1. DIFFERENTIATION

EXERCISE 1.1

(1) (i)
$$5(3x^2-2)(x^3-2x-1)^4$$

(ii)
$$\frac{5}{2} \left(3\sqrt{x} - 4\sqrt[3]{x} \right) \left(2x^{\frac{3}{2}} - 3x^{\frac{4}{3}} - 5 \right)^{\frac{3}{2}}$$

(iii)
$$\frac{x+2}{\sqrt{x^2+4x-7}}$$

(iv)
$$\frac{x(2\sqrt{x^2+1}+1)}{2\sqrt{x^2+1}\cdot\sqrt{x^2+\sqrt{x^2+1}}}$$

(v)
$$-\frac{4x-7}{(2x^2-7x-5)^{\frac{8}{3}}}$$

(vi)
$$\frac{15(3x-4)}{2(3x-5)^{\frac{3}{2}}} \left(\sqrt{3x-5} - \frac{1}{\sqrt{3x-5}}\right)^4$$

(2) (i)
$$-2x \sin(x^2 + a^2)$$
 (ii) $\frac{3e^{(3x+2)}}{2\sqrt{e^{(3x+2)} + 5}}$

(iii)
$$\csc x$$
 (iv) $\frac{\sec^2 \sqrt{x}}{4\sqrt{x} \cdot \sqrt{\tan \sqrt{x}}}$

(v)
$$\frac{-9\csc^2[\log(x^3)]\cdot\cot^2[\log(x^3)]}{x}$$

(vi)
$$3 \sin^2 x \cdot \cos x \cdot 5^{\sin^3 x + 3} \cdot \log 5$$

(vii)
$$\frac{\sin x \csc \sqrt{\cos x} \cdot \cot(\sqrt{\cos x})}{2\sqrt{\cos x}}$$

$$(viii) - 3x^2 \tan(x^3 - 5)$$

(ix)
$$5 \sin 2x \cdot e^{3 \sin^2 x - 2 \cos^2 x}$$

(x) $\frac{-2x \cdot \sin[2 \log(x^2 + 7)]}{x^2 + 7}$

(xi)
$$-\sec^2 \left[\cos (\sin x)\right] \cdot \sin (\sin x) \cdot \cos x$$

(xii)
$$4x^3 \cdot \sec^2(x^4 + 4) \cdot \sec\left[\tan(x^4 + 4)\right] \cdot \tan\left[\tan(x^4 + 4)\right]$$

(xiii)
$$\frac{2\log x}{x} - \frac{2}{x}$$

(xiv)
$$\frac{\cos\sqrt{\sin\sqrt{x}}\cdot\cos\sqrt{x}}{4\sqrt{x}\cdot\sqrt{\sin\sqrt{x}}}$$

(xv)
$$2x \cdot e^{x^2} \left[\tan \left(e^{x^2} \right) \right]$$
 (xvi) $\frac{1}{2x \log x}$

(xvii)
$$\frac{2 \left[\log \left[\log(\log x) \right] \right]}{x \log x \cdot \log(\log x)}$$

(xviii) $4x \sin(2x^2)$

(3) (i)
$$6(x+2)(x^2+4x+1)^2+4(3x^2-5)$$

 $(x^3-5x-2)^3$

(ii)
$$8(1-2x)(1+4x)^5(3+x-x^2)^7 + 20(1+4x)^4(3+x-x^2)^8$$

(iii)
$$\frac{14-3x}{2(7-3x)^{\frac{3}{2}}} \text{ (iv) } \frac{6x^2(x^3+15)(x^3-5)^4}{(x^3+3)^6}$$

(v)
$$\sin 2x (1 + \sin^2 x) (1 + \cos^2 x)^2 (1 - 5\sin^2 x)$$

(vi)
$$-\frac{\sin x}{2\sqrt{\cos x}} - \frac{\sin \sqrt{x}}{4\sqrt{x}} \cdot \sqrt{\cos \sqrt{x}}$$

(vii)
$$3 \sec 3x$$
 (viii) $\frac{\pi \cos x^{\circ}}{90 (1 - \sin x^{\circ})^2}$

(ix)
$$-\frac{\csc^2\left(\frac{\log x}{2}\right)}{2x} + \tan x \cdot \csc^2 x$$

(x)
$$\frac{8 e^{4x}}{(e^{4x}+1)^2}$$
 (xi) $-\frac{e^{\sqrt{x}}}{\sqrt{x}(e^{\sqrt{x}}-1)^2}$

(xii) 6 cosec
$$2x + 4 \cot x + \frac{14x}{x^2 + 7}$$

(xiii) 3 cosec
$$3x$$
 (xiv) $-\frac{5}{2}$ cosec $\left(\frac{5x}{2}\right)$

$$(xv) - \sec x$$

(xvi)
$$2 \log 4 + \frac{3x}{x^2 + 5} - \frac{9x^2}{2(2x^3 - 4)}$$

(xvii)
$$2x - \frac{6}{5 - 4x} + \frac{2}{7 - 6x}$$

$$(xviii) - \sin x \log a - \frac{6x}{x^2 - 3} - \frac{1}{x \log x}$$

(xix) 0 (xx)
$$\frac{x(x^2+2)^3 (7x^2+38)}{(x^2+5)^{\frac{3}{2}}}$$

(5) -5 (6)
$$\frac{12}{5}$$
 (7) $x = 0$ or $\frac{2\pi}{3}$ or 2π

(8)
$$e^{2x} + 6e^x + 14$$
, e^{x^2+5} , $2x$, e^x , $f'[g(x)] \cdot g'(x)$, $2e^{2x} + 6e^x$, 8 , $g'[f(x)] \cdot f'(x)$, $2xe^{x^2+5}$, $-2e^6$.

EXERCISE 1.2

(1) (i)
$$\frac{1}{2\sqrt{x}}$$
 (ii) $-\frac{1}{4\sqrt{x}\sqrt{2-\sqrt{x}}}$

$$(ii) - \frac{1}{4\sqrt{x}\sqrt{2-\sqrt{x}}}$$

(iii)
$$\frac{1}{3\sqrt[3]{(x-2)^2}}$$
, for $x > 2$ (iv) $\frac{2}{2x-1}$

- (v) 2

- (vii) $2e^{2x-3}$ (viii) $\frac{1}{x \log 2}$

(2) (i)
$$\frac{1}{x \cdot e^x(x+2)}$$
 (ii) $\frac{1}{\cos x - x \sin x}$

(ii)
$$\frac{1}{\cos x - x \sin x}$$

(iii)
$$\frac{1}{7^x(x \log 7 + 1)}$$
 (iv) $\frac{x}{2x^2 + 1}$

$$(v) \quad \frac{1}{1 + \log x}$$

(3) (i)
$$\frac{1}{14}$$
 (ii) $\frac{1}{4}$ (iii) $\frac{1}{12}$ (iv) $\frac{1}{5}$

- **(4)** 1
- (5) (i) and (ii) derivative proved.

(6) (i)
$$\frac{1}{x \left[1 + (\log x)^2\right]}$$
 (ii) $\frac{e^x}{\sqrt{1 - e^{2x}}}$

(iii)
$$-\frac{3x^2}{1+x^6}$$
 (iv) $-\frac{4^x \log 4}{1+4^{2x}}$

(v)
$$\frac{1}{2\sqrt{x}(1+x)}$$
 (vi) $\frac{x}{\sqrt{1-x^4}}$

(vii)
$$\frac{2}{\sqrt{2-x^2}}$$
 (viii) $\frac{3\sqrt{x}}{2\sqrt{1-x^3}}$

(ix)
$$9x^8$$
 (x) $2x$

(7) (i)
$$2xe^{x^2}$$
 (ii) $-5^x \log 5$ (iii) $\frac{1}{2}$

(iv)
$$-x$$
 (v) $-\frac{1}{2}$ (vi) -6

(vii)
$$-\frac{1}{6}$$
 (viii) $-\frac{3}{2}$ (ix) $-\frac{7}{2}$

(x)
$$-\frac{1}{2}$$
 (xi) $-\frac{1}{2}$ (xii) $\frac{2}{3}$

(8) (i) 1 (ii) 1 (iii)
$$\frac{1}{2\sqrt{x}}$$

(iv) 3 (v)
$$e^x$$
 (vi) $2^x \log 2$

(9) (i)
$$\frac{2}{1+x^2}$$
 (ii) $\frac{2}{1+x^2}$

(iii)
$$-\frac{2}{1+x^2}$$
 (iv) $\pm \frac{2}{\sqrt{1-x^2}}$

(v)
$$-\frac{3}{\sqrt{1-x^2}}$$
 (vi) $-\frac{2e^x}{1+e^{2x}}$

(vii)
$$\frac{2 \cdot 3^x \log 3}{1 + 3^{2x}}$$

(viii)
$$\frac{2 \cdot 4^x \log 4}{1 + 4^{2x}}$$
 or $\left(\frac{4^{x + \frac{1}{2}} \log 4}{1 + 4^{2x}}\right)$

