT:

{(6, -11, -7)}

Q.2) Find the solution of $AX=b$ by Gauss Jordan method where

$$A = \begin{pmatrix} 7 & 6 & -8 \\ 7 & -2 & 2 \\ 6 & -1 & 2 \end{pmatrix} \quad \text{and} \quad b = \begin{pmatrix} 3 \\ 0 \\ 9 \end{pmatrix}$$

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[7, 6, -8], [7, -2, 2], [6, -1, 2]])
B = Matrix([[3], [0], [9]])
sol,param = A.gauss_jordan_solve(b)
```

OUTPUT:

Matrix([
[7/11],
[106/11],
[163/22]])

Q.3) Find the solution of system $AX=b$ where $A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$ and $b = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
B = Matrix([[1], [2], [3]])
print(linsolve((A, b), [x, y, z]))
```

OUTPUT:

$$\{(z - 1/3, 2/3 - 2z, z)\}$$

Q.4) Find the solution by Gauss elimination method and Gauss Jordan method where $A = \begin{pmatrix} 2 & 1 \\ 1 & 2 \end{pmatrix}$ and $b = \begin{pmatrix} 5 \\ 7 \end{pmatrix}$

1) by Gauss elimination method

Program:

```
from sympy import *
x, y = symbols("x, y")
A = Matrix([[2, 1], [1, 2]])
B = Matrix([[5], [7]])
print(linsolve((A, b), [x, y]))
```

OUTPUT:

$\{(1, 3)\}$

2) Gauss Jordan method

Program:

```
from sympy import *
x, y = symbols("x, y")
A = Matrix([[2, 1], [1, 2]])
b = Matrix([[5], [7]])
sol,param=A.gauss_jordan_solve(b)
```

OUTPUT:

```
Matrix([
[1],
[3]])
```

Q.5) Using linsolve command find the solution of

$$5x - 2y + 3z = 2$$

$$x + y + z = 1$$

$$x + 2y - 2z = -10$$

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[5, -2, 3], [1, 1, 1], [1, 2, -2]])
b = Matrix([[2], [1], [-10]])
print(linsolve((A, b), [x, y, z]))
```

OUTPUT:

$\{(-44/23, -13/23, 80/23)\}$

Q.6) Find LU factorization of $A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$

Program:

```
from sympy import *
A = Matrix([[1,2,3],[4,5,6],[7,8,9]])
L,U,_=A.LUdecomposition()
```

OUTPUT:

```
>>> L
Matrix([
[1, 0, 0],
[4, 1, 0],
[7, 2, 1]])
>>> U
Matrix([
[1, 2, 3],
[0, -3, -6],
[0, 0, 0]])
```

Q.7) Use LU factorization to solve the system

$$2x + 2y + z = 6$$

$$2x + y + 2z = 8$$

$$x + 2y + 2z = 7$$

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
AB = Matrix([[2, 2, 1, 6], [2, 1, 2, 8], [1, 2, 2, 7]])
print(solve_linear_system_LU(AB, [x, y, z]))
```

OUTPUT:

```
{x: 7/5, y: 2/5, z: 12/5}
```

Q.8) Solve the system by using Gauss elimination method, Gauss Jordan method and LU decomposition method.

$$a) \begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 4 \\ 2 & 5 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 6 \\ 7 \\ 8 \end{pmatrix}$$

1) By Gauss Elimination Method

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[1, 2, 3], [2, 1, 4], [2, 5, 1]])
b = Matrix([[6], [7], [8]])
print(linsolve((A, b), [x, y, z]))
```

OUTPUT:

{(1, 1, 1)}

2) By Gauss Jordan Method

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[1, 2, 3], [2, 1, 4], [2, 5, 1]])
b = Matrix([[6], [7], [8]])
sol,param=A.gauss_jordan_solve(b)
```

OUTPUT:

```
Matrix([
[1],
[1],
[1]])
```

3) By LU Decomposition

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
AB = Matrix([[1, 2, 3, 6], [2, 1, 4, 7], [2, 5, 1, 8]])
print(solve_linear_system_LU(AB, [x, y, z]))
```

OUTPUT:

{x: 1, y: 1, z: 1}

Q.8 b) $-x + 2y + 2z = -1$

$$x + y + 2z = 2$$

$$5x + 2z = 8$$

1) By Gauss Elimination Method

Program:

```
from sympy import *
x, y, z = symbols("x, y, z")
A = Matrix([[-1, 2, 2], [1, 1, 2], [5, 0, 2]])
b = Matrix([[-1], [2], [8]])
print(linsolve((A, b), [x, y, z]))
```

OUTPUT:

{(3/2, 0, 1/4)}

2) By Gauss Jordan Method

```
from sympy import *
x, y, z = symbols("x, y, z")
```

```
A = Matrix([[-1, 2, 2], [1, 1, 2], [5, 0, 2]])
b = Matrix([[-1], [2], [8]])
sol,param=A.gauss_jordan_solve(b)
```

OUTPUT:

```
Matrix([
  3/2],
 [ 0],
 [1/4]])
```

3) By LU Decomposition

```
from sympy import *
x, y, z = symbols("x, y, z")
AB = Matrix([[-1, 2, 2, -1], [1, 1, 2, 2], [5, 0, 2, 8]])
print(solve_linear_system_LU(AB, [x, y, z]))
```

OUTPUT:

```
{x: 3/2, y: 0, z: 1/4}
```

Name of Student:

Roll No.:

Batch:

Practical – 8

Q.1) Using Sympy module of python, find the eigen values and the

corresponding eigen vectors of the matrix $A = \begin{bmatrix} 4 & 2 & 2 \\ 2 & 4 & 2 \\ 2 & 2 & 4 \end{bmatrix}$.

```

Ans- from sympy import *
A = Matrix([[4,2,2],[2,4,2],[2,2,4]])
>>> A.eigenvals()
O/P:
{8: 1, 2: 2}
>>> A.eigenvects()
O/p:
[(2, 2, [Matrix([
[-1],
[ 1],
[ 0]])], Matrix([
[-1],
[ 0],
[ 1]])]), (8, 1, [Matrix([
[1],
[1],
[1]])])]

```

Q.2) Using Sympy module of python, find the eigen values and the

corresponding eigen vectors of the matrix $A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$.

```

Ans- from sympy import *
A = Matrix([[1,1,1],[1,1,1],[1,1,1]])
>>> A.eigenvals()
{3: 1, 0: 2}
>>> A.eigenvects()
[(0, 2, [Matrix([
[-1],
[ 1],
[ 0]])], Matrix([
[-1],

```

```
[ 0],
[ 1]]]]), (3, 1, [Matrix([
[1],
[1],
[1]]]))]
```

Q.3) Using python find the eigen values of the following matrix:

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}.$$

Ans-

```
from sympy import *
A = Matrix([[1,1,1],[0,1,1],[0,0,1]])
>>> A.eigenvals()
{1: 3}
```

Q.4) Using python find the eigen vectors of the following matrix:

$$A = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 2 & 1 \\ 0 & 0 & 2 \end{bmatrix}.$$

Ans-

```
from sympy import *
A = Matrix([[2,1,1],[0,2,1],[0,0,2]])
>>> A.eigenvects()
[(2, 3, [Matrix([
[1],
[0],
[0]]]))]
```

Q.5) Using Sympy module of python, find the eigen values and the corresponding eigen vectors of the matrix $A = \begin{bmatrix} 3 & -2 \\ 6 & -4 \end{bmatrix}.$

Ans-

```
from sympy import *
A = Matrix([[3,-2],[6,-4]])
>>> A.eigenvals()
{-1: 1, 0: 1}
>>> A.eigenvects()
[(-1, 1, [Matrix([
[1/2],
[ 1]]])), (0, 1, [Matrix([
[2/3],
[ 1]]]))]
```


Name of Student:

Roll No.:

Batch:

Practical – 9

Q.1) Write a python program to diagonalizes the matrix $\begin{bmatrix} 3 & -2 \\ 6 & -4 \end{bmatrix}$ and find matrix P and D.

Program:

```
>>> from sympy import *
>>> A = Matrix([[3,-2],[6,-4]])
>>> P, D = A.diagonalize()
>>> P
```

OUTPUT:

```
Matrix([
[1, 2],
[2, 3]])
```

```
>>> D
```

OUTPUT:

```
Matrix([
[-1, 0],
[ 0, 0]])
```

Q.2) Using python program check whether the matrix $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 3 \end{bmatrix}$ is diagonalizable or not.

Program:

```
>>> from sympy import *
>>> A = Matrix([[0,1,0],[0,0,1],[0,0,3]])
>>> A.is_diagonalizable()
```

OUTPUT:

```
False
```

Q.3) Find the eigenvalues of the following matrix and hence check whether it is diagonalizable or not.

Program:

```
>>> from sympy import *
>>> A = Matrix([[1,2,2],[2,1,2],[2,2,1]])
>>> A.eigenvals()
```

OUTPUT:

```
{5: 1, -1: 2}
```

```
>>> A.is_diagonalizable()
```

OUTPUT:

True

Q.4) Using python program check whether the matrix $A = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ is diagonalizable or not.

Program:

```
>>> from sympy import *
>>> A = Matrix([[0,1,0],[0,0,1],[0,0,3]])
>>> A.is_diagonalizable()
```

OUTPUT:

True

Q.5) Write a python program to diagonalize the matrix $\begin{bmatrix} 1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$ and find matrix P and D.

Program:

```
>>> from sympy import *
>>> A = Matrix([[1,-1,1],[-1,1,-1],[1,-1,1]])
>>> P, D = A.diagonalize()
```

```
>>> P
```

OUTPUT:

```
Matrix([
[1, -1, 1],
[1, 0, -1],
[0, 1, 1]])
```

```
>>> D
```

OUTPUT:

```
Matrix([
[0, 0, 0],
[0, 0, 0],
[0, 0, 3]])
```

Name of Student:

Roll No.:

Batch:

Practical – 10

Q.1) Write a python program to find the correct root of the equation $x^3 - 4x^2 - 11x + 30$ using Newton Raphson method correct upto 4 decimal places. Take $x_0 = 10$.

Program:

```
def nr(f, g, x0, e):
    step = 1
    condition = True
    while condition:
        if g(x0) == 0.0:
            print("Divided by zero error.")
            break
        x1 = x0 - (f(x0)/g(x0))
        print('Iteration = ', step, 'x1 =', x1, 'and f(x1)=', f(x1))
        x0 = x1
        step = step + 1
        condition = abs(f(x1)) > e
    print('Required root is :', x1)

from math import *
deff(x):
    return x**3 - 4*x**2 - 11*x + 30
defg(x):
    return 3*x**2 - 8*x - 11
nr(f, g, 10, 0.00001)
```

OUTPUT:

```
Iteration = 1 x1= 7.511961722488039 and f(x1)= 145.54690711661283
Iteration = 2 x1= 6.029708528510192 and f(x1)= 37.46810047097503
Iteration = 3 x1= 5.2778576911468225 and f(x1)= 7.539290423642491
Iteration = 4 x1= 5.029400988117186 and f(x1)= 0.7151577286837636
Iteration = 5 x1= 5.000387815638643 and f(x1)= 0.009309229796429008
Iteration = 6 x1= 5.0000000689141375 and f(x1)= 1.653939342816102e-06
Required root is : 5.0000000689141375
```

Q.2) Using python programming find the correct root of the function $x^3 + 2x$, in $[-10, 10]$ using Newton Raphson method correct upto 4 decimal places. Take

$$x_0 = 3$$

Program:

```
def newtonraphson(f,g,x0,e):
    step = 1
    condition = True
    while condition:
        if g(x0) == 0.0:
            print('Divided by zero error!')
            break
        x1 = x0 - (f(x0)/g(x0))
        print('Iteration =',step,'x1=',x1,'and f(x1)=',f(x1))
        x0 = x1
        step = step + 1
        condition = abs(f(x1))> e
    print('Required root is :',x1)
from math import*
def f(x):
    return x**3+2*x
def g(x):
    return 3*x**2+2
newtonraphson(f,g,3,0.00001)
```

OUTPUT:

```
Iteration = 1 x1= 1.35 and f(x1)= 5.160375
Iteration = 2 x1= 0.839071782178218 and f(x1)= 2.2688848832741244
Iteration = 3 x1= 0.5165318379707146 and f(x1)= 1.1708770250983709
Iteration = 4 x1= 0.286911684752419 and f(x1)= 0.5974414559037061
Iteration = 5 x1= 0.12637258636310406 and f(x1)= 0.25476334679541873
Iteration = 6 x1= 0.03400797677253169 and f(x1)= 0.06805528521500116
Iteration = 7 x1= 0.0031305686951099317 and f(x1)= 0.006261168071234248
Iteration = 8 x1= 2.911262335528837e-05 and f(x1)= 5.822524673525099e-05
Iteration = 9 x1= 2.5424001309411746e-09 and f(x1)= 5.084800261882349e-09
Required root is : 2.5424001309411746e-09
```

Q.3) Using python find the correct root of the function $e^x - \sin x$, in $[0, 1]$ using Newton Raphson method correct upto 3 decimal places. Take $x_0 = 0.4$.

Program:

```
def newtonraphson(f,g,x0,e):
    step = 1
    condition = True
    while condition:
```

```

    if g(x0) == 0.0:
        print('Divided by zero error!')
        break
    x1 = x0 - (f(x0)/g(x0))
    print('Iteration =',step,'x1=',x1,'and f(x1)=',f(x1))
    x0 = x1
    step = step + 1
    condition = abs(f(x1))> e
    print('Required root is :',x1)
from math import*
def f(x):
    return e**x-sin(x)
def g(x):
    return e**x-cos(x)
newtonraphson(f,g,0.4,0.0001)

```

OUTPUT:

```

Iteration = 1 x1= -1.5314584096802757 and f(x1)= 1.2154464636832412
Iteration = 2 x1= -8.402567407072686 and f(x1)= 0.8534871583517203
Iteration = 3 x1= -10.038523764622981 and f(x1)= -0.575889990450599
Iteration = 4 x1= -9.334105736641906 and f(x1)= 0.09063639101087893
Iteration = 5 x1= -9.425107915627608 and f(x1)= -0.0002492819574764926
Iteration = 6 x1= -9.42485865376524 and f(x1)= 1.017479777190057e-11
Required root is : -9.42485865376524

```

Q.4) Using python find the correct root of the function e^x , in $[-1, 1]$ using Regula Falsi method correct upto 4 decimal places.

Program:

```

def falseposition(f,x0,x1,e):
    if (f(x0)*f(x1))>0.0:
        print('given guess values do not break the root')
        print('try again with different guess values')
    else:
        step = 1
        condition = True
        while condition:
            x2 = ((x0*f(x1))-(x1*f(x0)))/(f(x1)-f(x0))
            print('Iteration =',step,'x2=',x2,'and f(x2)=',f(x2))
            if (f(x0)*f(x2))<0:
                x1=x2
            else:

```

```

        x0=x2
        step = step + 1
        condition = abs(f(x2))> e
        print('Required root is :',x2)
from math import *
def f(x):
    return e**x
falseposition(f,-1,1,0.00001)

```

OUTPUT:

```

given guess values do not break the root
try again with different guess values

```

Q.5) Write a python program to estimate a root of an equation $\sin x = 8x$ in $[-1, 2]$ using Regula Falsi method correct upto 4 decimal places.

Program:

```

def falseposition(f,x0,x1,e):
    if (f(x0)*f(x1))>0.0:
        print('given guess values do not break the root')
        print('try again with different guess values')
    else:
        step = 1
        condition = True
        while condition:
            x2 = ((x0*f(x1))-(x1*f(x0)))/(f(x1)-f(x0))
            print('Iteration =',step,'x2=',x2,'and f(x2)=',f(x2))
            if (f(x0)*f(x2))<0:
                x1=x2
            else:
                x0=x2
            step = step + 1
            condition = abs(f(x2))> e
        print('Required root is :',x2)
from math import *
def f(x):
    return sin(x)-8*x
falseposition(f,-1,2,0.00001)

```

OUTPUT:

```

Iteration = 1 x2= -0.03477174210342762 and f(x2)= 0.24340920123557913
Iteration = 2 x2= -0.002472371150056373 and f(x2)= 0.017306600569171028

```

Iteration = 3 $x_2 = -0.00017848920441100228$ and $f(x_2) = 0.001249424431824746$
 Iteration = 4 $x_2 = -1.289949985729723e-05$ and $f(x_2) = 9.029649900143835e-05$
 Iteration = 5 $x_2 = -9.323246172555106e-07$ and $f(x_2) = 6.526272320788709e-06$
 Required root is : $-9.323246172555106e-07$

Q.6) Write a python program to estimate a root of an equation $x^6 - x^4 - x^3 - 1 = 0$ in [1, 2] using Regula Falsi method correct upto 3 decimal places.

Program:

```
def falseposition(f,x0,x1,e):
    if (f(x0)*f(x1))>0.0:
        print('given guess values do not break the root')
        print('try again with different guess values')
    else:
        step = 1
        condition = True
        while condition:
            x2 = ((x0*f(x1))-(x1*f(x0)))/(f(x1)-f(x0))
            print('Iteration =',step,'x2=',x2,'and f(x2)=',f(x2))
            if (f(x0)*f(x2))<0:
                x1=x2
            else:
                x0=x2
            step = step + 1
            condition = abs(f(x2))> e
        print('Required root is :',x2)
from math import *
def f(x):
    return x**6-x**4-x**3-1
falseposition(f,1,2,0.0001)
```

OUTPUT:

Iteration = 1 $x_2 = 1.048780487804878$ and $f(x_2) = -2.0326812065849147$
 Iteration = 2 $x_2 = 1.095902098406956$ and $f(x_2) = -2.02625465045382$
 Iteration = 3 $x_2 = 1.1405547871102417$ and $f(x_2) = -1.9745687858492924$
 Iteration = 4 $x_2 = 1.181971542449124$ and $f(x_2) = -1.8763188793993664$
 Iteration = 5 $x_2 = 1.2195209666846365$ and $f(x_2) = -1.736023605208181$
 Iteration = 6 $x_2 = 1.2527821911560477$ and $f(x_2) = -1.563485345302133$
 Iteration = 7 $x_2 = 1.2815830716506917$ and $f(x_2) = -1.3718177813280636$
 Iteration = 8 $x_2 = 1.3059945837122684$ and $f(x_2) = -1.1747759787016694$
 Iteration = 9 $x_2 = 1.3262884340768828$ and $f(x_2) = -0.9843518672063674$
 Iteration = 10 $x_2 = 1.3428741534122222$ and $f(x_2) = -0.8093081791125121$
 Iteration = 11 $x_2 = 1.3562332733435944$ and $f(x_2) = -0.6547960779081032$

Iteration = 12 $x_2 = 1.3668634106635338$ and $f(x_2) = -0.522787126619709$
 Iteration = 13 $x_2 = 1.3752382162468697$ and $f(x_2) = -0.4129045722984195$
 Iteration = 14 $x_2 = 1.3817834582154178$ and $f(x_2) = -0.32330643530603$
 Iteration = 15 $x_2 = 1.386866280706462$ and $f(x_2) = -0.25142151639549626$
 Iteration = 16 $x_2 = 1.3907936546333808$ and $f(x_2) = -0.1944716142576226$
 Iteration = 17 $x_2 = 1.3938163600436084$ and $f(x_2) = -0.14979341446752636$
 Iteration = 18 $x_2 = 1.3961357162726984$ and $f(x_2) = -0.11500652946132384$
 Iteration = 19 $x_2 = 1.397911207105988$ and $f(x_2) = -0.08807814104978506$
 Iteration = 20 $x_2 = 1.399267908794765$ and $f(x_2) = -0.06732573266722808$
 Iteration = 21 $x_2 = 1.4003031659417187$ and $f(x_2) = -0.05138733928068495$
 Iteration = 22 $x_2 = 1.4010923011498884$ and $f(x_2) = -0.039178108576233495$
 Iteration = 23 $x_2 = 1.4016933402083296$ and $f(x_2) = -0.029844100245050686$
 Iteration = 24 $x_2 = 1.4021508343219684$ and $f(x_2) = -0.022719021894551883$
 Iteration = 25 $x_2 = 1.402498902027785$ and $f(x_2) = -0.017286397718459412$
 Iteration = 26 $x_2 = 1.4027636216577326$ and $f(x_2) = -0.013147849509306475$
 Iteration = 27 $x_2 = 1.4029648967266968$ and $f(x_2) = -0.009997229582844547$
 Iteration = 28 $x_2 = 1.4031179010184252$ and $f(x_2) = -0.007599925145015174$
 Iteration = 29 $x_2 = 1.403234192697005$ and $f(x_2) = -0.005776522969814568$
 Iteration = 30 $x_2 = 1.4033225701554424$ and $f(x_2) = -0.004390041336661543$
 Iteration = 31 $x_2 = 1.4033897276876817$ and $f(x_2) = -0.0033360215325179965$
 Iteration = 32 $x_2 = 1.4034407567769334$ and $f(x_2) = -0.0025348791569839157$
 Iteration = 33 $x_2 = 1.403479528759222$ and $f(x_2) = -0.0019260231153448437$
 Iteration = 34 $x_2 = 1.4035089865920407$ and $f(x_2) = -0.001463347115464586$
 Iteration = 35 $x_2 = 1.403531367121615$ and $f(x_2) = -0.0011117810208047807$
 Iteration = 36 $x_2 = 1.4035483702908902$ and $f(x_2) = -0.0008446573178555461$
 Iteration = 37 $x_2 = 1.4035612878889117$ and $f(x_2) = -0.0006417025769653861$
 Iteration = 38 $x_2 = 1.4035711014776593$ and $f(x_2) = -0.00048750704395850164$
 Iteration = 39 $x_2 = 1.403578556853421$ and $f(x_2) = -0.0003703593861463794$
 Iteration = 40 $x_2 = 1.4035842206529576$ and $f(x_2) = -0.000281359952712279$
 Iteration = 41 $x_2 = 1.4035885233787233$ and $f(x_2) = -0.0002137462600102502$
 Iteration = 42 $x_2 = 1.4035917920972842$ and $f(x_2) = -0.00016238007107904906$
 Iteration = 43 $x_2 = 1.4035942752871293$ and $f(x_2) = -0.00012335744923852587$
 Iteration = 44 $x_2 = 1.4035961617193395$ and $f(x_2) = -9.371235608179873e-05$
 Required root is : 1.4035961617193395

Name of Student:

Roll No.:

Batch:

Practical – 11

Q.1 Write a python program to estimate the value of the integral $\int_0^1 1+x$ using trapezoidal rule, take $h=0.2$.

Program:

```
def trapezoidal(f, a, b, n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1, n):
        result = result + 2 * f(a + i*h)
    result = (h/2)*result
    print(result)
    return(result)

from math import *
def f(x):
    return 1 + x
trapezoidal(f, 0, 1, 5)
```

OUTPUT:

1.5

Q.2 find the value of $\int_0^5 \frac{dx}{1+x^2}$ using trapezoidal rule, take $h=0.5$.

Program:

```
def trapezoidal(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1,n):
        result=result+2*f(a+i*h)
    result=(h/2)*result
    print("Integration by Trap is: ", result)
    return(result)

from math import*
def f(x):
    return 1/(1+x**2)
trapezoidal(f,0,5,10)
```

OUTPUT:

```
trapezoidal(f,0,5,10)
Integration by Trap is: 17.5
```

Q.3 Solve the integral $\int_0^{10} (x+1)^3 dx$ using trapezoidal rule, take $h=1$.

Program:

```
def trapezoidal(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1,n):
        result = result + 2*f(a + i*h)
    result = (h/2) * result
    print("Integration by trap is: ", result)
    return(result)

from math import *
def f(x):
    return (x+1)**3
trapezoidal(f,0,10,10)
```

OUTPUT:

```
trapezoidal(f,0,10,10)
Integration by trap is: 60.0
```

Q.4 Solve the integral $\int_{0.2}^{1.4} (\sin x - \log x + e^x) dx$ using trapezoidal rule, take $h=0.2$.

Program:

```
def trapezoidal(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1,n):
        result = result + 2 * f(a + i*h)
    result = (h/2)*result
    print("Integration by trap is :", result)
    return(result)

from math import *
def f(x):
    return sin(x)-log(x)+exp(x)
trapezoidal(f,0.2,1.4,6)
```

OUTPUT:

```
trapezoidal(f,0.2,1.4,6)
Integration by trap is: 2.16
```

Q.5 Evaluate $\int_0^{2.5} e^x dx$ using trapezoidal rule, take $h=0.5$.

Program:

```
def trapezoidal(f, a, b, n):
    h = float(b-a)/n
```

```
    result = f(a) + f(b)
    for i in range(1,n):
        result = result +2*f(a + i*h)
    result = (h/2)*result
    print("Integration by trap is :", result)
    return(result)
from math import *
def f(x):
    return exp(x)
trapezoidal(f,0,2.5,5)
```

OUTPUT:

```
trapezoidal(f,0,2.5,5)
Integration by trap is : 5.625
```

Name of Student:
 Roll No.:
 Batch:
 Practical – 12

Q.1 Using Simpson's $(1/3)^{\text{rd}}$ rule, evaluate $\int_0^{10} \sqrt{1+x^2} dx$ with $h=0.25$.

Program:

```
def simpsons13(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1,n):
        k=a + i*h
        if i%2 == 0:
            result = result + 2*f(k)
        else:
            result = result + 4*f(k)
    result = (h/3)*result
    print("Simpson 1/3rd Result : ", result)
    return result

from math import *
def f(x):
    return sqrt(1+x**2)
simpsons13(f,0,10,40)
OUTPUT:
Simpson 1/3rd Result : 1.2644151038948792
```

Q.2 Write a python program to evaluate $\int_0^5 e^x dx$ by Simpson's $(1/3)^{\text{rd}}$ rule by considering 8 equal intervals.

Program:

```
def simpsons13(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1,n):
        k = a + i*h
        if i%2 == 0:
            result = result + 2*f(k)
        else:
            result = result + 4*f(k)
    result = (h/3)*result
    print("Simpson 1/3rd Result : ", result)
    return result

from math import *
def f(x):
```

```

    return exp(x)
simpsons13(f,0,5,8)

```

OUTPUT:

Simpson 1/3rd Result : 32.684613110896976

Q.3 Using Simpson's (3/8)th rule evaluate $\int_0^{10} \sqrt{1+x^2} dx$ with h= 0.2.

Program:

```

def simpsons38(f,a,b,n):
    h = float(b-a)/n
    result = f(a)+f(b)
    for i in range(1,n):
        k = a + i*h
        if i%3 == 0:
            result = result + 2*f(k)
        else:
            result = result + 3*f(k)
    result = (3*h/8)*result
    print("Simpson 3/8th Result : ", result)
    return result

from math import *
def f(x):
    return sqrt(1+x**2)
simpsons38(f,0,10,5)

```

OUTPUT:

Simpson 3/8th Result : 13.318559665215194

Q.4 Write a python program to estimate the value of the integral

$\int_0^2 (x^2 + 2x - 8) dx$ using Simpson's (1/3)rd rule, take h=0.25

Program:

```

def simpsons13(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1, n):
        k = a + i*h
        if i%2 == 0:
            result = result + 2*f(k)
        else:
            result = result + 4*f(k)
    result = (h/3)*result
    print("Simpson 1/3rd Result : ", result)
    return result

from math import *
def f(x):
    return x**2+2*x-8
simpsons13(f,0,2,8)

```

OUTPUT:

Simpson 1/3rd Result : -3.145833333333333

Q.5 Write a python program to estimate the value of the integral $\int_0^5 \cos(x) dx$ using Simpson's(3/8)th rule, take h=0.5.

Program:

```
def simpsons38(f,a,b,n):
    h = float(b-a)/n
    result = f(a) + f(b)
    for i in range(1, n):
        k = a + i*h
        if i%3 == 0:
            result = result + 2*f(k)
        else:
            result = result + 3*f(k)
    result = (3*h/8)*result
    print("Simpson 3/8th Result : ", result)
    return result

from math import*
def f(x):
    return cos(x)
simpsons38(f,0,5,10)
```

OUTPUT:

Simpson 3/8th Result : 0.7343268508376896