(ix)
$$-\frac{10}{1+25x^2}$$
 (x) $-\frac{3\sqrt{x}}{1+x^3}$

(xi)
$$\frac{5x\sqrt{x}}{1+x^5}$$
 (xii)
$$\frac{1}{2\sqrt{x}(1+x)}$$

(10) (i)
$$\frac{3}{1+9x^2} + \frac{5}{1+25x^2}$$

(ii)
$$\frac{7}{1+49x^2} - \frac{5}{1+25x^2}$$

(vi)
$$\frac{3a}{a^2 + 9x^2} + \frac{2a}{a^2 + 4x^2}$$
 (vii) 1

$$(iii)\frac{1}{2\sqrt{x}}\left(\frac{3}{1+9x}-\frac{1}{1+x}\right)$$

(viii)
$$\frac{2}{1+(2x+1)^2} - \frac{3}{1+(3x-4)^2}$$

(iv)
$$2^x \log 2 \left(\frac{3}{1 + 9(2^{2x})} + \frac{1}{1 + 2^{2x}} \right)$$

$$(ix)\frac{2}{1+(2x+3)^2} + \frac{1}{1+(x-1)^2}$$

(v)
$$2^x \log 2 \left(\frac{2}{1 + 4(2^{2x})} - \frac{1}{1 + 2^{2x}} \right)$$

EXERCISE 1.3

(1) (i)
$$\frac{(x+1)^2}{(x+3)^3(x+3)^4} \left[\frac{2}{x+1} - \frac{3}{x+2} - \frac{4}{x+3} \right]$$

(ii)
$$\frac{1}{3} \sqrt[3]{\frac{4x-1}{(2x+3)(5-2x)^2}} \left(\frac{4}{4x-1} - \frac{2}{2x+3} + \frac{4}{5-2x} \right)$$

(iii)
$$(x^2+3)^{\frac{3}{2}} \cdot \sin^3 2x \cdot 2^{x^2} \left[\frac{3x}{x^2+3} + 6 \cot 2x + 2x \log 2 \right]$$

(iv)
$$\frac{(x^2+2x+2)^{\frac{3}{2}}}{(\sqrt{x}+3)^3(\cos x)^x} \left[\frac{3(x+1)}{x^2+2x+2} - \frac{3}{2\sqrt{x}(\sqrt{x}+3)} + x \tan x - \log(\cos x) \right]$$

(v)
$$\frac{x^5 \cdot \tan^3 4x}{\sin^2 3x} \left[\frac{5}{x} + 24 \csc 8x - 6 \cot 3x \right]$$
 (vi) $x^{\tan^{-1}x} \left[\frac{\tan^{-1}x}{x} + \frac{\log x}{1 + x^2} \right]$

(vi)
$$x^{\tan^{-1}x} \left[\frac{\tan^{-1}x}{x} + \frac{\log x}{1+x^2} \right]$$

(vii)
$$\sin^x x \quad [x \cot x + \log(\sin x)]$$

(viii)
$$\cos(x^x) \cdot x^x (1 + \log x)$$

(2) (i)
$$ex^{e^{-1}} + e^x + x^x (1 + \log x)$$
 (ii) $x^{x^x} \cdot x^x \cdot \log x \left[1 + \log x + \frac{1}{x \log x} \right] + e^{x^x} \cdot x^x (1 + \log x)$

(iii)
$$(\log x)^x \left[\frac{1}{\log x} + \log(\log x) \right] + (\cos x)^{\cot x} \left[1 + \csc^2 x \log(\cos x) \right]$$

(iv)
$$x^{e^x} \cdot e^x \left[\frac{1}{x} + \log x \right] + (\log x)^{\sin x} \left[\frac{\sin x}{x \log x} + \cos x \log (\log x) \right]$$

(v)
$$\sec^2 x \cdot e^{\tan x} + (\log x)^{\tan x} \left[\frac{\tan x}{x \log x} + \sec^2 x \log (\log x) \right]$$

(vi)
$$(\sin x)^{\tan x} [1 + \sec^2 x \log (\sin x)] + (\cos x)^{\cot x} [1 + \csc^2 x \log (\cos x)]$$

(vii)
$$10^{x^x} x^x \log 10 (1 + \log x) + x^{x^{10}} \cdot x^9 (1 + 10 \log x) + x^{10^x} \cdot 10^x \left(\frac{1}{x} + \log x \cdot \log 10\right)$$

(viii) 2

(3) (i)
$$-\sqrt{\frac{y}{x}}$$
 (ii) $-\sqrt{\frac{x}{y}}$

(ii)
$$-\sqrt{\frac{x}{y}}$$

(iii)
$$-\frac{\sqrt{y}(2\sqrt{x}+\sqrt{y})}{\sqrt{x}(2\sqrt{y}+\sqrt{x})}$$
 (iv) $-\frac{3x^2+2xy+y^2}{x^2+2xy+3y^2}$

(v)
$$-\frac{y}{x}$$

$$(v) -\frac{y}{x} \qquad (vi) -\frac{e^y + ye^x}{e^x + xe^y}$$

(vii)
$$\frac{\sin(x-y) + e^{x+y}}{\sin(x-y) - e^{x+y}}$$
 (viii) $-\frac{1+y\sin(xy)}{1+x\sin(xy)}$

(ix)
$$\frac{y(1-xe^{x-y})}{x(1-ye^{x-y})}$$

(x)
$$\frac{\sin(x-y) - \cos(x+y) - 1}{\sin(x-y) + \cos(x+y) - 1}$$

EXERCISE 1.4

(1) (i)
$$\frac{1}{t}$$

(ii)
$$\frac{b}{a}\cos\theta$$

(1) (i)
$$\frac{1}{t}$$
 (ii) $\frac{b}{a}\cos\theta$ (iii) $\frac{2}{\sqrt{a^2+m^2}}$

(iv)
$$\sec^3 \theta$$
 (v) $\frac{b}{a} \tan \left(\frac{\theta}{2} \right)$

(vi)
$$\frac{y(t^2+1)\log a}{axt}$$
 (vii) $-\frac{1}{2}$ (viii) $\frac{1}{3}$

(2) (i)
$$\frac{3\sqrt{3}}{2}$$
 (ii) $-\sqrt{3}$ (iii) $-\frac{\pi}{6}$

(ii)
$$-\sqrt{3}$$

$$(iii) - \frac{\pi}{6}$$

(iv)
$$1 - \sqrt{2}$$
 (v) $3 + \pi$

(4) (i)
$$\frac{x \cos x + \sin x}{\sec^2 x}$$

(iii)
$$-\frac{1}{2}$$

(iii)
$$-\frac{1}{2}$$
 (iv) 2 (v) $-x (\log x)^2 \cdot 3^x$

$$(vi) - \frac{x\sqrt{x^2 - 1}}{2}$$

$$(vii) \frac{(1 + \log x) \cdot x^{x+1-\sin x}}{\sin x + x \cos x \cdot \log x}$$

$$(viii) \frac{\sqrt{1-x^2}}{4(1+x^2)}$$

EXERCISE 1.5

(1) (i)
$$40x^3 - 24x - \frac{12}{x^4}$$

(ii)
$$2e^{2x}(1 + \tan x) \cdot (2 + \tan x + \tan^2 x)$$

(iii)
$$-e^{4x} (9 \cos 5x + 40 \sin 5x)$$

(iv)
$$x(5+6\log x)$$
 (v) $-\frac{1+\log x}{(x\log x)^2}$

(iv)
$$x^{x-1} + x^x (1 + \log x)^2$$

(2) (i)
$$-\frac{1}{4a}\csc^4\left(\frac{\theta}{2}\right)$$
 (ii) $-\frac{1}{4at^3}$

(iii) 6 (iv)
$$-\frac{2\sqrt{2} b}{a^2}$$

(4) (i)
$$\frac{d^n y}{dx^n} = \frac{m! a^n (ax+b)^{m-n}}{(m-n)!} \text{ if } m > 0, m > n,$$

$$\frac{d^n y}{dx^n} = 0 \text{ if } m > 0, m < n$$

$$\frac{d^n y}{dx^n} = n! a^n \text{ if } m > 0, m = n$$

(ii)
$$\frac{(-1)^n n!}{r^{n+1}}$$
 (iii) $a^n e^{ax+b}$

(iv)
$$p^n a^{px+q} (\log a)^n$$

(v)
$$\frac{(-1)^{n-1}(n-1)! a^n}{(ax+b)^n}$$
 (vi)cos $\left(\frac{n\pi}{2} + x\right)$

(vii)
$$a^n \sin\left(\frac{n\pi}{2} + ax + b\right)$$

$$(viii) (-2)^n \cos\left(\frac{n\pi}{2} + 3 - 2x\right)$$

(ix)
$$\frac{(-1)^{n-1}(n-1)! 2^n}{(2x+3)^n}$$

(x)
$$\frac{(-1)^n \cdot n! \cdot 3^n}{(3x-5)^{n+1}}$$

(xi)
$$e^{ax} \left(a^2 + b^2\right)^{\frac{n}{2}} \cdot \cos \left[bx + c + n \tan^{-1}\left(\frac{b}{a}\right)\right]$$

(xii)
$$e^{8x} \cdot (10)^n \cos \left[6x + 7 + n \tan^{-1} \left(\frac{3}{4} \right) \right]$$

MISCELLANEOUS EXERCISE 1

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|---|---|---|---|---|---|---|---|---|----|----|----|
| D | С | С | В | Α | С | D | С | В | С | A | В |

- (II) (1) $\frac{3}{4}$ (ii) Does not exist (iii) -2
 - (2) (A) 3, (B) 5, (C) 4, (D) 1.
 - (3) (i) $-\frac{1}{9}$ (ii) $-\frac{40}{3}$ (iii) $-\frac{29}{96}$ (iv) $-\frac{4}{9}$
 - (4) (i) $-\frac{x}{\sqrt{1-x^2}}$ [Hint: $x = \cos 2\theta$]
 - (ii) $-\frac{1}{2}$ [Hint: $x = \cos 2\theta$]
 - (iii) $\frac{3}{2\sqrt{x}(1+x)}$ [Hint : $\sqrt{x} = \tan \theta$]

- (iv) $-\frac{1}{2 \cdot \sqrt{1 x^2}}$ [Hint : $x = \cos 2\theta$]
- (v) $\frac{3}{1+9x^2} + \frac{5}{1+25x^2}$
- (vi) $\frac{1}{2(1+x^2)}$ [Hint: $x = \tan \theta$]
- (6) (i) $\frac{\sqrt{1-x^2}}{4(1+x^2)}$
 - (ii) $-\frac{2x}{\sqrt{1+x^2}.\sin(\log x)}$ (iii) 1

2. APPLICATIONS OF DERIVATIVES

EXERCISE 2.1

- (1) (i) 2x y + 4 = 0, x + 2y 8 = 0
 - (ii) 4x 5y + 12 = 0, 5x + 4y 26 = 0,
 - (iii) $y = 2, x = \sqrt{3}$
 - (iv) $\pi x + 2y 2\pi = 0$, $4x - 2\pi y + \pi^2 - 4 = 0$
 - (v) 2x y = 0, $4x + 8y 5\pi = 0$
 - (vi) 4x + 2y 3 = 0, 2x 4y + 1 = 0
 - (vii) 17x 4y 20 = 0, 8x + 34y 135 = 0
- **(2)** (4, 1)

- (3) $(2,-2)\left(-\frac{2}{3},-\frac{14}{27}\right)$ (4) y=0 and y=4
- (5) x + 3y 8 = 0, x + 3y + 8 = 0
- (6) a = 2, b = -7 (7) (4, 11) and $\left(-4, -\frac{31}{3}\right)$
- (8) $0.8 \, \pi \, \text{cm}^2/\text{sec}$. (9) $6 \, \text{cm}^3/\text{sec}$.
- $(10) \frac{3\sqrt{6}}{2} \text{ cm}^2/\text{ sec.}$ (11) 8 cm²/ sec
- $(12) 7.2 \text{ cm}^3/\text{ sec}$ (13) 3 km/hr
- (14) (i) $\left(\frac{3}{8}\right)$ meter/sec. (ii) $\frac{9}{8}$ meter/sec.
- (15) 0.9 meter/sec. $(16) \left(\frac{4\pi}{3}\right) \text{ cm}^{3}/\text{ sec}$

EXERCISE 2.2

- (1) (i) 2.9168
- (ii) 3.03704
- (iii) 1.9997

- (iv) 248.32
 - (v) 64.48
- (2) (i) 0.953
- (ii) 0.42423
- (iii) 0.4924
- (iv) 1.02334
- (3) (i) 0.7845
- (ii) 0.7859
- (iii) 0.7859
- (4) (i) 2.70471 (ii) 8.1279
- (iii) 9.09887

- (5) (i) 4.6152
- (ii) 2.1983
- (iii) 3.006049

- (6) (i) 6.91
- (ii) 9.72

EXERCISE 2.3

- Valid (1) (i)
- Valid (ii)
- (iii) Invalid
- (iv) Valid
- (v) Invalid
- (vi) Invalid
- (2) b = 1
- (3) (i) $\frac{\pi}{4}$ or $\frac{5\pi}{4}$ (ii) $c = \pi$ (iii) $c = \frac{5}{2}$
- (4) p = -6, q = 11 (6) c = -2
- (7) (i) e-1 (ii) $2 \pm \frac{2}{\sqrt{3}}$ (iii) $\frac{1}{7}$

- (iv) $\frac{1}{2}$ (v) $3 + \sqrt{2}$

EXERCISE 2.4

- (1) (i) Increasing $\forall x \in R$
 - (ii) Decreasing $\forall x \in R$
 - (iii) Increasing $\forall x \in R$
- (2) (i) x < -1 and x > 2
- (ii) $R \{1\}$
- (iii) x < -2 and x > 6
- (3) (i) -1 < x < 2 (ii) $(-5, 5) \{0\}$

 - (iii) $x \in (2, 4)$
- (4) (a) $(-\infty, -4] \cup [12, \infty)$
 - (b) -4 < x < 12 i.e. [-4, 12]
- (5) (a) x < -3 and x > 8 (b) -3 < x < 8
- (6) (a) -1 < x < 1
- (b) (-∞, -1) ∪ (1, ∞)
- $Max = \frac{36}{25}$, $Min = -\frac{16}{27}$ (9) (i)
 - (ii) Max = -3, Min = -128
 - (iii) Max = 20, Min = 16 (iv) Min = 8
 - (v) Min = $-\frac{1}{\rho}$ (vi) Max = $\frac{1}{\rho}$
- (10) 15, 15 (11) 10, 10 (12) 9
- (13) 12.8
- (14) $l = \sqrt{2}$ and $b = \frac{1}{\sqrt{2}}$
- (15) Radius = Height = a
- (16) 3, 3
- (17) Side of square base = 8 cm, Height = 4 cm
- (18) x = 75, P = 4000
- (19)6,9

(22) $\frac{4\pi r^3}{3\sqrt{3}}$ cm³

MISCELLANEOUS EXERCISE 2

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|---|---|---|---|---|---|---|---|---|----|
| A | С | В | В | D | С | D | A | D | D |

(II) (2) 4

(3)
$$14x - 13y + 12 = 0$$
, $13x + 14y - 41 = 0$

(4)
$$\frac{2}{9\pi}$$
 ft/sec

(4)
$$\frac{2}{9\pi}$$
 ft/sec (5) $\left(\frac{16}{3}, 3\right), \left(-\frac{16}{3}, -3\right)$

(6)
$$c = 0$$

(7)
$$c = 2$$
 (8) 2.025

(10) Decreasing in
$$\left(0, \frac{1}{e}\right]$$
 and Increasing in $\left[\frac{1}{e}, \infty\right)$

(11) Increasing in $[e, \infty)$, Decreasing in (1, e]

(15)
$$l = \frac{60}{\pi + 4}, b = \frac{30}{\pi + 4}, r = \frac{30}{\pi + 4}$$

(17) Side =
$$\frac{l}{\pi + 4}$$
, Radius = $\frac{l}{2(\pi + 4)} = \frac{x}{2}$

(18) 24, 45 (21)
$$Max = \frac{5}{4}$$
, $Min = 1$

3. INDEFINITE INTEGRATION

EXERCISE 3.1

(1) (i)
$$\frac{x^4}{4} + \frac{x^3}{3} - \frac{x^2}{2} + x + c$$
 (ii) $\frac{x^3}{3} - 2x^2 + 4x + c$

(iii)
$$3 \tan x - 4 \log x - \frac{2}{\sqrt{x}} - 7x + c$$

(iv)
$$\frac{x^2}{4} - \frac{5x^2}{2} + 3 \log x - \frac{1}{x^4} + c$$

(v)
$$\frac{6}{5}x^2\sqrt{x}-4\sqrt{x}-\frac{10}{\sqrt{x}}+c$$

(2) (i)
$$\tan x - x + c$$
 (ii) $-2 \cos x + c$

(ii)
$$-2\cos x + c$$

(iii)
$$\sec x + c$$

$$(iv) - \cot x - 2x + c$$

(v)
$$-\cot x - \tan x + x + c$$

(vi)
$$\sec x - \tan x + x + c$$

(vii)sec
$$x - \tan x + x + c$$

(viii)
$$\sin x - \cos x + c$$
 (ix) $-\sqrt{2}\cos x + c$

(x)
$$-\frac{1}{14}\cos 7x - \frac{1}{2}\cos x + c$$

(3) (i)
$$x-2 \log (x+2) + c$$

(ii)
$$2x + \frac{1}{2}\log(2x+1) + c$$

(iii)
$$\frac{5}{3}x - \frac{26}{9}\log(3x - 4) + c$$

(iv)
$$\frac{2(x+5)^{\frac{3}{2}}}{3}$$
 - 14 $\sqrt{x+5}$ + c

(v)
$$\frac{1}{12} (4x-1)^{\frac{3}{2}} - \frac{13}{4} \sqrt{4x-1} + c$$

$$(vi) - \cos 2x + c$$

$$(vii) \frac{2}{5} \left(\sin \frac{5x}{2} - \cos \frac{5x}{2} \right) + c$$

$$(viii) \frac{1}{4} (2x + \sin 2x) + c$$

(ix)
$$-\frac{4}{9}\left[x^{\frac{3}{2}} + (x+3)^{\frac{3}{2}}\right] + c$$

(x)
$$\frac{2}{21} \left[(7x-2)^{\frac{3}{2}} + (7x-5)^{\frac{3}{2}} \right] + c$$

(4)
$$f(x) = \frac{x^2}{2} + \frac{3}{2x^2} + \frac{7}{2}$$

EXERCISE 3.2 (A)

I. 1.
$$\frac{(\log x)^{n+1}}{n+1} + c$$
 2. $\frac{2}{5} (\sin^{-1} x)^{\frac{5}{2}} + c$

$$2. \quad \frac{2}{5} (\sin^{-1} x)^{\frac{5}{2}} + c$$

$$3. \log \left(\operatorname{cosec} (x + \log x) - \cot (x + \log x)\right) + c$$

4.
$$\frac{-1}{\sqrt{\tan{(x^2)}}} + c$$

4.
$$\frac{-1}{\sqrt{\tan{(x^2)}}} + c$$
 5. $\frac{1}{3}(e^{3x} + 1) + c$

$$6. \quad \frac{1}{\log a} \cdot a^{x + \tan^{-1} x} + c$$

7.
$$\frac{1}{2} \left[\log \left(\sin e^{x} \right) \right]^{2} + c$$

8.
$$\log (e^x - e^{-x}) + c$$

9.
$$\frac{1}{5}\sin^5 x - \frac{1}{7}\sin^7 x + c$$

10.
$$\frac{1}{48}\log(4x^{12}+5)+c$$

11.
$$\frac{1}{10} \tan x^{10} + c$$
 12. $\frac{1}{4} \log (x^4 + 1) + c$

13.
$$2\sqrt{\tan x} + c$$
 14. $\tan^{-1} x + \frac{1}{x^2 + 1} + c$

15.
$$\log (3 \cos^2 x + 4 \sin^2 x) + c$$

16.
$$2 \tan^{-1} \sqrt{x} + c$$
 17. $\log (10^x + x^{10}) + c$

$$18. \ \frac{\sqrt{1+4x^n}}{2n} + c$$

19.
$$\frac{4}{5}(x+2)^{\frac{5}{2}}-2(x+2)^{\frac{3}{2}}+c$$

$$20.\frac{1}{7}(a^2+x^2)^{\frac{7}{2}} - \frac{4a^2}{5}(a^2+x^2)^{\frac{5}{2}} + \frac{2a^4}{3}(a^2+x^2)^{\frac{3}{2}} + c$$

21.
$$-2\sqrt{2-3x}-\frac{2}{9}(2-3x)^{\frac{3}{2}}+c$$

22.
$$\frac{5}{12}(2x+3)^{\frac{3}{2}} - \frac{11}{2}(2x+3)^{\frac{1}{2}} - \frac{49}{4\sqrt{2x+3}} + c$$

23.
$$\frac{1}{3}\sin^{-1}\left(\frac{x^3}{3}\right) + c$$
 25. $\frac{1}{3}\log\left(\frac{x^3-1}{x^3}\right) + c$

$$24. \log (\log (\log x)) + c$$

II. 1.
$$2 \cdot \log \left(\sec \frac{x}{2} \right) + c$$

2.
$$\cos a \cdot \log (\sin (x-a)) - (\sin a) x + c$$

3.
$$\cos(a+b)\cdot\log(\sec(x+b))$$

$$(\sin(a+b))\cdot x + c$$

4.
$$\log (\tan x + 2) + c$$

5.
$$\frac{11}{75}x + \frac{2}{25}\log(3\sin x + 4\cos x) + c$$

6.
$$\frac{2x}{13} + \frac{3}{13} \log(2 \cos x + 3 \sin x) + c$$

7.
$$5x - 3 \log |2e^x - 5| + c$$

8.
$$-5x - \log |3e^x - 4| + c$$

9.
$$-x + \frac{7}{8} \log |4e^{2x} - 5| + c$$

10.
$$\frac{\cos^8 x}{8} + \frac{\cos^6 x}{6} + \frac{\cos^4 x}{4} + \frac{\cos^2 x}{2} + \frac{1}{2} \log(\cos^2 x - 1) + c$$

11.
$$\frac{\tan^4 x}{4} - \frac{\tan^2 x}{2} + \log(\sec x) + c$$

12.
$$\sin x - \sin^3 x + \frac{3}{5} \sin^5 x - \frac{1}{7} \sin^7 x + c$$

13.
$$\frac{1}{6} \log \left[\frac{(\sec 3x)^2}{(\sec 2x)^3 (\sec x)^6} \right] + c$$

14.
$$\frac{1}{6}\cos^{11}x - \frac{1}{9}\cos^9x + \frac{1}{13}\cos^{13}x + c$$

15.
$$-\frac{1}{\log 3} \cdot 3^{\cos^2 x} + c$$

$$16. \ \frac{1}{20} \log \left[\frac{\sin^5 4x}{\sin^2 10x} \right] + c$$

17.
$$\frac{1}{2} \log \left[\left(1 + \cos^2 x \right) - \cos^2 x \right] + c$$

EXERCISE 3.2 (B)

I. 1.
$$\frac{1}{4\sqrt{3}} \log \left(\frac{2x - \sqrt{3}}{2x + \sqrt{3}} \right) + c$$

2.
$$\frac{1}{30} \log \left(\frac{5+3x}{5-3x} \right) + c$$

3.
$$\frac{1}{\sqrt{14}} \tan^{-1} \left(\frac{\sqrt{2}x}{\sqrt{7}} \right) + c$$

4.
$$\frac{1}{\sqrt{3}} \log \left(x + \sqrt{x^2 + \frac{8}{3}} \right) + c$$

5.
$$\frac{1}{2}\sin^{-1}\left(\frac{2x}{\sqrt{11}}\right) + c$$

6.
$$\frac{1}{\sqrt{2}} \log \left(x + \sqrt{x^2 - \frac{5}{2}} \right) + c$$

7.
$$9 \sin^{-1}\left(\frac{x}{9}\right) - \sqrt{9 - x^2} + c$$

8.
$$2 \sin^{-1}\left(\frac{x}{2}\right) - \sqrt{4 - x^2} + c$$

9.
$$2 \sin^{-1}\left(\frac{x}{10}\right) - \frac{1}{2}\left(\sqrt{100 - x^2}\right) + c$$

$$10. \quad \frac{1}{4} \log \left| \frac{x+2}{x+6} \right| + c$$

11.
$$\frac{1}{\sqrt{5}} \log \left(\frac{\sqrt{5} - 1 + 2x}{\sqrt{5} + 1 - 2x} \right) + c$$

12.
$$\frac{1}{8\sqrt{2}}\log\left(\frac{2x-5-2\sqrt{2}}{2x-5+2\sqrt{2}}\right)+c$$

13.
$$\frac{1}{2\sqrt{19}}\log\left(\frac{3x+2+\sqrt{19}}{3x+2-\sqrt{19}}\right)+c$$

14.
$$\frac{1}{\sqrt{3}}\log\left(x+\frac{5}{6}+\sqrt{x^2+\frac{5}{3}x+\frac{7}{3}}\right)+c$$

15.
$$\log (x+4+\sqrt{x^2-8x-20})+c$$

16.
$$\frac{1}{\sqrt{2}} \log \left(x - \frac{3}{4} + \sqrt{x^2 - \frac{3}{2}x + 4} \right) + c$$

17.
$$\log \left(x - \frac{1}{2} + \sqrt{x^2 - x - 6} \right) + c$$

18.
$$\frac{1}{2\sqrt{7}} \tan^{-1} \left(\frac{2 \tan x}{\sqrt{7}} \right) + c$$

19.
$$\frac{1}{\sqrt{2}} \tan^{-1} \left(\sqrt{2} \tan x \right) + c$$

20.
$$\frac{1}{2\sqrt{3}} \log \left| \frac{\sqrt{3} + \tan x}{\sqrt{3} - \tan x} \right| + c$$

II. 1.
$$\frac{2}{\sqrt{5}} \tan^{-1} \left(\frac{2 \tan \frac{x}{2} + 2}{\sqrt{5}} \right) + c$$

$$2. \frac{1}{3} \log \left[\frac{3 \tan \left(\frac{x}{2} \right) - 1}{3 \tan \left(\frac{x}{2} \right) + 1} \right] + c$$

3.
$$\sqrt{2} \tan^{-1} \left(\frac{\tan \frac{x}{2} - 1}{\sqrt{2}} \right) + c$$

4.
$$\tan^{-1} \left[2 \tan \left(\frac{x}{2} \right) + 1 \right] + c$$

5.
$$\frac{1}{\sqrt{5}} \tan^{-1} \left(\sqrt{5} \tan x \right) + c$$

6.
$$-\frac{1}{\sqrt{5}} \tan^{-1} \left(\frac{3 \tan x - 2}{\sqrt{5}} \right) + c$$

7.
$$\frac{1}{2\sqrt{11}}\log\left(\frac{\sqrt{11}-2+\tan x}{\sqrt{11}+2-\tan x}\right)+c$$

8.
$$\frac{1}{\sqrt{2}} \log \left[\sec \left(x + \frac{\pi}{4} \right) + \tan \left(x + \frac{\pi}{4} \right) \right] + c$$

9.
$$\frac{1}{2} \log \left[\sec \left(x + \frac{\pi}{4} \right) + \tan \left(x + \frac{\pi}{4} \right) \right] + c$$

EXERCISE 3.2 (C)

I. 1.
$$\frac{3}{2}\log(x^2+6x+5) - \frac{5}{4}\log\left(\frac{x+1}{x+5}\right) + c$$

2.
$$\log (x^2 + 4x - 5) - \frac{1}{2} \log \left(\frac{x - 1}{x + 5} \right) + c$$

3.
$$\frac{1}{2}\log(2x^2+3x-1)+\frac{3}{2\sqrt{17}}$$

$$\log\left(\frac{4x + 3 - \sqrt{17}}{4x + 3 + \sqrt{17}}\right) + c$$

4.
$$\frac{3}{2}\sqrt{2x^2+2x+1}+\frac{5}{2\sqrt{2}}$$
.

$$\log\left(x + \frac{1}{2} + \sqrt{x^2 + x + \frac{1}{2}}\right) + c$$

5.
$$-7\sqrt{3+2x-x^2} + 10\cdot\sin^{-1}\left(\frac{x-1}{2}\right) + c$$

6.
$$\sqrt{x^2-16x+63}$$
 +

$$\log\left\{(x-8) + \sqrt{x^2 - 16x + 63}\right\} + c$$

7.
$$\sqrt{9x-x^2} + \frac{9}{2}\sin^{-1}\left(\frac{2x-9}{9}\right) + c$$

8.
$$\frac{3}{4\sqrt{2}}\log\left(\frac{2\sqrt{2}\sin x + \sqrt{2} - 2}{2\sqrt{2}\sin x + \sqrt{2} + 2}\right) + c$$

9.
$$\sqrt{e^{2x}-1} - \log(e^x + \sqrt{e^{2x}-1}) + c$$

EXERCISE 3.3

I. 1.
$$\frac{x^3}{9} (3 \cdot \log x - 1) + c$$

2.
$$-\frac{x^2}{3}\cos 3x + \frac{2}{9}x\sin 3x + \frac{2}{27}\cos 3x + c$$

3.
$$\frac{x^2}{2} \tan^{-1} x - \frac{1}{2} (x - \tan^{-1} x) + c$$

4.
$$\frac{x^3}{3} \tan^{-1} x - \frac{x^2}{6} + \frac{1}{6} \log (1 + x^2) + c$$

5.
$$\frac{1}{4} (\tan^{-1} x) (x^4 - 1) - \frac{x}{12} (x^3 - 3x) + c$$

6.
$$x [(\log x)^2 - 2 (\log x) + 2] + c$$

7.
$$\frac{1}{2}\log(\sec x + \tan x) + \frac{1}{2}\sec x \cdot \tan x + c$$

8.
$$\frac{1}{4} \left[x^2 - x \cdot \sin 2x - \frac{1}{2} \cos 2x \right] + c$$

9.
$$\frac{x^4}{4} \log x - \frac{x^4}{16} + c$$

10.
$$\frac{e^{2x}}{13} \left[2 \cos 3x + 3 \sin 3x \right] + c$$

11.
$$\frac{x^2}{2}\sin^{-1}x + \frac{1}{4}x\sqrt{1-x^2} - \frac{1}{4}\sin^{-1}x + c$$

12.
$$\frac{x^3}{3}\cos^{-1}x - \frac{1}{3}\sqrt{1-x^2} + \frac{1}{9}(1-x^2)^{\frac{3}{2}} + c$$

13.
$$(\log x) [\log (\log x) - 1] + c$$

14.
$$-(\sin^{-1} t) \sqrt{1-t^2} + t + c$$

15.
$$2\left[\sqrt{x}\cdot\sin\sqrt{x} + \cos\sqrt{x}\right] + c$$

16.
$$(\cos \theta) \cdot [1 - \log(\cos \theta)] + c$$

17.
$$\frac{1}{4} \left[\frac{x}{3} \sin 3x + \frac{1}{9} \cos 3x + 3x \sin x + 3 \cos x \right] + c$$

18.
$$-\frac{1}{2}\cos(\log x)^2 + c$$

19.
$$-\frac{1}{2}(\log x)^2 + c$$

20.
$$\frac{x}{6}\sin 3x + \frac{1}{18}\cos x - \frac{1}{14}x\sin 7x - \frac{1}{98}\cos 7x + c$$

21.
$$(3x^{\frac{2}{3}} - 6) \sin \sqrt[3]{x} + 6 \sqrt[3]{x} \cos \sqrt[3]{x} + c$$

II. 1.
$$\frac{e^{2x}}{13} [2 \sin 3x - 3 \cos 3x] + c$$

2.
$$\frac{e^{-x}}{5} \left[-\cos x + 2\sin 2x \right] + c$$

3.
$$\frac{x}{2} \left[\sin (\log x) - \cos (\log x) \right] + c$$

4.
$$\sqrt{5} \left[\frac{x}{2} \sqrt{x^2 + \frac{3}{5}} + \frac{3}{10} \log \left(x + \sqrt{x^2 + \frac{3}{5}} \right) \right] + c$$

5.
$$\frac{x^3}{6} \cdot \sqrt{a^2 - x^6} + \frac{a^2}{2} \sin^{-1} \left(\frac{x^3}{a} \right) + c$$

6.
$$\frac{x-5}{2}\sqrt{(x-3)(7-x)}+2\sin^{-1}\left(\frac{x-5}{2}\right)+c$$

7.
$$\frac{1}{\log 2} \left\{ \frac{2^x}{2} \sqrt{4^x + 4} + 2 \log (2^x + \sqrt{4^x + 4}) \right\} + c$$

8.
$$\frac{1}{6}(2x^2+3)^{\frac{3}{2}}$$
 +

$$\sqrt{2} \left[\frac{x}{2} \sqrt{x^2 + \frac{3}{2}} + \frac{3}{4} \log \left(x + \sqrt{x^2 + \frac{3}{4}} \right) \right] + c$$

9.
$$-\frac{1}{3} (5-4x-x^2)^{\frac{3}{2}} - (x+2) \sqrt{5-4x-x^2} - 9 \sin^{-1} \left(\frac{x+2}{3}\right) + c$$

10.
$$\frac{(1+2\tan x)}{4}\sqrt{\tan^2 x + \tan x - 7} - \frac{29}{8}\log\left\{\frac{1}{2} + \tan x + \sqrt{\tan^2 x + \tan x - 7}\right\} + c$$

11.
$$\left(\frac{x+1}{2}\right)\sqrt{x^2+2x+5}+2\log\left\{x+1+\sqrt{x^2+2x+5}\right\}+c$$

12.
$$\sqrt{2} \left\{ \left(\frac{4x+3}{8} \right) \sqrt{x^2 + \frac{3}{2}x + 2} + \frac{23}{16\sqrt{2}} \log \left[\left(x + \frac{3}{4} \right) + \sqrt{x^2 + \frac{3}{2}x + 2} \right] \right\} + c$$

III. 1.
$$e^{x}(2 + \cot x) + c$$
 2. $e^{x} \cdot \tan \frac{x}{2} + c$ 3. $e^{x} \cdot \frac{1}{x} + c$ 4. $e^{x} \cdot \left(\frac{1}{x+1}\right) + c$

5.
$$e^x \cdot (\log x)^2 + c$$
 6. $e^{5x} \cdot \log x + c$ 7. $e^{\sin^{-1} x} \cdot x + c$

8.
$$\frac{(1+x)^2}{2} \left(\log (1+x) - \frac{1}{2} \right) + c$$
 9. $x \cdot \operatorname{cosec} (\log x) + c$

EXERCISE 3.4

I. 1.
$$\frac{1}{4} \log (x-1) - 2 \log (x+2) + \frac{11}{4} (x+3) + c$$

2.
$$\frac{1}{6} \tan^{-1} x + \frac{1}{15\sqrt{2}} \log \left(\frac{x - \sqrt{2}}{x + \sqrt{2}} \right) - \frac{\sqrt{3}}{10} \tan^{-1} \left(\frac{x}{\sqrt{3}} \right) + c$$

3.
$$\frac{51}{41}\log(2x+9) + \frac{31}{41}\log(3x-7) + c$$
 4. $-\frac{8}{5}\log(x+4) - \frac{2}{5}\log(x-1) + c$

5.
$$x - \log(x+3) + \log(x-2) + c$$
 6. $x^2 + 3x + \frac{5}{3}\log(3x+1) + \log(x-1) + c$

7.
$$\frac{1}{2} \log \left| \frac{2x+1}{2x-1} \right| + 3 \log (x+3) + c$$
 8. $\frac{1}{5} \log \left(\frac{x^5}{x^5+1} \right) + c$ 9. $\frac{11}{\sqrt{5}} \tan^{-1} \left(\frac{x}{2} \right) - \frac{9}{2} \tan^{-1} \left(\frac{x}{2} \right) + c$

10.
$$2 \log \left(\frac{x+1}{x-1} \right) + \frac{5}{2\sqrt{2}} \log \left(\frac{x+\sqrt{2}}{x-\sqrt{2}} \right) + c$$
 11. $\log \left(\frac{2+x^2}{3+x^2} \right) + c$

12.
$$\frac{1}{5 \cdot \log 2} \log \left(\frac{2^x - 4}{2^x + 1} \right) + c$$
 13. $\frac{5}{2} \left(\frac{1}{x + 1} \right) + \frac{11}{4} \log \left(\frac{x + 1}{x + 3} \right) + c$

14.
$$6 \cdot \log x - \log (x+1) - \frac{9}{x+1} + c$$
 15. $\frac{1}{8} \log \left(\frac{x^6 (x^3 + 3)}{(3x^3 + 1)^3} \right) + c$

16.
$$\frac{1}{3}\log(x-1) - \frac{1}{6}\log(x^2+x+1) - \frac{1}{\sqrt{3}}\tan^{-1}\left(\frac{2x+1}{\sqrt{3}}\right) + c$$

17.
$$3 \cdot \log (\sin x - 2) - \frac{4}{\sin x - 2} + c$$

18.
$$\frac{1}{2}\log(\cos x + 1) + \frac{1}{6}\log(\cos x - 1) - \frac{2}{3}\log(2\cos x + 1) + c$$

19.
$$\frac{1}{8} \log \left(\frac{\cos x - 1}{\cos x + 1} \right) + \frac{1}{4 \cdot (\cos x + 1)} + c$$
 20. $\frac{1}{6} \log \left[\frac{(1 + 2 \sin x)^4}{(1 - \sin x)(1 + \sin x)^3} \right] + c$

21.
$$\frac{1}{10}\log(1-\cos x) - \frac{1}{2}\log(1+\cos x) + \frac{2}{5}\log(3+2\cos x) + c$$

22.
$$\frac{1}{2} \log \left[\frac{e^{x} + 1}{(e^{2x} + 9)^{\frac{1}{2}}} \right] + \frac{1}{6} \tan^{-1} \left(\frac{e^{x}}{3} \right) + c$$
 23.
$$\frac{5}{26} \log \left[\frac{(3 \log x + 2)^{2}}{\sqrt{(\log x)^{2} + 1}} \right] + \frac{11}{26} \tan^{-1} (\log x) + c$$

MISCELLANEOUS EXERCISE 3

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|----|----|----|----|----|----|----|----|----|
| В | A | В | A | D | В | A | A | С | В |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| Α | A | D | С | А | D | A | D | С | Α |

(II) (1)
$$\frac{2}{7}x^{\frac{7}{2}} - \frac{8}{5}x^{\frac{5}{2}} - \frac{8}{3}x^{\frac{3}{2}} + c$$

(2)
$$\frac{x^7}{7} - \frac{x^6}{6} + \frac{x^5}{5} - \frac{x^4}{4} + \frac{x^3}{3} - \frac{x^2}{2} + x - \log(x+1) + c$$

(3)
$$\frac{1}{15}(6x+5)^{\frac{5}{2}}+c$$

(4)
$$\frac{t^2}{2} - 2t + 3 \cdot \log(t+1) + \frac{1}{t+1} + c$$

(5)
$$3 \tan x - 2 \sec x + c$$

(6)
$$\tan \theta - \cot \theta - 3 \theta + c$$

(7)
$$\frac{1}{48} (2 \sin 6x + 3 \sin 4x + 6 \sin 2x + 12 x) + c$$
 (8) $\frac{1}{2} \sin 2x - \frac{1}{3} \sin 3x + c$

(8)
$$\frac{1}{2}\sin 2x - \frac{1}{3}\sin 3x + c$$

(9)
$$\frac{\pi}{4}x - \frac{1}{4}x^2 + c$$

(III) (1)
$$\frac{1}{4} (1 + \log x)^4 + c$$

(2)
$$(\tan^{-1} x) x - \frac{1}{2} \log (1 + x^2) - (1 - x) \tan^{-1} (1 - x) + \frac{1}{2} \log (x^2 - 2x + 2) + c$$

$$(3) - \cot(\log x) + c$$

(4)
$$\frac{2}{3} \sec x^{\frac{3}{2}} + c$$

(5) $x \log (1 + \cos x) + c$

(6) $\frac{1}{3}\sin^{-1}(x^3) + c$

(7) $\frac{1}{4} \log (3 - 2 \cot x) + c$

(8) $x \cdot \left(\log(\log x) - \frac{1}{\log x}\right) + c$

- (9) $\frac{2}{\sqrt{13}} \tan^{-1} \left(\frac{2 \tan \left(\frac{\lambda}{2} \right) 3}{\sqrt{13}} \right) + c$
- (10) $\frac{1}{4} \left(2 \sec^{-1} x + \frac{2\sqrt{x^2 1}}{x^2} \right) + c$
- (11) $-\frac{3}{2}\sqrt{-2x^2+x+3}+\frac{7}{4\sqrt{2}}\sin^{-1}\left(\frac{2x-1}{\sqrt{7}}\right)+c$
- (12) $x \cdot \log(x^2 + 1) 2[x \tan^{-1}x] + c$

- (13) $\frac{1}{4}e^{2x} \cdot [\sin 2x \cos 2x] + c$
- (14) $\frac{1}{18}\log(3x-1) + \frac{1}{2}\log(x-1) \frac{4}{9}\log(3x-2) + c$
- (15) $\frac{1}{6} \log \left\{ \frac{(\cos x 1)(\cos x + 1)^3}{(2\cos x + 1)^4} \right\} + c$
- (16) $\left(\frac{\tan x 1}{2}\right) \sqrt{7 + 2 \tan x \tan^2 x} + 4 \sin^{-1} \left(\frac{\tan x 1}{2\sqrt{2}}\right) + c$
- (17) $\frac{1}{4} \log \left\{ \frac{(x-1)^3(x+3)}{(x+1)^4} \right\} + c$

(18) $\frac{1}{5} \log \left(\frac{x^5}{x^5 + 1} \right) + c$

(19) $2 \sqrt{\tan x} + c$

(20) $\frac{1}{3 \cot^3 x} + \frac{2}{\cot x} - \cot x + c$

4. DEFINITE INTEGRATION

EXERCISE 4.1

- I. (1) 4 (2) $\frac{64}{3}$ (3) $e^2 1$ (4) 6

EXERCISE 4.2

- I. (1) $\frac{64}{3}$ (2) $\log\left(\frac{25}{24}\right)$ (3) $-\left(1+\frac{\pi}{4}\right)$ (4) 2

 - (5) $\frac{1}{18} \left[13\sqrt{13} + 7\sqrt{7} 3\sqrt{3} 27 \right]$ (6) $1 \frac{3\pi}{4}$ (7) $\frac{4}{7\sqrt{2}}$ (8) 1 (9) $\frac{3\pi}{16}$

- $(10) \frac{1}{3} \left(\tan^{-1} \frac{4}{3} + \tan^{-1} \frac{2}{3} \right) \qquad (11) \pi \qquad (12) \frac{\pi}{6} \qquad (13) 1 \qquad (14) \frac{\pi}{4} \frac{1}{2}$

II. (1) $\frac{\pi}{4} - \frac{1}{2} \log 2$

 $(2) \frac{1}{2} \log 2$

(3) $\frac{\pi}{4}$

(4) 0

- (5) $\frac{2}{3} \tan^{-1} \left(\frac{1}{3} \right)$ (6) $\frac{1}{4} \log \left(\frac{2\sqrt{2}+1}{2\sqrt{2}-1} \right)$

(7) $\log\left(\frac{4}{3}\right)$

(8) $\frac{1}{ab} \left[\tan^{-1} \left(\frac{ae}{b} \right) - \tan^{-1} \left(\frac{a}{be} \right) \right]$

 $(9) \frac{\pi}{4}$

 $(10) \frac{4}{3}$

 $(11) \frac{\pi}{2} - 1$

 $(12) \frac{8}{3}$

- (13) $\frac{\pi}{2} 1$
- (14) $e^{\frac{\pi}{4}} \left| \frac{\pi}{4} + 1 \right| \left| \frac{\pi}{2} + 1 \right|$ (15) $\sin(\log 3)$
- III. (1) $\frac{\pi}{4}$ (2) 0
- (3) 0
- (4) 0 (5) $\frac{16}{77}(3)^{\frac{7}{2}}$

- (6) 0 (7) 0 (8) $\frac{\pi^2}{6\sqrt{3}}$ (9) 0 (10) 0
- (11) $4 \log \left(\frac{1+\sqrt{5}}{2} \right)$ (12) 0 (13) $\frac{16}{105}$ (14) $\frac{\pi}{3}$ (15) $\frac{\pi}{2} \log \left(\frac{1}{2} \right)$

MISCELLANEOUS EXERCISE 4

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|---|---|---|---|---|---|---|---|---|----|
| A | A | С | С | D | С | A | D | В | A |

- (II) (1) $\frac{1}{10}$ (3 log 3) (2) $2 \sqrt{2}$ (3) $6 4 \log 2$ (4) $\frac{1}{8}$

- $(5) \frac{1}{21}$

- (6) $\pi 2$ (7) $\frac{1}{3} \log 2$ (8) $\frac{\pi}{5}$ (9) 0
- $(10) \frac{\pi}{2}$

- (III)(1) $\frac{\pi^2}{16}$ (2) $\frac{2}{\sqrt{35}} \tan^{-1} \sqrt{\frac{7}{5}}$ (3) $\frac{1}{\sqrt{5} a} \log \left(\frac{7+3\sqrt{5}}{2} \right)$
- $(4) \quad \frac{\pi}{20}$

- (5) $\frac{\pi}{2} \log 2$ (6) $\frac{1}{2} \left(\frac{\pi}{4} \log \sqrt{2} \right)$ (7) $-\frac{\pi}{2} \log 2$ (8) $\frac{\pi^3}{6}$

- (9) $\log\left(\frac{5+3\sqrt{3}}{1+\sqrt{3}}\right)$ (10) $\frac{17}{2}$
- (IV)(1) $\frac{1}{2}$ when a = 0; $\frac{9}{2}$ when a = 4 (2) $k = \frac{1}{2}$

5. APPLICATION OF DEFINITE INTEGRAL

EXERCISE 5.1

- (1) (i)
- (ii) 16
- (iii) 20

- (vii) $\frac{128}{3}$ sq. units

- (2) (i) $\frac{128}{3}$ (ii) $\frac{16}{3}$
- (iv) 1 (v) $2 \log 4$ (vi) $\frac{32}{3}$ (3) (i) $\frac{1}{12}$ (ii) $\frac{8}{3}$ (iii) $\frac{32}{3}$
- (iv) $8\frac{a^2}{3}$ (v) $\frac{1}{6}$

MISCELLANEOUS EXERCISE 5

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|----|----|----|----|----|----|----|----|----|
| A | A | С | В | A | D | В | D | A | В |
| | | | | | | | | | |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| A | D | В | В | С | С | A | D | A | С |

- **(II)**
- 1. (i)
- 10 (ii) 2 (iii) $\frac{1}{2}$ 5. $\frac{\pi}{3}$

- 6. $\frac{1}{6}$ 7. $\frac{\pi}{4} \frac{1}{2}$

- 9π
- 4. (i) $\frac{16}{3}$ (ii) $\frac{8}{3}$
- (iii) $\frac{1}{2}$
- 8. $\frac{56}{3}$
- 9. $36\frac{3}{4}$ 10. $\frac{7}{3}$

6. DIFFERENTIAL EQUATIONS

EXERCISE 6.1

- 2, 1 (1) (i)
- (ii) 2, 3
- (iii) 1, 2

- (iv) 3, 1
- (v) 2, 1
- (vi) 3, 2
- (vii) 2, not definded
- (viii) 2, 2

- (ix) 3, 3
- (x) 2, 1

EXERCISE 6.2

(1) (i)
$$2x^3 + 3xy^2 \frac{dy}{dx} - y^3 = 0$$

(ii)
$$xy \frac{d^2y}{dx^2} + x \left(\frac{dy}{dx}\right)^2 - y \frac{dy}{dx} = 0$$

(iii)
$$x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$$
 (iv) $8 \left(\frac{dy}{dx}\right)^3 - 27y = 0$

(v)
$$\frac{d^2y}{dx^2} - 25y = 0$$

(v)
$$\frac{d^2y}{dx^2} - 25y = 0$$
 (vi) $2\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^3 = 0$

(vii)
$$(x^2 + xy)\frac{dy}{dx} + y = 0$$
 (viii) $\frac{d^2y}{dx^2} - 7\frac{dy}{dx} + 10y = 0$

(ix)
$$xy \frac{d^2y}{dx^2} + x\left(\frac{dy}{dx}\right)^2 - 2y\frac{dy}{dx} = 0$$

(x)
$$\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y = 0$$

$$(2) \quad \frac{d^2y}{dx^2} = 0$$

(2)
$$\frac{d^2y}{dx^2} = 0$$
 (3) $2a\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^3 = 0$

(4)
$$x + 4y \frac{dy}{dx} = 0$$
 (5) $3 \frac{dy}{dx} + 2 = 0$

$$(5) \ 3 \frac{dy}{dx} + 2 = 0$$

(6)
$$81 \left(\frac{d^2y}{dx^2}\right)^2 = \left[\left(\frac{dy}{dx}\right)^2 + 1\right]^3$$

$$(7) \quad y \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0$$

EXERCISE 6.3

(2) (i)
$$\tan^{-1} y = \tan^{-1} x + c$$

(ii)
$$2e^{-3y} + 3e^{2x} = c$$
 (iii) $x = cy$

(iv)
$$\tan x \cdot \tan y = c$$
 (v) $\sin y \cdot \cos x = c$

(vi)
$$y = -kx + c$$

(vii)
$$2(x^2+y^2) + 2(x \sin 2x + y \sin 2y) + \cos 2y + \cos 2x + c = 0$$

(viii)
$$2y^2 \tan^{-1} x + 1 = cy^2$$

(ix)
$$4e^x + 3e^{-2y} = c$$

(x)
$$3e^x + 3e^{-y} + x^3 = c$$

(3) (i)
$$(1 + e^x)^3 \tan y = 0$$

(ii)
$$(1+x^2)(1-y^2)=5$$

(iii)
$$y = ex \log x$$
 (iv) $(\sin x)(e^y + 1) = \sqrt{2}$

(v)
$$2(2+e^y)=3(x+1)$$

(vi)
$$\cos\left(\frac{y-2}{x}\right) = a$$

(4) (i)
$$\tan\left(\frac{x+y}{2}\right) = x+c$$

(ii)
$$c + 2y = a \log \left(\frac{x - y - a}{x - y + a} \right)$$

(iii)
$$\sin(x^2 + y^2) + 2x = c$$

(iv)
$$x = \tan(x - 2y) + c$$

(v)
$$(2x-y) - \log(x-y+2) + 1 = 0$$

EXERCISE 6.4

(1)
$$\cos\left(\frac{y}{x}\right)dy = \log(x) + c$$

(2)
$$x^2 - v^2 = cx$$

(2)
$$x^2 - y^2 = cx$$
 (3) $x + 2ye^{\frac{x}{y}} = c$

(4)
$$xy^2 = c^2(x+2y)$$
 (5) $x^2 + y^2 = cx$

(5)
$$x^2 + y^2 = cx$$

(6)
$$y = c (x + y)^3 + x$$

(7)
$$x \left[1 - \cos \left(\frac{y}{x} \right) \right] = \sin \left(\frac{y}{x} \right)$$

(8)
$$x + ye^{\frac{x}{y}} = c$$

(8)
$$x + ye^{\frac{x}{y}} = c$$
 (9) $\log(y) + \frac{y}{x} = c$

$$(10) x^2 y = 4$$

$$(11) x^2 + y^2 = x^4$$

$$(12) \tan^{-1} \left(\frac{y}{x} \right) = \log(x) + c$$

$$(13) (3x + y)^3 (x + y)^2 = c$$

(14)
$$c = \log(x) + \frac{x}{x+y}$$
 (15) $x^2 - y^2 = cx$

EXERCISE 6.5

1. (i)
$$\frac{x^5}{5} - \frac{3x^2}{2} - xy = c$$

(ii)
$$ye^{\tan x} = e^{\tan x} (\tan x - 1) + c$$

(iii)
$$x = y(c + y^2)$$

(iv)
$$y (\sec x + \tan x) = \sec x + \tan x - x + c$$

(v)
$$x^2y = \frac{x^4 \log x}{4} - \frac{x^4}{16} + c$$

(vi)
$$x + y + 1 = ce^y$$

(vii)
$$2y = (x+a)^5 + 2c (x+a)^3$$

(viii)
$$r \sin^2 \theta + \frac{\sin^4 \theta}{2} = c$$

(ix)
$$\frac{y^3}{3} = xy + c$$

(x)
$$y = \sqrt{1 - x^2} + c (1 - x^2)$$

(xi)
$$y = \frac{1}{2} e^{\tan^{-1} x} + c e^{-\tan^{-1} x}$$

- 2. $3(x+3y) = 2(1-e^{3x})$
- $3. \quad 4x^2 + 9y^2 = 36$

- 5. $1 + v = 2e^{\frac{x^2}{2}}$

EXERCISE 6.6

- 8 times of original.
- 2. 95·4 years
- 3. 36·36°c 4. 5656

- 6. $\frac{27}{5}$ gms 7. $(3000) \left(\frac{4}{9}\right)^{\frac{1}{40}}$

1 hour

- 10. r = 3 t 11. 27,182 12. $\left(10 \frac{p}{10}\right)^2 \%$

MISCELLANEOUS EXERCISE 6

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|
| D | A | С | В | A | D | С | В | С | D | В | A | В | В | В |

- (II) (1) (i) 2, 1
- (ii) 3, 10
- (iii) 2, 3
- (iv) 1.4 (v) 4, not defined
- (3) (i) $xy \frac{d^2y}{dx^2} + x \left(\frac{dy}{dx}\right)^2 2y \frac{dy}{dx} = 0$ (ii) $\frac{d^2y}{dx^2} + y = 0$ (iii) $(y a) \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0$

- (iv) $2x^2y \frac{d^2y}{dx^2} + 2x^2 \left(\frac{dy}{dx}\right)^2 + y = 0$
- (v) $\frac{d^2y}{dx^2} 9y = 0$
- (4) (i) $2xy\frac{dy}{dx} + x^2 y^2 = 0$ (ii) $2b\frac{d^2y}{dx^2} 1 = 0$ (iii) $x + 4y\frac{dy}{dx} = 0$ (iv) $2\frac{dy}{dx} 3 = 0$

- (5) (i) $2e^{-3y} + 3e^{2x} + 6c = 0$
- (ii) $\log(y) = \frac{x^3}{2} + x + c$ (iii) $y = \frac{x}{2} \log(x^2) + 2 + cx$
- (iv) $y = 1 + x \log x + cx$
- (v) $y = x^2 + c \cdot \csc x$
- $(vi) x \log y = (\log y)^2 + c$

- (vii) $4xe^{2y} + 5e^{-y} = c$
- (6) (i) $ex \log x y = 0$
- (ii) $x = 2y^2$

(iii) $y \csc^2 x + 2 = 4 \sin 2x$

(iv) $\log \sqrt{x^2 + y^2} + \tan^{-1} \left(\frac{y}{x} \right) = \frac{\pi}{4}$

(v) $x + 2ye^{\frac{x}{y}} = 2$

- (8) $x^2 + y^2 = 4x + 5$ (9) $r = (63 t + 27)^{\frac{1}{3}}$
- $(10)\frac{20}{9}$ years

7. PROBABILITY DISTRIBUTIONS

EXERCISE 7.1

- 1. $\{-6, -4, -2, 0, 2, 4, 6\}$
- 2. { 0, 1, 2 }
- 3. (i) p.m.f. (ii) Not p.m.f

 - (iii) p.m.f (iv) Not p.m.f
 - (v) Not p.m.f. (iv) p.m.f

5.

| X | 0 | 1 | 2 |
|------|---------------|---------------|---------------|
| P(X) | $\frac{2}{3}$ | $\frac{2}{9}$ | $\frac{1}{9}$ |

(i)

| X | 0 | 1 | 2 |
|------|---------------|---------------|---------------|
| P(X) | $\frac{1}{4}$ | $\frac{1}{2}$ | $\frac{1}{4}$ |

(ii)

| X | 0 | 1 | 2 | 3 |
|------|---------------|---------------|---------------|---------------|
| P(X) | $\frac{1}{8}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{8}$ |

(iii)

| X | 0 | 1 | 2 | 3 | 4 |
|------|----------------|---------------|---------------|---------------|----------------|
| P(X) | $\frac{1}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{4}$ | $\frac{1}{16}$ |

6.

| X | 0 | 1 | 2 | 3 | 4 |
|------|------------------------------|--|---|---|------------------------------|
| P(X) | $\left(\frac{4}{5}\right)^4$ | $\left(\frac{4}{5}\right)^3 \frac{1}{5}$ | $\left(\frac{4}{5}\right)^2 \left(\frac{1}{5}\right)^2$ | $\frac{4}{5}\left(\frac{1}{5}\right)^3$ | $\left(\frac{1}{5}\right)^4$ |

7.

| X | 0 | 1 | 2 |
|--------------------|---------|---------------|----------------|
| $P\left(X\right)$ | 9 16 | $\frac{3}{8}$ | $\frac{1}{16}$ |

- 8. (i) $\frac{1}{10}$ (ii) $\frac{3}{10}$ (iii) $\frac{1}{5}$ 9. -0.05, 2.2475 10. $\frac{7}{3}$, $\frac{524}{54}$ 11. 1.5
- 12. $\frac{1}{3}$ 13. 4.67 14. 2.41

EXERCISE 7.2

- (i) p.d.f.
- Not a p.d.f (ii)
- 2. (a) $\frac{2.25}{16}$, (b) $\frac{3}{16}$, (c) $\frac{3}{4}$

(iii) Not a p.d.f

- 3. (i) p.d.f. (ii) $\frac{1}{9}$ (iii) $\frac{1}{9}$

4. (i)
$$\frac{1}{2}$$
, $\frac{35}{64}$ (ii) 6 , $\frac{11}{32}$, $\frac{1}{2}$

(ii)
$$6, \frac{11}{32}, \frac{1}{2}$$

8. (i)
$$\frac{x^2}{16}$$

8. (i)
$$\frac{x^2}{16}$$
 (ii) $\frac{1}{64}$, 0·18, 1

5. (i)
$$\frac{1}{4}$$
 (ii) $\frac{1}{2}$ (iii) $\frac{7}{16}$

$$(ii) \frac{1}{2}$$

(iii)
$$\frac{7}{16}$$

9.
$$\frac{2}{9}$$
, 0, $\frac{8}{9}$, $\frac{7}{9}$

6. (i)
$$\frac{2}{5}$$
 (ii) $\frac{1}{5}$

(ii)
$$\frac{1}{5}$$

10.
$$\frac{1}{\log 3}$$
, $\frac{4}{\log 3}$, $\frac{4(\log 3 - 1)}{(\log 3)^2}$

7. (i)
$$\frac{1}{2}$$
 (ii) $\frac{11}{16}$ (iii) 0.6328

(ii)
$$\frac{11}{16}$$

MISCELLANEOUS EXERCISE 7

(I)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|---|---|---|---|---|---|---|---|---|----|
| В | С | A | В | С | В | В | A | D | В |

(II) Solve the following:

- (1) (i) Discrete {1, 2, 3, ..., 100000}
- (ii) Continuous.
- (iii) Continuous.

- (iv) Discrete $\{0, 1, 2, 3, 4, 5\}$
- (v) Continuous

- (2) (i) $\frac{1}{21}$ (ii) $\frac{10}{21}$, $\frac{1}{7}$, $\frac{6}{7}$
- (3)
- (i) 0.5 (ii) 0.7 (iii) 0.55
 - (iv) 0.45

(5) $\frac{1}{4}$

| x | 1 | 2 | 3 | 4 | 5 |
|------|----------------|----------------|----------------|-----------------|----------------|
| P(X) | $\frac{1}{20}$ | $\frac{3}{20}$ | $\frac{1}{4}$ | $\frac{1}{2}$ | $\frac{1}{20}$ |
| F(x) | $\frac{1}{20}$ | $\frac{1}{5}$ | $\frac{9}{20}$ | $\frac{19}{20}$ | 1 |

(6)

| X | 0 | 1 | 2 | 3 | 4 |
|------|----------------|---------------|---------------|---------------|----------------|
| P(X) | $\frac{1}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{4}$ | $\frac{1}{16}$ |

(i) **(7)**

| X | 0 | 1 | 2 |
|------|---------------|---------------|---------------|
| P(X) | $\frac{4}{9}$ | $\frac{4}{9}$ | $\frac{1}{9}$ |

(ii)

| X | 0 | 1 | 2 |
|------|-----------------|-----------------|----------------|
| P(X) | $\frac{25}{36}$ | $\frac{10}{36}$ | $\frac{1}{36}$ |

- (8) (i) $\frac{1}{10}$ (ii) $\frac{17}{100}$

 $(iii) \frac{3}{10}$

(9)

| X | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
|------|-----|-----|-----|------|------|------|------|------|
| F(X) | 0.1 | 0.3 | 0.5 | 0.65 | 0.75 | 0.85 | 0.9 | 1 |
| P(x) | 0.1 | 0.2 | 0.2 | 0.15 | 0.10 | 0.10 | 0.05 | 0.10 |

- (i) 0.55
- (ii) 0.25

- (10) (i) $\frac{11}{5}$, $\frac{14}{25}$, $\frac{\sqrt{14}}{5}$ (ii) $\frac{1}{5}$, $\frac{14}{25}$, $\frac{\sqrt{14}}{5}$ (iii) $\frac{n+1}{2}$, $\frac{n^2-1}{12}$, $\sqrt{\frac{n^2-1}{12}}$ (iv) $\frac{5}{2}$, $\frac{5}{4}$, $\frac{\sqrt{5}}{2}$

- (11) ₹ 5·5, 8·25 (12) 0, 1 (13) (i) $\frac{1}{2}$ (ii) $\frac{11}{16}$ (iii) $\frac{81}{128}$

(15) $k = \frac{1}{\theta}, \frac{1}{e}$

(16)
$$k = \frac{1}{4}$$
, $F(x) = \frac{\sqrt{x}}{2}$, $\frac{1}{\sqrt{2}}$, $\frac{1}{2}$

8. BINOMIAL DISTRIBUTION

EXERCISE 8.1

- 1. (i) $\frac{3}{2^5}$ (ii) $\frac{7}{2^6}$ (iii) $\frac{63}{64}$
- 8. (i) $1 \left(\frac{99}{100}\right)^{50}$ (ii) $50 \left(\frac{99^{49}}{100^{50}}\right)$

- 2. $\frac{25}{216}$ 3. $29\left(\frac{19^9}{20^{10}}\right)$

(iii) $1 - 149 \left(\frac{99^{49}}{100^{50}} \right)$

- 4. (i) $\frac{1}{1024}$ (ii) $\frac{45}{1024}$
- 9. (i) $\frac{1}{20^3}$ (ii) $3\left(\frac{19}{20^3}\right)$ (iii) $3\left(\frac{19^2}{20^3}\right)$ (iv) $\left(\frac{19}{20}\right)^3$

- 5. (i) $(0.95)^5$
- (ii) $(1.2) (0.95)^4$
- (iii) $1 (1.2) (0.95)^4$ (iv) $1 (0.95)^5$
- 10. $\frac{7}{3} \left(\frac{5}{6}\right)^3$ 11. $22 \left(\frac{9^3}{10^{11}}\right)$

- 6. $\left(\frac{9}{10}\right)^4$ 7. $\frac{11}{243}$

12. (i) 4, 2.4 (ii) 10, 2.4 (iii) $\frac{2}{5}$; $\sqrt{6}$ (iv) $\frac{8}{5}$

MISCELLANEOUS EXERCISE 8

(I)

| 1 | 2 | 2 | 4 | | | |
|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| В | D | D | С | В | С | В |

(II) Solve the following:

- (i) $2 \times (0.8)^9$ (ii) $1 (0.8)^{10}$ **(1)**
 - (iii) $1 (8.2)(0.2)^9$
- (2) (i) $p = \frac{1}{2}$, Var(X) = 2.5
 - (ii) $n = 10, p = \frac{1}{2}$
- (3) (i) $\frac{63}{256}$ (ii) $\frac{105}{512}$
- $(4) \quad 45 \left(\frac{2^{26}}{2^{10}}\right)$
- (i) $0.65 \times (0.95)^{16}$ **(5)**
 - (ii) $(2.0325) \times (0.95)^{14}$
 - (iii) $1 (1.6) \times (0.95)^{16}$
- **(6)** 0.2114
- $(7) 1.4 \times (0.9)^4$
- $6.97 \times (0.97)^{19}$ (8)
- (9)
- 0.3456 (10) $\frac{30.44}{5^8}$

- (11) (i) $(0.998)^8$ (ii) $1.014 \times (0.998)^7$
 - (iii) $1 1.014 \times (0.998)^7$
- (12) $775.44 \times (0.003)^{38}$
- (13) (i) 0.9^{10}
- (ii) 0.9^9
- (iii) $0.45 \times (0.9)^8$
- (iv) $1 2.16 \times (0.9)^8$
- (14) (i) $\frac{1}{5^4}$, $\frac{16}{5^4}$, $\frac{96}{5^4}$, $\frac{256}{5^4}$, $\frac{256}{5^4}$
 - (ii) (a) $\frac{608}{5^4}$ (b) $1 \frac{33}{5^8}$
- (15) (i) $35 \times 8 \times \frac{81}{5^7}$ (ii) $1 \frac{12393}{5^7}$
- (16) (i) $\frac{\log 0.5}{\log 0.99}$
- $(17) \frac{1}{5}$